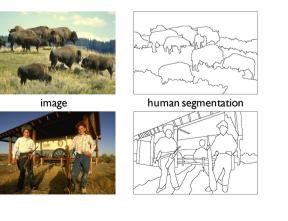
# BBM 413 Fundamentals of Image Processing

Erkut Erdem Dept. of Computer Engineering Hacettepe University

# Segmentation – Part 2

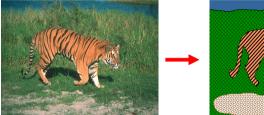
#### **Review-** The goals of segmentation

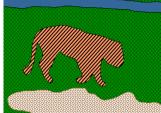
• Separate image into coherent "objects"



#### **Review-Image segmentation**

• Goal: identify groups of pixels that go together





Slide credit: S. Seitz, K. Grauman

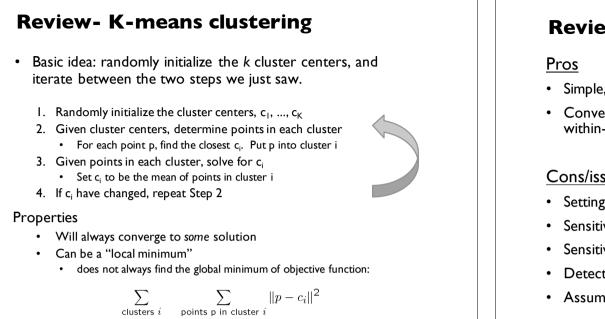
#### **Review- What is segmentation?**

- Clustering image elements that "belong together"
  - Partitioning
    - Divide into regions/sequences with coherent internal properties
  - Grouping
    - Identify sets of coherent tokens in image

http://www.eecs.berkeley.edu/Research/Projects/CS/vision/grouping/segbench/

Slide credit: S. Lazebnik

Slide credit: Fei-Fei Li



Slide credit: S. Seitz

## **Segmentation methods**

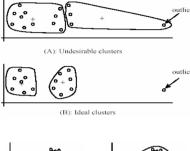
- Segment foreground from background
- Histogram-based segmentation
- Segmentation as clustering
  - K-means clustering
  - Mean-shift segmentation
- Graph-theoretic segmentation
  - Min cut
  - Normalized cuts
- Interactive segmentation

## **Review - K-means: pros and cons**

- Simple, fast to compute
- Converges to local minimum of within-cluster squared error

#### Cons/issues

- Setting k?
- Sensitive to initial centers
- Sensitive to outliers
- Detects spherical clusters
- Assuming means can be computed





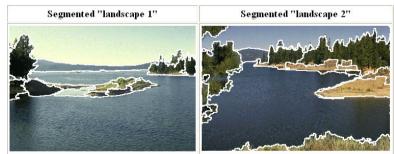


(A): Two natural clusters (B): k-means cluste

Slide credit: K Grauman

## Mean shift clustering and segmentation

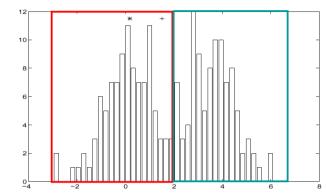
· An advanced and versatile technique for clustering-based segmentation



http://www.caip.rutgers.edu/~comanici/MSPAMI/msPamiResults.html

D. Comaniciu and P. Meer, Mean Shift: A Robust Approach toward Feature Space Analysis, PAMI 2002. Slide credit: S. Lazebnik

#### Finding Modes in a Histogram



- How Many Modes Are There?
  - Easy to see, hard to compute

Slide credit: S. Seitz

## Mean shift algorithm

 The mean shift algorithm seeks modes or local maxima of density in the feature space

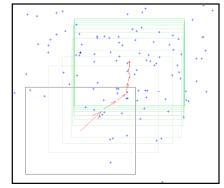
#### Slide credit: S. Lazebnik

## Mean shift algorithm

Mean Shift Algorithm

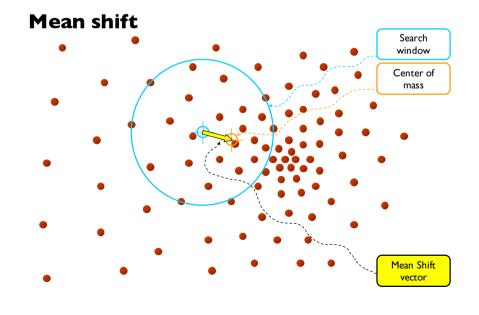
- I. Choose a search window size.
- 2. Choose the initial location of the search window.
- 3. Compute the mean location (centroid of the data) in the search window.
- 4. Center the search window at the mean location computed in Step 3.
- 5. Repeat Steps 3 and 4 until convergence.

