BIL 717 Image Processing

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Clustering-based Image Segmentation

Image segmentation

• Goal: identify groups of pixels that go together



The goals of segmentation

• Separate image into coherent "objects"



http://www.eecs.berkeley.edu/Research/Projects/CS/vision/grouping/segbench/

Slide credit: S. Lazebnik

The goals of segmentation

- Separate image into coherent "objects"
- Group together similar-looking pixels for efficiency of further processing



X. Ren and J. Malik. Learning a classification model for segmentation. ICCV 2003.

Slide credit: S. Lazebnik

Segmentation

- Compact representation for image data in terms of a set of <u>components</u>
- Components share "common" visual properties
- Properties can be defined at <u>different level of abstractions</u>

What is segmentation?

- Clustering image elements that "belong together"
 - Partitioning
 - Divide into regions/sequences with coherent internal properties
 - Grouping
 - Identify sets of coherent tokens in image

Segmentation is a global process



What are the occluded numbers?

Segmentation is a global process



What are the occluded numbers?

Occlusion is an important cue in grouping.

... but not too global



Slide credit: B. Freeman and A. Torralba



Magritte, 1957

Groupings by Invisible Completions



Groupings by Invisible Completions



1970s: R. C. James

Groupings by Invisible Completions



2000s: Bev Doolittle

Perceptual organization

"...the processes by which the bits and pieces of visual information that are available in the retinal image are structured into the larger units of perceived objects and their interrelations"



Stephen E. Palmer, Vision Science, 1999

Gestalt Psychology

- German: Gestalt "form" or "whole"
- Berlin School, early 20th century
 - Kurt Koffka, Max Wertheimer, and Wolfgang Köhler
- Gestalt: whole or group
 - Whole is greater than sum of its parts
 - Relationships among parts can yield new properties/features
- Psychologists identified series of factors that predispose set of elements to be grouped (by human visual system)

"I stand at the window and see a house, trees, sky. Theoretically I might say there were 327 brightnesses and nuances of colour. Do I have "327"? No. I have sky, house, and trees."

Max Wertheimer (1880-1943)



Slide credit: J. Hays and Fei-Fei Li

Gestalt Psychology

WOLFGANG METZGER

LAWS OF SEEING

Laws of Seeing, Wolfgang Metzger, 1936 (English translation by Lothar Spillmann, MIT Press, 2006)





Parallelism



Symmetry



Continuity



Closure

Familiarity

Similarity







http://chicagoist.com/attachments/chicagoist_alicia/GEESE.jpg, http://wwwdelivery.superstock.com/WI/223/1532/PreviewComp/SuperStock_1532R-0831.jpg

Slide credit: K. Grauman

Symmetry









Common fate





Image credit: Arthus-Bertrand (via F. Durand)

Slide credit: K. Grauman

Proximity





Slide credit: K. Grauman

Familiarity



Familiarity



Influences of grouping



http://web.mit.edu/persci/people/adelson/publications/gazzan.dir/koffka.html

Emergence



http://en.wikipedia.org/wiki/Gestalt_psychology

Slide credit: S. Lazebnik

Grouping phenomena in real life



Images: Forsyth and Ponce, Computer Vision: A Modern Approach

Slide credit: K. Grauman

Grouping phenomena in real life



Images: Forsyth and Ponce, Computer Vision: A Modern Approach

Slide credit: K. Grauman

Gestalt cues

- Good intuition and basic principles for grouping
- Basis for many ideas in segmentation and occlusion reasoning
- Some (e.g., symmetry) are difficult to implement in practice

Segmentation methods

- Segment foreground from background
- Histogram-based segmentation
- Segmentation as clustering
 - K-means clustering
 - Mean-shift segmentation
- Graph-theoretic segmentation
 - Min cut
 - Normalized cuts
- Interactive segmentation

A simple segmentation technique: Background Subtraction

- If we know what the background looks like, it is easy to identify "interesting bits
- Applications
 - Person in an office
 - Tracking cars on a road
 - surveillance

