# BIL 717 Image Processing Mar. 4, 2015

# **Nonlinear Filtering**

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### Review - Signals

A signal is composed of low and high frequency components



low frequency components: smooth / piecewise smooth Neighboring pixels have similar brightness values You're within a region

high frequency components: oscillatory Neighboring pixels have different brightness values You're either at the edges or noise points

### Review - Linear Diffusion

- Let f (x) denote a grayscale (noisy) input image and u(x, t) be initialized with u(x,0) = u<sup>0</sup>(x) = f(x).
- The linear diffusion process can be defined by the equation:

$$\frac{\partial u}{\partial t} = \nabla \cdot (\nabla u) = \nabla^2 u$$

where  $\nabla \cdot$  denotes the divergence operator. Thus,

$$\frac{\partial u}{\partial t} = \frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2}$$



### Review - Linear Diffusion (cont'd.)

- As we move to coarser scales.
  - Evolving images become more and more simplified
  - Diffusion process removes the image structures at finer scales.



### **Review - Numerical Implementation**

- Original model:
  - $\frac{\partial u}{\partial t} = \frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial u^2}$
- Space discrete version:

$$\frac{du_{i,j}}{dt} = u_{i+1,j} + u_{i-1,j} + u_{i,j+1} + u_{i,j-1} - 4u_{i,j}$$

• Space-time discrete version:

$$\frac{u_{i,j}^{k+1} - u_{i,j}^{k}}{\Delta t} = u_{i+1,j}^{k} + u_{i-1,j}^{k} + u_{i,j+1}^{k} + u_{i,j-1}^{k} - 4u_{i,j}^{k}$$

homogeneous Neumann boundary condition  $\Delta t \leq 0.25$  is required for along the image boundary

numerical stability

### Review - Linear Diffusion and Gaussian Filtering

• Solution of the linear diffusion can be explicitly estimated as:

$$u(x,T) = \left(G_{\sqrt{2T}} * f\right)(x)$$
  
with  $G_{\sigma}(x) = \frac{1}{2\pi\sigma^2} exp\left(-\frac{|x|^2}{2\sigma^2}\right)$ 

- Solution of the linear diffusion equation is equivalent to a proper convolution of the input image with the Gaussian kernel  $G_{\sigma}(x)$  with standard deviation  $\sigma = \sqrt{2T}$
- The higher the value of T, the higher the value of  $\sigma$ , and the more smooth the image becomes.

### Variational interpretation of heat diffusion

- $E[u] = \iint_{\Omega} \|\nabla u\|^2 dx dy$ • Cost functional:  $= \iint_{\Omega} \left( u_x^2 + u_y^2 \right) dxdy$
- $\frac{\delta E}{\delta u} = \frac{\partial E}{\partial u} \frac{\partial}{\partial x} \left(\frac{\partial E}{\partial u_x}\right) \frac{\partial}{\partial y} \left(\frac{\partial E}{\partial u_y}\right)$ • Euler-Lagrange:  $= -2\frac{\partial u_x}{\partial x} - 2\frac{\partial u_y}{\partial y}$  $= -2(u_{xx} + u_{yy})$
- Heat diffusion: modifies temperature to decrease E quickly

Slide credit: I. Kokkinos

### Today – Nonlinear (Diffusion) Filters

- Median filter
- use nonlinear PDEs to create a scale space representation
  - consists of gradually simplified images
  - some image features such as edges are maintained or even enhanced.
- Perona-Malik Type Nonlinear Diffusion (1990)
- Total Variation (TV) Regularization (1992)
- Weickert's Edge Enhancing Diffusion (1994)

### Median filters

- A <u>Median Filter</u> operates over a window by selecting the median intensity in the window.
- What advantage does a median filter have over a mean filter?
- Is a median filter a kind of convolution?

adapted from: S. Seitz

### Median filter



- No new pixel values introduced
- Removes spikes: good for impulse, salt & pepper noise

Slide credit: K. Grauman

• Non-linear filter

### Median filter



### Median filter

- What advantage does median filtering have over Gaussian filtering?
- Robustness to outliers
- Median filter is edge preserving



Slide credit: K. Grauman

# Perona-Malik Type Nonlinear Diffusion

• The Perona-Malik equation is:

$$\frac{\partial u}{\partial t} = \nabla \cdot (g(|\nabla u|) \nabla u)$$

with homogeneous Neumann boundary conditions and the initial condition uO(x) = f(x), *f* denoting the input image.

