BSB663
Image Processing

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Slides are adapted from
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Image matching

- Image matching is a fundamental aspect of many problems in computer vision.
  - Object or scene recognition
  - Solving for 3D structure from multiple images
  - Stereo correspondence
  - Image alignment & stitching
  - Image indexing and search
  - Motion tracking
- Find "interesting" pieces of the image.
  - Focus attention of algorithms
  - Speed up computation

Image matching applications

Object recognition: Find correspondences between feature points in training and test images.

Image matching applications

Stereo correspondence and 3D reconstruction

Image matching applications
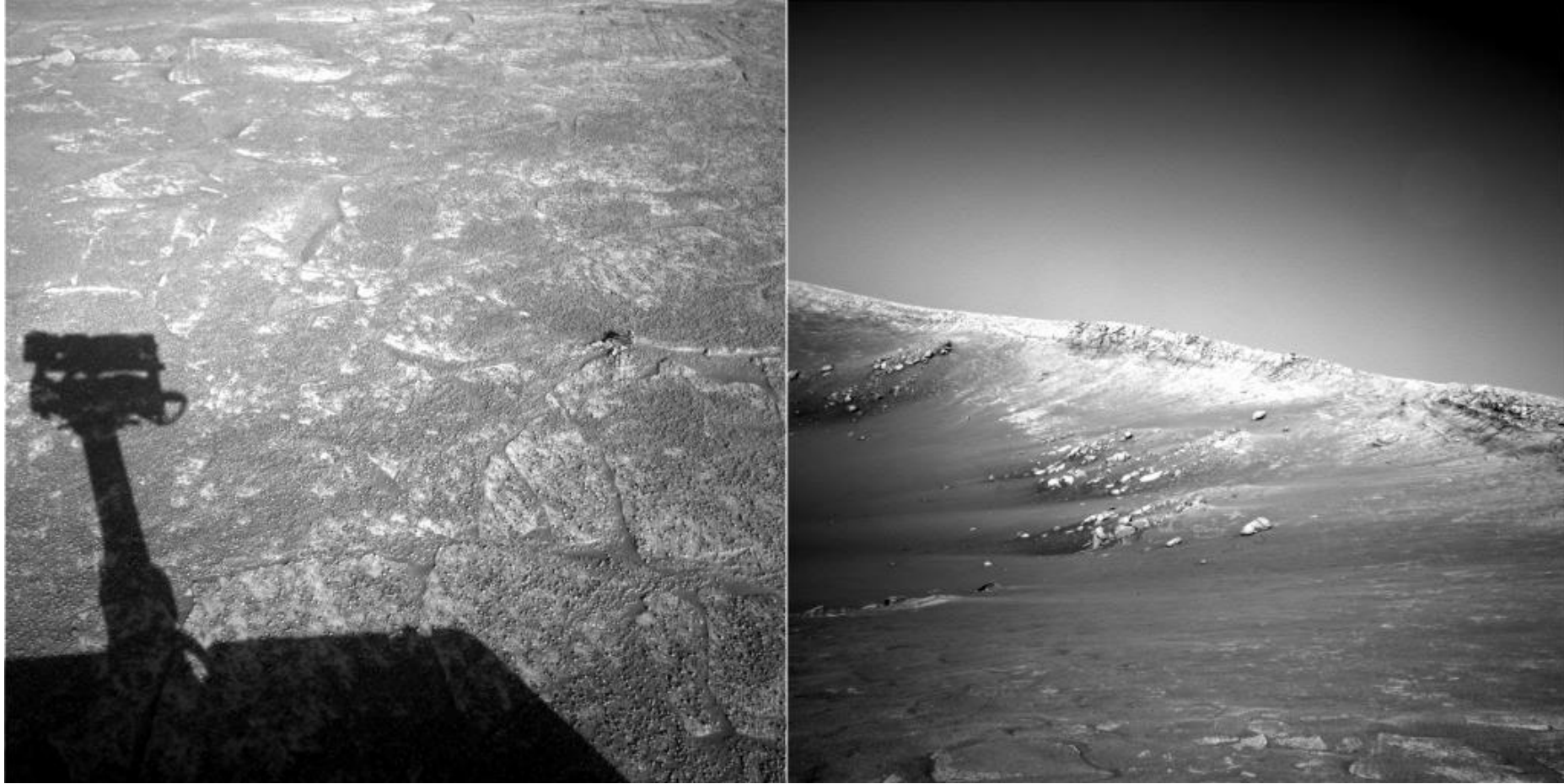

Two images of Rome from Flickr

Image matching applications
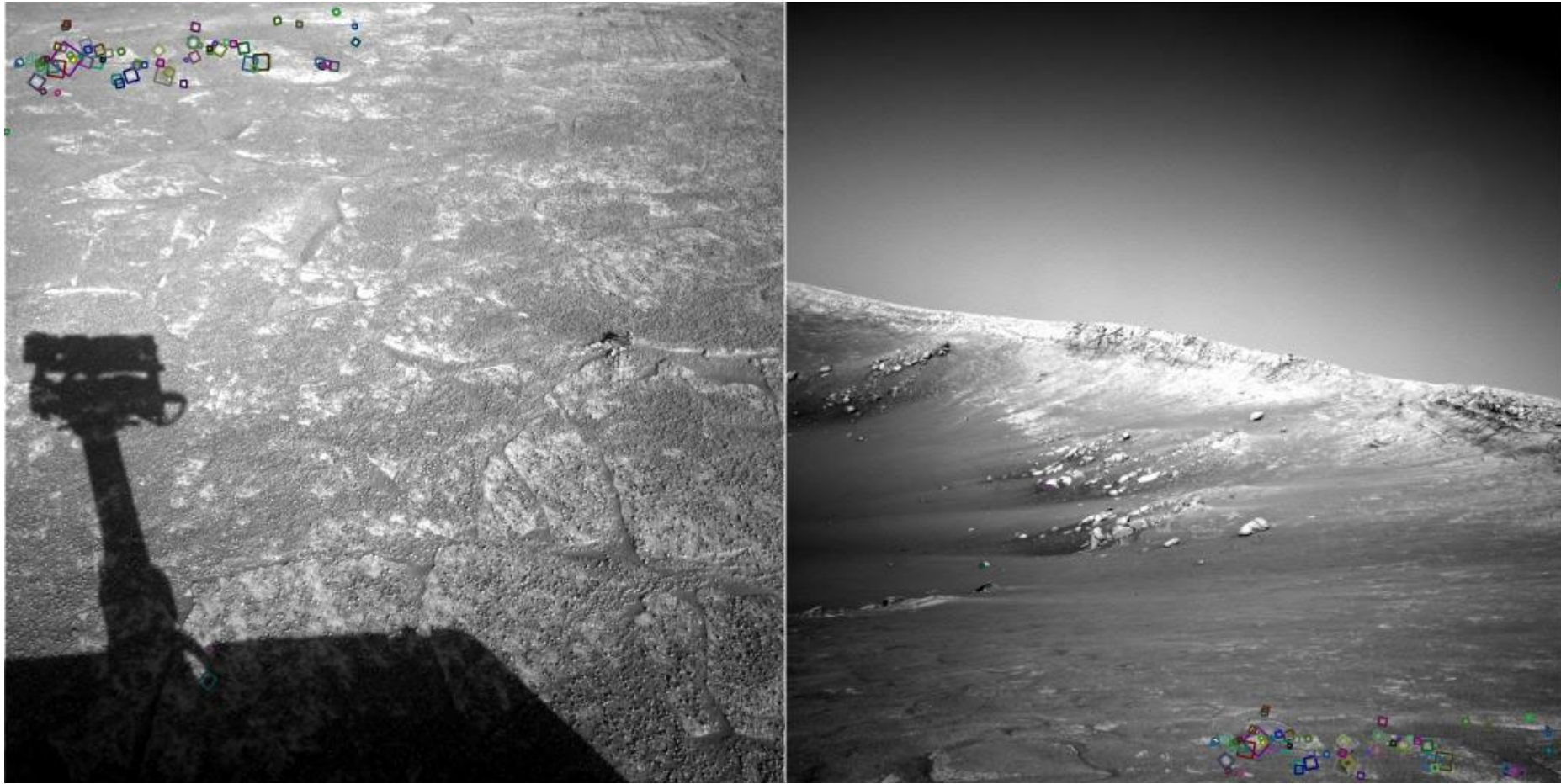

Two images of Rome from Flickr: harder case

Image matching applications

Two images from NASA Mars Rover: even harder case
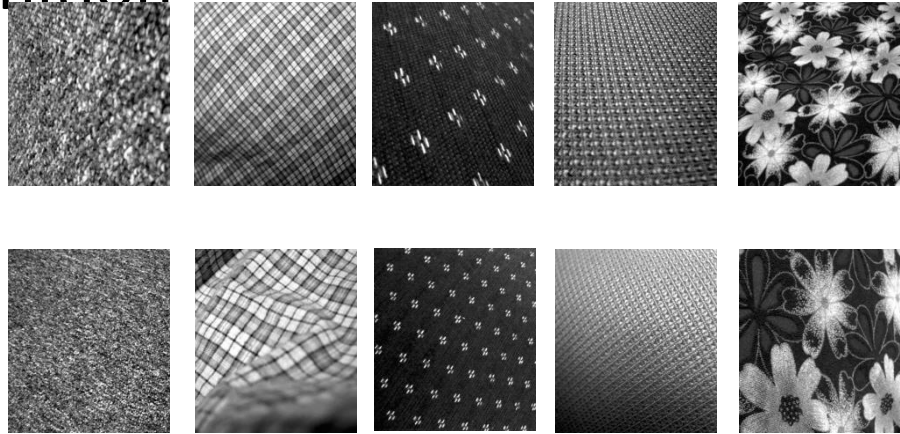
Image matching applications

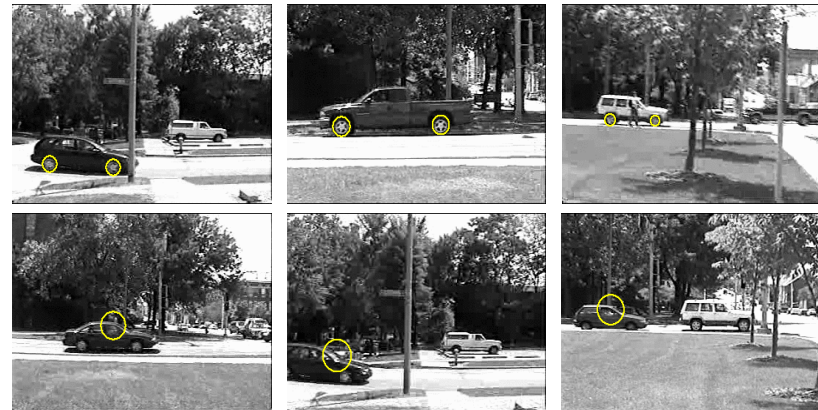Two images from NASA Mars Rover: matching using local features

Image matching applications

Recognition


Texture recognition

Car detection

Advantages of local features

- Locality
  - features are local, so robust to occlusion and clutter
- Distinctiveness
  - can differentiate a large database of objects
- Quantity
  - hundreds or thousands in a single image
- Efficiency
  - real-time performance achievable
- Generality
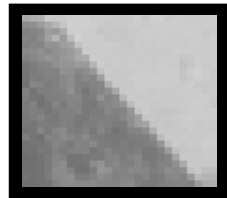 - exploit different types of features in different situations

Local features

- What makes a good feature?

- We want **uniqueness**.
    - Look for image regions that are **unusual**.
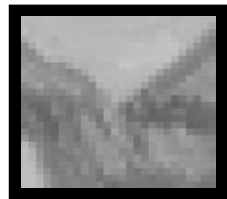   - Lead to **unambiguous** matches in other images.