The mean shift algorithm seeks the "mode" or point of highest density of a data distribution:

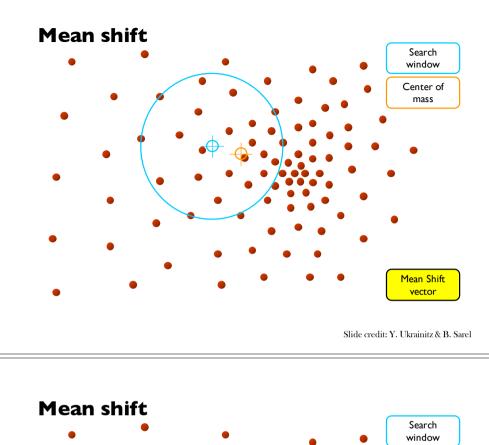


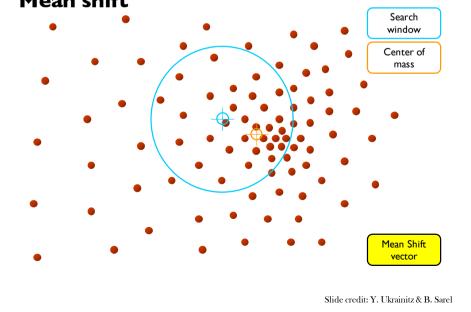
Two issues:

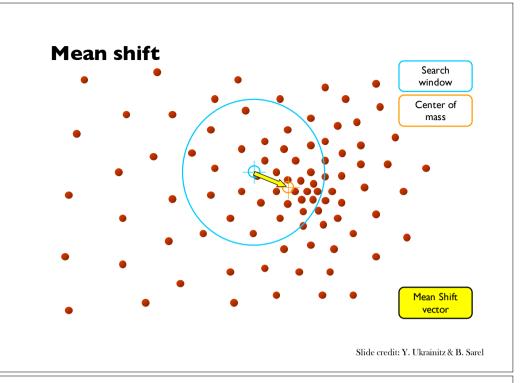
 Kernel to interpolate density based on sample positions.
Gradient ascent to mode.

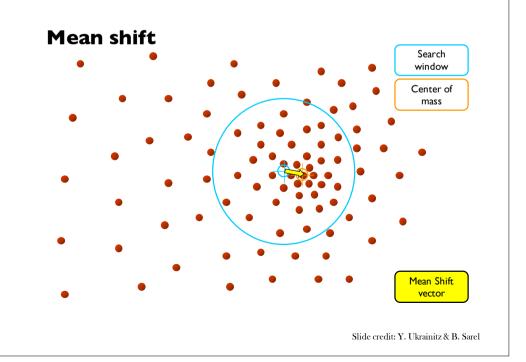


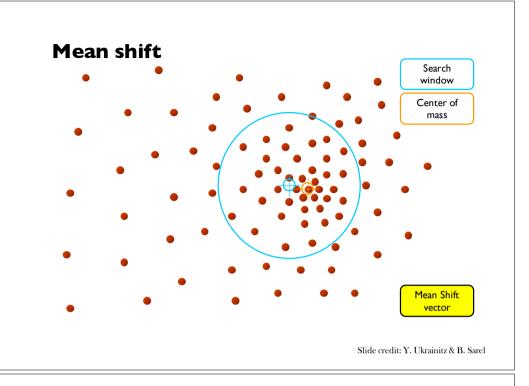
Slide credit: B. Freeman and A. Torralba

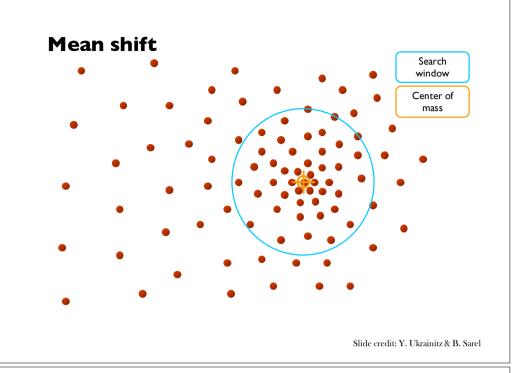






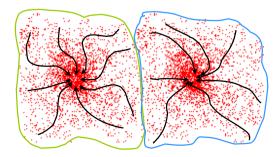






## Mean shift clustering

- Cluster: all data points in the attraction basin of a mode
- Attraction basin: the region for which all trajectories lead to the same mode