- Approach:
 - use a moving average to estimate background image
 - subtract from current frame
 - large absolute values are interesting pixels
 - trick: use morphological operations to clean up pixels

Movie frames from which we want to extract the foreground subject



Images: Forsyth and Ponce, Computer Vision: A Modern Approach

Two different background removal models

Background estimate Average over frames



EM background estimate

Foreground estimate

Foreground estimate



low thresh



high thresh





EM Images: Forsyth and Ponce, Computer Vision: A Modern Approach

Slide credit: B. Freeman

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Image segmentation: toy example



- These intensities define the three groups.
- We could label every pixel in the image according to which of these primary intensities it is.
 - i.e., segment the image based on the intensity feature.
- What if the image isn't quite so simple?





Slide credit: K. Grauman


- Now how to determine the three main intensities that define our groups?
- We need to **cluster.**



- Goal: choose three "centers" as the representative intensities, and label every pixel according to which of these centers it is nearest to.
- Best cluster centers are those that minimize SSD between all points and their nearest cluster center ci:

$$\sum_{\text{clusters } i} \sum_{\text{points p in cluster } i} ||p - c_i||^2$$

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Clustering

- With this objective, it is a "chicken and egg" problem:
 - If we knew the cluster centers, we could allocate points to groups by assigning each to its closest center.



centers by computing the mean per group.



- Cluster together (pixels, tokens, etc.) that belong together...
- Agglomerative clustering
 - attach closest to cluster it is closest to repeat
- Divisive clustering
 - split cluster along best boundary repeat
- Dendrograms
 - yield a picture of output as clustering process continues

Greedy Clustering Algorithms

 ${f Algorithm} \ 15.3:$ Agglomerative clustering, or clustering by merging

Make each point a separate cluster Until the clustering is satisfactory Merge the two clusters with the smallest inter-cluster distance

end

Algorithm 15.4: Divisive clustering, or clustering by splitting

Construct a single cluster containing all points Until the clustering is satisfactory Split the cluster that yields the two components with the largest inter-cluster distance end



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K-means and Hierarchical Clustering: Slide 40

Slide credit: D. Hoiem



- Say "Every point is its own cluster"
- Find "most similar" pair of clusters



K-means and Hierarchical Clustering: Slide 41



- Say "Every point is its own cluster"
- 2. Find "most similar" pair of clusters
- 3. Merge it into a parent cluster

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K-means and Hierarchical Clustering: Slide 42



- Say "Every point is its own cluster"
- 2. Find "most similar" pair of clusters
- 3. Merge it into a parent cluster
- 4. Repeat



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K-means and Hierarchical Clustering: Slide 43

Slide credit: D. Hoiem



- Say "Every point is its own cluster"
- Find "most similar" pair of clusters
- 3. Merge it into a parent cluster
- 4. Repeat



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K-means and Hierarchical Clustering: Slide 44

Common similarity/distance

measures

- P-norms
 - City Block (LI)
 - Euclidean (L2)
 - L-infinity

$$\|\mathbf{x}\|_{p} := \left(\sum_{i=1}^{n} |x_{i}|^{p}\right)^{1/p}$$

$$\|\mathbf{x}\|_{1} := \sum_{i=1}^{n} |x_{i}|$$

$$\|\mathbf{x}\| := \sqrt{x_{1}^{2} + \dots + x_{n}^{2}}$$

$$\|\mathbf{x}\|_{\infty} := \max(|x_{1}|, \dots, |x_{n}|)$$

Here x_i is the distance btw. two points

- Mahalanobis
 - Scaled Euclidean

$$d(\vec{x}, \vec{y}) = \sqrt{\sum_{i=1}^{N} \frac{(x_i - y_i)^2}{\sigma_i^2}}$$

• Cosine distance

similarity =
$$\cos(\theta) = \frac{A \cdot B}{\|A\| \|B\|}$$

Dendograms



Data set

agglomerative clustering using single-link clustering.

How to define cluster similarity?

- Average distance between points, maximum distance, minimum distance
- Distance between means or medoids

How many clusters?

