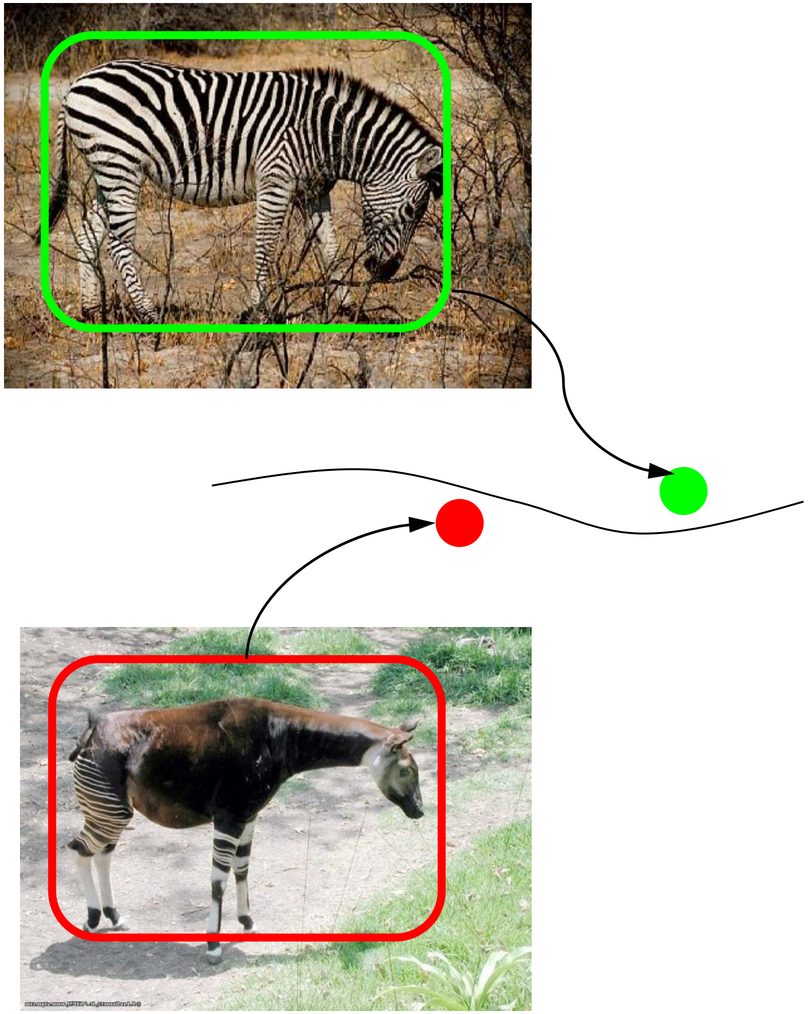
Classifier based methods for Object Recognition

CMP 719– Computer Vision

Pinar Duygulu

(Slide credits:

Kristen Grauman, Fei fei Li, Antonio Torralba, Hames Hays)



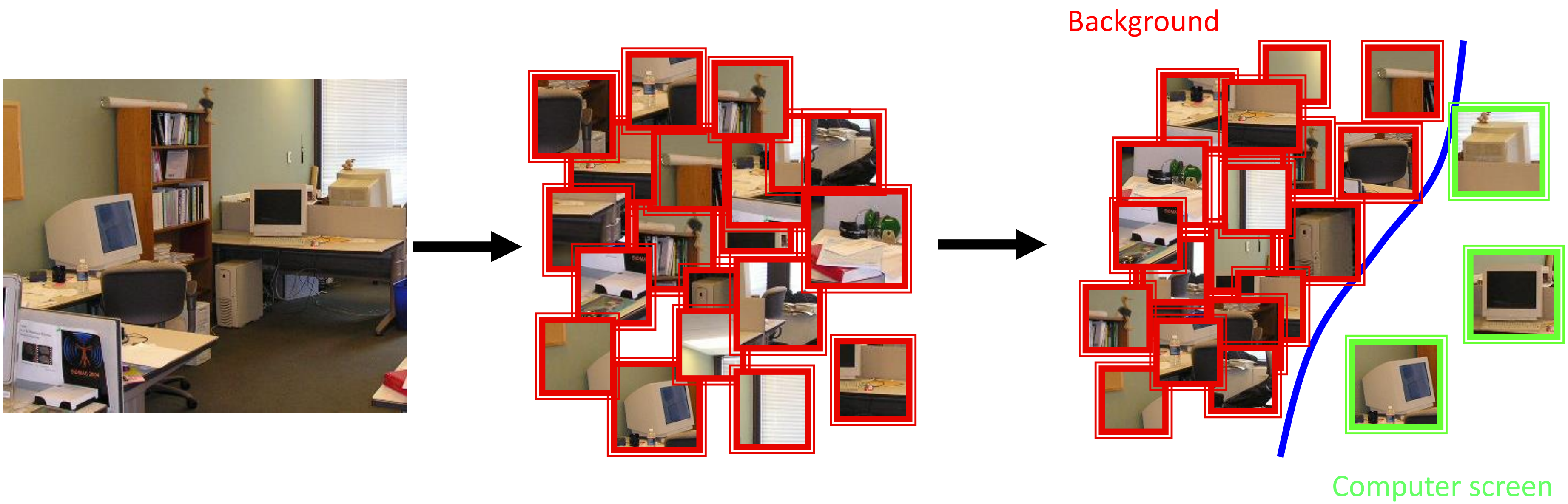
Classifier-based methods

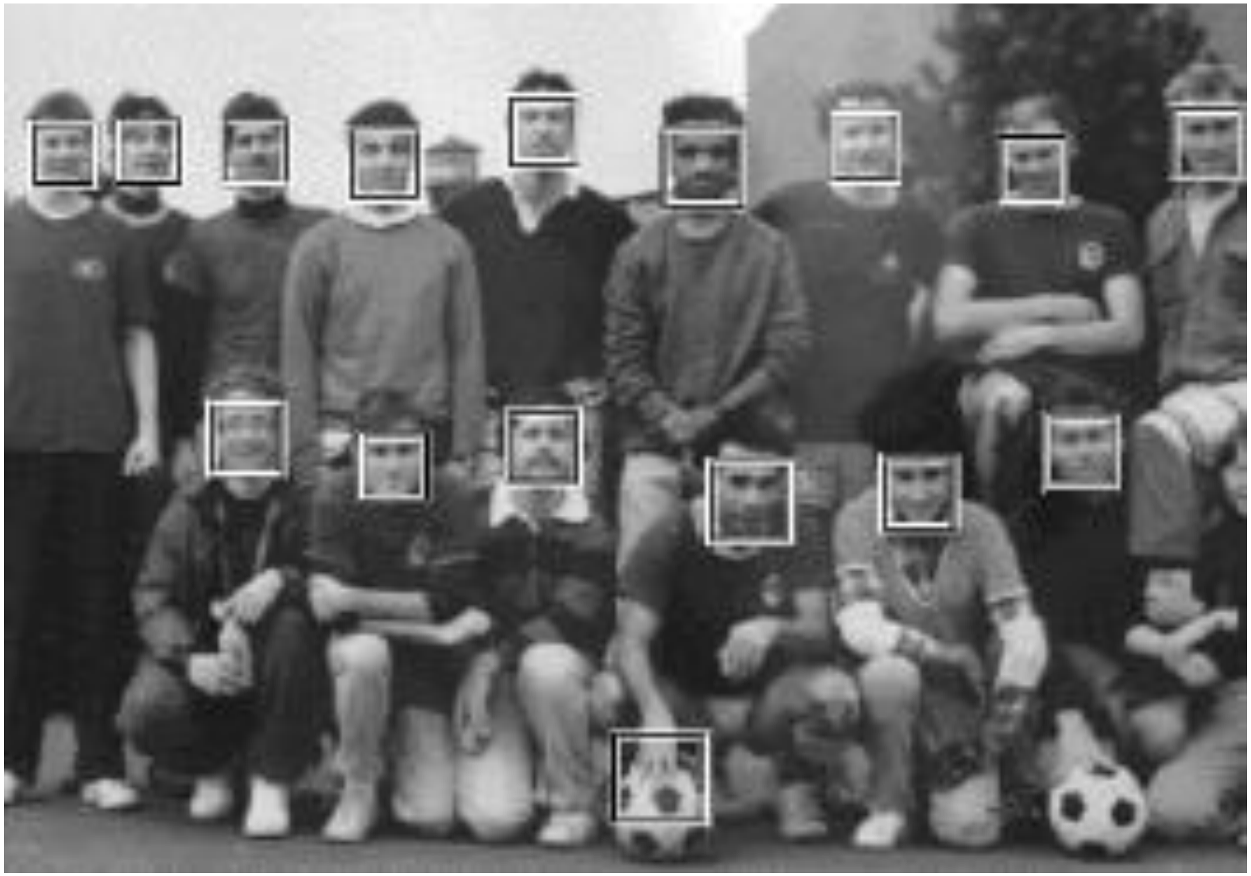
Classifier based methods

Object detection and recognition is formulated as a classification problem.

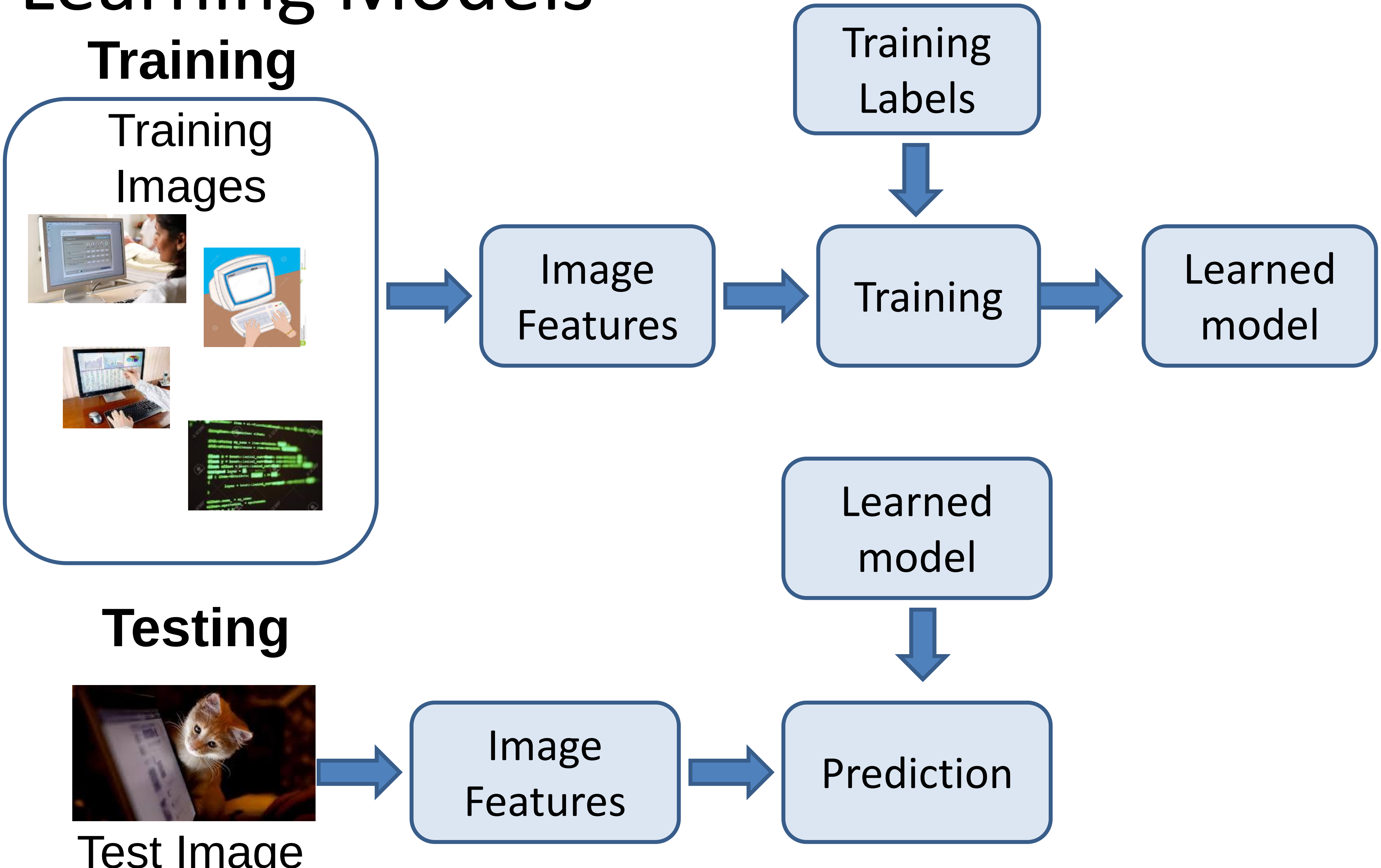
The image is partitioned into a set of overlapping windows

… and a decision is taken at each window about if it contains a target object or not.





Learning Models



Slide credit: Derek Hoiem

Supervised classification

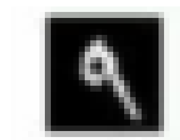
- Given a collection of *labeled* examples, come up with a function that will predict the labels of new examples.

Training examples

"four"

"nine"

Novel input



?

- How good is some function we come up with to do the classification?
- Depends on
  - Mistakes made
  - Cost associated with the mistakes

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Supervised classification

- Given a collection of *labeled* examples, come up with a function that will predict the labels of new examples.

- Consider the two-class (binary) decision problem
  - L(4→9): Loss of classifying a 4 as a 9
  - L(9→4): Loss of classifying a 9 as a 4

- **Risk** of a classifier *s* is expected loss:

$$R(s) = \Pr(4 \to 9 \mid \text{using } s) L(4 \to 9) + \Pr(9 \to 4 \mid \text{using } s) L(9 \to 4)$$

- We want to choose a classifier so as to minimize this total risk

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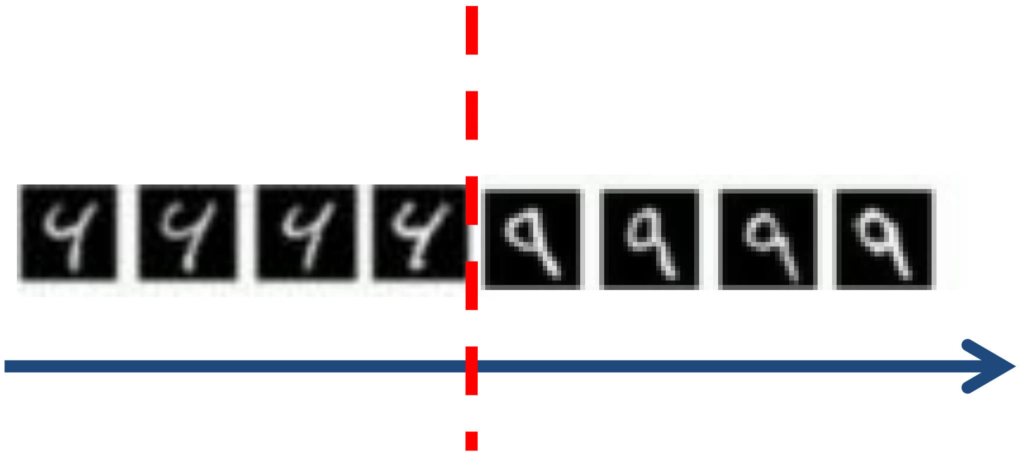
Supervised classification



Feature value **x**

Optimal classifier will minimize total risk.