- How to define ~~"unusual"~~?
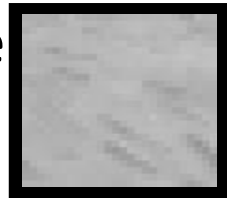
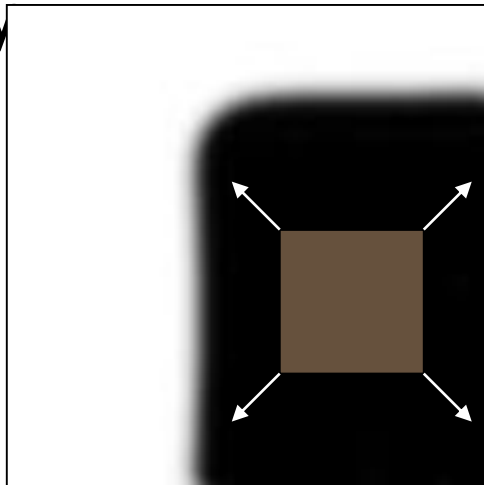**0D** structure
not useful for matching

1D structure
edge, can be localized in 1D,
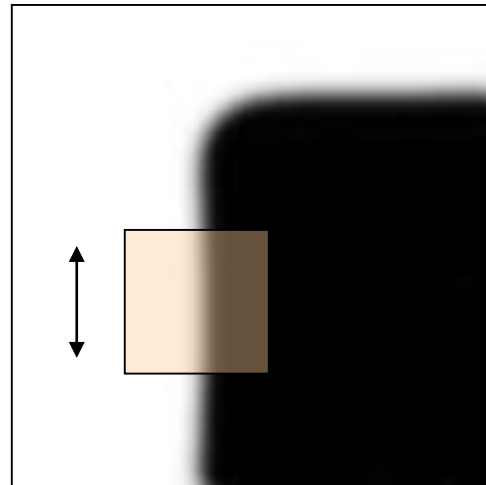subject to the aperture problem

2D structure
corner, can be localized in 2D,
good for matching
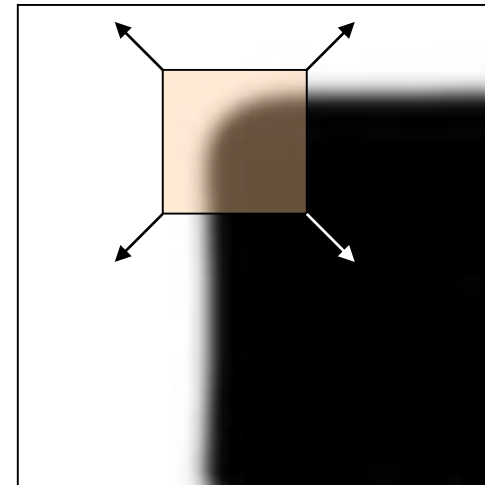
Local measures of uniqueness

- We should easily recognize the local feature by looking through a small window.

- Shifting the window in *any direction* should give a *large change* in intensity

"flat" region:
no change in all
directions

"edge":
no change along the
edge direction

"corner":
significant change in
all directions

Local features and image matching

- There are three important requirements for feature points to have a better correspondence for matching:
  - Points corresponding to the same scene points should be detected consistently over different views.
  - They should be invariant to image scaling, rotation and to change in illumination and 3D camera viewpoint.
  - There should be enough information in the neighborhood of the points so that corresponding points can be automatically matched.
- These points are also called interest points.

Overview of the approach

interest points

local descriptor

1. Extraction of interest points (characteristic locations).
2. Computation of local descriptors.
3. Determining correspondences.
4. Using these correspondences for matching/recognition/etc.
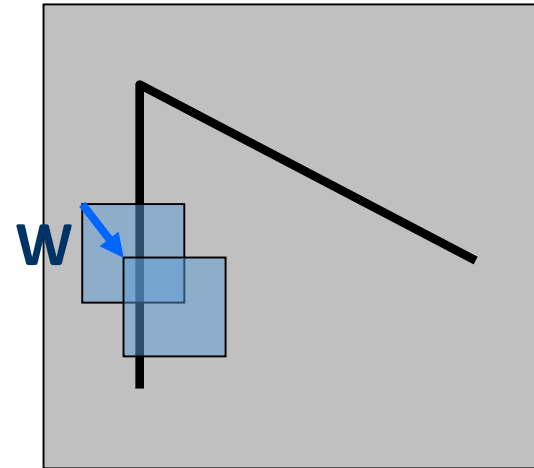
Local features: detection

- We will now talk about one particular feature detection algorithm.
- Idea: find regions that are dissimilar to its neighbors.
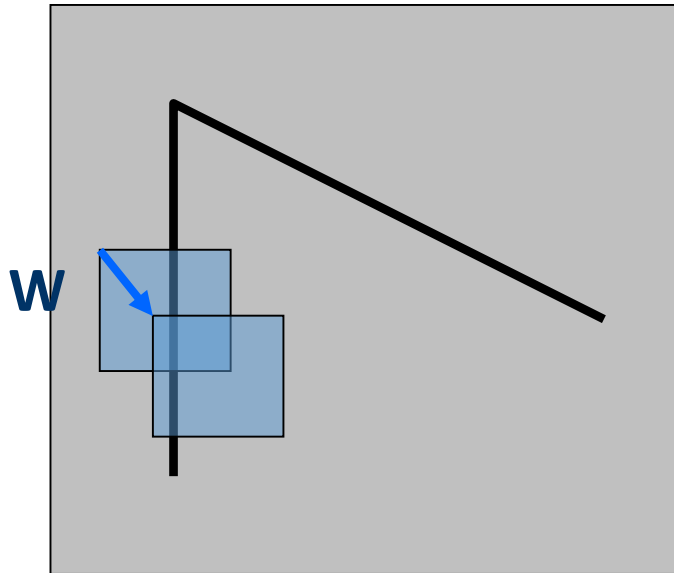
Local features: detection

- Consider shifting the window W by (u,v):
  - How do the pixels in W change?
  - Auto-correlation function measures the self similarity of a signal and is related to the sum-of-squared difference.
  - Compare each pixel before and after the shift by summing up the squared differences (SSD).
  - This defines an SSD "error" of E(u,v):

$$E(u, v) = \sum_{(x,y) \in W} [I(x + u, y + v) - I(x, y)]^2$$

W

Local features: detection

- Taylor Series expansion of I:

$$I(x+u, y+v) = I(x, y) + \frac{\partial I}{\partial x}u + \frac{\partial I}{\partial y}v + \text{higher order terms}$$

- If the motion (u,v) is assumed to be small, then first order approximation is good.

$$I(x + u, y + v) \approx I(x, y) + \frac{\partial I}{\partial x}u + \frac{\partial I}{\partial y}v$$

$$\approx I(x, y) + [I_x \ I_y]\begin{bmatrix} u \\ v \end{bmatrix}$$

shorthand: $I_x = \frac{\partial I}{\partial x}$

- Plugging this into the formula on the previous slide…

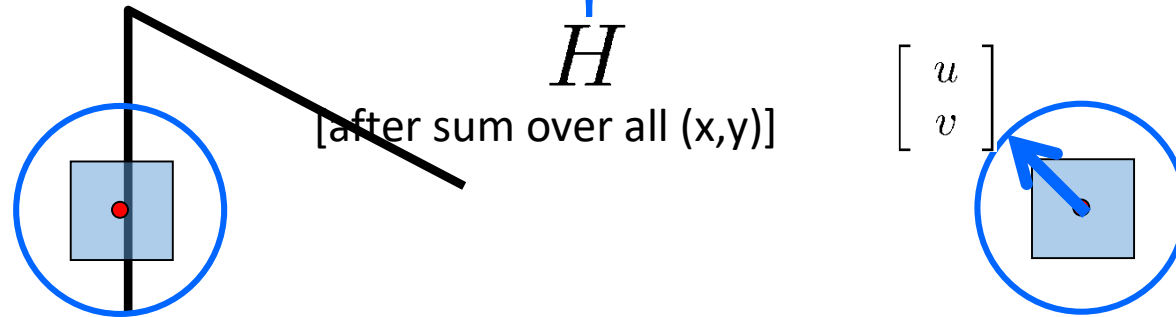# Local features: detection

- Sum-of-squared differences error E(u,v):

$$E(u,v) = \sum_{(x,y)\in W} [I(x+u, y+v) - I(x,y)]^2$$

$$\approx \sum_{(x,y)\in W} [I(x,y) + [I_x \; I_y]\begin{bmatrix} u \\ v \end{bmatrix} - I(x,y)]^2$$

$$\approx \sum_{(x,y)\in W} \left[[I_x \; I_y]\begin{bmatrix} u \\ v \end{bmatrix}\right]^2$$

Local features: detection

- This can be $E(u, v) = \sum_{(x,y) \in W} [u \ v] \begin{bmatrix} I_x^2 & I_x I_y \\ I_y I_x & I_y^2 \end{bmatrix} \begin{bmatrix} u \\ v \end{bmatrix}$

$\underbrace{\qquad\qquad}_{H}$ [after sum over all (x,y)]

$\begin{bmatrix} u \\ v \end{bmatrix}$

- For the example above:
  - You can move the center of the green window to anywhere on the blue unit circle.
  - Which directions will result in the largest and smallest E values?

Local features: detection

- We want to find (u,v) such that E(u,v) is maximized or minimized:

$$E(u, v) = \begin{bmatrix} u \\ v \end{bmatrix}^T \mathbf{H} \begin{bmatrix} u \\ v \end{bmatrix}$$

- By definition, we can find these directions by looking at the eigenvectors of **H**.

- First eigenvector of **H** is a unit vector that maximizes E(u,v).

- Second eigenvector of **H** is a unit vector that minimizes E(u,v).

Quick eigenvector/eigenvalue review

- Re **THEOREM 2.5** If A and B are symmetric and $B > 0$, then the maximum of $x^\top A x$ under the constraints

$x^\top B x = 1$ is given by the largest eigenvalue of $B^{-1}A$. More generally,

$$\max_{\{x:x^\top B x=1\}} x^\top A x = \lambda_1 \geq \lambda_2 \geq \cdots \geq \lambda_p = \min_{\{x:x^\top B x=1\}} x^\top A x,$$

where $\lambda_1, \ldots, \lambda_p$ denote the eigenvalues of $B^{-1}A$. The vector which maximizes (minimizes) $x^\top A x$ under

the constraint $x^\top B x = 1$ is the eigenvector of $B^{-1}A$ which corresponds to the largest (smallest) eigenvalue

of $B^{-1}A$.

Quick eigenvector/eigenvalue review

- The eigenvectors of a matrix **A** are the vectors **x** that satisfy:

$$Ax = \lambda x$$

- The scalar λ is the eigenvalue corresponding to **x**
  - The eigenvalues are found by solving:

$$det(A - \lambda I) = 0$$

  - In our case, **A** = **H** is a 2x2 matrix. so we have

$$det \begin{bmatrix} h_{11} - \lambda & h_{12} \\ h_{21} & h_{22} - \lambda \end{bmatrix} = 0$$
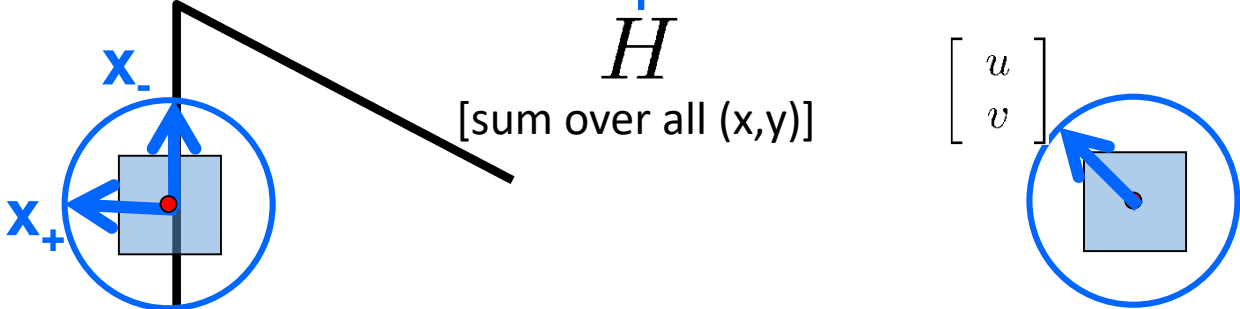
  - The solution:

$$\lambda_{\pm} = \frac{1}{2} \left[(h_{11} + h_{22}) \pm \sqrt{4h_{12}h_{21} + (h_{11} - h_{22})^2} \right]$$

- Once you know λ, you find **x** by solving

$$\begin{bmatrix} h_{11} - \lambda & h_{12} \\ h_{21} & h_{22} - \lambda \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = 0$$

Local features: detection

- This can be rewritten:

$$E(u,v) = \sum_{(x,y) \in W} [u \; v] \begin{bmatrix} I_x^2 & I_x I_y \\ I_y I_x & I_y^2 \end{bmatrix} \begin{bmatrix} u \\ v \end{bmatrix}$$

$$\underbrace{\quad\quad}_{H}$$

H

[sum over all (x,y)]

$\begin{bmatrix} u \\ v \end{bmatrix}$

x$_-$

x$_+$

- Eigenvalues and eigenvectors of **H**:
  - Define shifts with the smallest and largest change (E value).
  - x$_+$ = direction of largest increase in E.
  - λ_+ = amount of increase in direction x$_+$.
  - x$_-$ = direction of smallest increase in E.
  - λ_- = amount of increase in direction x$_-$.

$$Hx_+ = \lambda_+ x_+$$
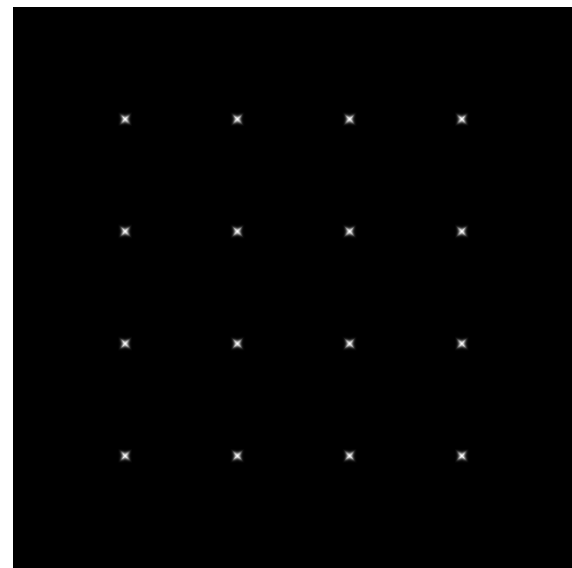$$Hx_- = \lambda_- x_-$$