- Constant diffusion coefficient of linear equation is replaced
  with a smooth non-increasing diffusivity function g satisfying
  - -g(0) = 1,
  - $-g(s) \ge 0,$
  - $-\lim_{s\to\infty}g(s)=0$
- The diffusivities become variable in both space and time (image dependent).

# Perona-Malik Type Nonlinear Diffusion

- · earliest nonlinear diffusion model for image smoothing
- called *anisotropic diffusion* by Perona and Malik.
- a scalar-valued diffusivity
- It is in fact an isotropic nonhomogeneous equation.
  - A true example of anisotropic diffusion model: Weickert's Edge-enhancing diffusion (more later on)

### Perona-Malik Type Nonlinear Diffusion

- The Perona-Malik equation:  $\frac{\partial u}{\partial t} = \nabla \cdot (g(|\nabla u|)\nabla u)$
- Two different choices for the diffusivity function:

(1) 
$$g(s) = \frac{1}{1 + s^2 / \lambda^2}$$
  
(2)  $g(s) = e^{-\frac{s^2}{\lambda^2}}$ 

- $\lambda$  corresponds to a contrast parameter.
- What is the effect of the parameter  $\lambda$ ?

### 1D Analysis of Perona-Malik Diffusion

- 1D version to demonstrate the role of the contrast parameter
- For 1D case, the Perona-Malik equation is as follows:

$$\frac{\partial u}{\partial t} = \frac{\partial}{\partial x} \underbrace{(g(|u_x|)u_x)}_{\Phi(u_x)} = \Phi'(u_x)u_{xx}$$

with 
$$g(|u_x|) = \frac{1}{1+|u_x|^2/\lambda^2}$$
 or  $g(|u_x|) = e^{-\frac{|u_x|^2}{\lambda^2}}$ 

### 1D Analysis of Perona-Malik Diffusion



- For linear diffusion the diffusivity is constant (g(s) = 1), which results in a linearly increasing flux function.
- For linear diffusion all points, including the discontinuities, are smoothed equally.

### 1D Analysis of Perona-Malik Diffusion

• Diffusivities and the corresponding flux functions for the linear diffusion (*plotted in dashed line*) and the Perona-Malik type nonlinear diffusion (*plotted in solid line*).



### 1D Analysis of Perona-Malik Diffusion



- Diffusivity is variable and decreases as  $|u_x|$  increases.
- Decay in diffusivity is particularly rapid after the contrast parameter  $\boldsymbol{\lambda}.$
- Two different behaviors in the diffusion process



- For the points where  $|u_x| < \lambda$ ,  $\Phi'(u_x) > 0$  we have lost in the material.
- For the points where  $|u_x| > \lambda$ , on the contrary,  $\Phi'(u_x) < 0$  which generates an enhancement in the material.

### Perona-Malik Type Nonlinear Diffusion

- In 2D case, diffusivities are reduced at the image locations where |∇u|<sup>2</sup> is large (|∇u|<sup>2</sup> : a measure of edge likelihood)
- Amount of smoothing is low along image edges.
- Contrast parameter λ specifies a measure that determines which edge points are to be preserved or blurred during the diffusion process.
- Even edges can be sharpened due to the local backward diffusion behavior as discussed for the 1D case.
- Since the backward diffusion is a well-known ill-posed process, this may cause an instability, the so-called *staircasing effect.*





- Diffusivity is always nonnegative, but *forward* and *backward* diffusions are observed during the smoothing.
- Contrast parameter  $\lambda$  separates the regions of forward diffusion from the regions of backward diffusion.



### Staircasing Effect

• Due to backward diffusion, a piece-wise smooth region in the original image evolves into many unintuitive piecewise constant regions.





Original noisy image

Perona-Malik Diffusion

Credit: S. Paris

Solution: Use pre-filtered (regularized) gradients in diffusivity computations

### Regularized Perona-Malik (cont'd.)



### Regularized Perona-Malik Model

• Replacing the diffusivities  $g(|\nabla u|)$  with the regularized ones  $g(|\nabla u_{\sigma}|)$  leads to the following equation:

$$\frac{\partial u}{\partial t} = \nabla \cdot (g(|\nabla u_{\sigma}|)\nabla u)$$

where  $u_{\sigma} = G_{\sigma} * u$  represents a Gaussian-smoothed version of the image.