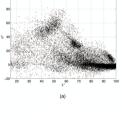
Slide credit: Y. Ukrainitz & B. Sarel

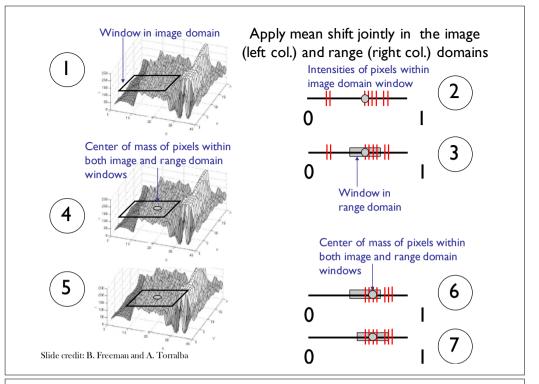
## Mean shift clustering/segmentation

- Find features (color, gradients, texture, etc)
- Initialize windows at individual feature points
- Perform mean shift for each window until convergence
- Merge windows that end up near the same "peak" or mode

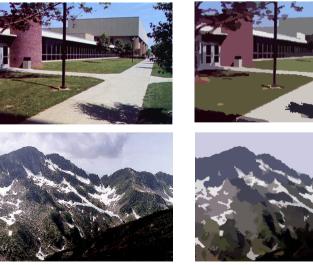


Slide credit: S. Lazebnik





## Mean shift segmentation results



http://www.caip.rutgers.edu/~comanici/MSPAMI/msPamiResults.html Slide credit: S. Lazebnik

## More results



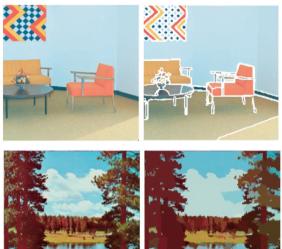
(c)

Fig. 4. Visualization of mean shift-based filtering and segmentation for gray-level data. (a) Input. (b) Mean shift paths for the pixels on the plateau and on the line. The black dots are the points of convergence. (c) Filtering result  $(h_s, h_r) = (8, 4)$ . (d) Segmentation result.

Comaniciu and Meer, IEEE PAMI vol. 24, no. 5, 2002

Slide credit: B. Freeman and A. Torralba

#### **More results**



Slide credit: S. Lazebnik

### **Segmentation methods**

- Segment foreground from background
- Histogram-based segmentation
- Segmentation as clustering
  - K-means clustering
  - Mean-shift segmentation
- Graph-theoretic segmentation
  - Min cut
  - Normalized cuts
- Interactive Segmentation

## Mean shift pros and cons

- Pros
  - Does not assume spherical clusters
  - Just a single parameter (window size)
  - Finds variable number of modes
  - Robust to outliers
- Cons
  - Output depends on window size
  - Computationally expensive
  - Does not scale well with dimension of feature space