At decision boundary, either choice of label yields same expected loss.

So, best decision boundary is at point **x** where

$$P(\text{class is } 9 \mid \mathbf{x})\, L(9 \rightarrow 4) = \mathrm{P}(\text{class is } 4 \mid \mathbf{x}) L(4 \rightarrow 9)$$

To classify a new point, choose class with lowest expected loss; i.e., choose “four” if

$$P(4 \mid \mathbf{x}) L(4 \rightarrow 9) > P(9 \mid \mathbf{x}) L(9 \rightarrow 4)$$

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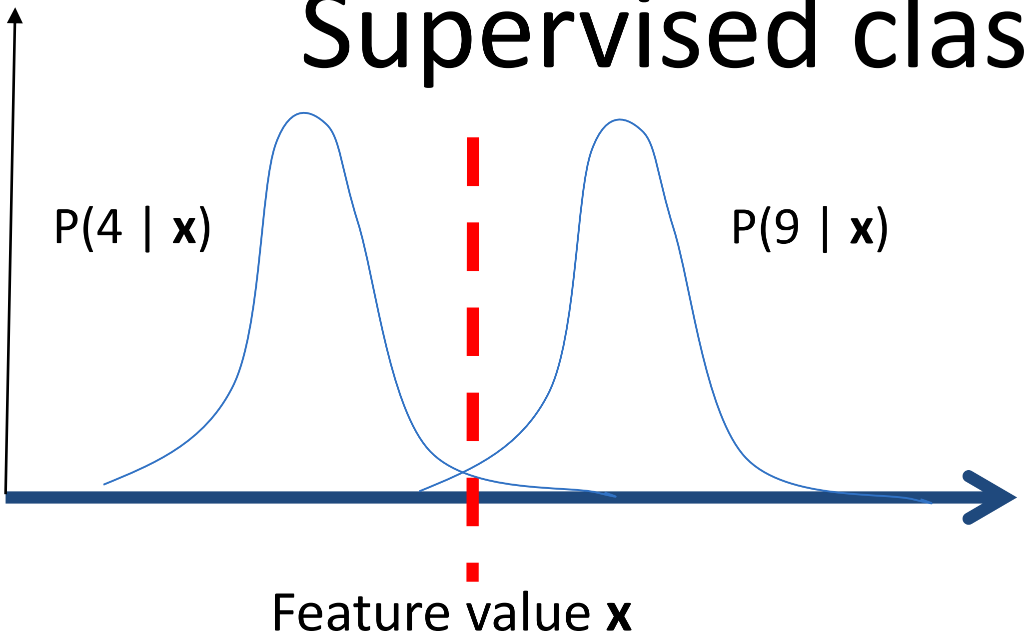
Supervised classification



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$$\boxed{P(4 \mid \mathbf{x})} L(4 \rightarrow 9) > \boxed{P(9 \mid \mathbf{x})} L(9 \rightarrow 4)$$

How to evaluate these probabilities?

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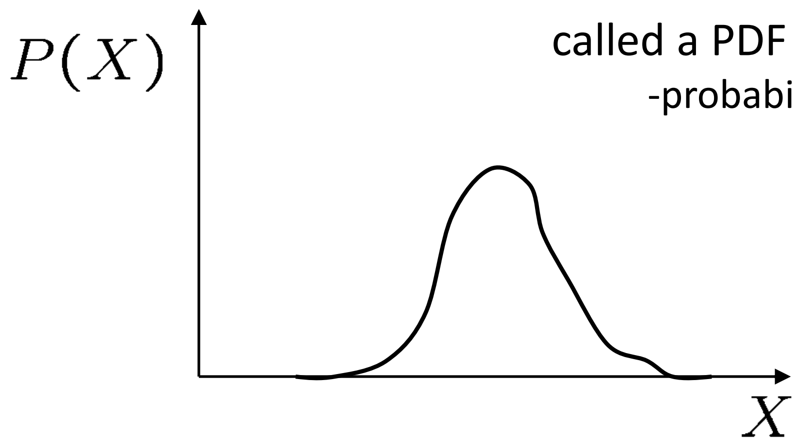
Probability

- Basic probability
  - X is a random variable
  - P(X) is the probability that X achieves a certain value



called a PDF
-probability distribution/density function

  - $0 \leq P(X) \leq 1$
  - $\int_{-\infty}^{\infty} P(X)dX = 1$ or $\sum P(X) = 1$

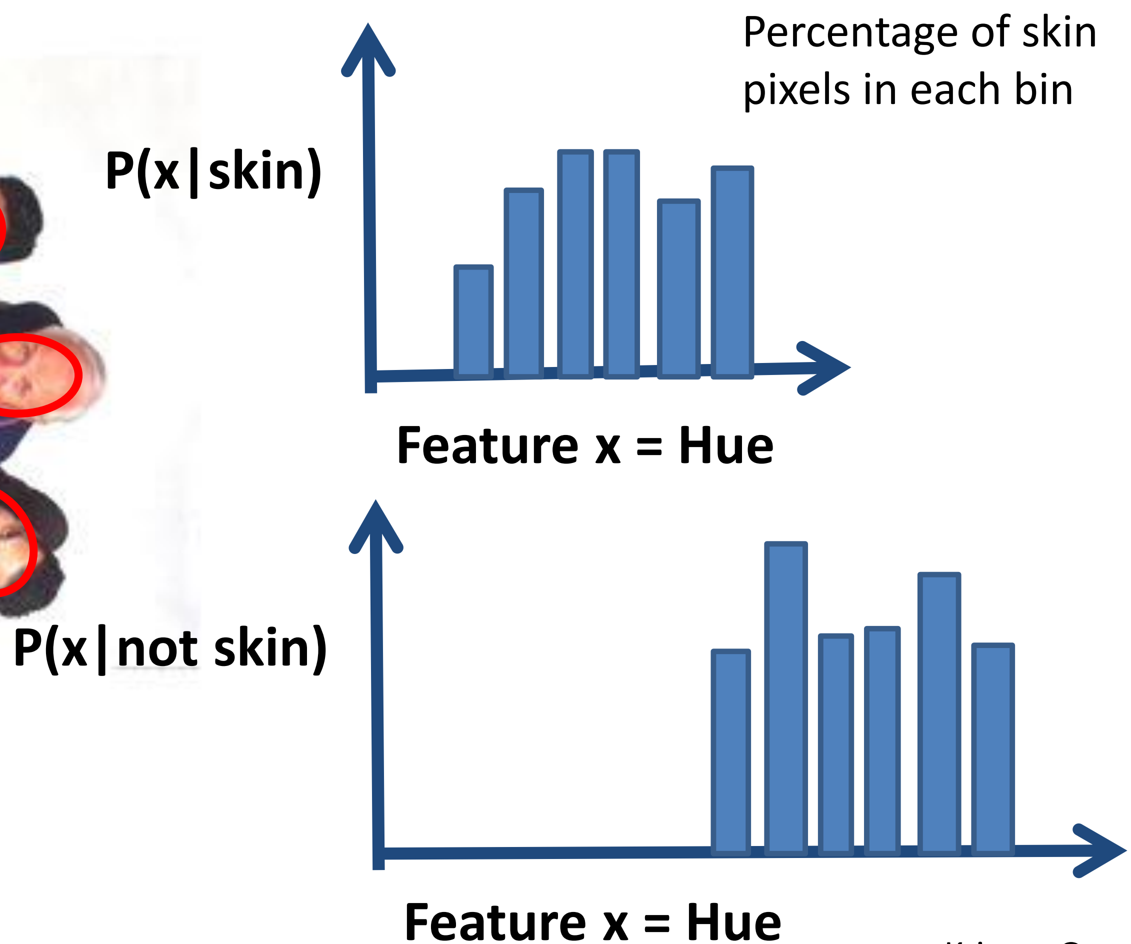
continuous X — discrete X

  - Conditional probability: P(X | Y)
    - probability of X given that we already know Y

Source: Steve Seitz

Example: learning skin colors

- We can represent a class-conditional density using a histogram (a “non-parametric” distribution)



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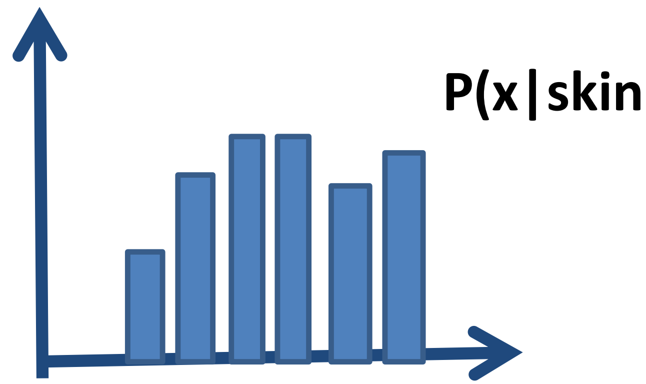
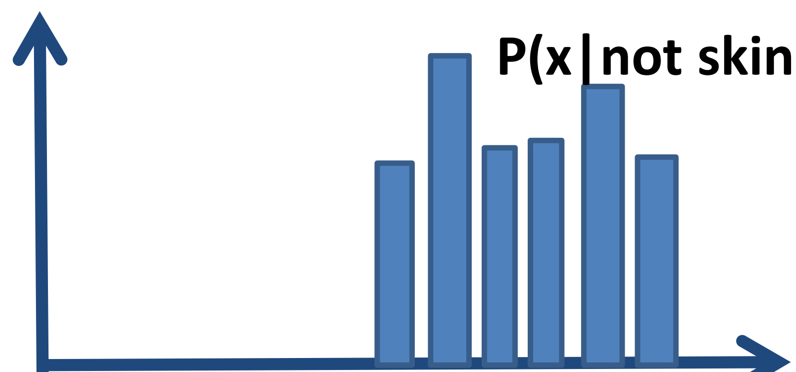


Feature x = Hue



Feature x = Hue

Now we get a new image, and want to label each pixel as skin or non-skin.

What’s the probability we care about to do skin detection?

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Bayes rule

$$\underbrace{P(skin \mid x)}_{\text{posterior}} = \frac{\overbrace{P(x \mid skin)}^{\text{likelihood}}\overbrace{P(skin)}^{\text{prior}}}{P(x)}$$

$$P(skin \mid x) \;\alpha\; P(x \mid skin)P(skin)$$

Example: classifying skin pixels

Now for every pixel in a new image, we can estimate probability that it is generated by skin.

Brighter pixels → higher probability of being skin

Classify pixels based on these probabilities

- if $p(\text{skin}|\boldsymbol{x}) > \theta$, classify as skin
- if $p(\text{skin}|\boldsymbol{x}) < \theta$, classify as not skin

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Example: classifying skin pixels

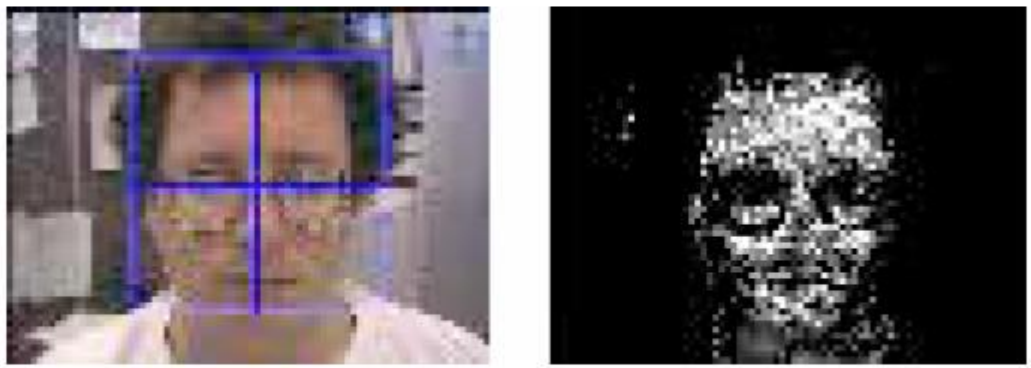

Figure 6: A video image and its flesh probability image

Figure 7: Orientation of the flesh probability distribution marked on the source video image

Gary Bradski, 1998

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Example: classifying skin pixels

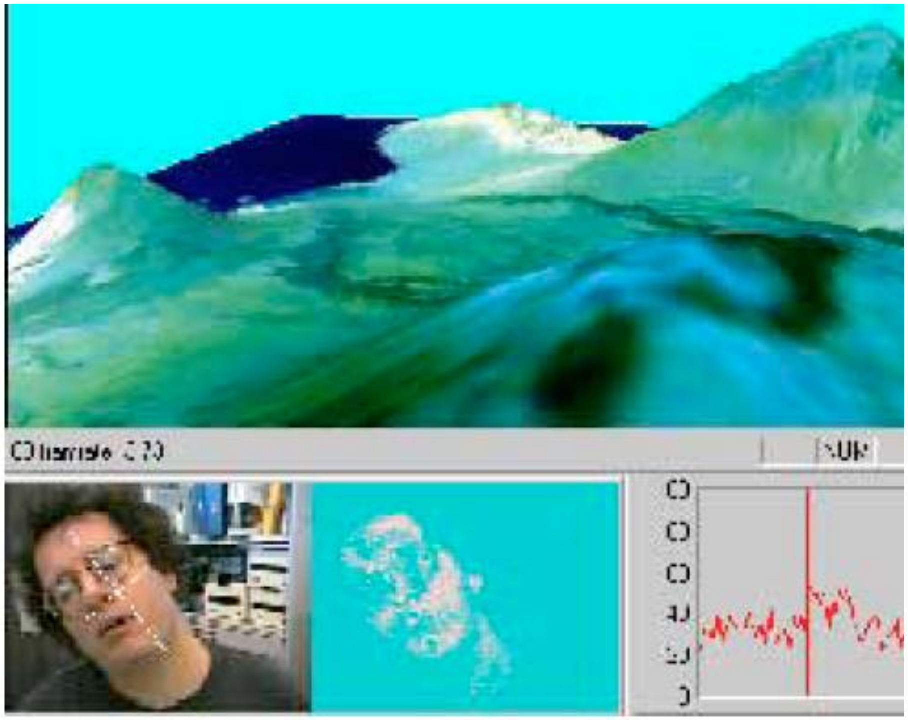

Figure 13: CAMSHIFT-based face tracker used to over a 3D graphic's model of Hawaii