Original noisy image

Perona-Malik Diffusion

Regularized Perona-Malik Diffusion

### Regularized Perona-Malik Model

 Smoothing process diminishes noise while retaining or enhancing edges



### Regularized Perona-Malik Model

 Smoothing process diminishes noise while retaining or enhancing edges



### Numerical Implementation

• Original model:

$$\frac{\partial u}{\partial t} = \nabla \cdot (g(|\nabla u|)\nabla u)$$

• Space discrete version:

$$\begin{aligned} \frac{\partial u}{\partial t} &= \frac{\partial}{\partial x} \left( g(|\nabla u|) u_x \right) + \frac{\partial}{\partial y} \left( g(|\nabla u|) u_y \right) \\ \frac{d u_{i,j}}{dt} &= g_{i+\frac{1}{2},j} \cdot \left( u_{i+1,j} - u_{i,j} \right) - g_{i-\frac{1}{2},j} \cdot \left( u_{i,j} - u_{i-1,j} \right) \\ &+ g_{i,j+\frac{1}{2}} \cdot \left( u_{i,j+1} - u_{i,j} \right) - g_{i,j-\frac{1}{2}} \cdot \left( u_{i,j} - u_{i,j-1} \right) \end{aligned}$$

### Numerical Implementation

Central differences is used to approximate the gradient magnitude at a pixel (*i*, *j*) in the diffusivity estimation,
 g<sub>i,j</sub> = g(|∇u<sub>i,j</sub>|)



### Numerical Implementation

• Space discrete version:

$$\frac{du_{i,j}}{dt} = g_{i+\frac{1}{2},j} \cdot (u_{i+1,j} - u_{i,j}) - g_{i-\frac{1}{2},j} \cdot (u_{i,j} - u_{i-1,j}) + g_{i,j+\frac{1}{2}} \cdot (u_{i,j+1} - u_{i,j}) - g_{i,j-\frac{1}{2}} \cdot (u_{i,j} - u_{i,j-1})$$

- This discretization scheme requires the diffusivities to be estimated at mid-pixel points.
- computed by taking averages of the diffusivities over neighboring pixels:  $g_{i\pm\frac{1}{2},j} = \frac{g_{i\pm1,j} + g_{i,j}}{2}$  $u_i = \frac{g_{i,j\pm\frac{1}{2},j} - g_{i+\frac{1}{2},j}}{2}$  $u_i = \frac{g_{i,j\pm\frac{1}{2},j}}{2}$

### Numerical Implementation

• Space discrete version:

$$\begin{array}{lll} \frac{du_{i,j}}{dt} & = & g_{i+\frac{1}{2},j} \cdot \left(u_{i+1,j} - u_{i,j}\right) - g_{i-\frac{1}{2},j} \cdot \left(u_{i,j} - u_{i-1,j}\right) \\ & + & g_{i,j+\frac{1}{2}} \cdot \left(u_{i,j+1} - u_{i,j}\right) - g_{i,j-\frac{1}{2}} \cdot \left(u_{i,j} - u_{i,j-1}\right) \end{array}$$

• Space-time discrete version:

$$\begin{array}{lcl} \displaystyle \frac{u_{i,j}^{k+1} - u_{i,j}^k}{\Delta t} & = & g_{i+\frac{1}{2},j}^k \cdot u_{i+1,j}^k + g_{i-\frac{1}{2},j}^k \cdot u_{i-1,j}^k + g_{i,j+\frac{1}{2}}^k \cdot u_{i,j+1}^k + g_{i,j-\frac{1}{2}}^k \cdot u_{i,j-1}^k \\ & - & \left(g_{i+\frac{1}{2},j}^k + g_{i-\frac{1}{2},j}^k + g_{i,j+\frac{1}{2}}^k + g_{i,j-\frac{1}{2}}^k\right) \cdot u_{i,j}^k \end{array}$$

- homogeneous Neumann boundary condition along the image boundary
- $\Delta t \le 0.25$  is required for numerical stability