Slide credit: S. Lazebnik

## **Graph-Theoretic Image Segmentation**

#### Build a weighted graph G=(V,E) from image

V: image pixels

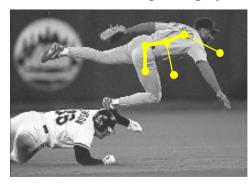
region

E: connections between

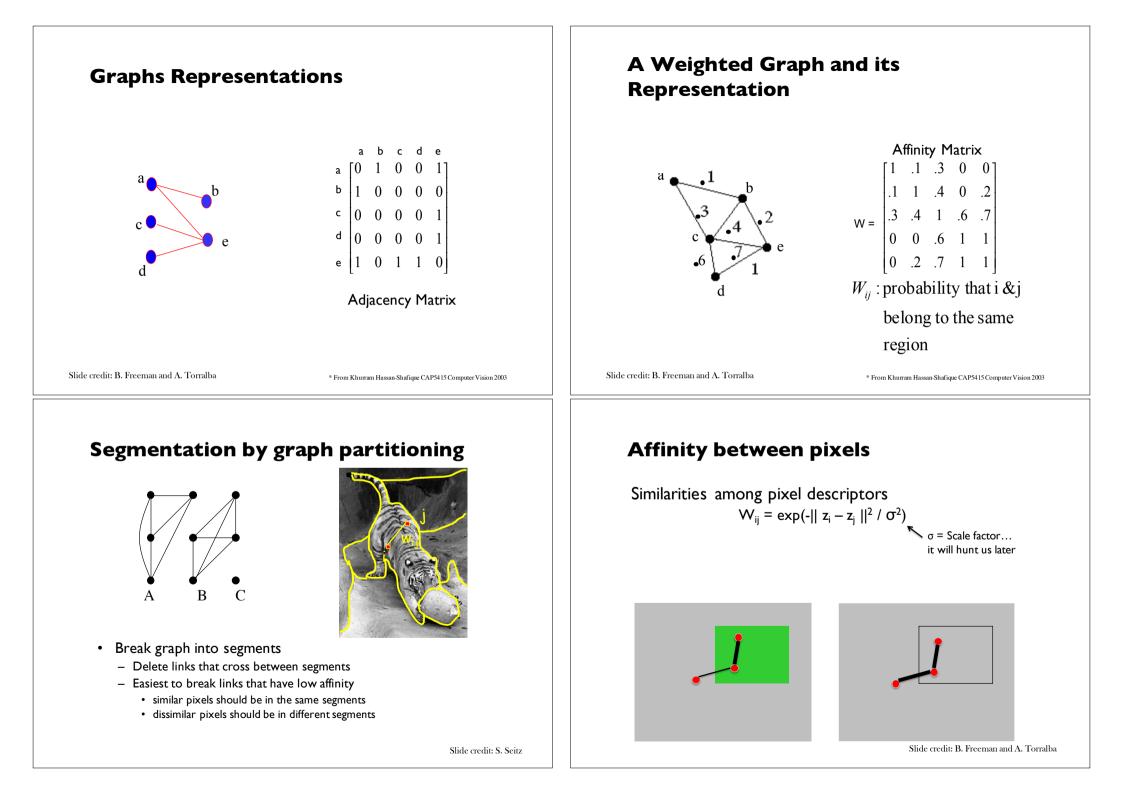
 $W_{ii}$ : probability that i &j

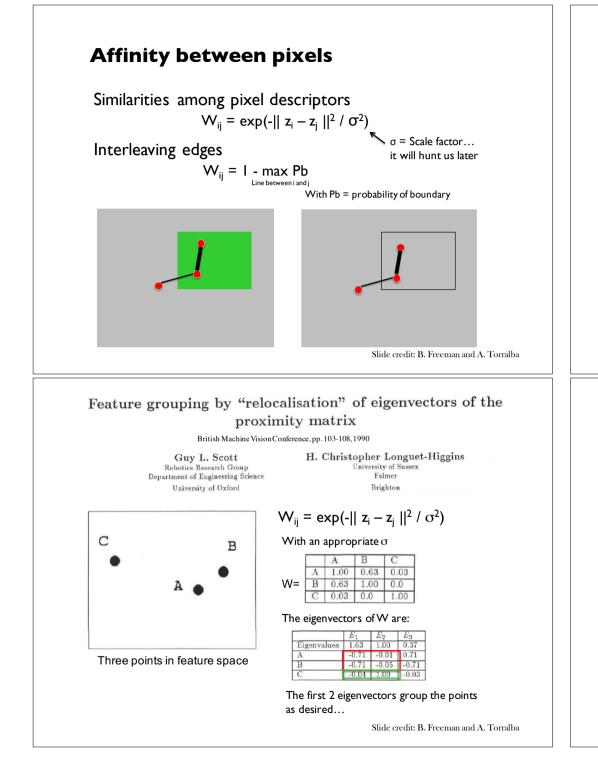
pairs of nearby pixels

belong to the same



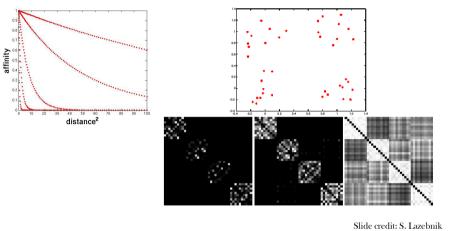
## Segmentation = graph partition



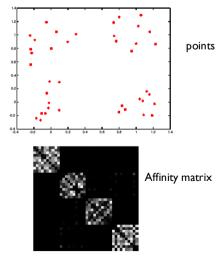


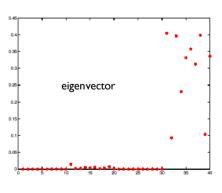
## Scale affects affinity

- Small σ: group only nearby points
- Large σ: group far-away points

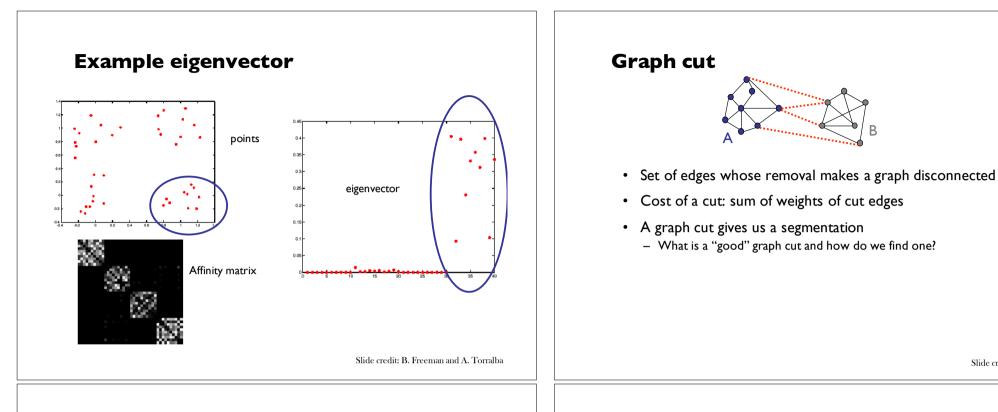


## **Example eigenvector**





Slide credit: B. Freeman and A. Torralba

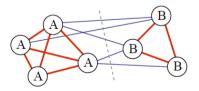


### **Segmentation methods**

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## **Minimum cut**

A cut of a graph G is the set of edges S such that removal of S from G disconnects G.



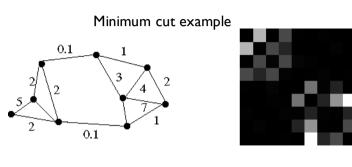
**Cut**: sum of the weight of the cut edges:



Slide credit: S. Seitz

#### Minimum cut

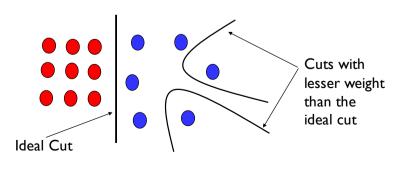
- We can do segmentation by finding the *minimum cut* in a graph