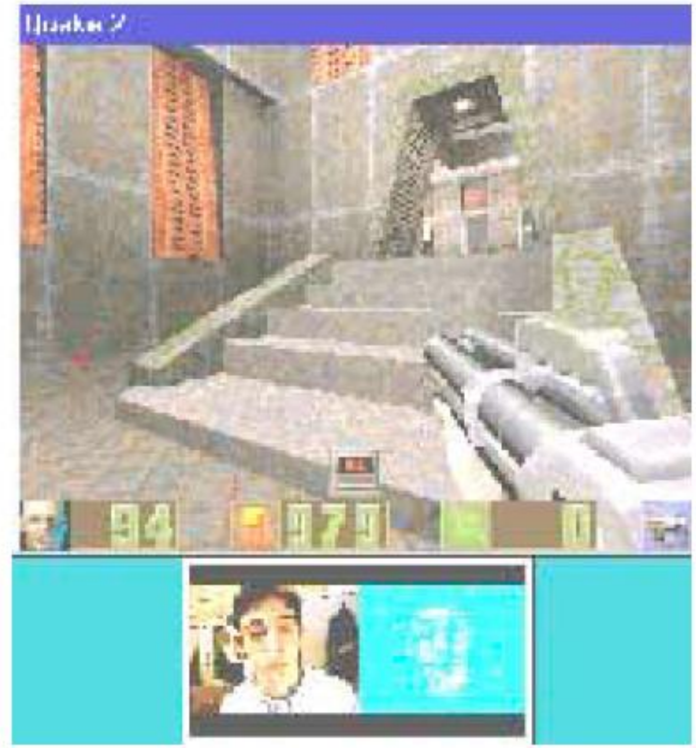

Figure 12: CAMSHIFT-based face tracker used to play Quake 2 hands free by inserting control variables into the mouse queue

Using skin color-based face detection and pose estimation as a video-based interface

Gary Bradski, 1998

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Supervised classification

- Want to minimize the expected misclassification
- Two general strategies
  - Use the training data to build representative probability model; separately model class-conditional densities and priors (*generative*)
  - Directly construct a good decision boundary, model the posterior (*discriminative*)

Discriminative classifiers for image recognition

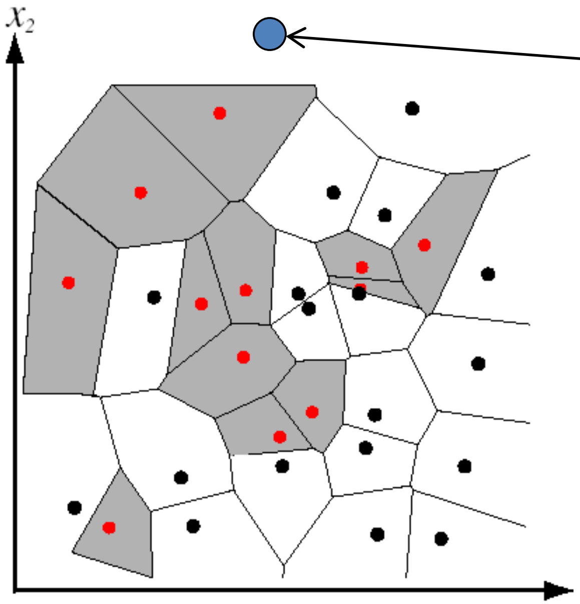
– nearest neighbors (+ scene match app)

– support vector machines (+ gender, person app)

Nearest Neighbor classification

- Assign label of nearest training data point to each test data point

Black = negative
Red = positive



Novel test example

Closest to a positive example from the training set, so classify it as positive.

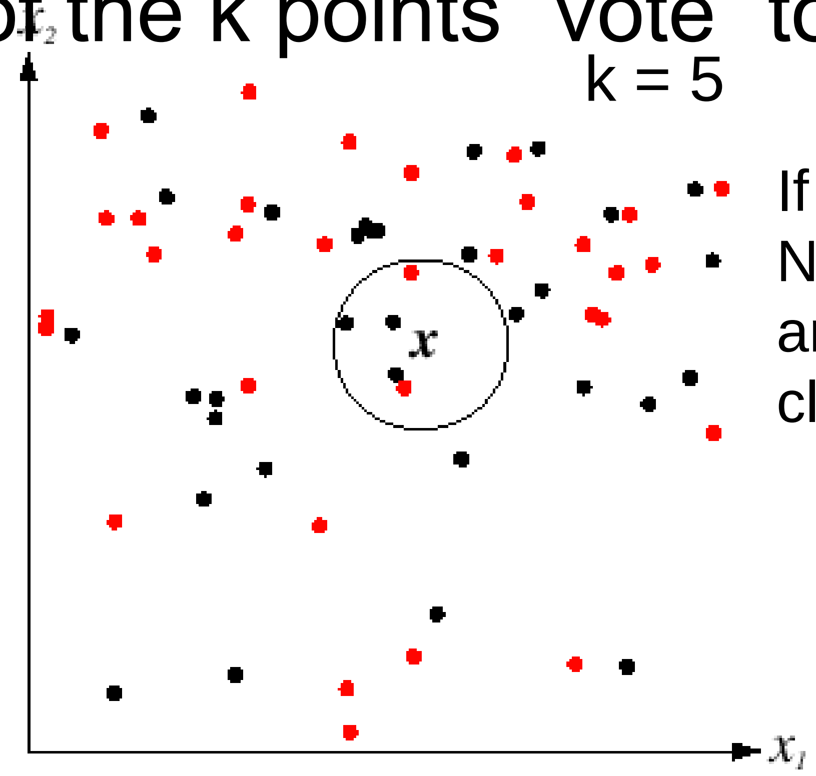
from Duda *et al.*

Voronoi partitioning of feature space for 2-category 2D data

K-Nearest Neighbors classification

- For a new point, find the k closest points from training data
- Labels of the k points "vote" to classify

Black = negative
Red = positive



If query lands here, the 5 NN consist of 3 negatives and 2 positives, so we classify it as negative.

Source: D. Lowe

A nearest neighbor recognition example

Where in the World?

[Hays and Efros. **im2gps**: Estimating Geographic Information from a Single Image. CVPR 2008.]

Slides: James Hays

Where in the World?

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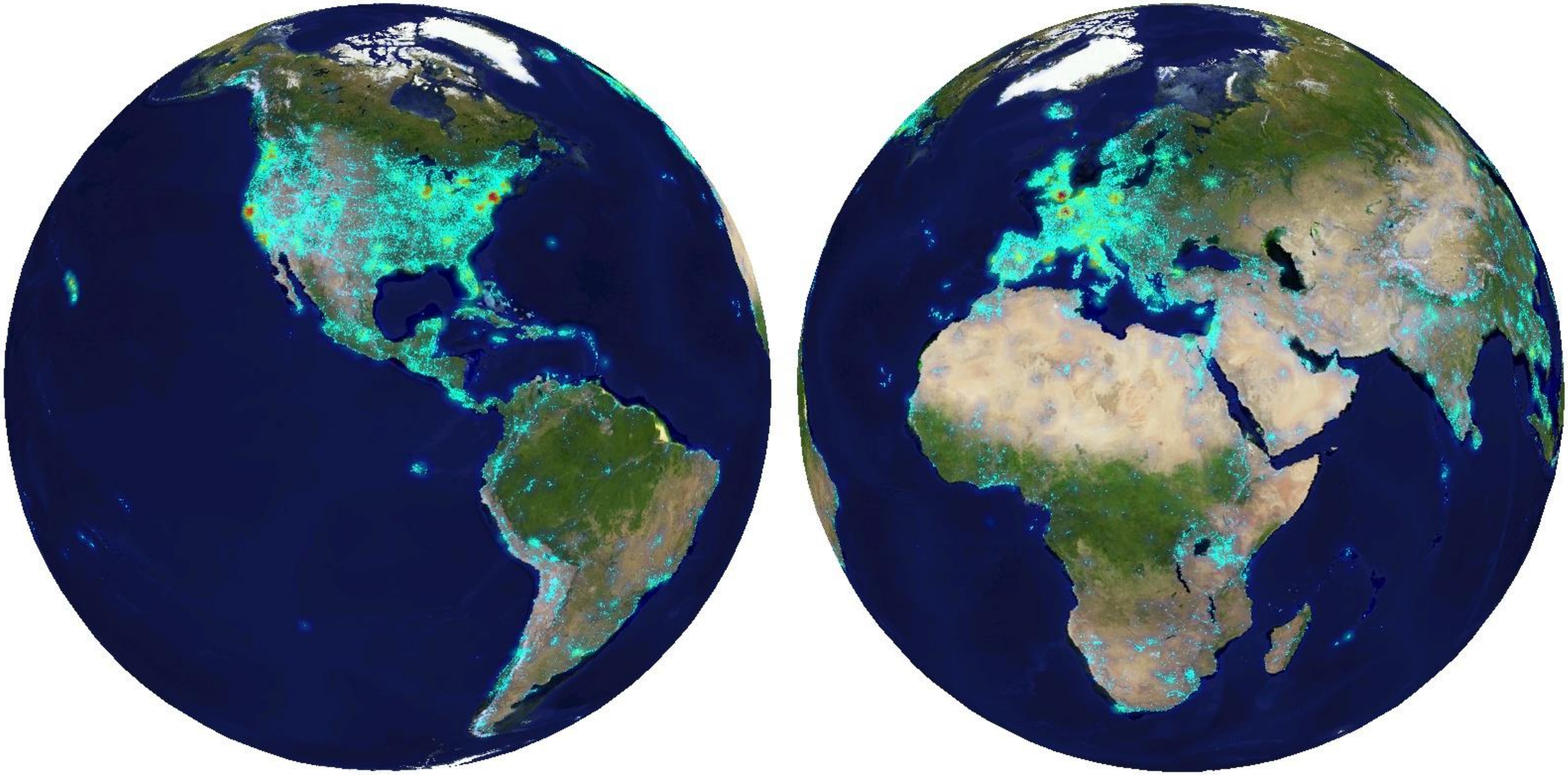
Where in the World?

Slides: James Hays

6+ million geotagged photos by 109,788 photographers



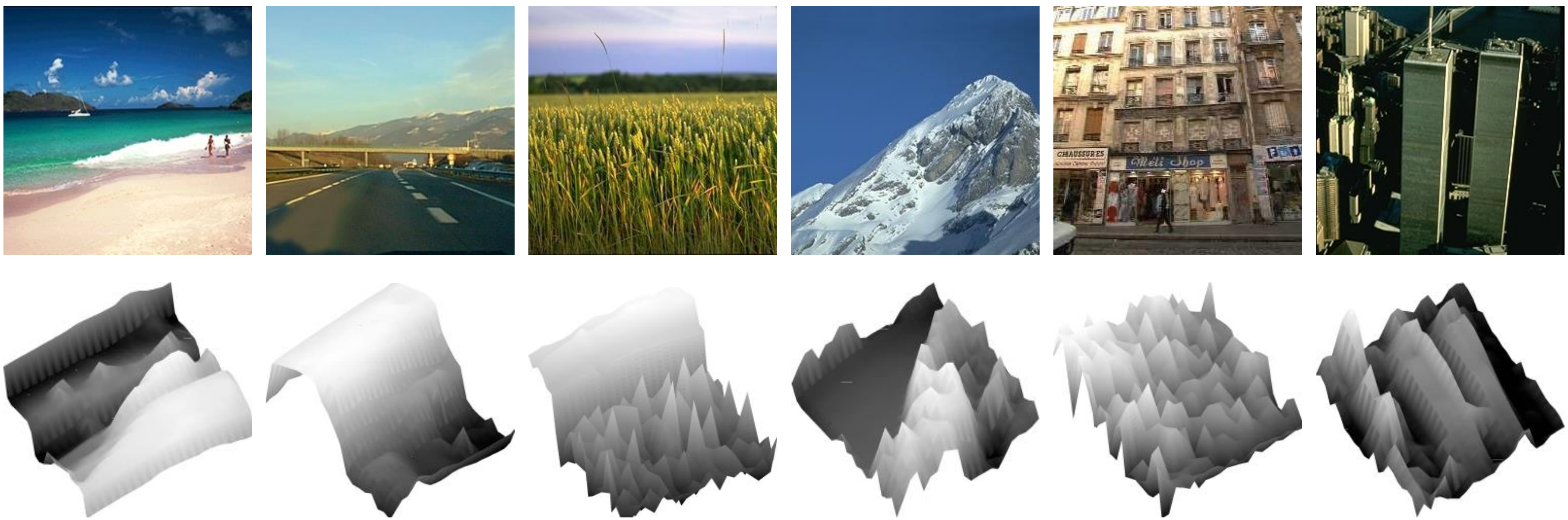
Annotated by Flickr users

Slides: James Hays

Which scene properties are relevant?

Spatial Envelope Theory of Scene Representation

Oliva & Torralba (2001)

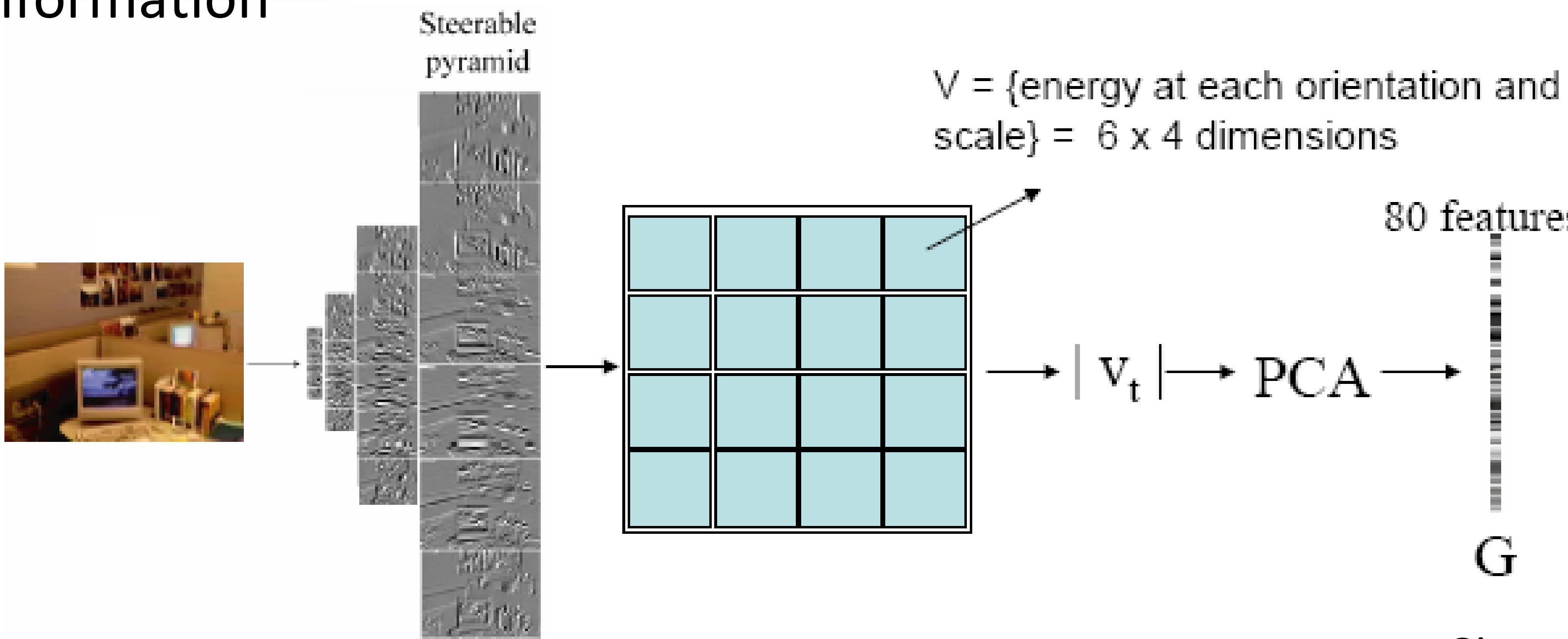


A scene is a single surface that can be represented by global (statistical) descriptors