Local features: detection

- How are λ_+, x_+, λ_-, and x_- relevant for feature detection?
  - What's our feature scoring function?
- Want E(u,v) to be large for small shifts in all directions.
  - The minimum of E(u,v) should be large, over all unit vectors [u v].
  - This minimum is given by the smaller eigenvalue (λ_-) of H.
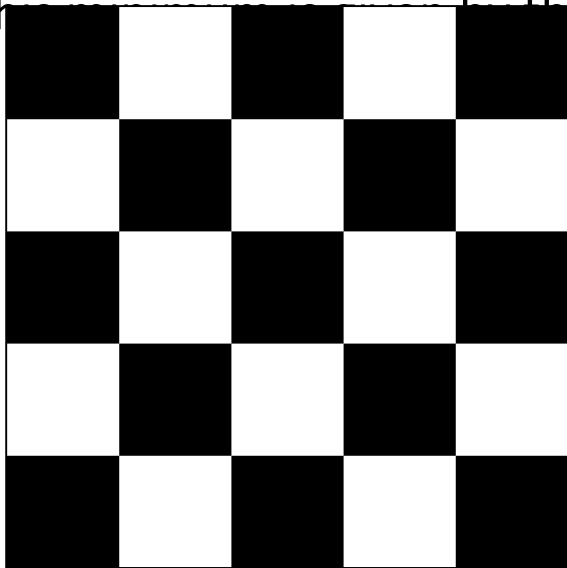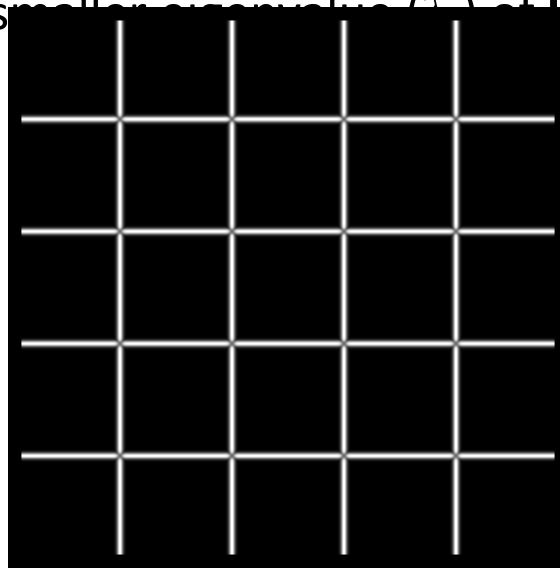
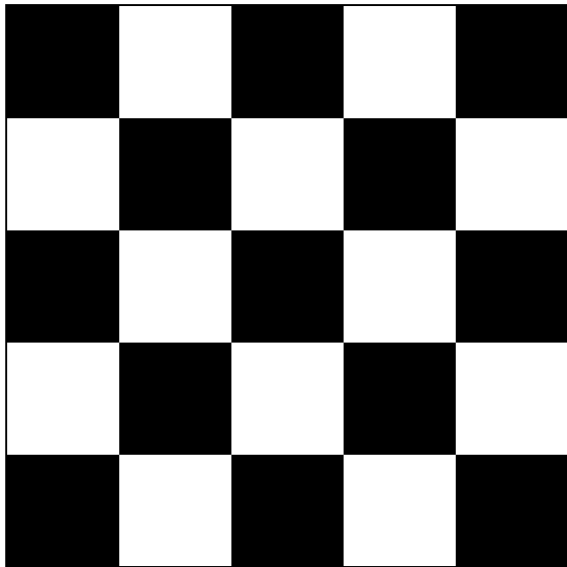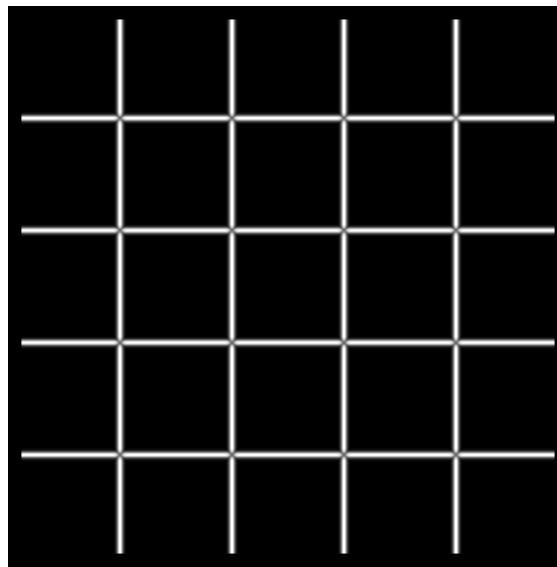I λ_+ λ_-

Local features: detection
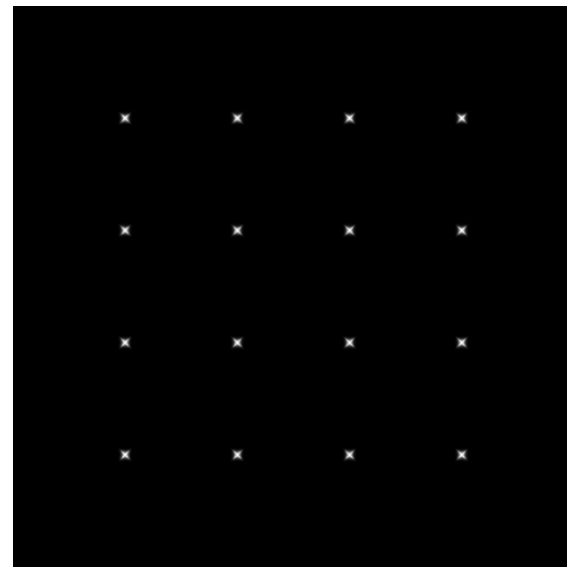
- Here's what you do:
  - Compute the gradient at each point in the image.
  - Create the **H** matrix from the entries in the gradient.
  - Compute the eigenvalues.
  - Find points with large response ($\lambda_- >$ threshold).
  - Choose those points where λ_- is a local maximum as features.

$$I \qquad \lambda_+ \qquad \lambda_-$$

Local features: detection

- Here's what you do:
    - Compute the gradient at each point in the image.
    - Create the **H** matrix from the entries in the gradient.
    - Compute the eigenvalues.
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    - Choose those points where λ_- is a local maximum as features.

$$\lambda_-$$
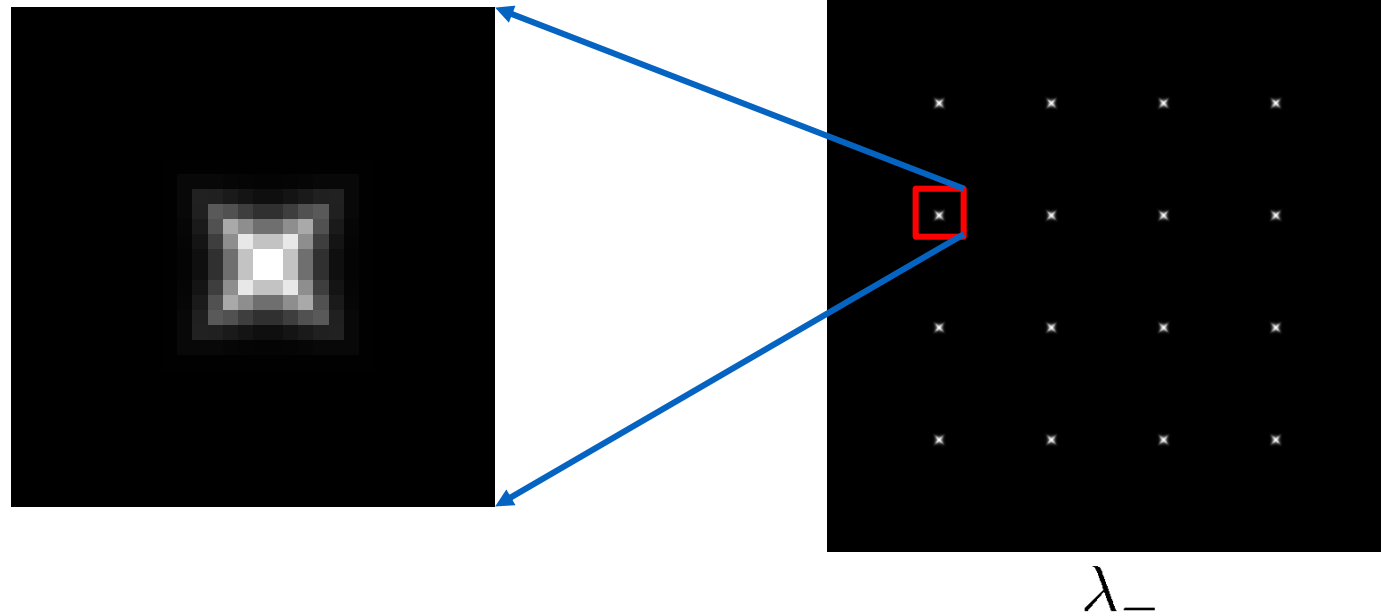
Harris detector

- To measure the corner strength:

    $R = \det(H) - k(\text{trace}(H))^2$

    where

    $\text{trace}(H) = \lambda_1 + \lambda_2$

    $\det(H) = \lambda_1 \times \lambda_2$

    (λ_1 and λ_2 are the eigenvalues of H).
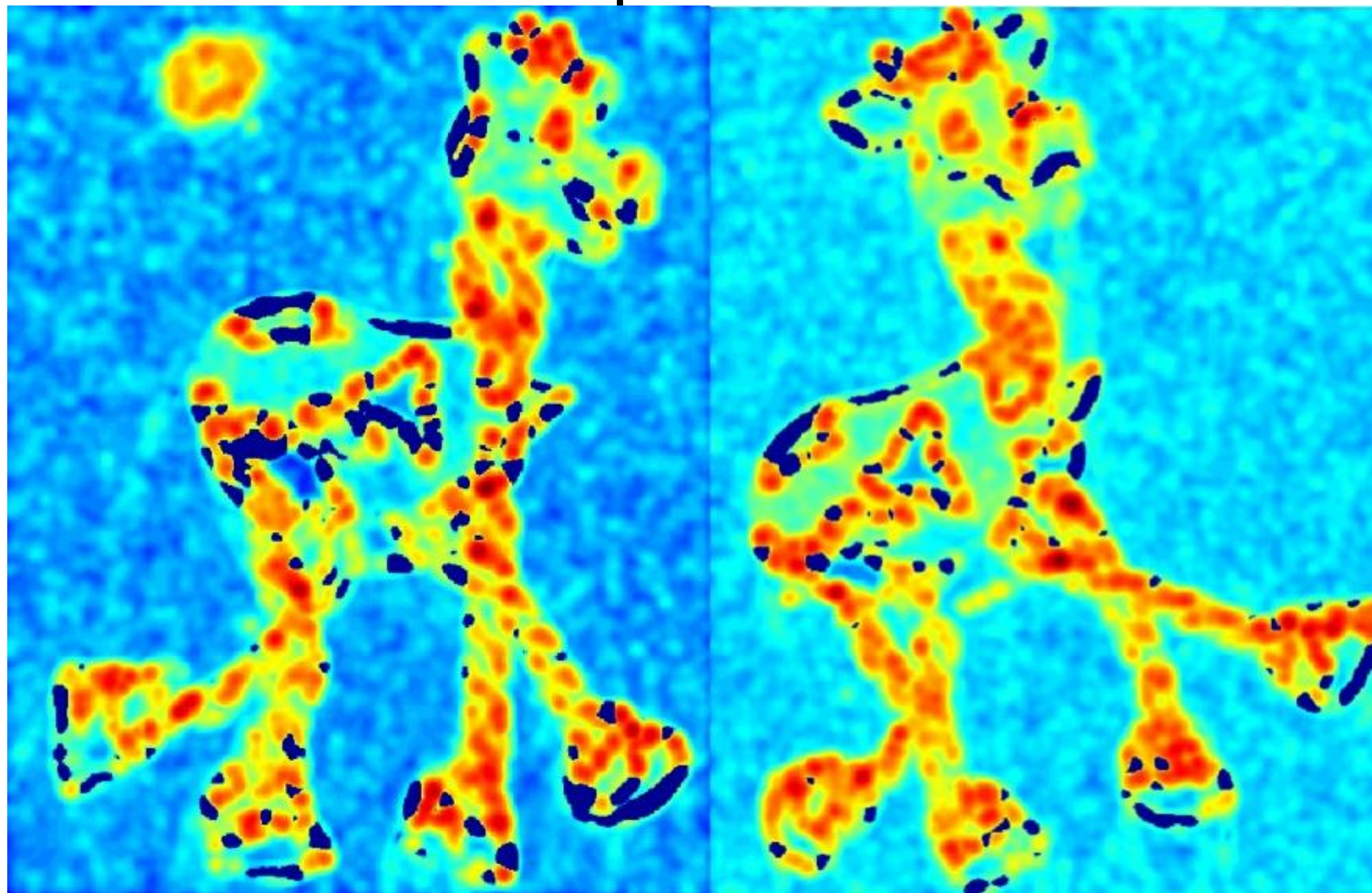
- R is positive for corners, negative in edge regions, and small in flat regions.