### Perona-Malik results for color images



Slide credit: I. Kokkinos

### Extension to vectorial images

• Extension of nonlinear diffusion to vectorial images:

$$\begin{split} \boldsymbol{u} &= \begin{pmatrix} u_1, u_2, \dots, u_N \end{pmatrix} \\ \frac{\partial u}{\partial t} &= \operatorname{div} \left( g(\|\nabla u\|) \nabla u \right) \\ & \text{generalization} \\ \\ \frac{\partial u_i}{\partial t} &= \operatorname{div} \left( g(\|\nabla u\|) \nabla u_i \right), \ i = 1, \dots, N \\ & \text{where:} \quad \|\nabla u\| = \sqrt{\sum_{i=1}^N \|\nabla u_i\|^2} \end{split}$$

Slide credit: I. Kokkinos

### Total Variation (TV) Regularization

- Rudin et al. (1992): image restoration as minimization of the total variation (TV) of a given image.
- The Total Variation (TV) regularization model is generally defined as:

$$E_{TV}(u) = \int_{\Omega} \left( \frac{1}{2} (u - f)^2 + \alpha |\nabla u| \right) dx$$

- $\Omega \subset I\!\!R^2$  is connected, bounded, open subset representing the image domain,
- f is an image defined on  $\Omega$ ,
- u is the smooth approximation of f,
- a > 0 is a scalar.

### Total Variation (TV) Regularization

• The Total Variation (TV) regularization model:

$$E_{TV}(u) = \int_{\Omega} \left( \frac{1}{2} (u - f)^2 + \alpha |\nabla u| \right) dx$$

• The gradient descent equation for Equation (10) is defined by:

$$\frac{\partial u}{\partial t} = \nabla \cdot \left( \frac{\nabla u}{|\nabla u|} \right) - \frac{1}{\alpha} (u - f); \quad \frac{\partial u}{\partial n} \Big|_{\partial \Omega} = 0$$

- The value of  $\boldsymbol{\alpha}$  specifies the relative importance of the fidelity term.
- It can be interpreted as a scale parameter that determines the level of smoothing.

### **TV Regularization**

- Observed image *f* was assumed to be degraded by additive Gaussian noise with zero mean and known variance  $\sigma^2$ .
- To restore a given image, solve the following constrained optimization problem:

$$\min_{u} \int_{\Omega} |\nabla u| dx$$

subject to

$$\int\limits_{\Omega} (u-f)^2 dx = \sigma^2$$

•  $\frac{1}{\alpha}$  can be considered as a Lagrange multiplier.

### Sample TV Restoration results



- The value of  $\alpha$  specifies the relative importance of the fidelity term and thus the level of smoothing.

### TV Regularization and TV Flow

- TV regularization can be associated with a nonlinear diffusion filter, the so-called *TV flow.*
- Ignoring the fidelity term in the TV regularization model leads to the PDE:

$$\frac{\partial u}{\partial t} = \nabla \cdot (g(|\nabla u|)\nabla u)$$

with  $u^0 = f$  and the diffusivity function  $g(|\nabla u|) = \frac{1}{|\nabla u|}$ 

 Notice that this diffusivity function has no additional contrast parameter as compared with the Perona-Malik diffusivities.

# • Corresponding smoothing process yields segmentation-like, piecewise constant images. $T = 0 \qquad T = 25 \qquad T = 50$ $T = 100 \qquad T = 200 \qquad T = 400$ T = 400

### Numerical Implementation

Sample TV Flow results

- The evolution equation can be discretized by using standard finite differences.
- The solution of TV regularization or equivalently TV flow leads to singular diffusivities.
- In numerical implementations based on standard discretization, this leads to stability problems as the image gradient tends to zero.
- A common solution to this problem is to add a small positive constant ε to image gradients.
- More accurate numerical implementations are suggested.

# Sample TV Flow results

• Corresponding smoothing process yields segmentation-like, piecewise constant images.