Slide Credit: Aude Olivia

Global texture: capturing the "Gist" of the scene

Capture global image properties while keeping some spatial information



Gist descriptor

Oliva & Torralba IJCV 2001, Torralba et al. CVPR 2003

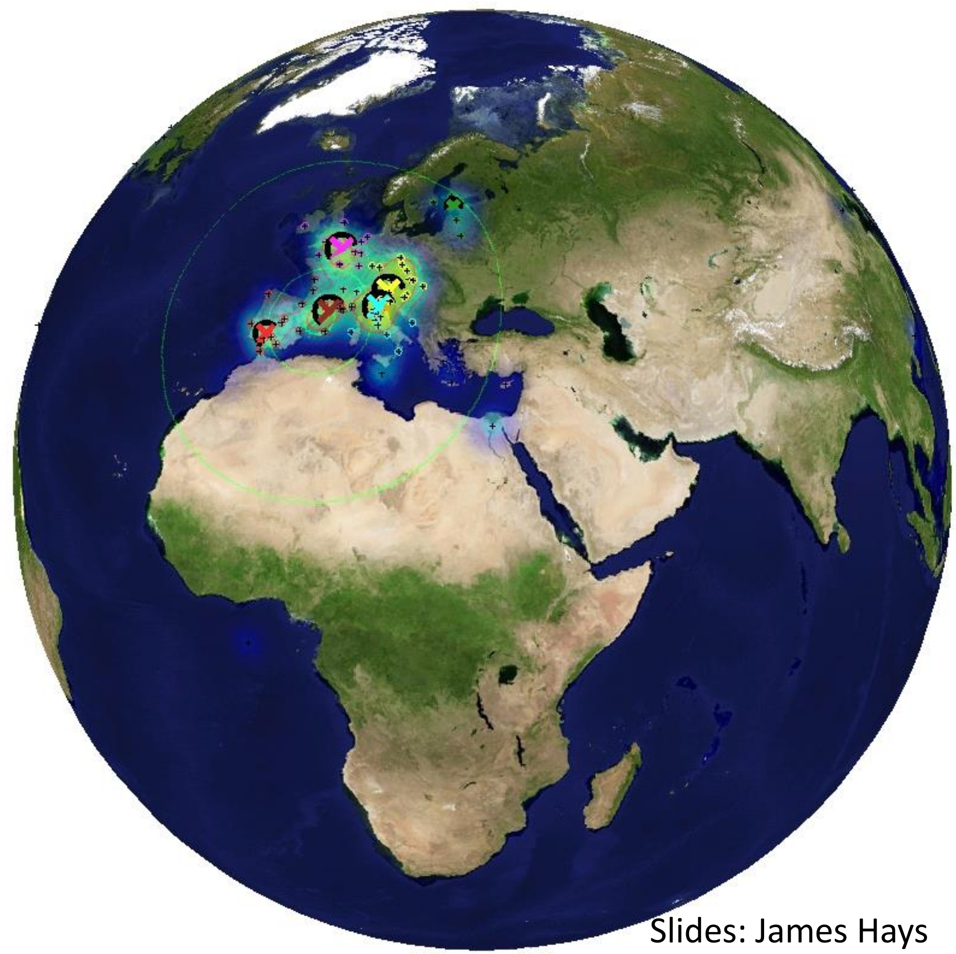
Which scene properties are relevant?

- **Gist scene descriptor**
- **Color Histograms** - L*A*B* 4x14x14 histograms
- **Texton Histograms** – 512 entry, filter bank based
- **Line Features** – Histograms of straight line stats

Scene Matches

[Hays and Efros. **im2gps**: Estimating Geographic Information from a Single Image. CVPR 2008.]

Slides: James Hays



Slides: James Hays

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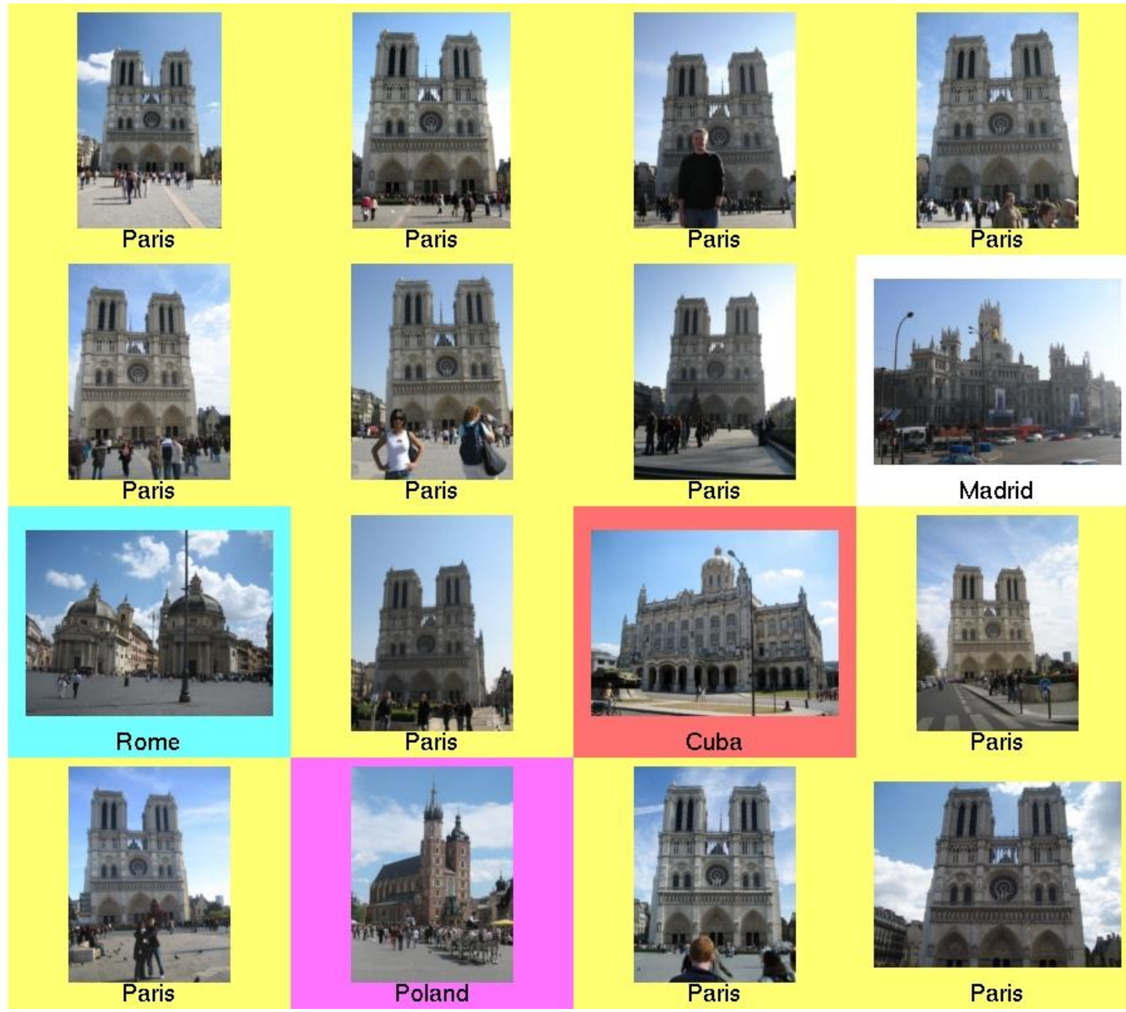

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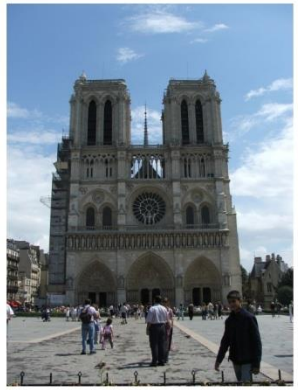

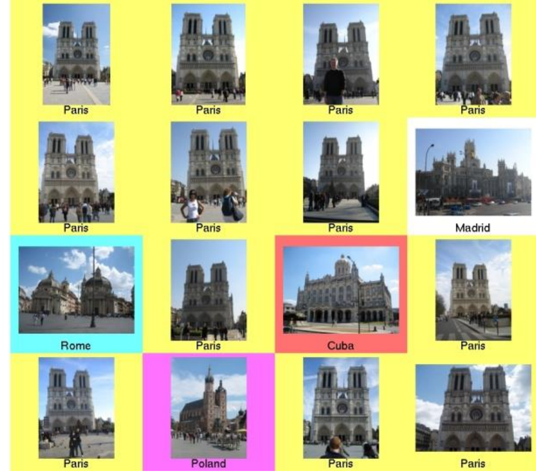

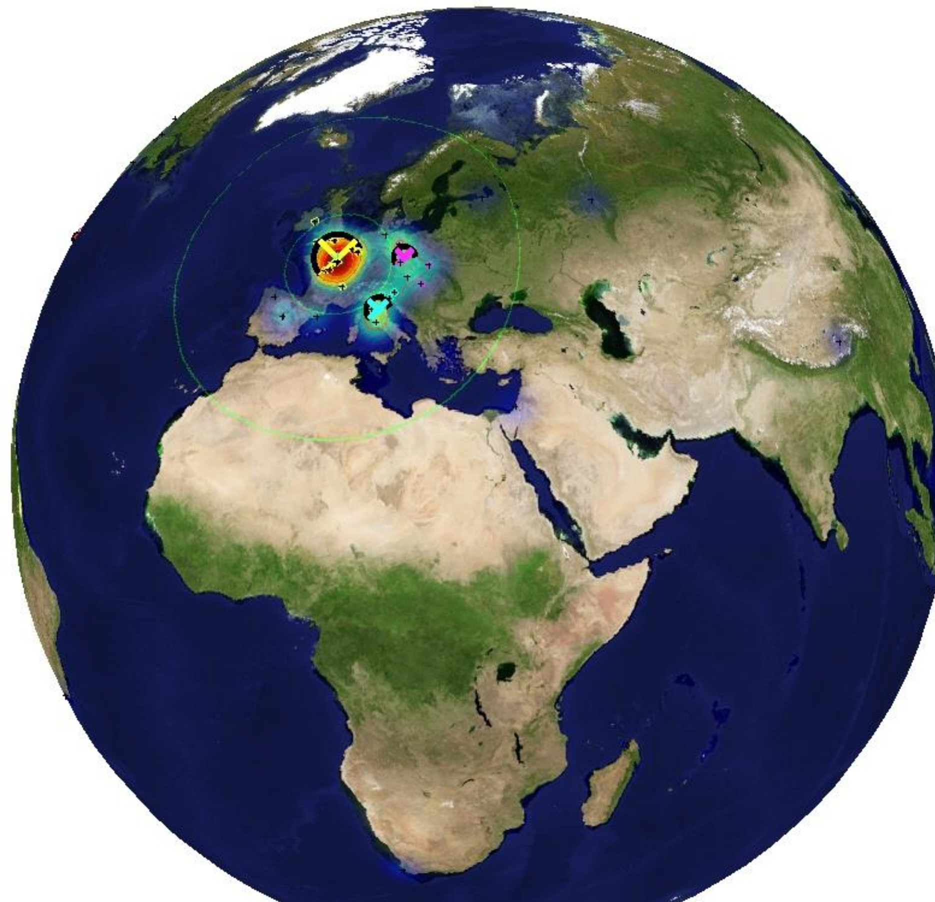

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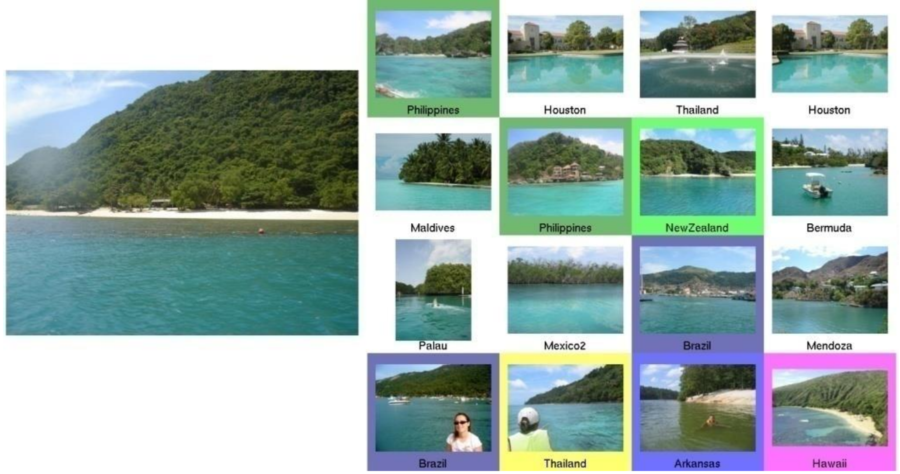
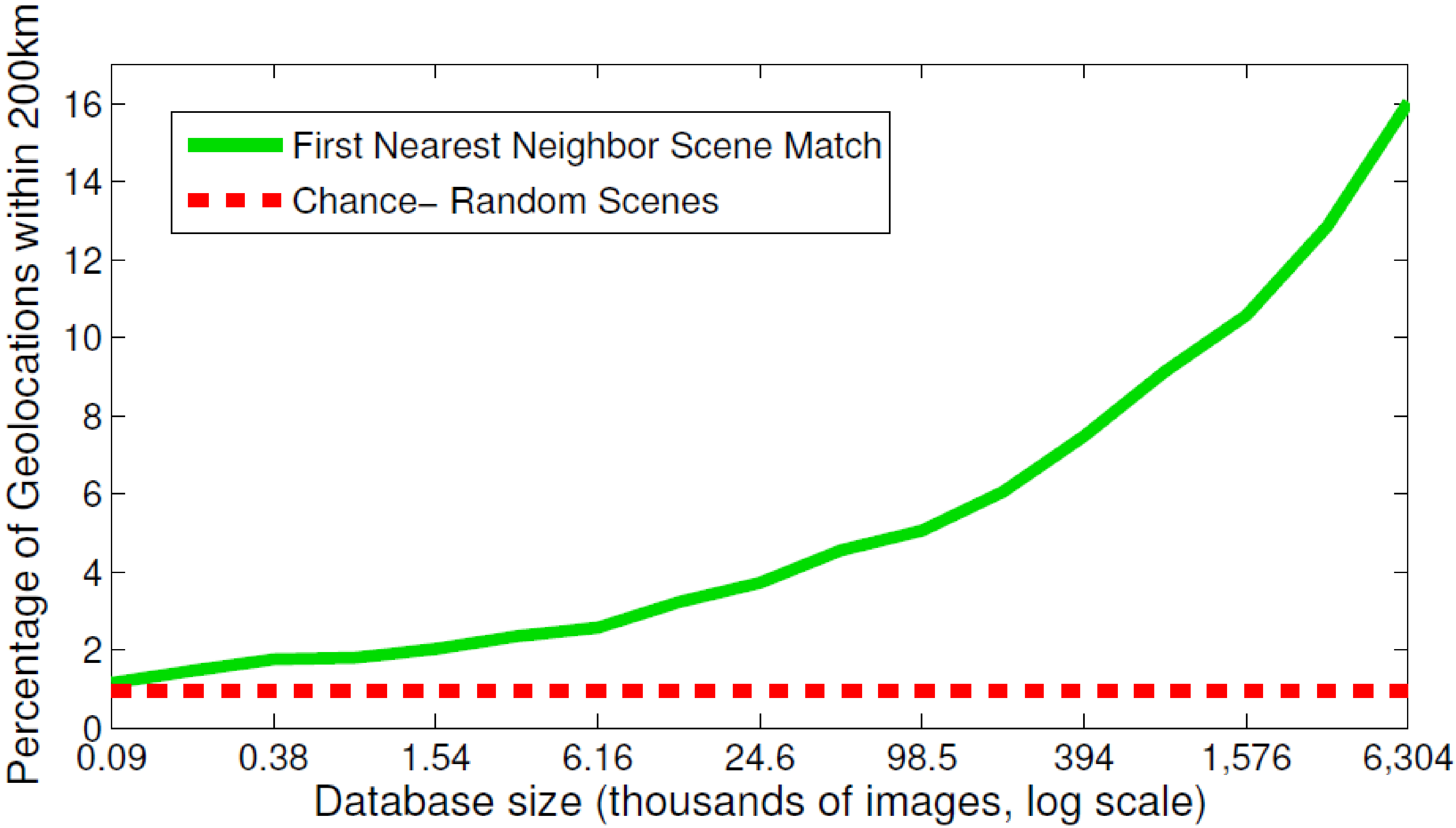