- Very similar to λ_- but less expensive (no square root).

- Also called the "Harris Corner Detector" or "Harris Operator".

- Lots of other detectors, this is one of the most popular.
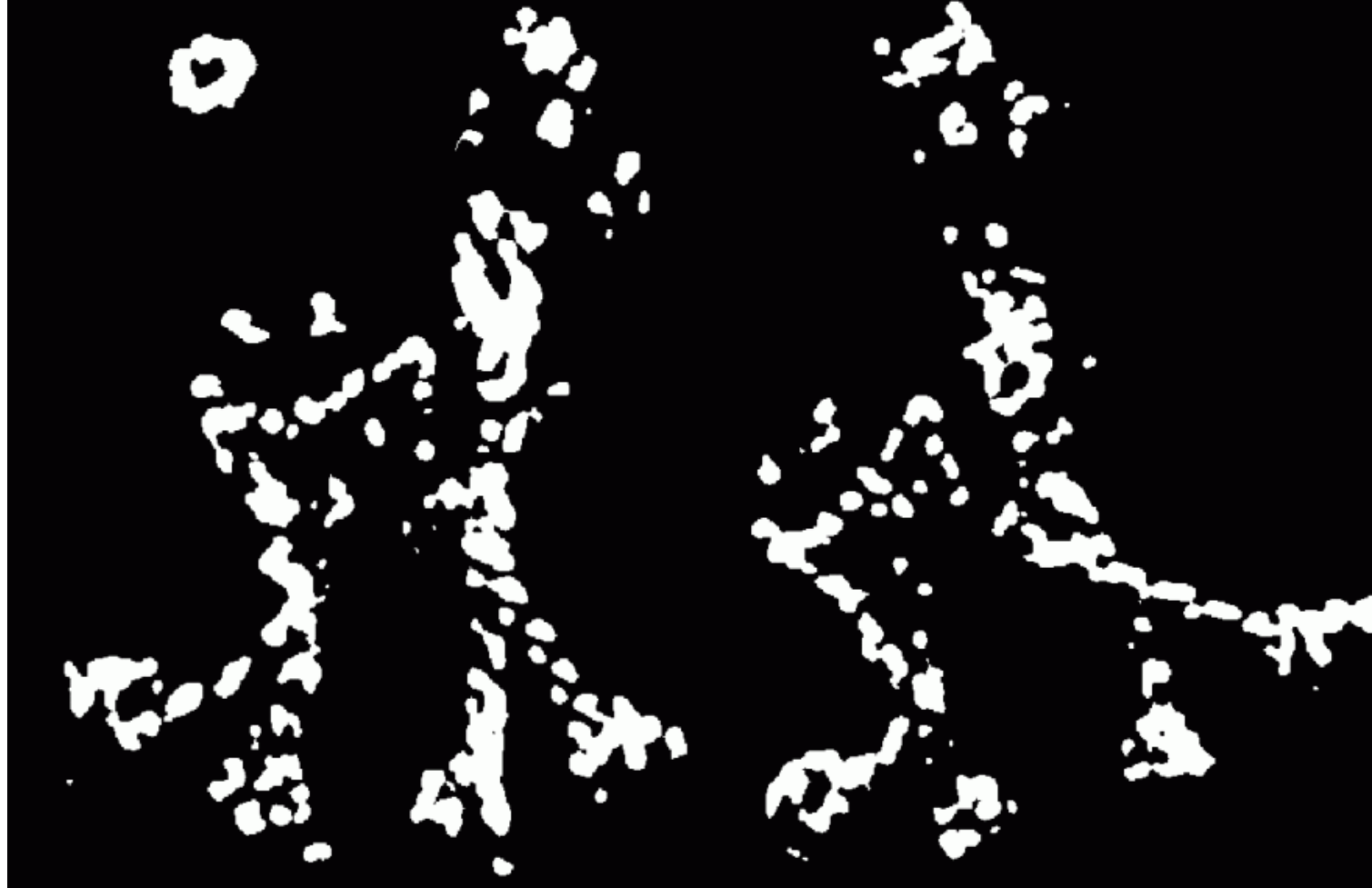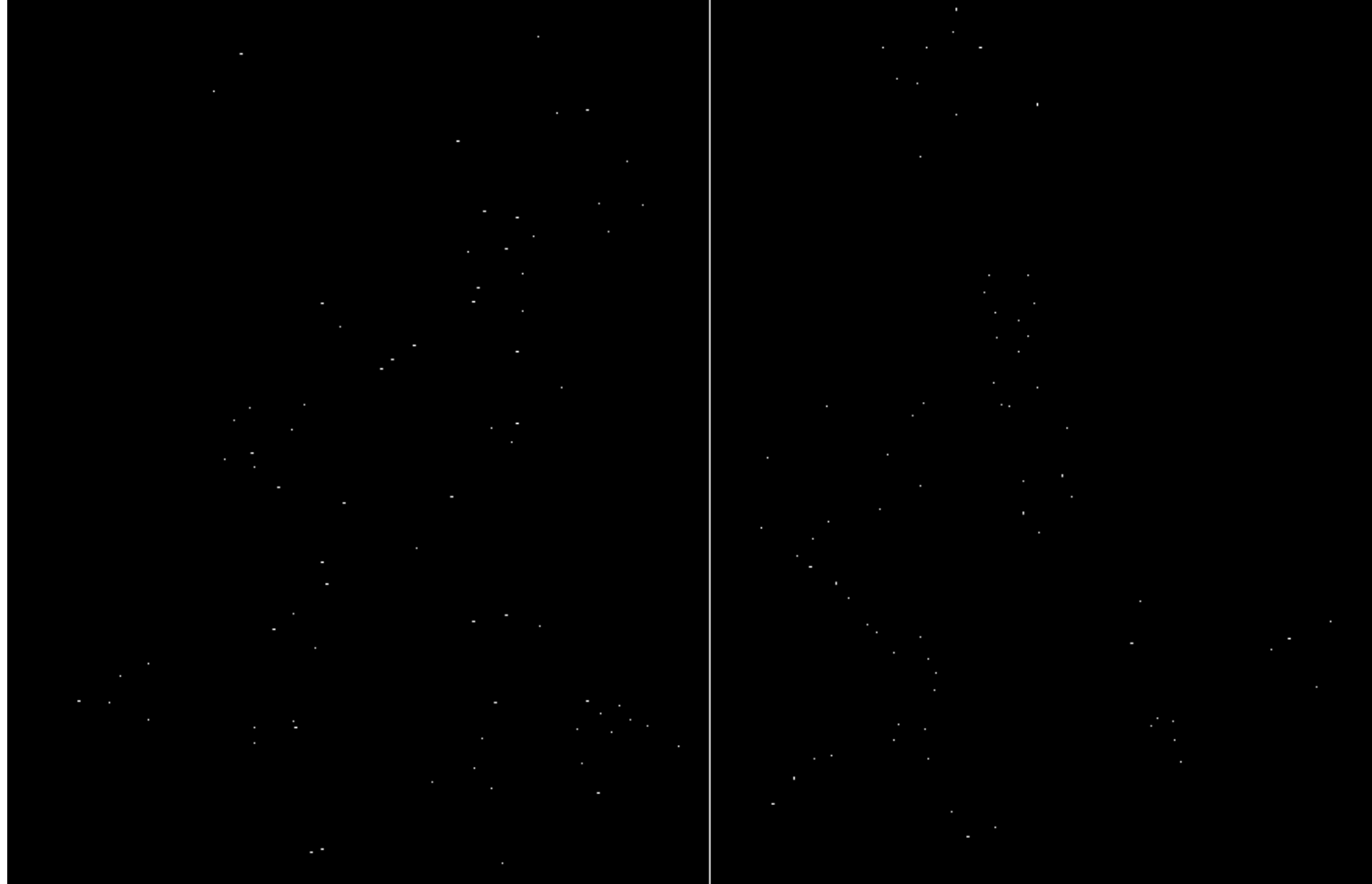
Harris detector example

Harris detector example

R values (red high, blue low)

Harris detector example

Threshold (R > value)

Harris detector example

Local maxima of R

Harris detector example

Harris features (red)
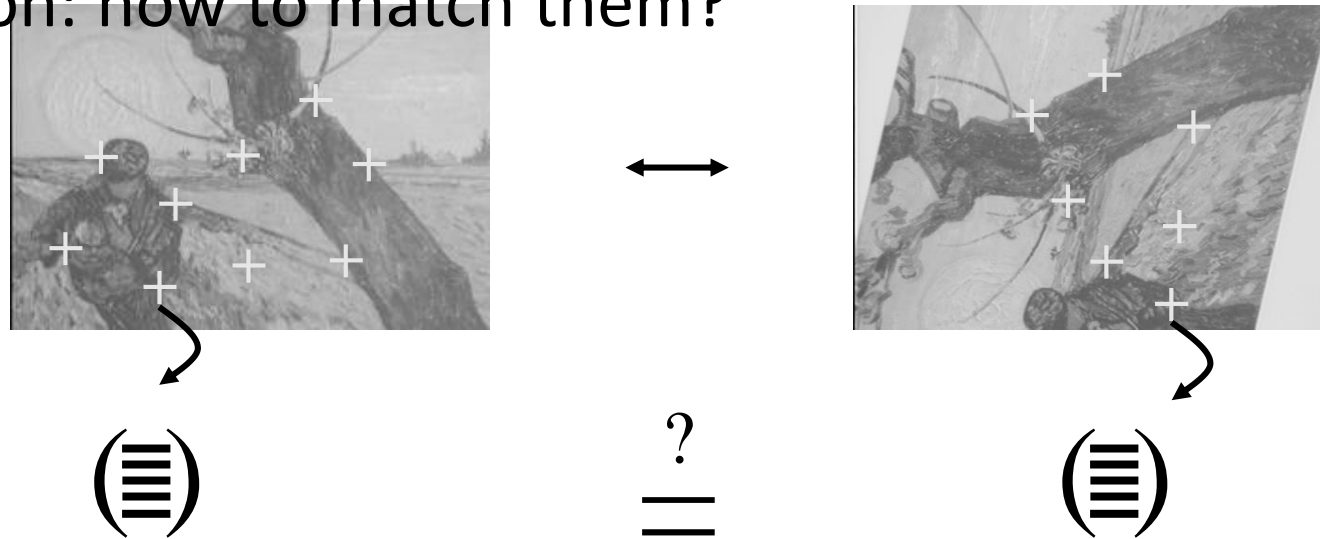
Local features: descriptors

local descriptor

- Describe points so that they can be compared.
- Descriptors characterize the local neighborhood of a point.

Local features: matching

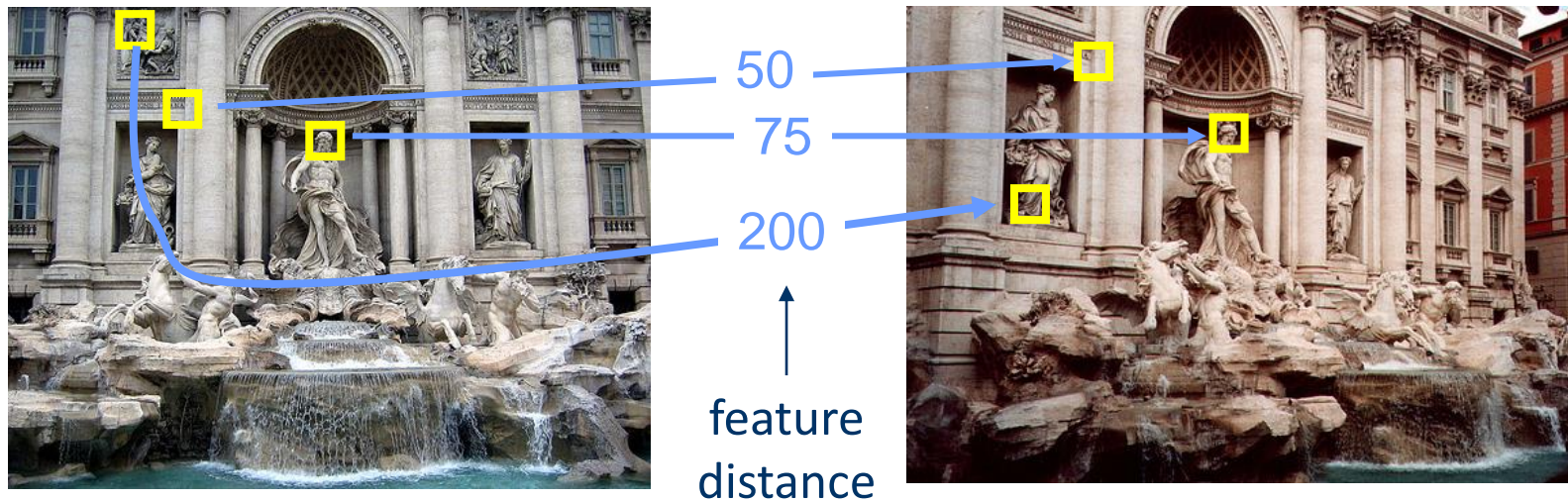- We know how to detect good features.
- Next question: how to match them?