  - Efficient algorithms exist for doing this



Slide credit: S. Lazebnik

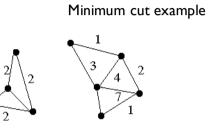
## **Drawbacks of Minimum cut**

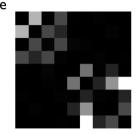
• Weight of cut is directly proportional to the number of edges in the cut.



## **Minimum cut**

We can do segmentation by finding the *minimum cut* in a graph
Efficient algorithms exist for doing this

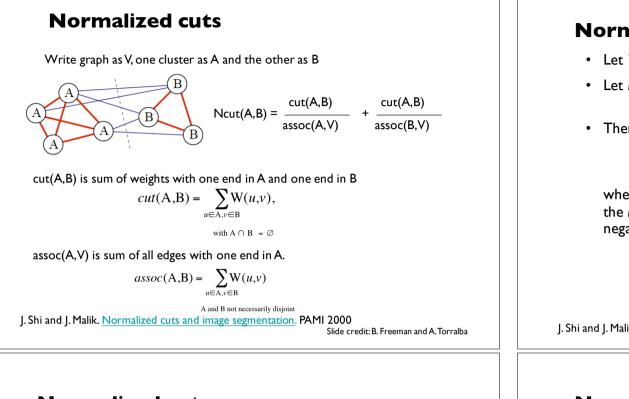




Slide credit: S. Lazebnik

## **Segmentation methods**

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#### **Normalized cut**

- Finding the exact minimum of the normalized cut cost is NPcomplete, but if we relax y to take on arbitrary values, then we can minimize the relaxed cost by solving the generalized eigenvalue problem  $(D - W)y = \lambda Dy$
- The solution y is given by the generalized eigenvector corresponding to the second smallest eigenvalue
- Intitutively, the *i*th entry of *y* can be viewed as a "soft" indication of the component membership of the *i*th feature
  - Can use 0 or median value of the entries as the splitting point (threshold), or find threshold that minimizes the Ncut cost