### Numerical Implementation

• Space discrete version:

$$\begin{split} \frac{\partial u}{\partial t} &= \frac{\partial}{\partial x} \left( \frac{u_x}{\sqrt{|\nabla u|^2 + \epsilon^2}} \right) + \frac{\partial}{\partial y} \left( \frac{u_y}{\sqrt{|\nabla u|^2 + \epsilon^2}} \right) - \frac{1}{\alpha} (u - f) \\ &= \frac{u_{xx} \left( u_y^2 + \epsilon^2 \right) - 2u_x u_y u_{xy} + u_{yy} \left( u_x^2 + \epsilon^2 \right)}{\left( u_x^2 + u_y^2 + \epsilon^2 \right)^{\frac{3}{2}}} - \frac{1}{\alpha} (u - f) , \end{split}$$

### Numerical Implementation

• Space discrete version:

$$\frac{du_{i,j}}{dt} = \frac{\frac{d^2 u_{i,j}}{dx^2} \left( \left( \frac{du_{i,j}}{dy} \right)^2 + \epsilon^2 \right) - 2 \left( \frac{du_{i,j}}{dx} \right) \left( \frac{du_{i,j}}{dy} \right) \left( \frac{d^2 u_{i,j}}{dxdy} \right) + \frac{d^2 u_{i,j}}{dy^2} \left( \left( \frac{du_{i,j}}{dx} \right)^2 + \epsilon^2 \right)^2} \\ \left( \left( \frac{du_{i,j}}{dx} \right)^2 + \left( \frac{du_{i,j}}{dy} \right)^2 + \epsilon^2 \right)^{\frac{3}{2}} \\ - \frac{1}{\alpha} \left( u_{i,j} - f_{i,j} \right) \\ \text{with} \quad d^2 u_{i,j} \quad u_{i+1,j+1} - u_{i+1,j-1} - u_{i-1,j+1} + u_{i-1,j-1}$$

$$\frac{d^2 u_{i,j}}{dxdy} \approx \frac{u_{i+1,j+1} - u_{i+1,j-1} - u_{i-1,j+1} + u_{i-1,j-1}}{4}$$

### Structure Tensor

• Structure tensor  $J(\nabla u)$  is described by:

$$J(\nabla u) = \nabla u \nabla u^T = \begin{bmatrix} u_x^2 & u_x u_y \\ u_x u_y & u_y^2 \end{bmatrix}$$

- Structure tensor  $J(\nabla u)$  can be interpreted as an image feature describing the local orientation information.
- It has an orthonormal basis of eigenvectors  $v_1$  and  $v_2$  with  $v_1 \parallel \nabla u$  and  $v_2 \perp \nabla u$ , and
- The corresponding eigenvalues  $\lambda_1 = |\nabla u|^2$  and  $\lambda_2 = 0$ .

### Numerical Implementation

• Space-time discrete version:

$$\begin{split} \frac{u_{i,j}^{k+1} - u_{i,j}^{k}}{\Delta t} &= \left( \left( \frac{u_{i+1,j}^{k} - u_{i-1,j}^{k}}{2} \right)^{2} + \left( \frac{u_{i,j+1}^{k} - u_{i,j-1}^{k}}{2} \right)^{2} + \epsilon^{2} \right)^{-\frac{3}{2}} \\ &\cdot \left[ \left( u_{i+1,j}^{k} - 2u_{i,j}^{k} + u_{i-1,j}^{k} \right) \left( \left( \frac{u_{i,j+1}^{k} - u_{i,j-1}^{k}}{2} \right)^{2} + \epsilon^{2} \right) \right. \\ &- \left. \frac{1}{8} \left( u_{i+1,j}^{k} - u_{i-1,j}^{k} \right) \left( u_{i,j+1}^{k} - u_{i,j-1}^{k} \right) \right. \\ &\left. \left( u_{i+1,j+1}^{k} - u_{i+1,j-1}^{k} - u_{i-1,j+1}^{k} + u_{i-1,j-1}^{k} \right) \right. \\ &+ \left. \left( u_{i,j+1}^{k} - 2u_{i,j}^{k} + u_{i,j-1}^{k} \right) \left( \left( \frac{u_{i+1,j}^{k} - u_{i-1,j}^{k}}{2} \right)^{2} + \epsilon^{2} \right) \right] \\ &- \left. \frac{1}{\alpha} \left( u_{i,j}^{k} - f_{i,j} \right) \end{split}$$

homogeneous Neumann boundary condition along the image boundary

 $\Delta t \le 0.25\epsilon$  is required for numerical stability

### Structure Tensor

$$J(\nabla u) = \nabla u \nabla u^T = \begin{bmatrix} u_x^2 & u_x u_y \\ u_x u_y & u_y^2 \end{bmatrix}$$