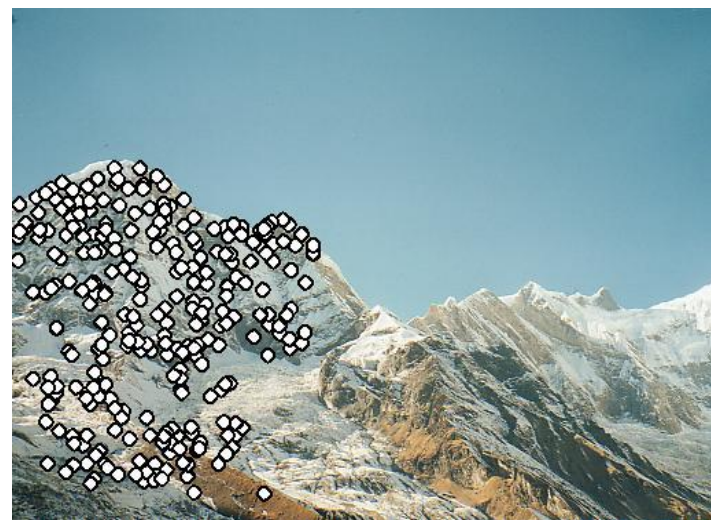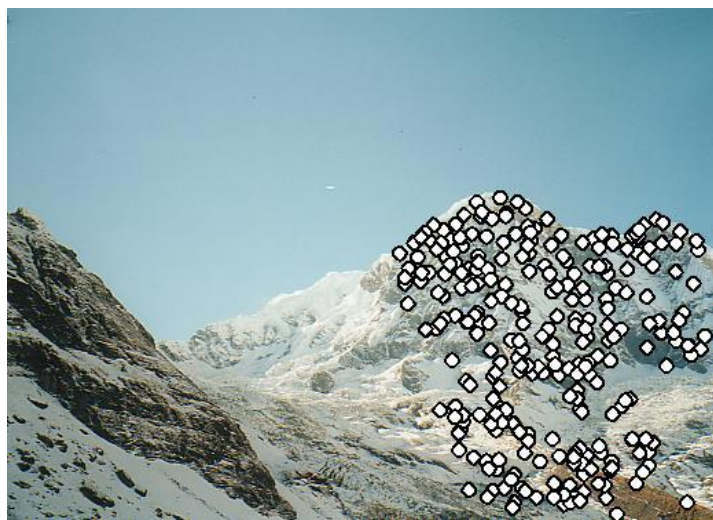- Vector comparison using a distance measure can be used.

Local features: matching

- Given a feature in I_1, how to find the best match in I_2?
    1. Define a distance function that compares two descriptors.
    2. Test all the features in I_2, find the one with minimum distance.

50

75

200

feature distance
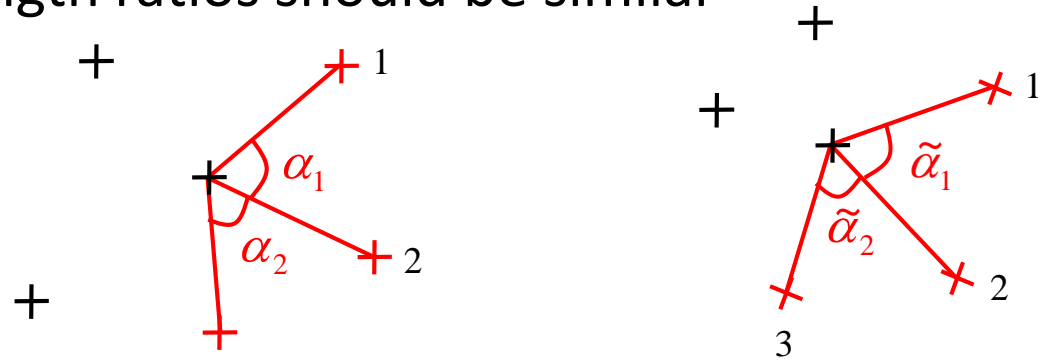
Matching examples

Matching examples

Local features: matching

- Matches can be improved using local constraints
  - neighboring points should match
  - angles, length ratios should be similar

Summary of the approach

- Detection of interest points/regions
  - Harris detector
  - Blob detector based on Laplacian
- Computation of descriptors for each point
  - Gray value patch, differential invariants, steerable filter, SIFT descriptor
- Similarity of descriptors
  - Correlation, Mahalanobis distance, Euclidean distance
- Semi-local constraints
  - Geometrical or statistical relations between neighborhood points
- Global verification
  - Robust estimation of geometry between images

Local features: invariance

- Suppose you rotate the image by some angle.
  - Will you still pick up the same features?
- What if you change the brightness?
- What about scale?
- We'd like to find the same features regardless of the transformation.
  - This is called transformational invariance.
  - Most feature methods are designed to be invariant to
    - Translation, 2D rotation, scale.
  - They can usually also handle
    - Limited 3D rotations.
    - Limited affine transformations (some are fully affine invariant).
    - Limited illumination/contrast changes.

How to achieve invariance?

Need both of the following:

1. Make sure your detector is invariant.
   - Harris is invariant to translation and rotation.
   - Scale is trickier.
     - Common approach is to detect features at many scales using a Gaussian pyramid (e.g., MOPS).
     - More sophisticated methods find "the best scale" to represent each feature (e.g., SIFT).

2. Design an invariant feature descriptor.
   - A descriptor captures the information in a region around the detected feature point.
   - The simplest descriptor: a square window of pixels.
   - Let's look at some better approaches…

Rotation invariance for descriptors

- Find dominant orientation of the image patch.
  - This is given by $\mathbf{x}_+$, the eigenvector of $\mathbf{H}$ corresponding to λ_+ (larger eigenvalue).
 - Rotate the patch according to this angle

Multi-scale Oriented Patches (MOPS)

- Take 40x40 square window around detected feature.
  - Scale to 1/5 size (using prefiltering).
  - Rotate to horizontal.
  - Sample 8x8 square window centered at feature.
  - Intensity normalize the window by subtracting the mean, dividing by the standard deviation in the window.
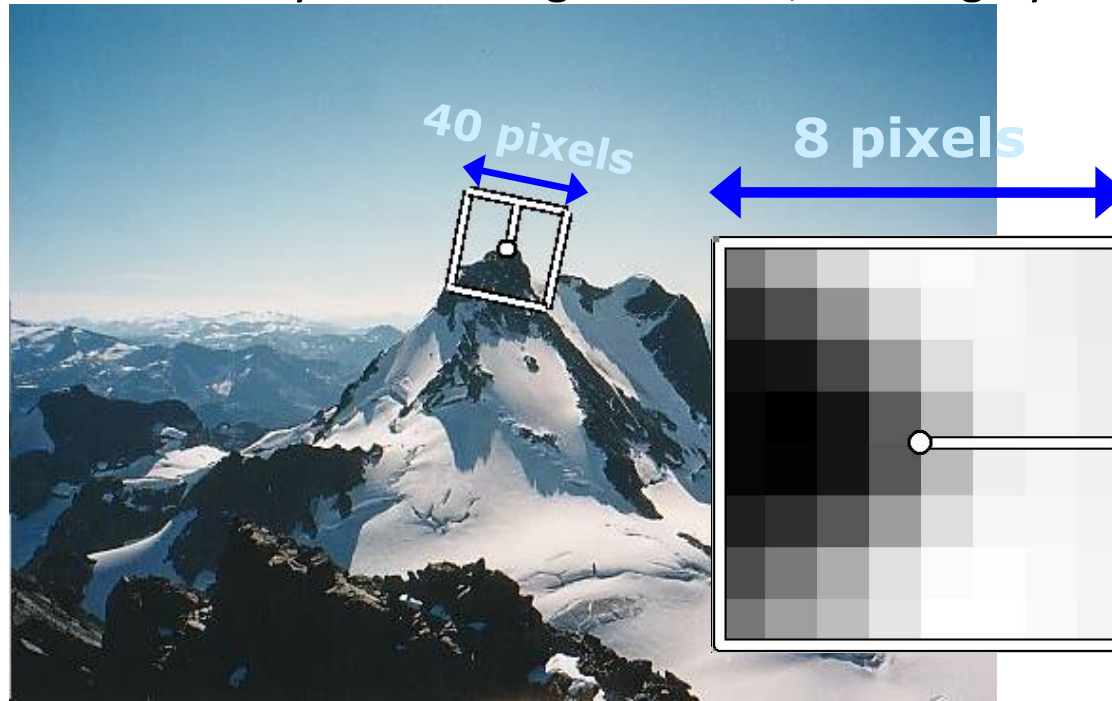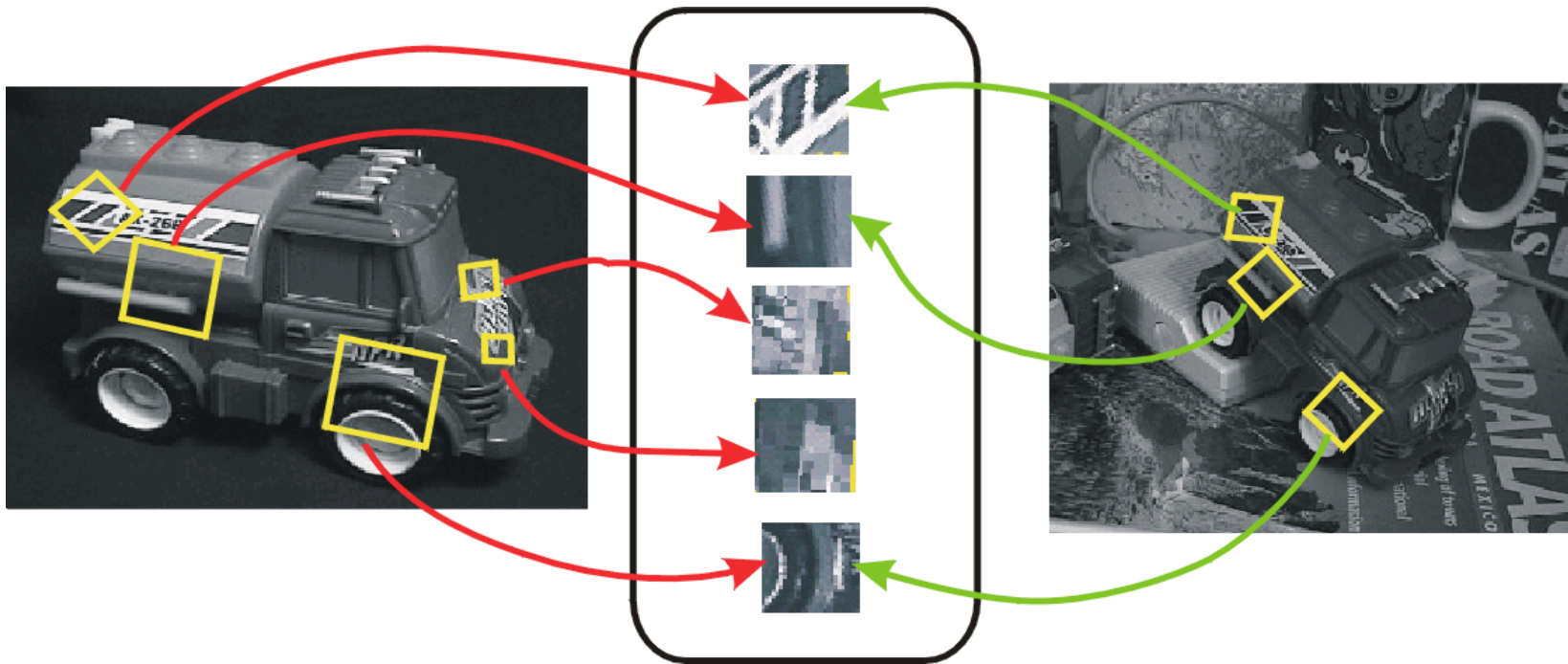
Multi-scale Oriented Patches (MOPS)