[Hays and Efros. **im2gps**: Estimating Geographic Information from a Single Image. CVPR 2008.]

Slides: James Hays

The Importance of Data



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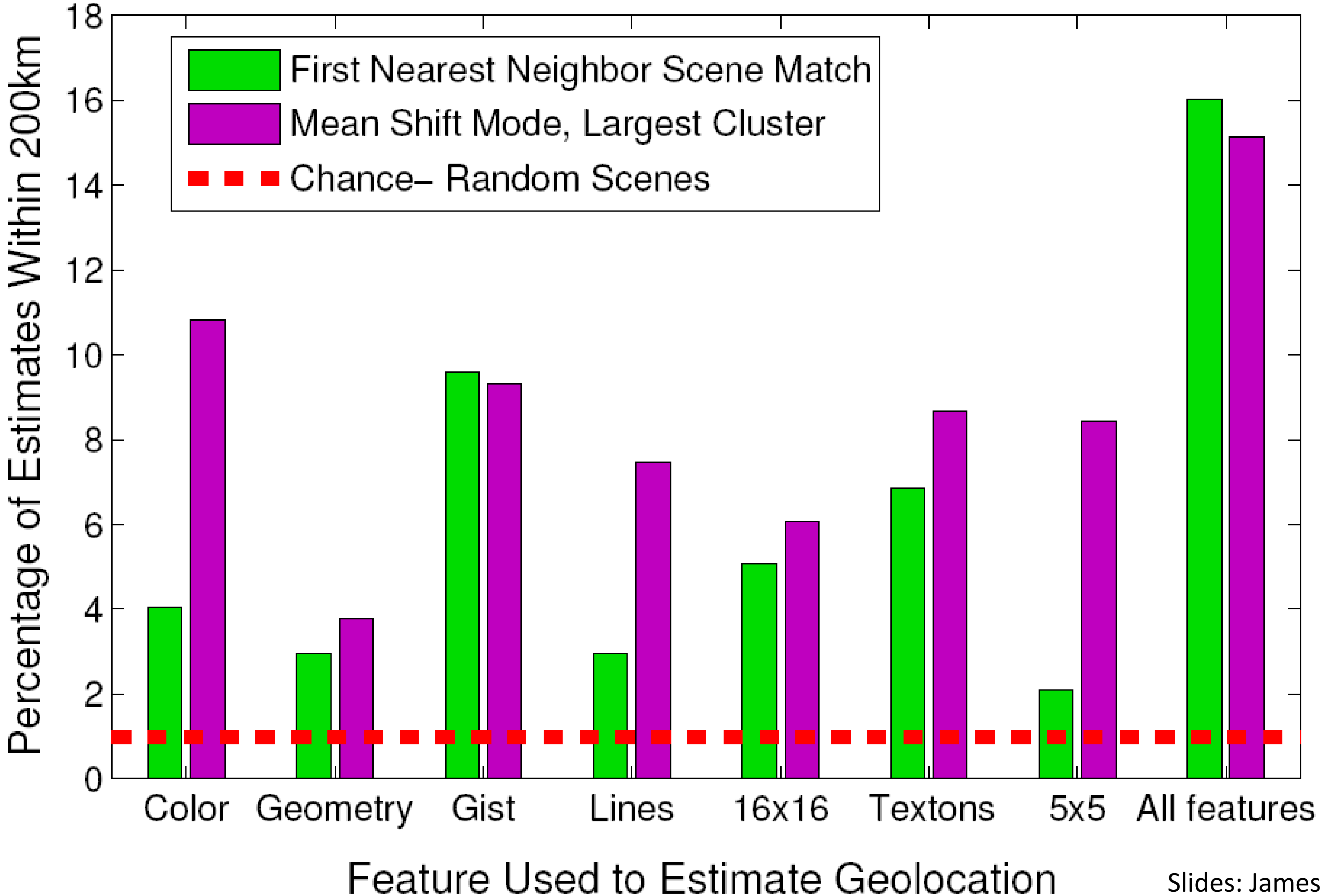
Slides: James Hays

Feature Performance

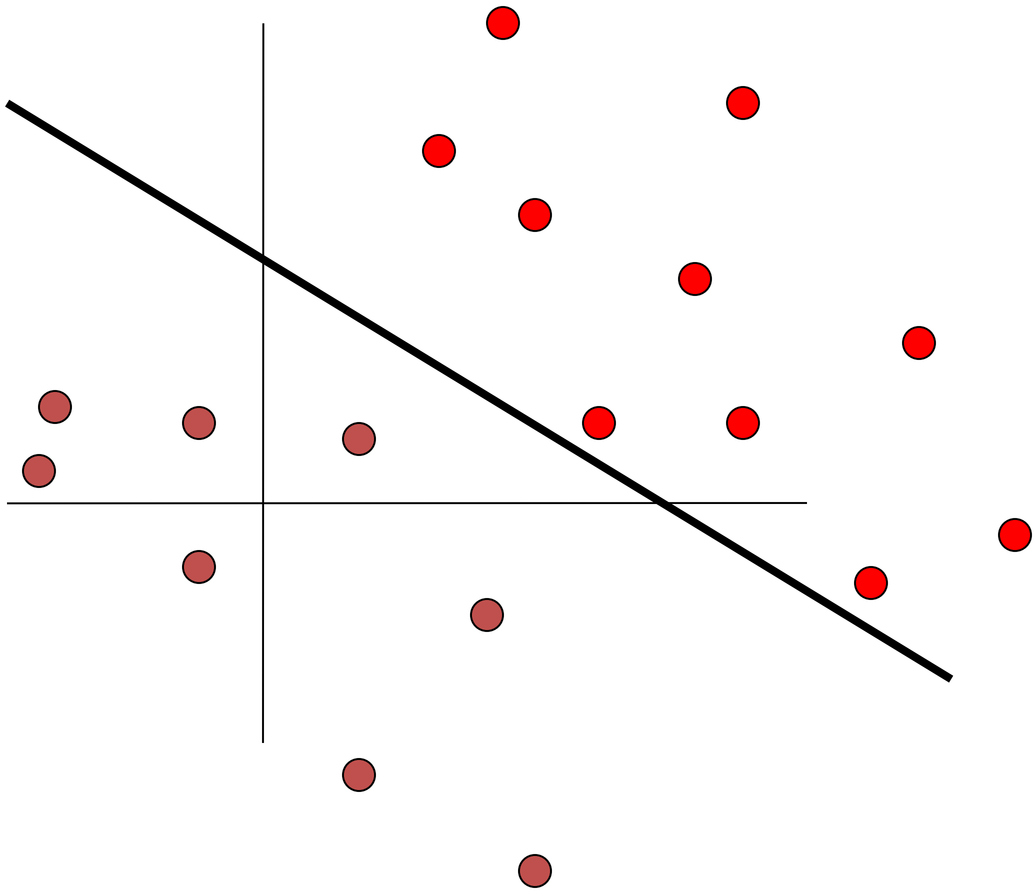


Slides: James Hays

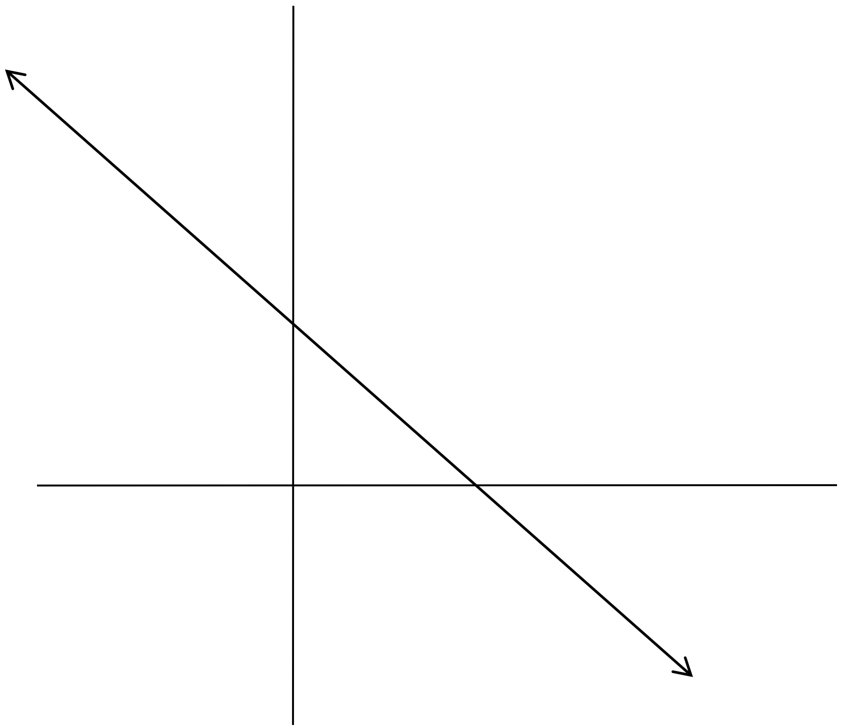
Nearest neighbors: pros and cons

- **Pros**:
  - Simple to implement
  - Flexible to feature / distance choices
  - Naturally handles multi-class cases
  - Can do well in practice with enough representative data
- **Cons:**
  - Large search problem to find nearest neighbors
  - Storage of data
  - Must know we have a meaningful distance function

Linear classifiers



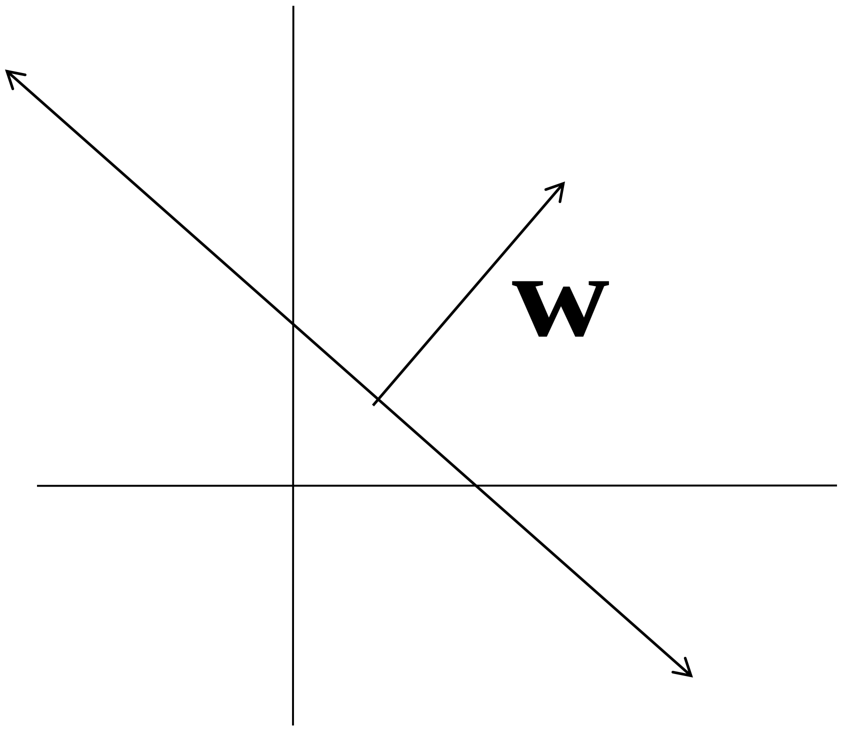
Lines in R^2



Let $\mathbf{w} = \begin{bmatrix} a \\ c \end{bmatrix}$ $\mathbf{x} = \begin{bmatrix} x \\ y \end{bmatrix}$