 $J(\nabla u) = \nabla u \nabla u^T$ 

Images are taken from Brox et al., 2004



### Structure Tensor

$$J = \sum_{x',y'} \left( \nabla G_{\sigma} * u \right)^T \left( \nabla G_{\sigma} * u \right)$$

- Eigenvectors w<sub>+</sub>, w<sub>-</sub>: directions of maximal and minimal variation of u
- Eigenvalues: amounts of minimal and maximal variation *u*



Slide credit: I. Kokkinos

### Edge Enhancing Diffusion

$$\frac{\partial u}{\partial t} = \nabla \cdot (D(\nabla u)\nabla u)$$

- For linear diffusion the diffusion tensor can be defined as
  D(∇u) = I with I denoting the identity matrix.
  - This results in a constant diffusion coefficient for all image points in all directions.
- For Perona-Malik type nonlinear diffusion,  $D(\nabla u) = g(|\nabla u_{\sigma}|)I$ .
  - Such a choice reduces the amount of smoothing at image edges, but in an equal amount in all directions.
- In actual anisotropic setting, the diffusion tensor *D* is defined as a function of the structure tensor *J*(∇*u*).

# Edge Enhancing Diffusion

- Proposed by Weickert (1994)
- an anisotropic nonlinear diffusion model with better edge enhancing capabilities than the Perona-Malik model
- can be described by the equation:

$$\frac{\partial u}{\partial t} = \nabla \cdot (D(\nabla u)\nabla u)$$

where

- u is the smoothed image,
- f is the input image  $(u^0(x) = f(x))$ ,
- *D* represents a matrix-valued diffusion tensor that describes the smoothing directions and the corresponding diffusivities

### Edge Enhancing Diffusion

- use the structure tensor as an image/edge descriptor to construct a diffusion tensor that
  - reduces the amount of smoothing across the edges
  - while smoothing is still carried out along the edges
- Use the same orthonormal basis of eigenvectors v<sub>1</sub> || ∇u<sub>σ</sub> and v<sub>2</sub> ⊥ ∇u<sub>σ</sub> estimated from the structure tensor J(∇u<sub>σ</sub>) with the following choice of eigenvalues satisfying

$$\frac{\lambda_1(|\nabla u_\sigma|)}{\lambda_2(|\nabla u_\sigma|)} \to 0 \quad \text{for } |\nabla u_\sigma| \to \infty$$

# Edge Enhancing Diffusion

• Suggested eigenvalues are

$$\lambda_{1}(|\nabla u_{\sigma}|) = \begin{cases} 1 & \text{if } |\nabla u_{\sigma}| = 0\\ 1 - exp\left(-\frac{3.31488}{(|\nabla u_{\sigma}|/\lambda)^{8}}\right) & \text{otherwise,} \end{cases}$$
$$\lambda_{2}(|\nabla u_{\sigma}|) = 1$$

where  $\boldsymbol{\lambda}$  denotes the contrast parameter.

- preserves and enhances edges by reducing the diffusivity  $\lambda_1$  perpendicular to edges for sufficiently large values of  $|\nabla u_{\sigma}|$ .
- Specifically, the diffusion tensor is given by the formula:

$$D = \begin{bmatrix} (u_{\sigma})_x & -(u_{\sigma})_y \\ (u_{\sigma})_y & (u_{\sigma})_x \end{bmatrix} \cdot \begin{bmatrix} \lambda_1(|\nabla u_{\sigma}|) & 0 \\ 0 & \lambda_2(|\nabla u_{\sigma}|) \end{bmatrix} \cdot \begin{bmatrix} (u_{\sigma})_x & -(u_{\sigma})_y \\ (u_{\sigma})_y & (u_{\sigma})_x \end{bmatrix}^{-1}$$

# Sample Results of Edge Enhancing Diffusion

• Smoothing process diminishes noise and fine image details while retaining and enhancing edges as in the Perona-Malik type nonlinear diffusion.



### Sample Results of Edge Enhancing Diffusion

- Corners become more rounded in the anisotropic model compared to the Perona-Malik filter. T = 0 T = 100 T = 200
- Smoothing along edges and not across them
- causes a slight shrinking effect in the image structures
- eliminates fine or thin structures





 $(\lambda ~=~ 1.8,~\sigma=1)$