• Extract oriented patches at multiple scales of the Gaussian pyramid.
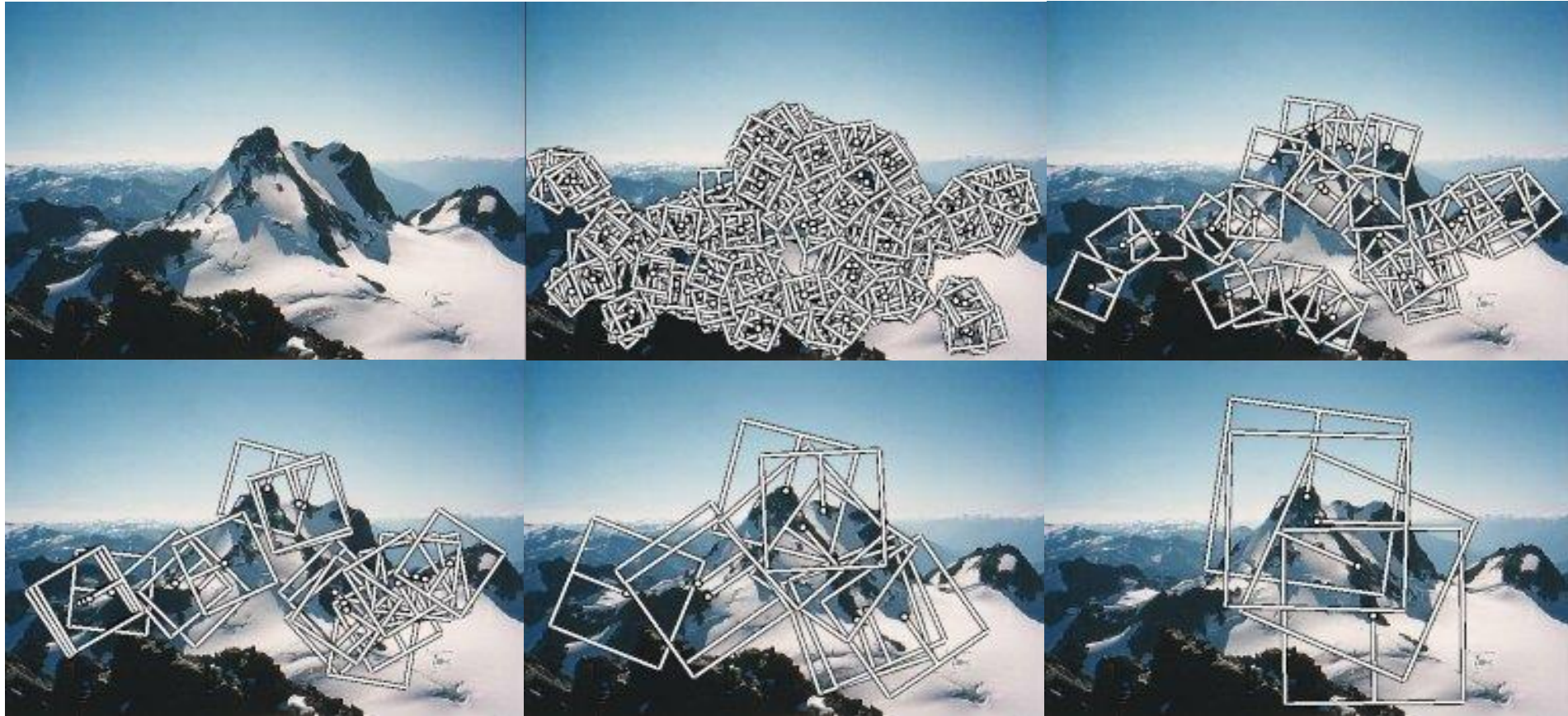
Scale Invariant Feature Transform (SIFT)

- The SIFT operator developed by David Lowe is both a detector and a descriptor that are invariant to translation, rotation, scale, and other imaging parameters.

Overall approach for SIFT

1. **Scale space extrema detection**

   - Search over multiple scales and image locations.

2. **Interest point localization**

   - Fit a model to determine location and scale.
   - Select interest points based on a measure of stability.

3. **Orientation assignment**

   - Compute best orientation(s) for each interest point region.

4. **Interest point description**

   - Use local image gradients at selected scale and rotation to describe each interest point region.

Scale space extrema detection

- Goal: Identify locations and scales that can be repeatably assigned under different views of the same scene or object.

- Method: search for stable features across multiple scales using a continuous function of scale.

- Prior work has shown that under a variety of assumptions, the best function is a Gaussian function.

- The scale space of an image is a function $L(x,y,\sigma)$ that is produced from the convolution of a Gaussian kernel (at different scales) with the input image.

Scale space interest points

- Laplacian of Gaussian (LoG) kernel

$$G(x, y, \sigma) = \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{1}{2}\frac{x^2+y^2}{\sigma^2}}$$

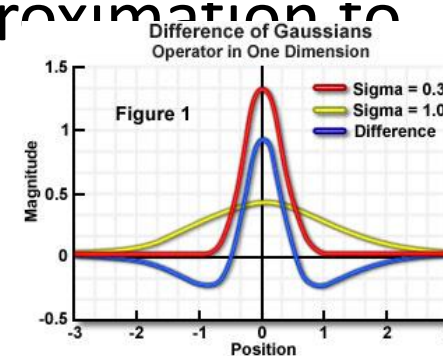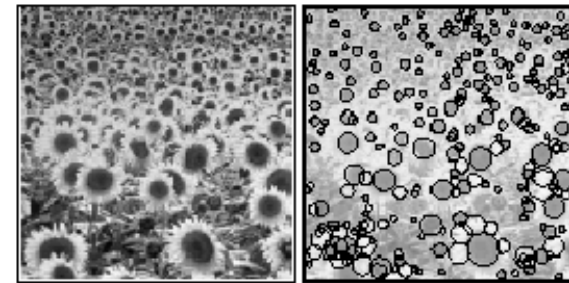$$\nabla^2 G(x, y, \sigma) = \frac{\partial^2 G}{\partial x^2} + \frac{\partial^2 G}{\partial y^2}$$
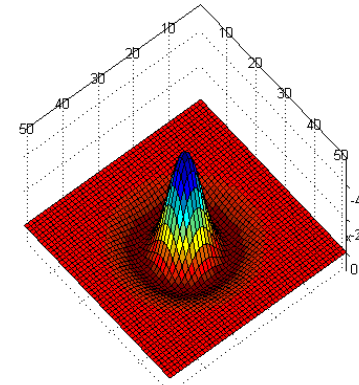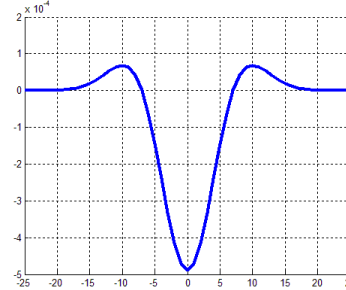
- Scale space detection
  - Find local maxima across scale-space

$$L(x, y, \sigma) = G(x, y, \sigma) * I(x, y)$$

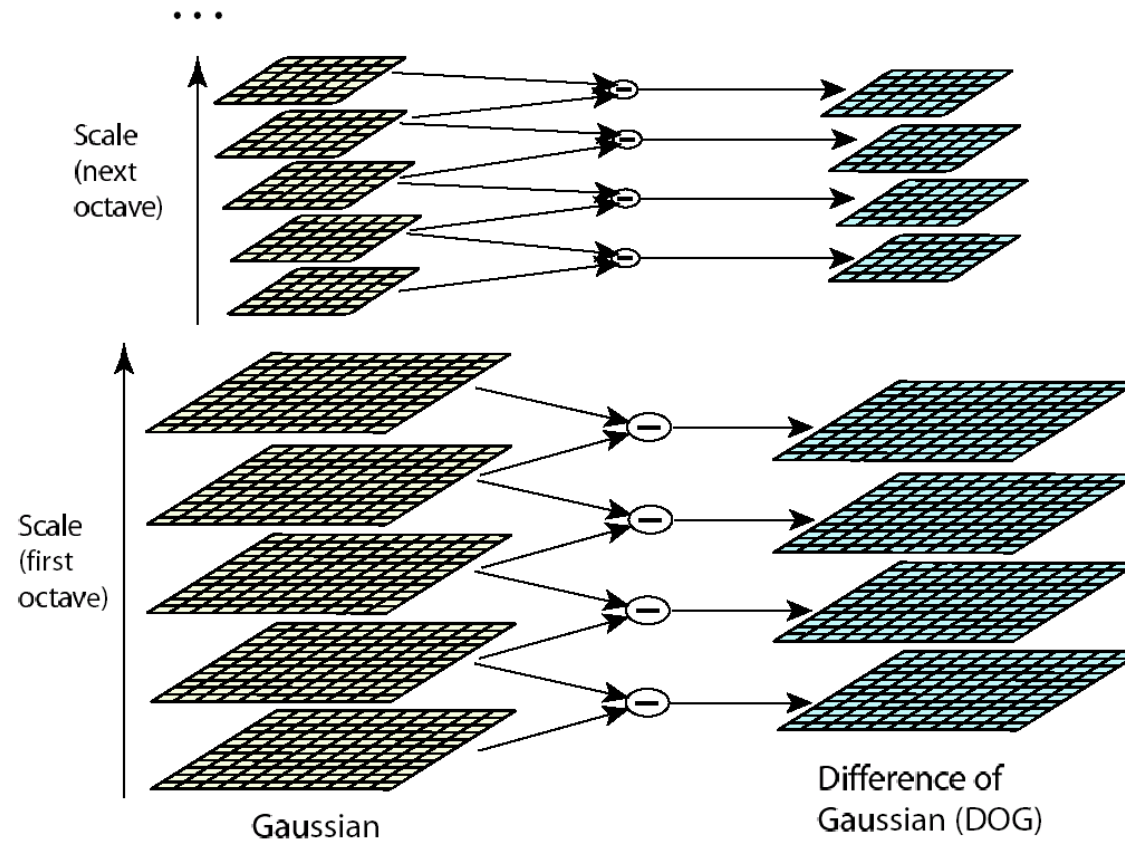- Difference of Gaussian kernel is a close approximation to scale-normalized LoG.

$$
\begin{aligned}
D(x, y, \sigma) &= (G(x, y, k\sigma) - G(x, y, \sigma)) * I(x, y) \\
&= L(x, y, k\sigma) - L(x, y, \sigma).
\end{aligned}
$$

Lowe's pyramid scheme

Scale (next octave)

Scale (first octave)

Gaussian

Difference of Gaussian (DOG)

For each octave of scale space, the initial image is repeatedly convolved with Gaussian to produce the set of scale space images (left). Adjacent Gaussian images are subtracted to produce difference of Gaussian images (right). After each octave Gaussian image is downsampled by a factor of 2.
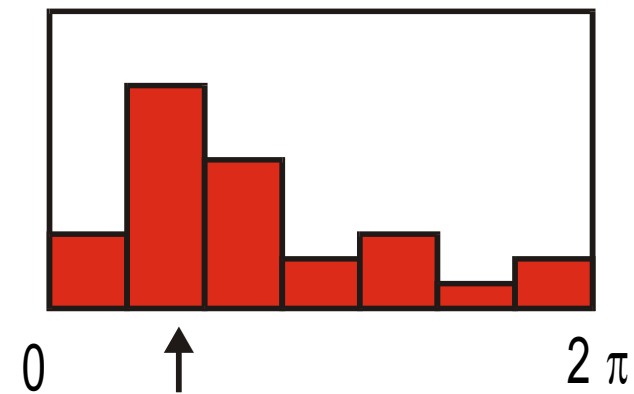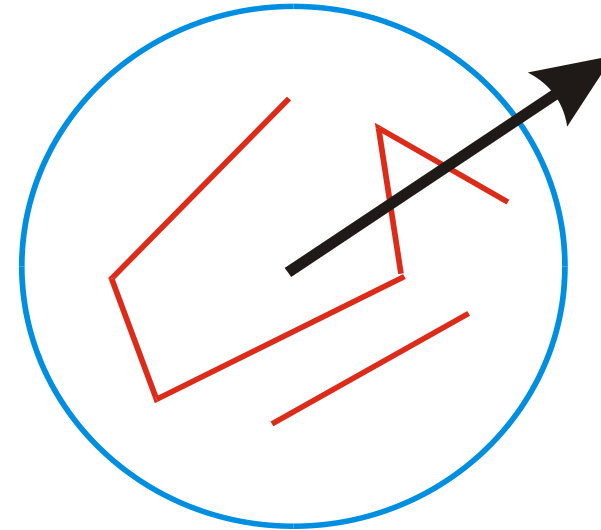
Interest point localization

- Detect maxima and minima of difference of Gaussian in scale space.

- Each point is compared to its 8 neighbors in the current image and 9 neighbors each in the scales above and below.

- Select only if it is greater or smaller than all the others.
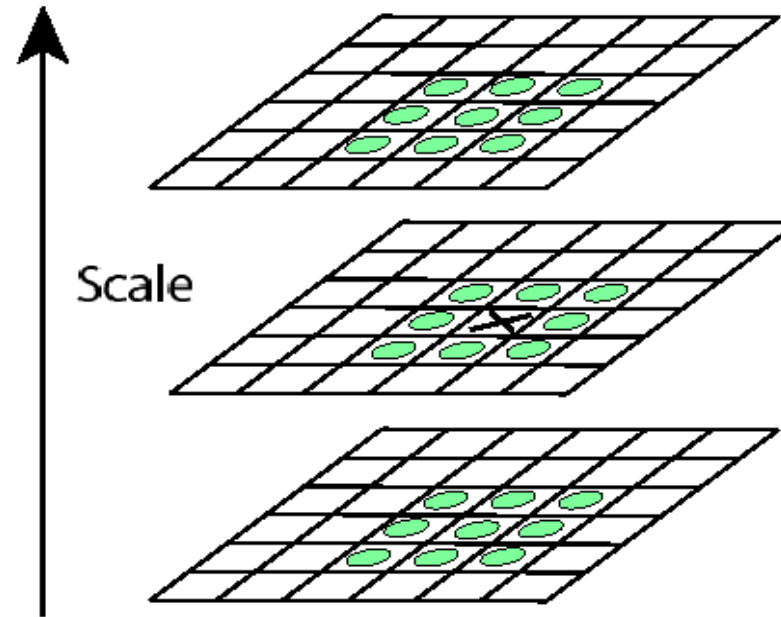
Scale

- For each max or min found, output is the location and the scale.