- Clustering creates a dendrogram (a tree)
- Threshold based on max number of clusters or based on distance between merges





Good

- Simple to implement, widespread application
- Clusters have adaptive shapes
- Provides a hierarchy of clusters

Bad

- May have imbalanced clusters
- Still have to choose number of clusters or threshold
- Need to use an "ultrametric" to get a meaningful hierarchy

Segmentation methods

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K-means clustering

- Basic idea: randomly initialize the k cluster centers, and iterate between the two steps we just saw.
 - I. Randomly initialize the cluster centers, c_1 , ..., c_K
 - 2. Given cluster centers, determine points in each cluster
 - For each point p, find the closest c_i. Put p into cluster i
 - 3. Given points in each cluster, solve for c_i
 - Set c_i to be the mean of points in cluster i
 - 4. If c_i have changed, repeat Step 2

Properties

- Will always converge to some solution
- Can be a "local minimum"
 - does not always find the global minimum of objective function:





1. Ask user how many clusters they'd like. *(e.g. k=5)*



Slide credit: K Grauman, A. Moore

- 1. Ask user how many clusters they'd like. *(e.g. k=5)*
- 2. Randomly guess k cluster Center locations



Slide credit: K Grauman, A. Moore

- Ask user how many clusters they'd like. (e.g. k=5)
- 2. Randomly guess k cluster Center locations
- Each datapoint finds out which Center it's closest to. (Thus each Center "owns" a set of datapoints)



Slide credit: K Grauman, A. Moore

- 1. Ask user how many clusters they'd like. *(e.g. k=5)*
- 2. Randomly guess k cluster Center locations
- Each datapoint finds out which Center it's closest to.
- 4. Each Center finds the centroid of the points it owns



Slide credit: K Grauman, A. Moore

- 1. Ask user how many clusters they'd like. *(e.g. k=5)*
- 2. Randomly guess k cluster Center locations
- Each datapoint finds out which Center it's closest to.
- Each Center finds the centroid of the points it owns...
- 5. ...and jumps there
-Repeat until terminated!



Slide credit: K Grauman, A. Moore

K-means clustering

• Java demo:

http://kovan.ceng.metu.edu.tr/~maya/kmeans/index.html

http://home.dei.polimi.it/matteucc/Clustering/tutorial html/ AppletKM.html

K-means: pros and cons

<u>Pros</u>

- Simple, fast to compute
- Converges to local minimum of within-cluster squared error



<u>Cons/issues</u>

- Setting k?
- Sensitive to initial centers
- Sensitive to outliers
- Detects spherical clusters
- Assuming means can be computed





(A): Two natural clusters

(B): k-means clusters

An aside: Smoothing out cluster assignments

• Assigning a cluster label per pixel may yield outliers:



ullet

Depending on what we choose as the *feature space*, we can group pixels in different ways.

Grouping pixels based on intensity similarity



Feature space: intensity value (I-d)

Slide credit: K Grauman







quantization of the feature space; segmentation label map



Slide credit: K Grauman

Depending on what we choose as the *feature space*, we can group pixels in different ways.

Grouping pixels based on <u>color</u> similarity





Feature space: color value (3-d)

Slide credit: K Grauman

Depending on what we choose as the *feature space*, we can group pixels in different ways.

Grouping pixels based on **intensity** similarity

Clusters based on intensity similarity don't have to be spatially coherent.



 Image
 Clusters on intensity (K=5)
 Clusters on color (K=5)

 Image
 Image
 Image

K-means clustering using intensity alone and color alone

Image

Clusters on color



K-means using color alone, 11 segments



K-means using color alone, 11 segments.

Color alone often will not yield salient segments!



Depending on what we choose as the *feature space*, we can group pixels in different ways.

Grouping pixels based on <u>intensity+position</u> similarity





Both regions are black, but if we also include position (x,y), then we could group the two into distinct segments; way to encode both similarity & proximity. Slide credit: K Grauman

• Color, brightness, position alone are not enough to distinguish all regions...



Depending on what we choose as the *feature space*, we can group pixels in different ways.