## Normalized cut

- Let W be the adjacency matrix of the graph
- Let D be the diagonal matrix with diagonal entries D(i, i) = Σ<sub>j</sub> W(i, j)
- Then the normalized cut cost can be written as  $\frac{y^{T}(D-W)y}{y^{T}Dy}$

where y is an indicator vector whose value should be I in the *i*th position if the *i*th feature point belongs to A and a negative constant otherwise

J. Shi and J. Malik. Normalized cuts and image segmentation. PAMI 2000

Slide credit: S. Lazebnik

## Normalized cut algorithm

- 1. Given an image or image sequence, set up a weighted graph  $\mathbf{G} = (\mathbf{V}, \mathbf{E})$ , and set the weight on the edge connecting two nodes being a measure of the similarity between the two nodes.
- 2. Solve  $(\mathbf{D} \mathbf{W})\mathbf{x} = \lambda \mathbf{D}\mathbf{x}$  for eigenvectors with the smallest eigenvalues.
- 3. Use the eigenvector with second smallest eigenvalue to bipartition the graph.
- 4. Decide if the current partition should be sub-divided, and recursively repartition the segmented parts if necessary.

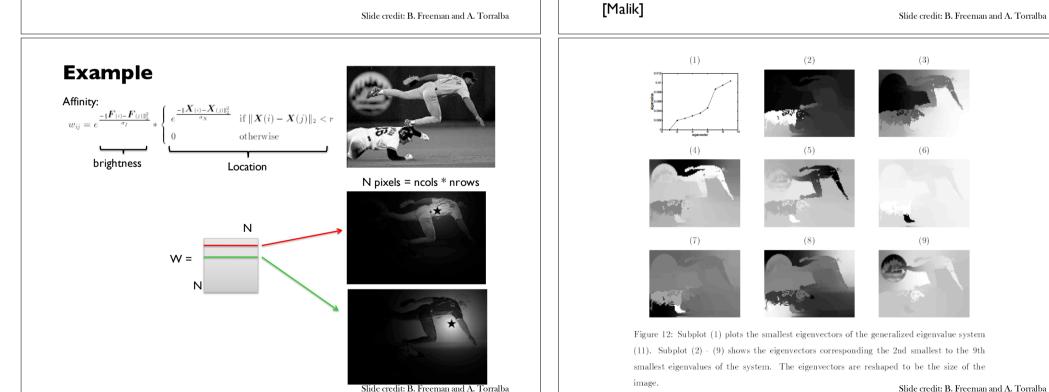
## **Global optimization**

- In this formulation, the segmentation becomes a global process.
- Decisions about what is a boundary are not local (as in Canny edge detector)

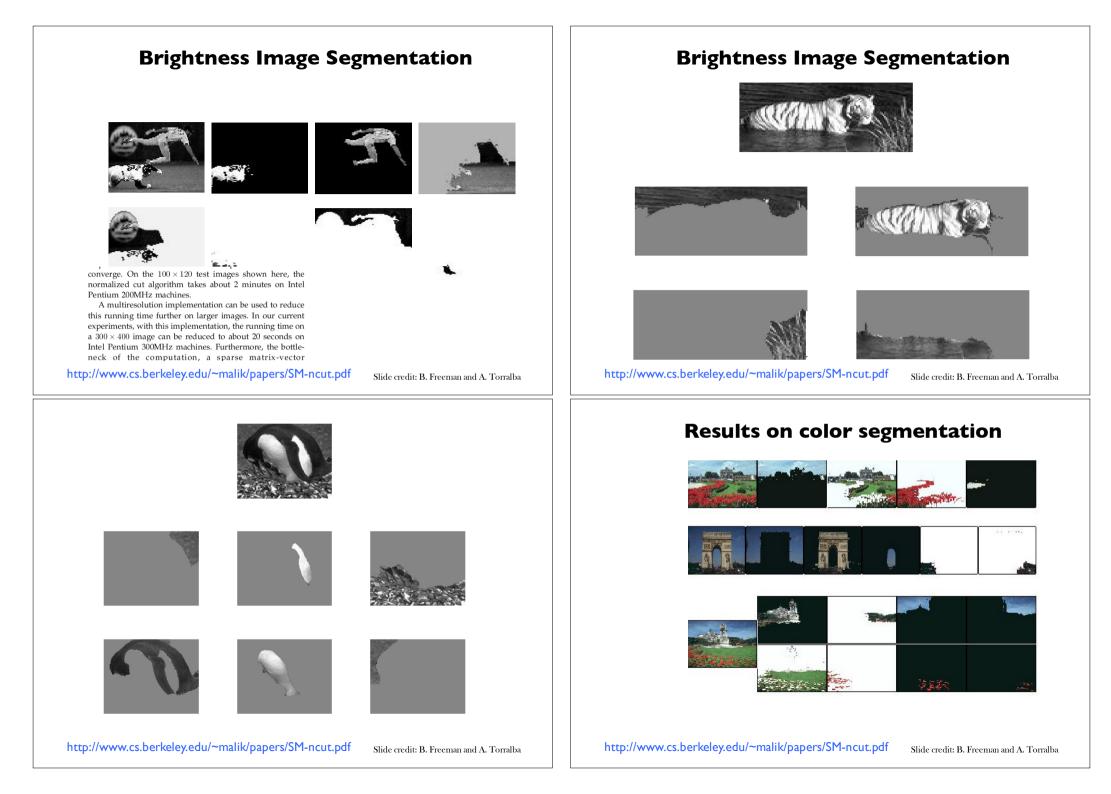
## **Boundaries of image regions defined** by a number of attributes