Orientation assignment

- Create histogram of local gradient directions computed at selected scale.

- Assign canonical orientation at peak of smoothed histogram.

- Each key specifies stable 2D coordinates (x, y, scale, orientation).

0 2π

Interest point descriptors

- At this point, each interest point has
  - location,
  - scale,
  - orientation.
- Next step is to compute a descriptor for the local image region about each interest point that is
  - highly distinctive,
  - invariant as possible to variations such as changes in viewpoint and illumination.

Lowe's interest point descriptor

- Use the normalized circular region about the interest point.
  - Rotate the window to standard orientation.
  - Scale the window size based on the scale at which the point was found.
- Compute gradient magnitude and orientation at each point in the region.
- Weight them by a Gaussian window overlaid on the circle.
- Create an orientation histogram over the 4x4 subregions of the window.
- 4x4 descriptors over 16x16 sample array were used in practice. 4x4 times 8 directions gives a vector of 128 values.

Lowe's interest point descriptor

An input image
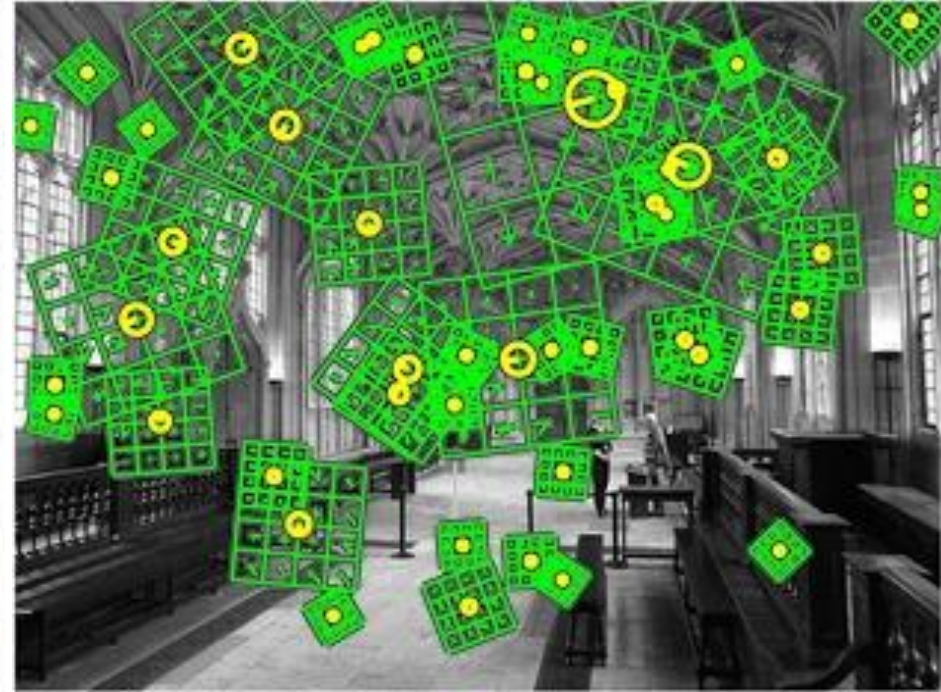
Overlayed descriptors

Example applications

- Object and scene recognition
- Stereo correspondence
- 3D reconstruction
- Image alignment & stitching
- Image indexing and search
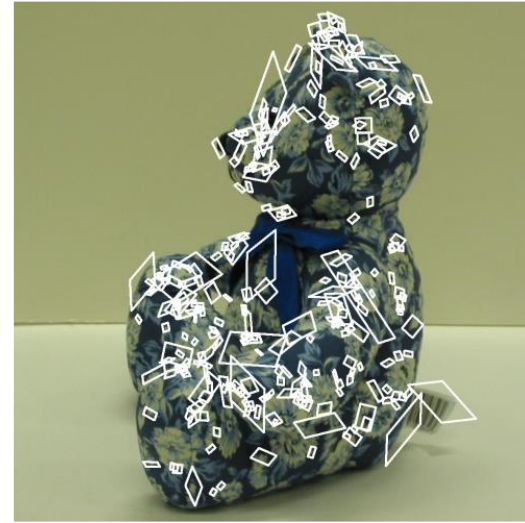- Motion tracking
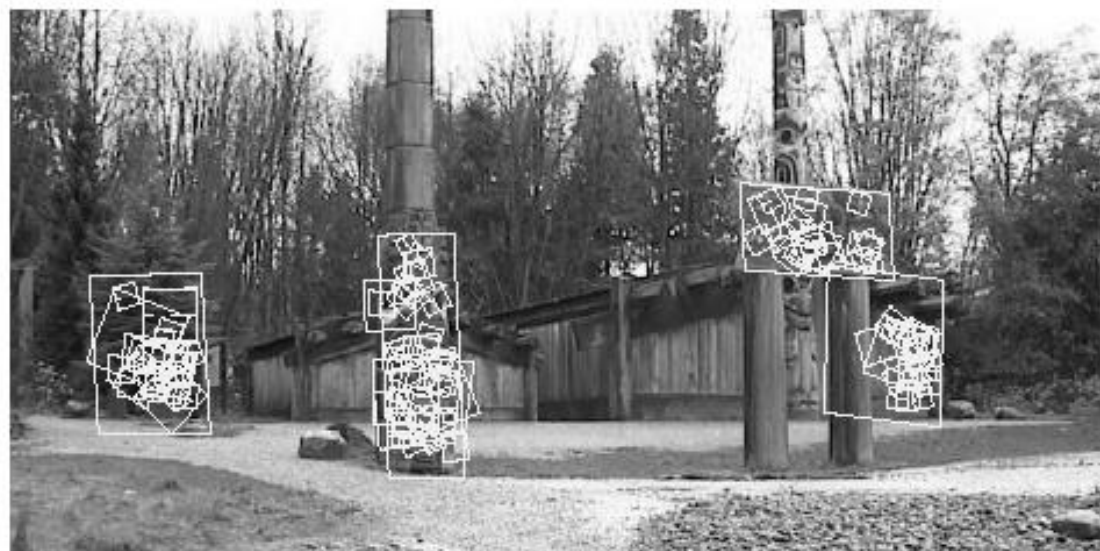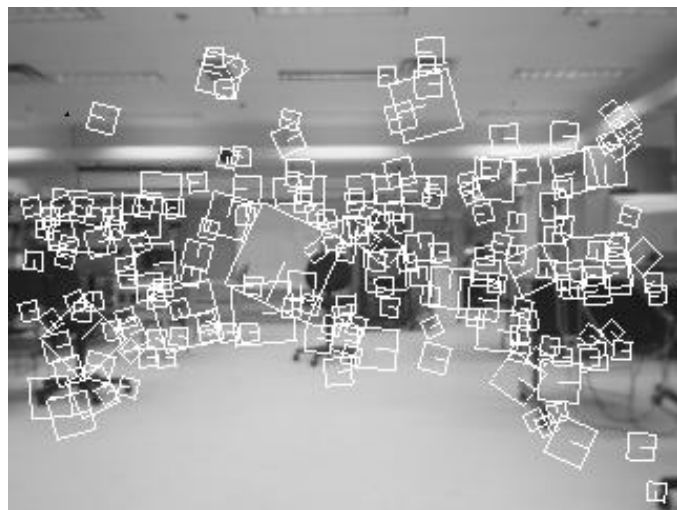- Robot navigation

Examples: 3D recognition
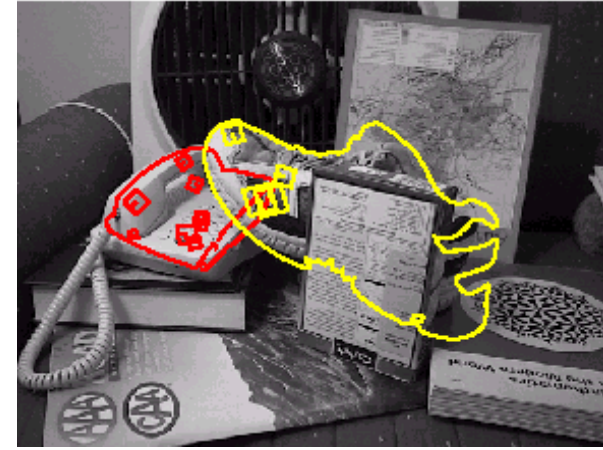
Examples: 3D reconstruction
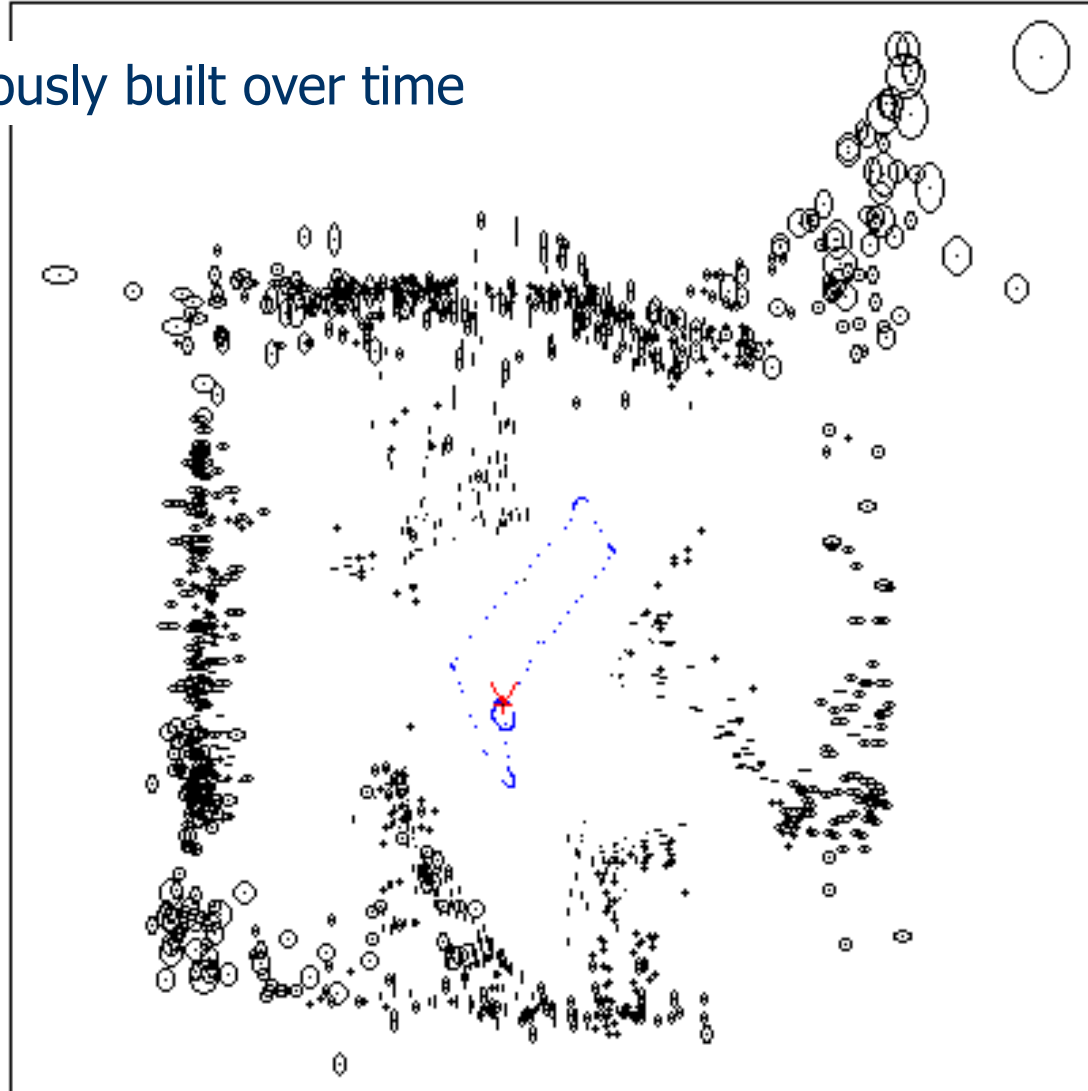
Examples: location recognition

Examples: robot localization

Examples: robot localization

Map continuously built over time

Examples: panaromas

- Recognize overlap from an unordered set of images and automatically stitch together.

- SIFT features provide initial feature matching.

- Image blending at multiple scales hides the seams.