Grouping pixels based on <u>texture</u> similarity







Filter bank of 24 filters

Feature space: filter bank responses (e.g., 24-d)

Slide credit: K Grauman

Texture representation example





statistics to summarize patterns in small windows

Slide credit: K Grauman
Segmentation with texture features

- Find "textons" by **clustering** vectors of filter bank outputs
- Describe texture in a window based on *texton histogram*



Texton index Texton index

Malik, Belongie, Leung and Shi. IJCV 2001.

Slide credit: K Grauman, L. Lazebnik

Image segmentation example



Slide credit: K Grauman

Pixel properties vs. neighborhood properties

query



These look very similar in terms of their color distributions (histograms).

How would their *texture* distributions compare?

Material classification example

For an image of a single texture, we can classify it according to its global (image-wide) texton histogram.



Material classification example

Nearest neighbor classification: label the input according to the nearest known example's label.



Plastic



Novel Image

Model

Manik Varma http://www.robots.ox.ac.uk/~vgg/research/texclass/with.html

Slide credit: K Grauman

Written Assignment #5



- E. Borenstein and S. Ullman, <u>Class-specific, top-down segmentation</u>, ECCV 2002
- Due on 25th of December

Segmentation methods

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Mean shift clustering and segmentation

• An advanced and versatile technique for clustering-based segmentation



http://www.caip.rutgers.edu/~comanici/MSPAMI/msPamiResults.html

D. Comaniciu and P. Meer, <u>Mean Shift: A Robust Approach toward Feature Space Analysis</u>, PAMI 2002.

Slide credit: S. Lazebnik

Finding Modes in a Histogram



- How Many Modes Are There?
 - Easy to see, hard to compute

Mean shift algorithm

 The mean shift algorithm seeks modes or local maxima of density in the feature space



Mean shift algorithm

Mean Shift Algorithm

- I. Choose a search window size.
- 2. Choose the initial location of the search window.
- 3. Compute the mean location (centroid of the data) in the search window.
- 4. Center the search window at the mean location computed in Step 3.
- 5. Repeat Steps 3 and 4 until convergence.

The mean shift algorithm seeks the "mode" or point of highest density of a data distribution:



Two issues: (1) Kernel to interpolate density based on sample positions. (2) Gradient ascent to mode.















Mean shift clustering

- Cluster: all data points in the attraction basin of a mode
- Attraction basin: the region for which all trajectories lead to the same mode



Mean shift clustering/segmentation

- Find features (color, gradients, texture, etc)
- Initialize windows at individual feature points
- Perform mean shift for each window until convergence
- Merge windows that end up near the same "peak" or mode





Mean shift clustering/segmentation

- Find features (color, gradients, texture, etc)
- Initialize windows at individual feature points
- Perform mean shift for each window until convergence
- Merge windows that end up near the same "peak" or mode









Fig. 4. Visualization of mean shift-based filtering and segmentation for gray-level data. (a) Input. (b) Mean shift paths for the pixels on the plateau and on the line. The black dots are the points of convergence. (c) Filtering result $(h_s, h_r) = (8, 4)$. (d) Segmentation result.

Comaniciu and Meer, IEEE PAMI vol. 24, no. 5, 2002

Slide credit: B. Freeman and A. Torralba

Mean shift segmentation results









http://www.caip.rutgers.edu/~comanici/MSPAMI/msPamiResults.html Slide credit: S. Lazebnik

More results









Slide credit: S. Lazebnik

More results



Mean shift pros and cons

- Pros
 - Does not assume spherical clusters
 - Just a single parameter (window size)
 - Finds variable number of modes
 - Robust to outliers
- Cons
 - Output depends on window size
 - Computationally expensive
 - Does not scale well with dimension of feature space

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Graph-Theoretic Image Segmentation

Build a weighted graph G=(V,E) from image



- V: image pixels
- E: connections between pairs of nearby pixels
- W_{ij} : probability that i &j belong to the same region

Segmentation = graph partition

Graphs Representations



	а	b	С	d	е
а	$\begin{bmatrix} 0 \end{bmatrix}$	1	0	0	1
b	1	0	0	0	0
С	0	0	0	0	1
d	0	0	0	0	1
е	1	0	1	1	0