$$ax + cy + b = 0$$

Lines in R^2



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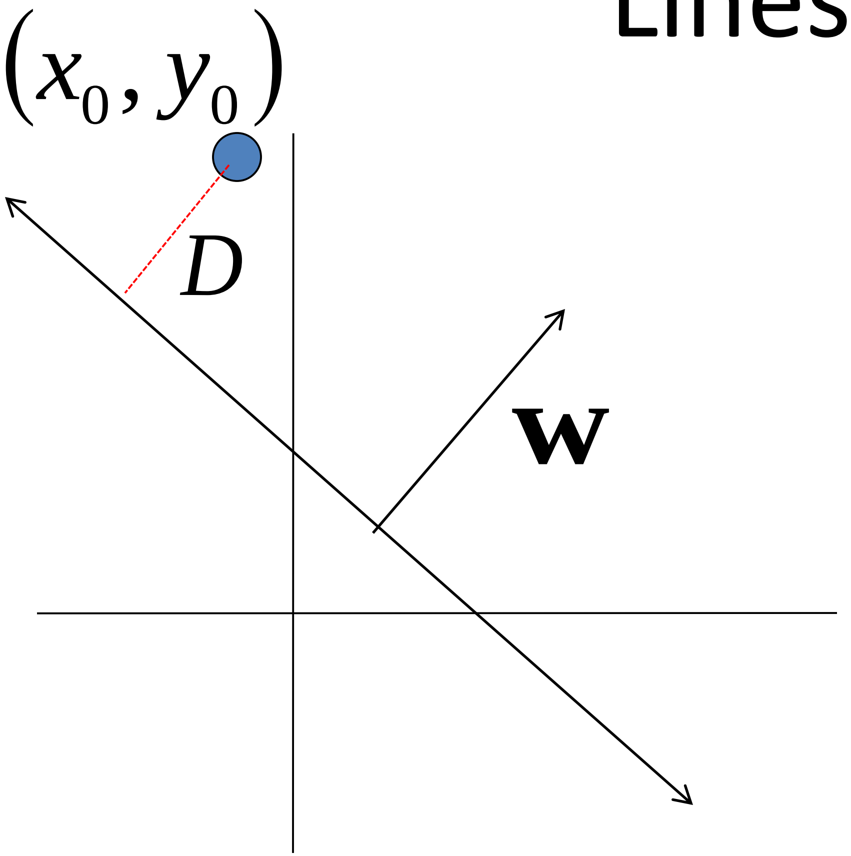
$$ax + cy + b = 0$$

$$\Updownarrow$$

$$\mathbf{w} \cdot \mathbf{x} + b = 0$$

Lines in R^2



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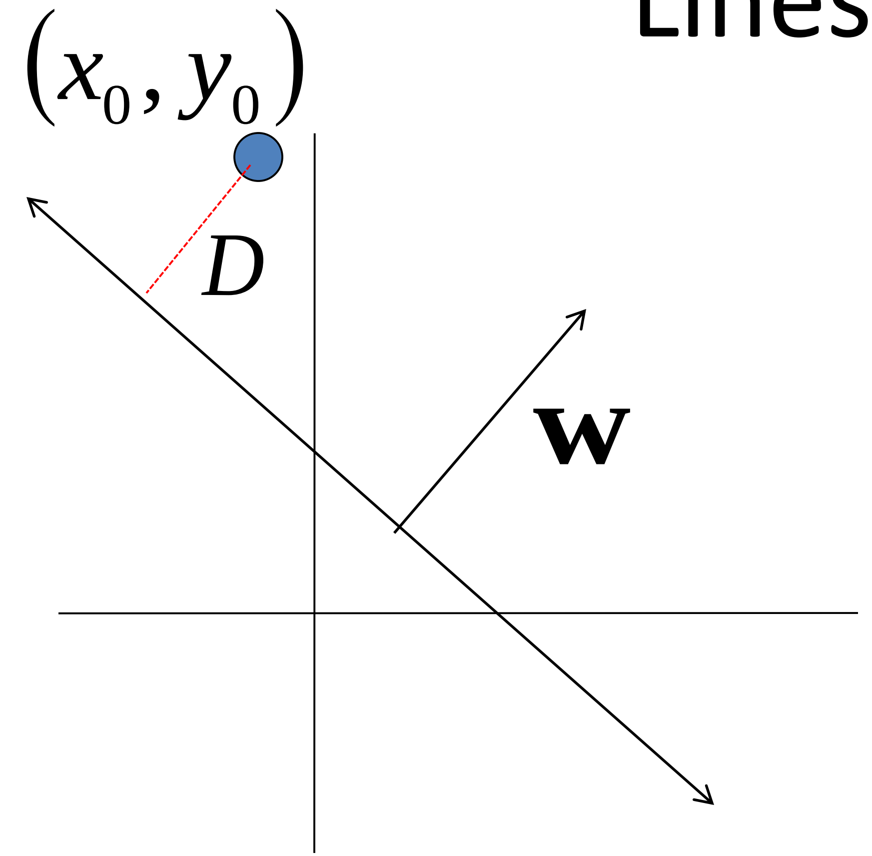

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$$ax + cy + b = 0$$

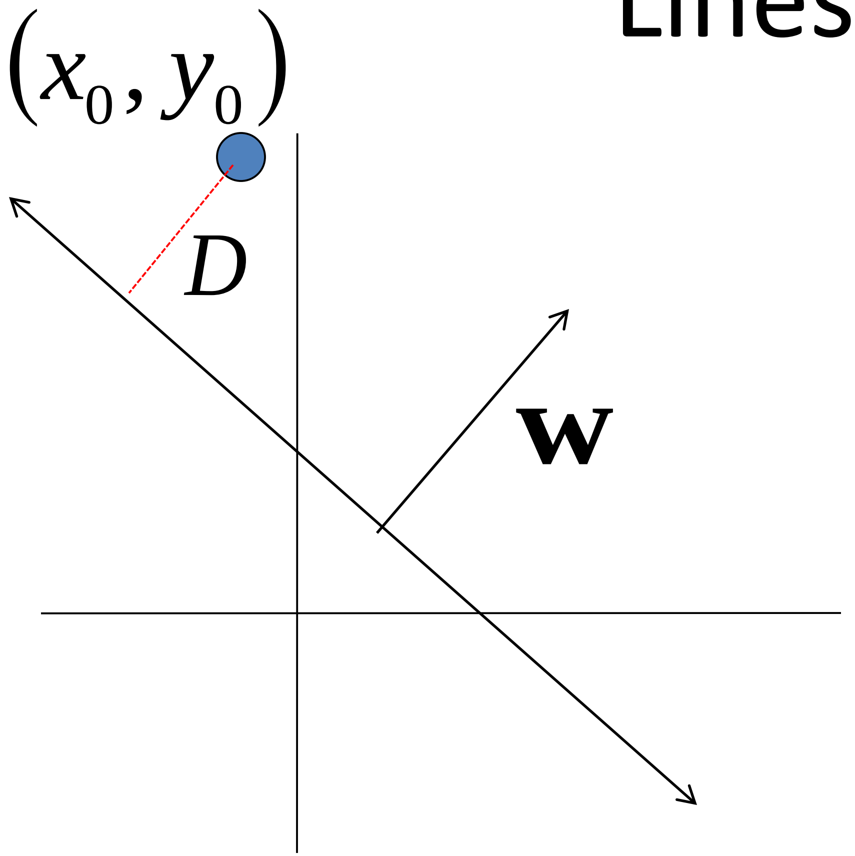
$$\Updownarrow$$

$$\mathbf{w} \cdot \mathbf{x} + b = 0$$

$$D = \frac{\left| a x_0 + c y_0 + b \right|}{\sqrt{a^2 + c^2}}$$

distance from point to line

Lines in R^2



Let $\mathbf{w} = \begin{bmatrix} a \\ c \end{bmatrix}$ $\mathbf{x} = \begin{bmatrix} x \\ y \end{bmatrix}$

$$ax + cy + b = 0$$

$$\Updownarrow$$

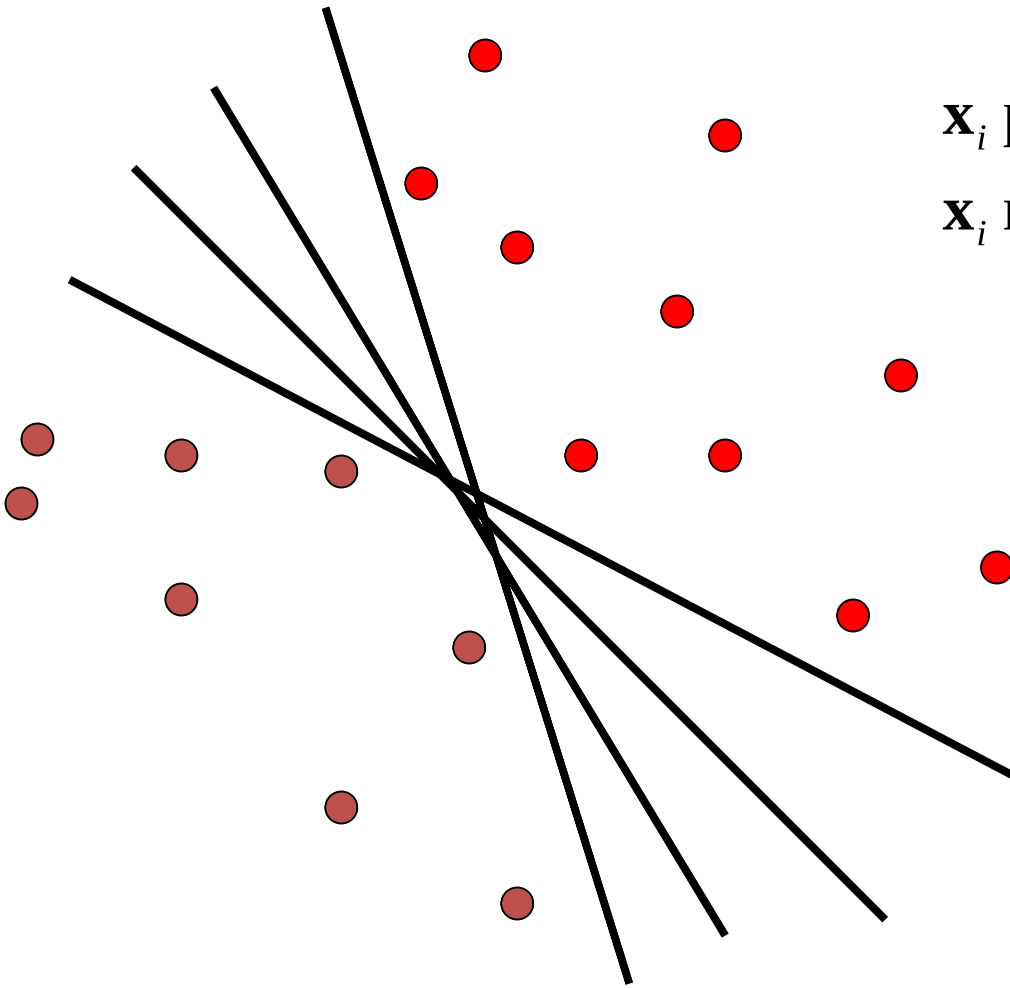
$$\mathbf{w} \cdot \mathbf{x} + b = 0$$

$$D = \frac{|ax_0 + cy_0 + b|}{\sqrt{a^2 + c^2}} = \frac{\mathbf{w}^{\mathrm{T}}\mathbf{x} + b}{\|\mathbf{w}\|}$$

distance from point to line

Linear classifiers

- Find linear function to separate positive and negative examples

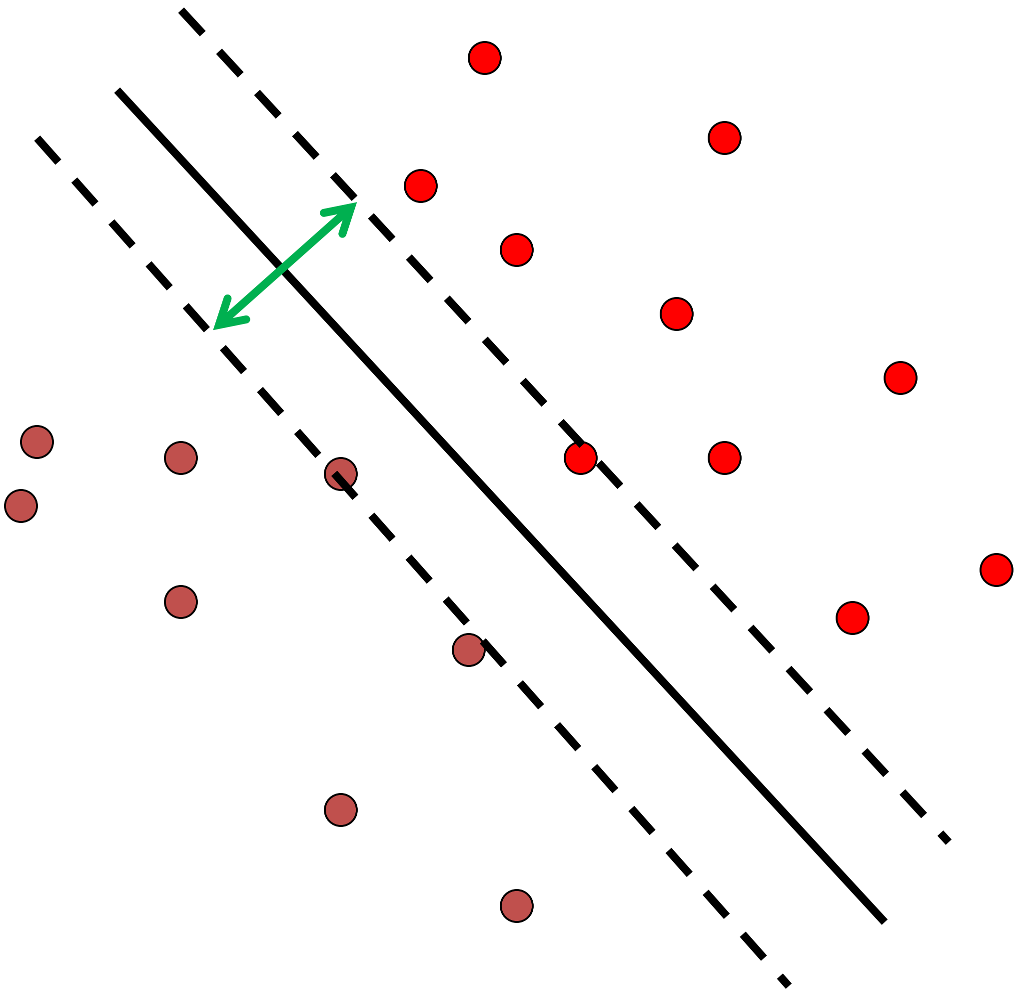


$$\mathbf{x}_i \text{ positive}: \quad \mathbf{x}_i \cdot \mathbf{w} + b \geq 0$$

$$\mathbf{x}_i \text{ negative}: \quad \mathbf{x}_i \cdot \mathbf{w} + b < 0$$

Which line
is best?