Panorama of Lowe's lab automatically assembled from 143 images

Examples: panaromas

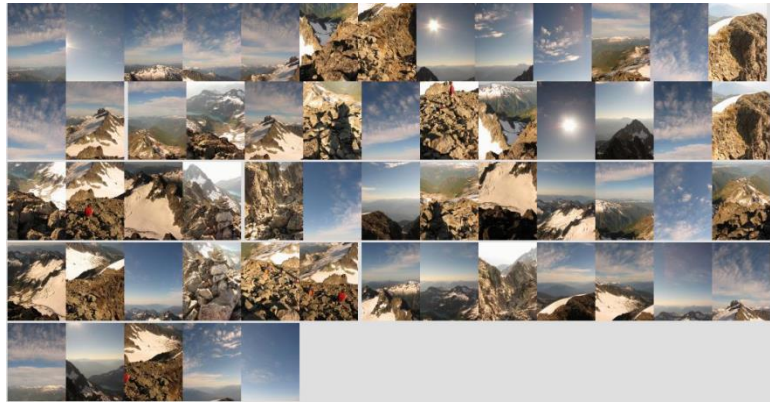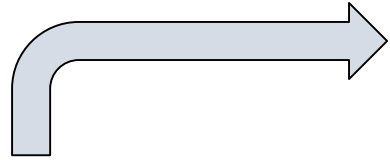Image registration and blending

(a) 40 of 80 images registered

(b) All 80 images registered

(c) Rendered with multi-band blending

Examples: panaromas

25 of 57 images aligned

All 57 images aligned

Final result

Sony Aibo

- SIFT usage:
  - Recognize charging station
  - Communicate with visual cards
  - Teach object recognition

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Photo tourism: exploring photo collections

- Joint work by University of Washington and Microsoft Research
  - http://phototour.cs.washington.edu/
  - http://research.microsoft.com/IVM/PhotoTours/

- Photosynth Technology Preview at Microsoft Live Labs
  - http://photosynth.net/

- Don't forget to check the cool video and demo at http://phototour.cs.washington.edu/.
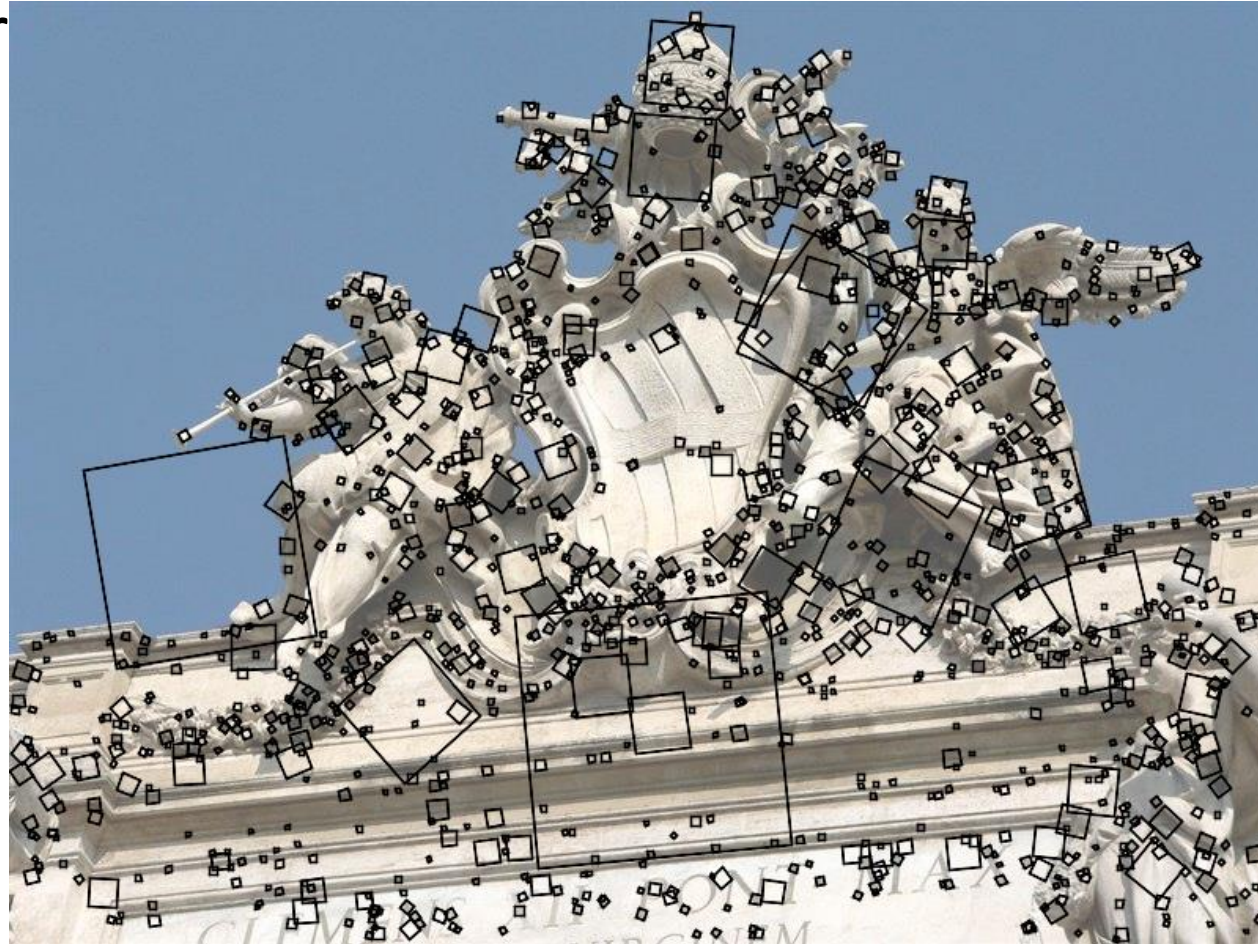
Photo tourism: exploring photo collections

- Detect featur

Photo tourism: exploring photo collections

- Detect features using SIFT

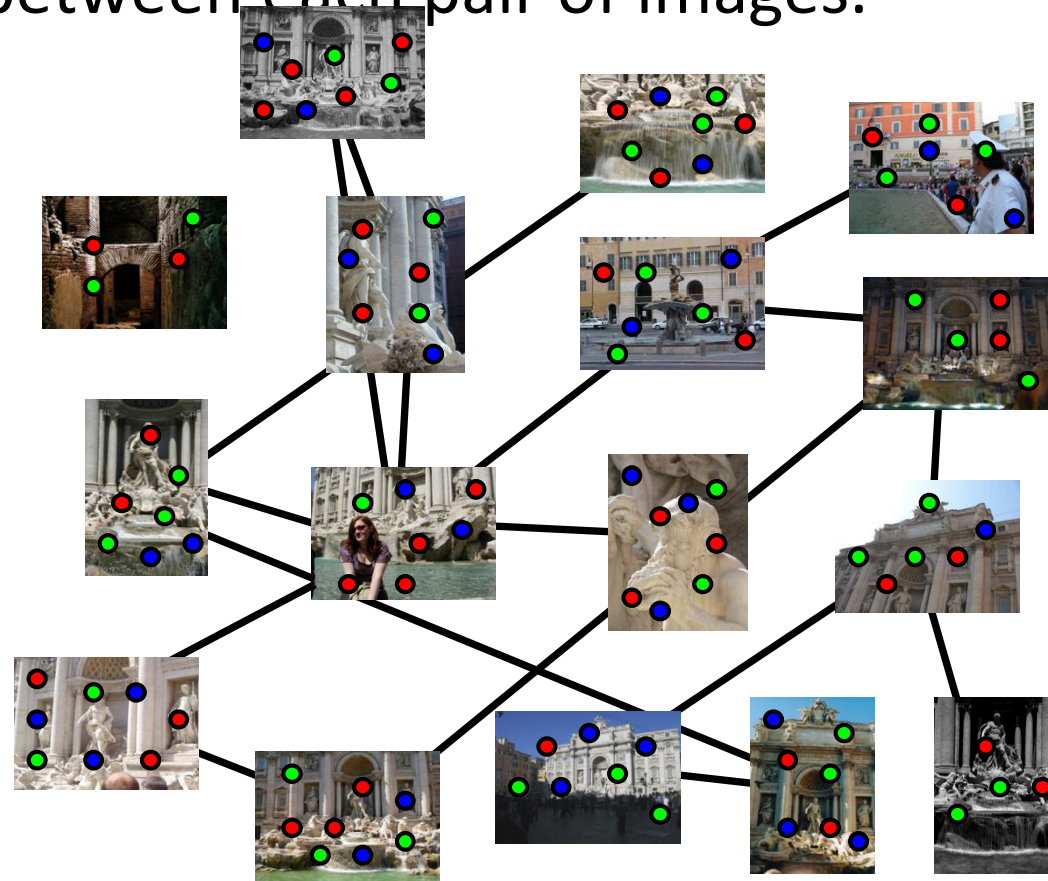# Photo tourism: exploring photo collections

- Detect features using SIFT

Photo tourism: exploring photo collections

- Match features between each pair of images.

Photo tourism: exploring photo collections

- Link up pairwise matches to form connected components of matches across several images.
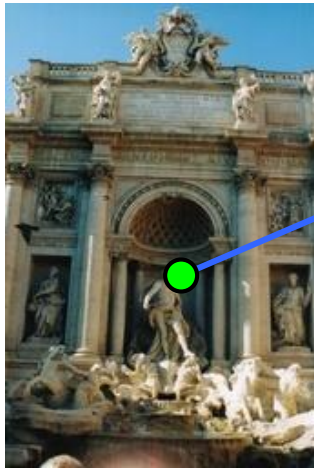

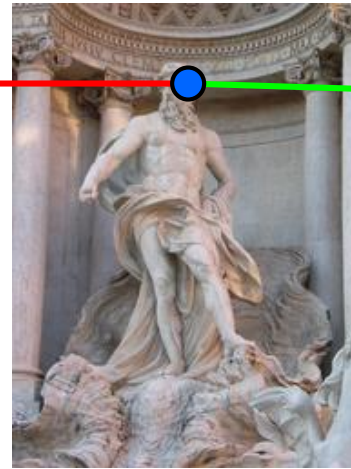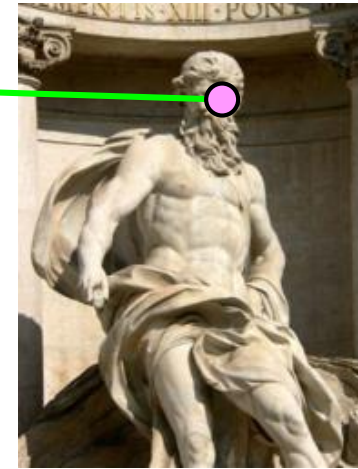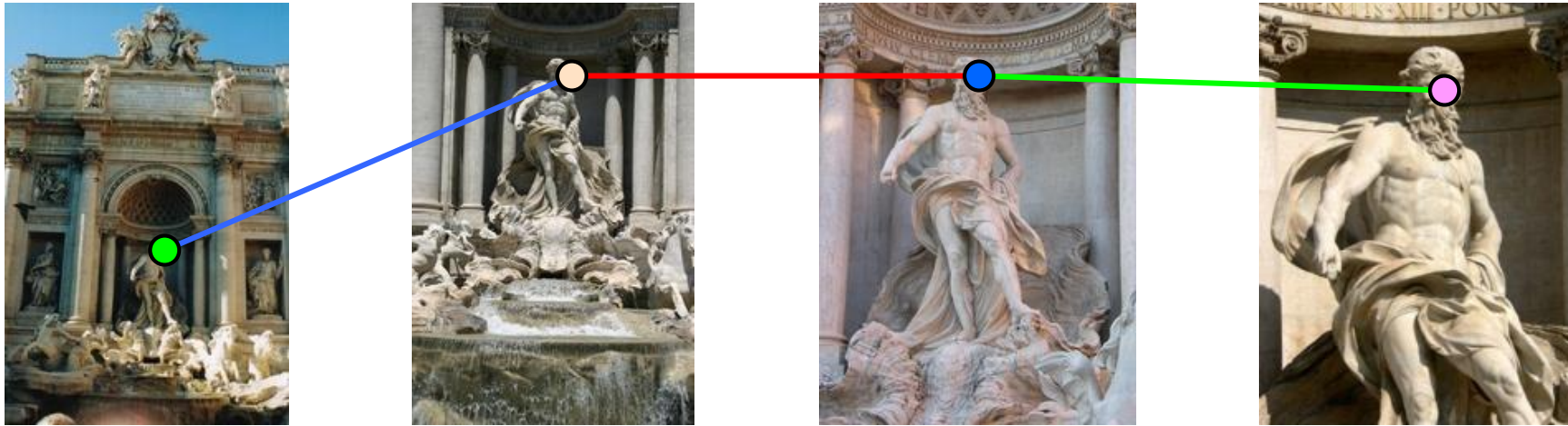Image 1   Image 2   Image 3   Image 4

Photo tourism: exploring photo collections

Photo tourism: exploring photo collections

Photos are automatically placed inside a sketchy 3D model of the scene; an optional overhead map also shows each photo's location.

Photo tourism: exploring photo collections

An info pane on the left shows information about the current image and navigation buttons for moving around the collection; the filmstrip view on the bottom shows related images; mousing over these images brings them up as a registered overlay.

Photo tourism: exploring photo collections

Photographs can also be taken in outdoor natural environments. The photos are correctly placed in 3-D, and more free-form geometric models can be used for inter-image transitions.

Photo tourism: exploring photo collections

Annotations entered in one image (upper left) are automatically transferred to all other related images.

Scene summarization for online collections

- http://grail.cs.washington.edu/projects/canonview

Scene summary browsing

Enhanced 3D browsing