Adjacency Matrix

A Weighted Graph and its Representation



	Affinity Matrix					
	1	.1	.3	0	0	
	.1	1	.4	0	.2	
\// =	.3	.4	1	.6	.7	
	0	0	.6	1	1	
	0	.2	.7	1	1	
W_{ij} :	pro	bał	oilit	y th	nati	&j
belong to the same						
	reg	ion				

Segmentation by graph partitioning





- Break graph into segments
 - Delete links that cross between segments
 - Easiest to break links that have low affinity
 - similar pixels should be in the same segments
 - dissimilar pixels should be in different segments

Affinity between pixels

Similarities among pixel descriptors

$$W_{ij} = \exp(-|| z_i - z_j ||^2 / \sigma^2)$$

\$\sigma \sigma = Scale factor..
it will hunt us later



Slide credit: B. Freeman and A. Torralba

Affinity between pixels

Similarities among pixel descriptors $W_{ij} = \exp(-|| z_i - z_j ||^2 / \sigma^2)$ Interleaving edges $W_{ij} = I - \max_{\text{Line between i and j}} \sigma = \text{Scale factor...}$

With Pb = probability of boundary



Slide credit: B. Freeman and A. Torralba

Scale affects affinity

- Small σ : group only nearby points
- Large σ : group far-away points





Feature grouping by "relocalisation" of eigenvectors of the proximity matrix

British Machine Vision Conference, pp. 103-108, 1990

Guy L. Scott

Robotics Research Group Department of Engineering Science University of Oxford H. Christopher Longuet-Higgins

C B

Three points in feature space

University of Sussex Falmer Brighton

$$W_{ij} = \exp(-|| z_i - z_j ||^2 / s^2)$$

With an appropriate s

	A	1.00	0.63	0.03
N=	В	0.63	1.00	0.0
	С	0.03	0.0	1.00

The eigenvectors of W are:

	E_1	E_2	E_3
Eigenvalues	1.63	1.00	0.37
A	-0.71	-0.01	0.71
В	-0.71	-0.05	-0.71
C	-0.04	1.00	-0.03

The first 2 eigenvectors group the points as desired...

Slide credit: B. Freeman and A. Torralba
Example eigenvector



Slide credit: B. Freeman and A. Torralba

Example eigenvector





- Set of edges whose removal makes a graph disconnected
- Cost of a cut: sum of weights of cut edges
- A graph cut gives us a segmentation
 - What is a "good" graph cut and how do we find one?

Segmentation methods

- Segment foreground from background
- Histogram-based segmentation
- Segmentation as clustering
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 - Normalized cuts
- Interactive segmentation

Minimum cut

A cut of a graph G is the set of edges S such that removal of S from G disconnects G.



Cut: sum of the weight of the cut edges:

$$cut(\mathbf{A},\mathbf{B}) = \sum_{u \in \mathbf{A}, v \in \mathbf{B}} W(u,v),$$

with $A \cap B = \emptyset$

Minimum cut

- We can do segmentation by finding the *minimum cut* in a graph
 - Efficient algorithms exist for doing this



Minimum cut example



Minimum cut

- We can do segmentation by finding the *minimum cut* in a graph
 - Efficient algorithms exist for doing this



Minimum cut example



Drawbacks of Minimum cut

• Weight of cut is directly proportional to the number of edges in the cut.



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Normalized cuts

Write graph as V, one cluster as A and the other as B



cut(A,B) is sum of weights with one end in A and one end in B $cut(A,B) = \sum_{u \in A, v \in B} W(u,v),$

with $A \cap B = \emptyset$

assoc(A,V) is sum of all edges with one end in A.

$$assoc(A,B) = \sum_{u \in A, v \in B} W(u,v)$$

A and B not necessarily disjoint

J. Shi and J. Malik. Normalized cuts and image segmentation. PAMI 2000

Normalized cut

- Let W be the adjacency matrix of the graph
- Let D be the diagonal matrix with diagonal entries $D(i, i) = \sum_{j} W(i, j)$
- Then the normalized cut cost can be written as

$$\frac{y^T (D - W)y}{y^T D y}$$

where y is an indicator vector whose value should be 1 in the *i*th position if the *i*th feature point belongs to A and a negative constant otherwise