- Brightness/color
- Texture
- Motion
- Stereoscopic depth
- Familiar configuration





Slide credit: B. Freeman and A. Torralba



#### **Example results**



#### Normalized cuts: Pro and con

- Pros
  - Generic framework, can be used with many different features and affinity formulations
- Cons
  - High storage requirement and time complexity
  - Bias towards partitioning into equal segments

#### **Results: Berkeley Segmentation Engine**



http://www.cs.berkeley.edu/~fowlkes/BSE/

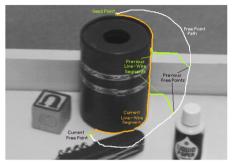
Slide credit: S. Lazebnik

#### Segmentation methods

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## Intelligent Scissors [Mortensen 95]

- Approach answers a basic question
  - Q: how to find a path from seed to mouse that follows object boundary as closely as possible?



Mortensen and Barrett, Intelligent Scissors for Image Composition, Proc. 22nd annual conference on Computer graphics and interactive techniques, 1995

**Figure 2:** Image demonstrating how the live-wire segment adapts and snaps to an object boundary as the free point moves (via cursor movement). The path of the free point is shown in white. Live-wire segments from previous free point positions  $(t_0, t_1, and t_2)$  are shown in green.

Slide credit: S. Seitz

# Path Search (basic idea)

- Graph Search Algorithm
  - Computes minimum cost path from seed to all other pixels

#### 

## Intelligent Scissors

- Basic Idea
  - Define edge score for each pixel
    - edge pixels have low cost
  - Find lowest cost path from seed to mouse



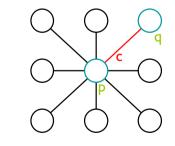
#### Questions

- How to define costs?
- How to find the path?

Slide credit: S. Seitz

## How does this really work?

• Treat the image as a graph



#### Graph

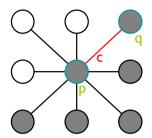
- node for every pixel p
- link between every adjacent pair of pixels, p,q
- cost **c** for each link

Note: each link has a cost

 this is a little different than the figure before where each pixel had a cost
Slide credit: S. Seitz

### **Defining the costs**

• Treat the image as a graph



Want to hug image edges: how to define cost of a link?

- the link should follow the intensity edge
  - want intensity to change rapidly  $\perp$  to the link
- $\mathbf{c} \approx |\text{difference of intensity} \perp \text{ to link}|$

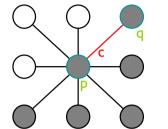
Slide credit: S. Seitz

# **Defining the costs** $\frac{1}{\sqrt{2}}$ • c can be computed using a cross-correlation filter assume it is centered at p • Also typically scale c by its length - set c = (max-|filter response|)