Support Vector Machines (SVMs)

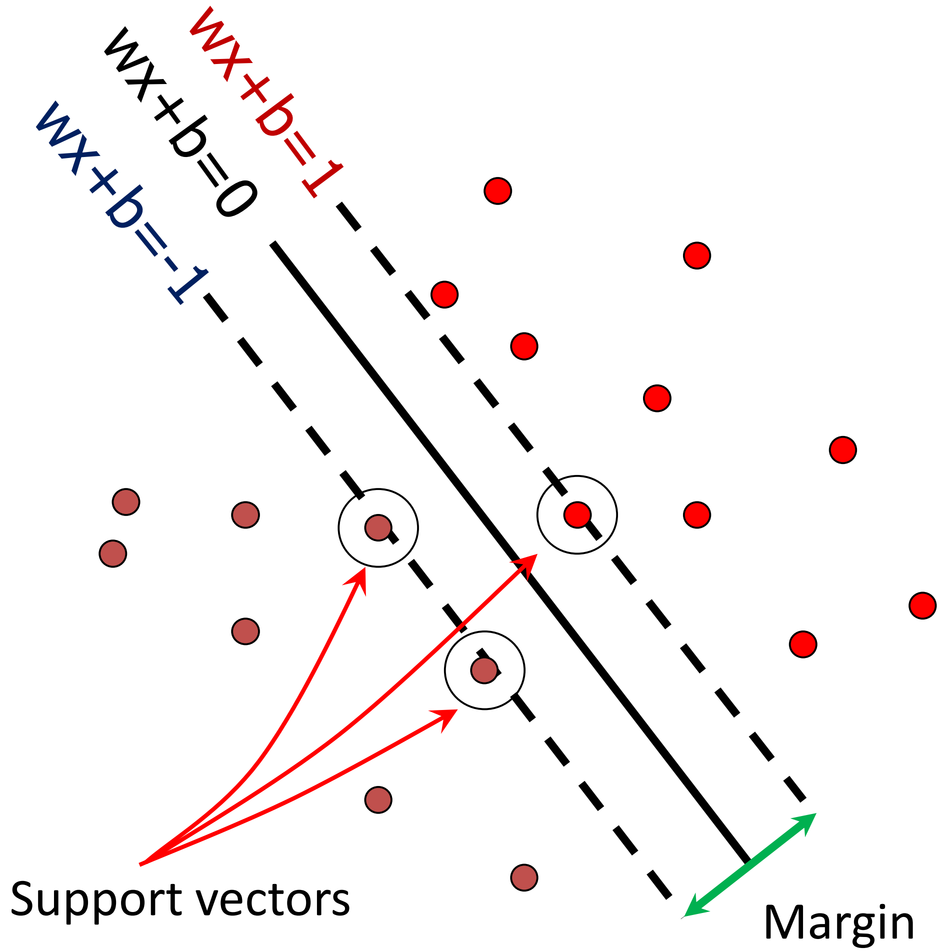


- Discriminative classifier based on *optimal separating line (for 2d case)*

- Maximize the *margin* between the positive and negative training examples

Support vector machines

- Want line that maximizes the margin.



$\mathbf{x}_i$ positive $(y_i = 1)$: $\quad \mathbf{x}_i \cdot \mathbf{w} + b \geq 1$

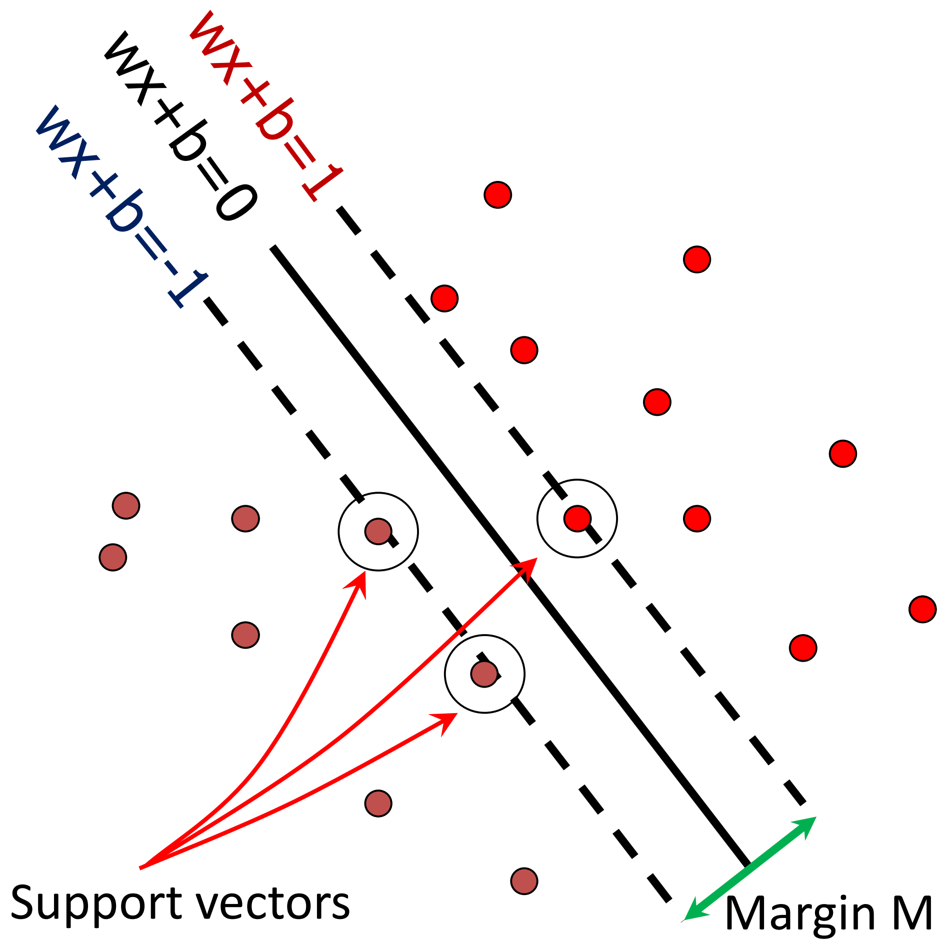
$\mathbf{x}_i$ negative $(y_i = -1)$: $\quad \mathbf{x}_i \cdot \mathbf{w} + b \leq -1$

For support, vectors, $\quad \mathbf{x}_i \cdot \mathbf{w} + b = \pm 1$

C. Burges, [A Tutorial on Support Vector Machines for Pattern Recognition](), Data Mining and Knowledge Discovery, 1998

Support vector machines

- Want line that maximizes the margin.



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For support, vectors, $\quad \mathbf{x}_i \cdot \mathbf{w} + b = \pm 1$

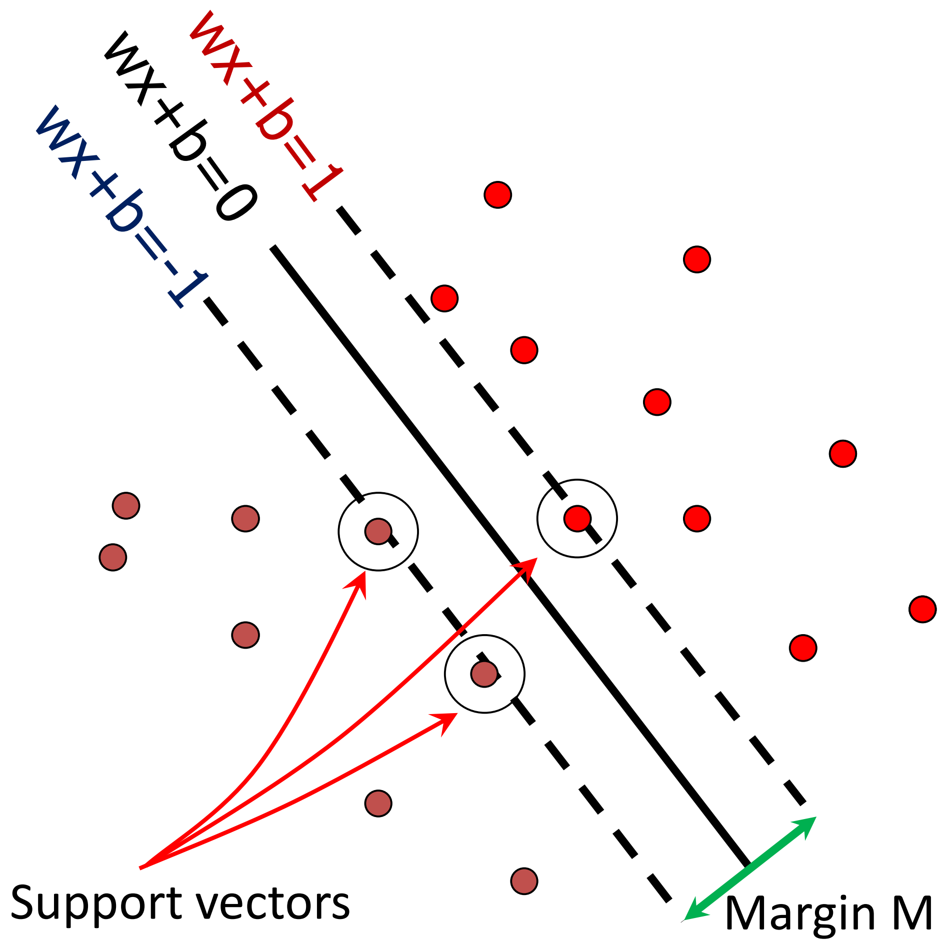
Distance between point and line: $\quad \dfrac{|\mathbf{x}_i \cdot \mathbf{w} + b|}{\|\mathbf{w}\|}$

For support vectors:

$$\frac{\mathbf{w}^T\mathbf{x} + b}{\|\mathbf{w}\|} = \frac{\pm 1}{\|\mathbf{w}\|} \qquad M = \left| \frac{1}{\|\mathbf{w}\|} - \frac{-1}{\|\mathbf{w}\|} \right| = \frac{2}{\|\mathbf{w}\|}$$

Support vector machines

- Want line that maximizes the margin.



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For support, vectors, $\quad \mathbf{x}_i \cdot \mathbf{w} + b = \pm 1$

Distance between point and line: $\quad \dfrac{|\mathbf{x}_i \cdot \mathbf{w} + b|}{\|\mathbf{w}\|}$

Therefore, the margin is $2 / \|\mathbf{w}\|$

Finding the maximum margin line

1. Maximize margin $2/\|\mathbf{w}\|$
2. Correctly classify all training data points:

$$\mathbf{x}_i \text{ positive } (y_i = 1): \quad \mathbf{x}_i \cdot \mathbf{w} + b \geq 1$$

$$\mathbf{x}_i \text{ negative } (y_i = -1): \quad \mathbf{x}_i \cdot \mathbf{w} + b \leq -1$$

- *Quadratic optimization problem*:
- Minimize $\frac{1}{2}\mathbf{w}^T\mathbf{w}$

  Subject to $y_i(\mathbf{w}\cdot\mathbf{x}_i+b) \geq 1$

Finding the maximum margin line

- Solution: $\mathbf{w} = \sum_i \alpha_i y_i \mathbf{x}_i$

learned weight

Support vector

Finding the maximum margin line

- Solution: $\mathbf{w} = \sum_i \alpha_i y_i \mathbf{x}_i$

  $b = y_i - \mathbf{w} \cdot \mathbf{x}_i$ (for any support vector) $\mathbf{w} \cdot \mathbf{x} + b = \sum_i \alpha_i y_i \mathbf{x}_i \cdot \mathbf{x} + b$

- Classification function:

$$f(x) = \text{sign}\,(\mathbf{w} \cdot \mathbf{x} + \text{b})$$
$$= \text{sign}\left(\sum_i \alpha_i \mathbf{x}_i \cdot \mathbf{x} + b\right)$$

If f(x) < 0, classify as negative,
if f(x) > 0, classify as positive

C. Burges, A Tutorial on Support Vector Machines for Pattern Recognition, Data Mining and Knowledge Discovery, 1998

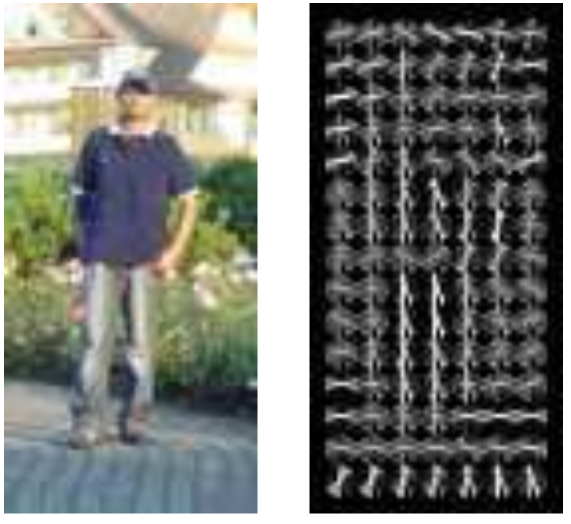
Questions

- **What if the features are not 2d?**
- What if the data is not linearly separable?
- What if we have more than just two categories?

Questions

- What if the features are not 2d?
  - Generalizes to d-dimensions – replace line with "hyperplane"
- What if the data is not linearly separable?
- What if we have more than just two categories?

Person detection with HoG's & linear SVM's



- Map each grid cell in the input window to a histogram counting the gradients per orientation.
- Train a linear SVM using training set of pedestrian vs. non-pedestrian windows.