Normalized cut

- Finding the exact minimum of the normalized cut cost is NPcomplete, but if we relax y to take on arbitrary values, then we can minimize the relaxed cost by solving the generalized eigenvalue problem $(D - W)y = \lambda Dy$
- The solution y is given by the generalized eigenvector corresponding to the second smallest eigenvalue
- Intitutively, the *i*th entry of *y* can be viewed as a "soft" indication of the component membership of the *i*th feature
 - Can use 0 or median value of the entries as the splitting point (threshold), or find threshold that minimizes the Ncut cost

Normalized cut algorithm

- 1. Given an image or image sequence, set up a weighted graph $\mathbf{G} = (\mathbf{V}, \mathbf{E})$, and set the weight on the edge connecting two nodes being a measure of the similarity between the two nodes.
- 2. Solve $(\mathbf{D} \mathbf{W})\mathbf{x} = \lambda \mathbf{D}\mathbf{x}$ for eigenvectors with the smallest eigenvalues.
- 3. Use the eigenvector with second smallest eigenvalue to bipartition the graph.
- 4. Decide if the current partition should be sub-divided, and recursively repartition the segmented parts if necessary.

Global optimization

- In this formulation, the segmentation becomes a global process.
- Decisions about what is a boundary are not local (as in Canny edge detector)

Boundaries of image regions defined by a number of attributes

- Brightness/color
- Texture
- Motion
- Stereoscopic depth
- Familiar configuration





Example





N pixels = ncols * nrows





Slide credit: B. Freeman and A. Torralba



Figure 12: Subplot (1) plots the smallest eigenvectors of the generalized eigenvalue system (11). Subplot (2) - (9) shows the eigenvectors corresponding the 2nd smallest to the 9th smallest eigenvalues of the system. The eigenvectors are reshaped to be the size of the image.

Brightness Image Segmentation







converge. On the 100×120 test images shown here, the normalized cut algorithm takes about 2 minutes on Intel Pentium 200MHz machines.

A multiresolution implementation can be used to reduce this running time further on larger images. In our current experiments, with this implementation, the running time on a 300×400 image can be reduced to about 20 seconds on Intel Pentium 300MHz machines. Furthermore, the bottleneck of the computation, a sparse matrix-vector





http://www.cs.berkeley.edu/~malik/papers/SM-ncut.pdf

Brightness Image Segmentation











http://www.cs.berkeley.edu/~malik/papers/SM-ncut.pdf





http://www.cs.berkeley.edu/~malik/papers/SM-ncut.pdf

Results on color segmentation







http://www.cs.berkeley.edu/~malik/papers/SM-ncut.pdf

Example results



nde credit. S. Lazebnik

Results: Berkeley Segmentation Engine



http://www.cs.berkeley.edu/~fowlkes/BSE/

Normalized cuts: Pro and con

- Pros
 - Generic framework, can be used with many different features and affinity formulations
- Cons
 - High storage requirement and time complexity
 - Bias towards partitioning into equal segments

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Intelligent Scissors [Mortensen 95]

- Approach answers a basic question
 - Q: how to find a path from seed to mouse that follows object boundary as closely as possible?



Mortensen and Barrett, Intelligent Scissors for Image Composition, Proc. 22nd annual conference on Computer graphics and interactive techniques, 1995

Figure 2: *Image demonstrating how the live-wire segment adapts and snaps to an object boundary as the free point moves (via cursor move-ment). The path of the free point is shown in white. Live-wire segments from previous free point positions (t*₀, t_1 , and t_2) are shown in green.

Intelligent Scissors

- Basic Idea
 - Define edge score for each pixel
 - edge pixels have low cost
 - Find lowest cost path from seed to mouse



Questions

- How to define costs?
- How to find the path?