• where max = maximum |filter response| over all pixels in the image

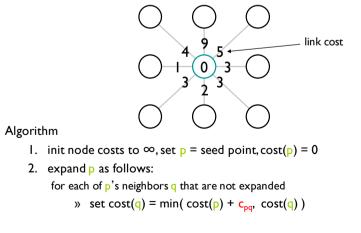
Slide credit: S. Seitz

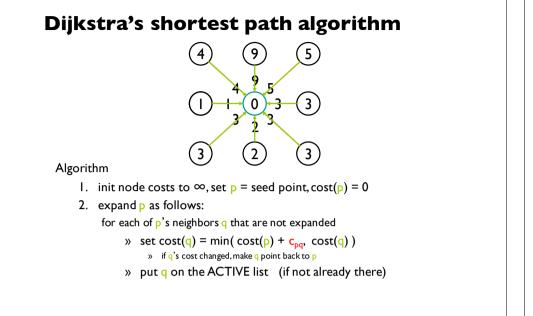
## **Defining the costs**



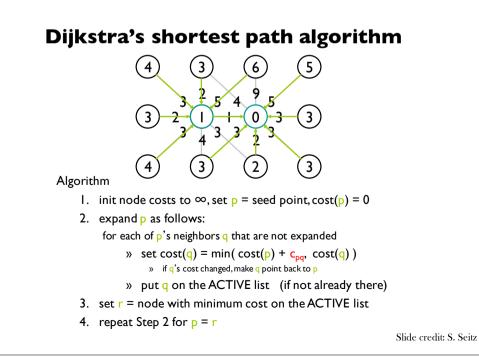
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- Also typically scale c by its length
  - set c = (max-|filter response|)
    - where max = maximum |filter response| over all pixels in the image Slide credit: S. Seitz

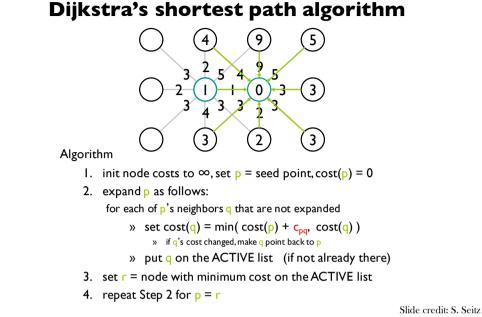
# Dijkstra's shortest path algorithm

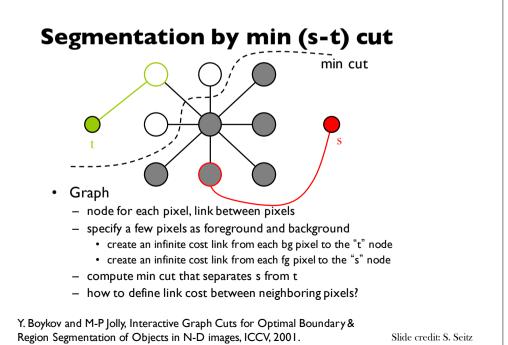




Slide credit: S. Seitz







#### **Random Walker**

• Compute probability that a random walker arrives at seed



L. Grady, Random Walks for Image Segmentation, IEEE T-PAMI, 2006

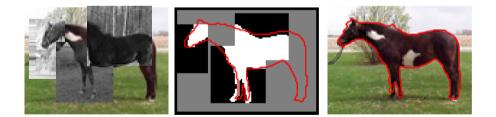
http://cns.bu.edu/~lgrady/Random\_Walker\_Image\_Segmentation.html

#### Do we need recognition to take the next step in performance?



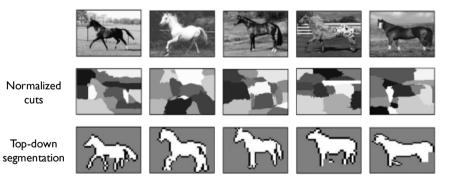
Slide credit: B. Freeman and A. Torralba

## **Top-down** segmentation



- E. Borenstein and S. Ullman, <u>Class-specific, top-down segmentation</u>, ECCV 2002
- A. Levin and Y. Weiss, <u>Learning to Combine Bottom-Up and Top-</u> <u>Down Segmentation</u>, ECCV 2006.

## **Top-down** segmentation



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Slide credit: S. Lazebnik

## Motion segmentation



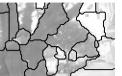


Image Segmentation





Motion Segmentation



Input sequence



Image Segmentation

Motion Segmentation

A. Barbu, S.C. Zhu. Generalizing Swendsen-Wang to sampling arbitrary posterior probabilities, IEEE TPAMI, 2005. Slide credit: K. Grauman