Path Search (basic idea)

- Graph Search Algorithm
 - Computes minimum cost path from seed to all other pixels









Slide credit: S. Seitz

How does this really work?

• Treat the image as a graph



Graph

- node for every pixel p
- link between every adjacent pair of pixels, p,q
- cost **c** for each link

Note: each link has a cost

 this is a little different than the figure before where each pixel had a cost
Slide credit: S. Seitz

Defining the costs

• Treat the image as a graph



Want to hug image edges: how to define cost of a link?

- the link should follow the intensity edge
 - want intensity to change rapidly $^{\perp}$ to the link
- c \mathbb{M} |difference of intensity $^{\perp}$ to link|

Defining the costs





- c can be computed using a cross-correlation filter
 - assume it is centered at p
- Also typically scale c by its length
 - set c = (max-|filter response|)
 - where max = maximum |filter response| over all pixels in the image

Defining the costs



- c can be computed using a cross-correlation filter
 - assume it is centered at p
- Also typically scale c by its length
 - set c = (max-|filter response|)
 - where max = maximum |filter response| over all pixels in the image



Algorithm

- I. init node costs to \mathbb{M} , set p = seed point, cost(p) = 0
- 2. expand p as follows:

for each of p's neighbors q that are not expanded

» set $cost(q) = min(cost(p) + c_{pq}, cost(q))$



Algorithm

- I. init node costs to \mathbb{K} , set p = seed point, cost(p) = 0
- 2. expand p as follows:

for each of p's neighbors q that are not expanded

- » set $cost(q) = min(cost(p) + c_{pq}, cost(q))$
 - » if q's cost changed, make q point back to p
- » put q on the ACTIVE list (if not already there)



Algorithm

- I. init node costs to \mathbb{K} , set p = seed point, cost(p) = 0
- 2. expand p as follows:

for each of p's neighbors q that are not expanded

- » set $cost(q) = min(cost(p) + c_{pq}, cost(q))$
 - » if q's cost changed, make q point back to p
- » put q on the ACTIVE list (if not already there)
- 3. set r = node with minimum cost on the ACTIVE list
- 4. repeat Step 2 for p = r



Algorithm

- I. init node costs to \mathbb{W} , set p = seed point, cost(p) = 0
- 2. expand p as follows:

for each of p's neighbors q that are not expanded

- » set $cost(q) = min(cost(p) + c_{pq}, cost(q))$
 - » if q's cost changed, make q point back to p
- » put q on the ACTIVE list (if not already there)
- 3. set r = node with minimum cost on the ACTIVE list
- 4. repeat Step 2 for p = r
Segmentation by min (s-t) cut min cut Graph

- - node for each pixel, link between pixels
 - specify a few pixels as foreground and background
 - create an infinite cost link from each bg pixel to the "t" node
 - create an infinite cost link from each fg pixel to the "s" node
 - compute min cut that separates s from t
 - how to define link cost between neighboring pixels?

Y. Boykov and M-P Jolly, Interactive Graph Cuts for Optimal Boundary & Region Segmentation of Objects in N-D images, ICCV, 2001.

Slide credit: S. Seitz

Random Walker

• Compute probability that a random walker arrives at seed



L. Grady, <u>Random Walks for Image Segmentation</u>, IEEE T-PAMI, 2006

http://cns.bu.edu/~lgrady/Random_Walker_Image_Segmentation.html



Do we need recognition to take the next step in performance?

Slide credit: B. Freeman and A. Torralba

Top-down segmentation



- E. Borenstein and S. Ullman, <u>Class-specific, top-down segmentation</u>, ECCV 2002
- A. Levin and Y. Weiss, <u>Learning to Combine Bottom-Up and Top-</u> <u>Down Segmentation</u>, ECCV 2006.

Top-down segmentation



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Motion segmentation



Input sequence



Image Segmentation



Motion Segmentation



Input sequence



Image Segmentation



Motion Segmentation

A. Barbu, S.C. Zhu. Generalizing Swendsen-Wang to sampling arbitrary posterior probabilities, IEEE TPAMI, 2005.

Slide credit: K. Grauman