Code available:
http://pascal.inrialpes.fr/soft/olt/

Dalal & Triggs, CVPR 2005

Person detection with HoG's & linear SVM's

- Histograms of Oriented Gradients for Human Detection, [Navneet Dalal](), [Bill Triggs](), International Conference on Computer Vision & Pattern Recognition - June 2005
- http://lear.inrialpes.fr/pubs/2005/DT05/

Histograms of oriented gradients

Histograms of oriented gradients

SIFT, D. Lowe, ICCV 1999

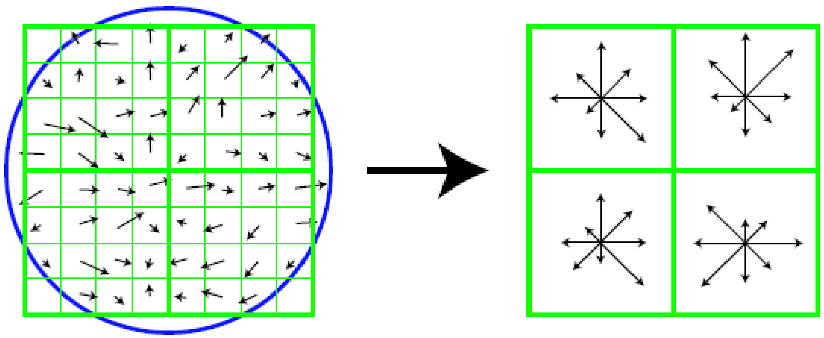
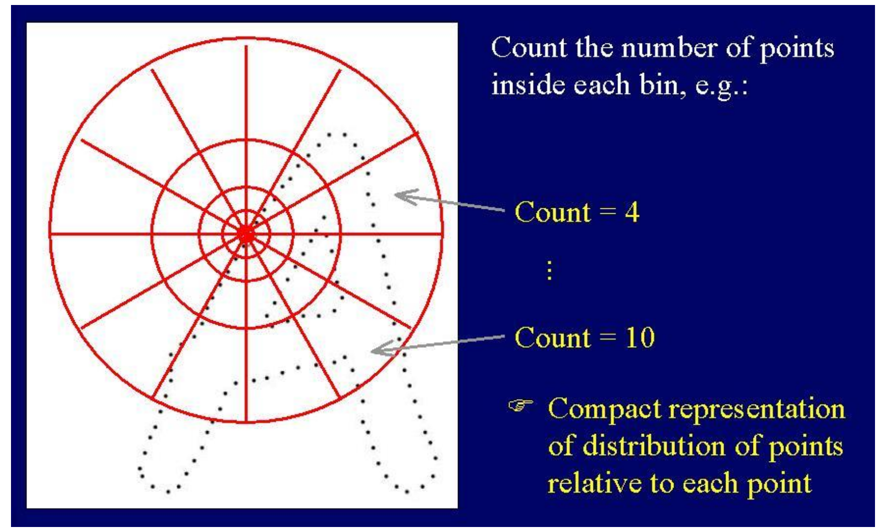


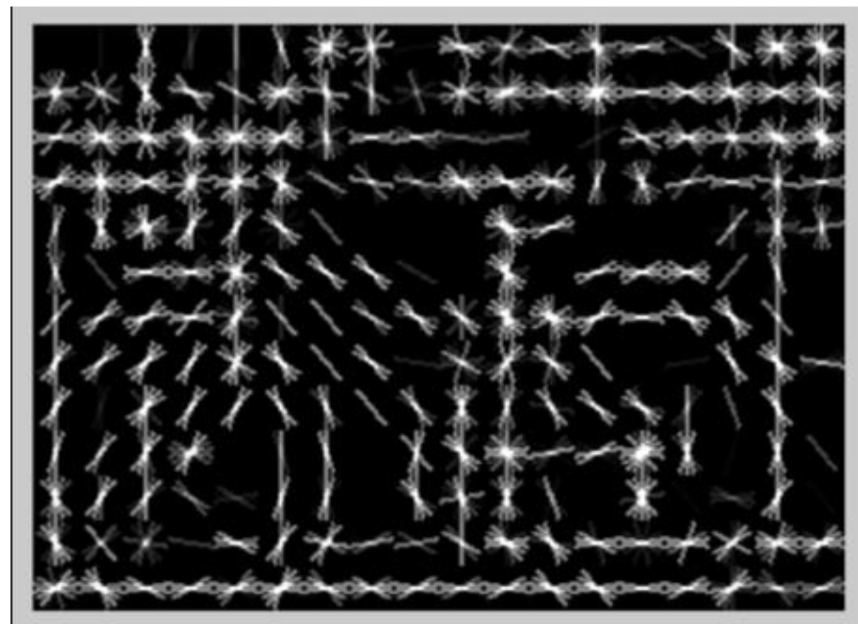
Image gradients

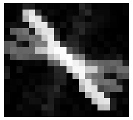
Keypoint descriptor

Shape context

Belongie, Malik, Puzicha, NIPS 2000







Source: Deva Ramanan

Histograms of Oriented Gradients for Human Detection

Navneet Dalal and Bill Triggs

INRIA Rhône-Alps, 655 avenue de l'Europe, Montbonnot 38334, France
{Navneet.Dalal,Bill.Triggs}@inrialpes.fr, http://lear.inrialpes.fr

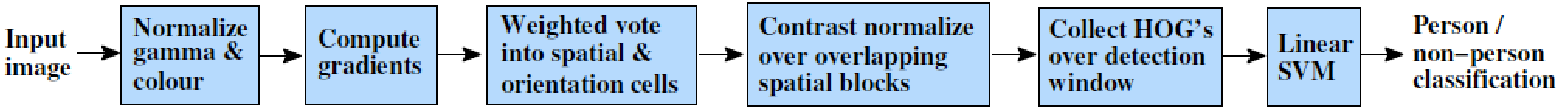


Figure 1. An overview of our feature extraction and object detection chain. The detector window is tiled with a grid of overlapping blocks in which Histogram of Oriented Gradient feature vectors are extracted. The combined vectors are fed to a linear SVM for object/non-object classification. The detection window is scanned across the image at all positions and scales, and conventional non-maximum suppression is run on the output pyramid to detect object instances, but this paper concentrates on the feature extraction process.

Histograms of Oriented Gradients for Human Detection

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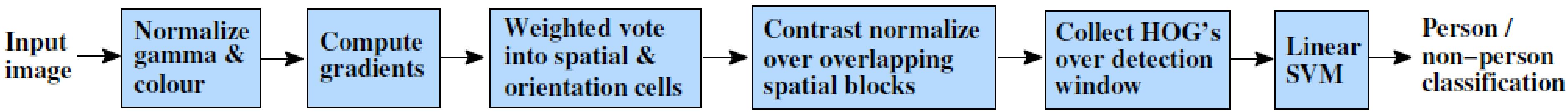

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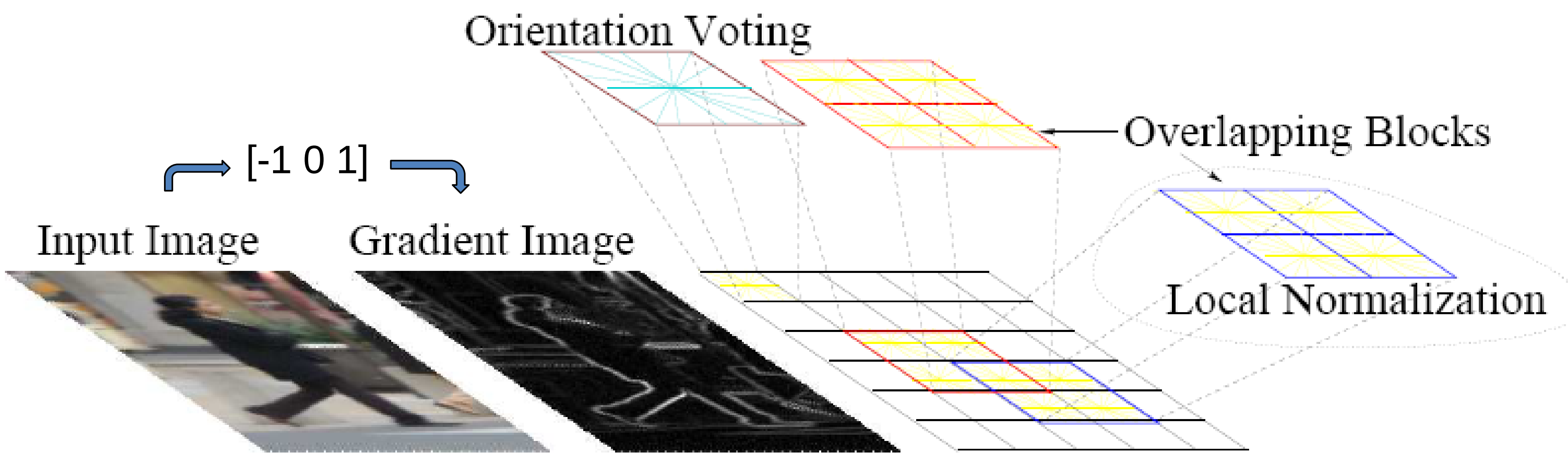


SVM

A Support Vector Machine (SVM) learns a classifier with the form:

$$H(x) = \sum_{m=1}^{M} a_m y_m k(x, x_m)$$

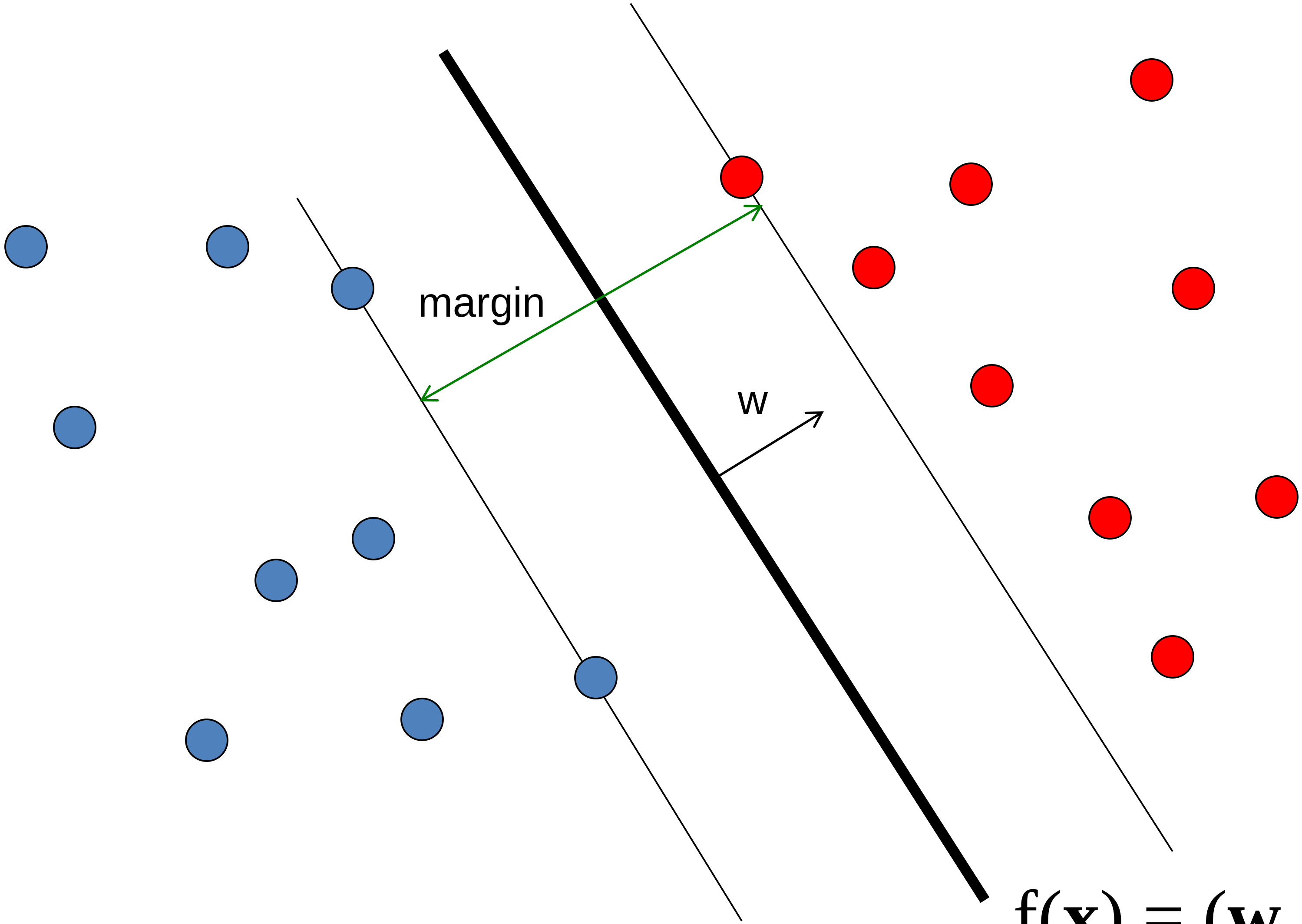
Where $\{x_m, y_m\}$, for m = 1 . . .M, are the training data with x_m being the input feature vector and $y_m = +1,-1$ the class label. $k(x, x_m)$ is the kernel and it can be any symmetric function satisfying the Mercer Theorem.

The classification is obtained by thresholding the value of H(x).

There is a large number of possible kernels, each yielding a different family of decision boundaries:

- Linear kernel: $k(x, x_m) = x^T x_m$
- Radial basis function: $k(x, x_m) = \exp(-|x - x_m|^2/\sigma^2)$.
- Histogram intersection: $k(x,x_m) = \text{sum}_i(\min(x(i), x_m(i)))$

Linear SVM

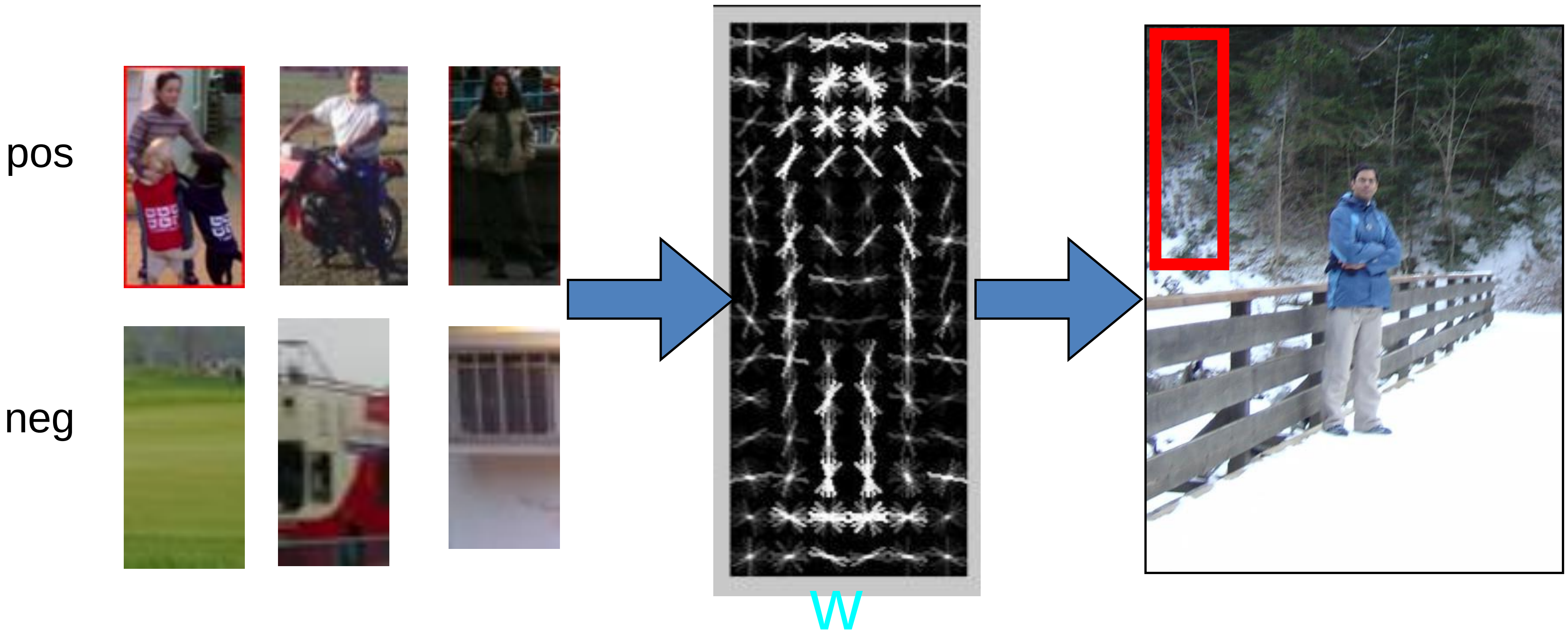


$$f(\mathbf{x}) = (\mathbf{w} \, . \, \mathbf{x} + b)$$

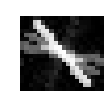
Scanning-window templates

Dalal and Triggs CVPR05 (HOG)

Papageorgiou and Poggio ICIP99 (wavelets)



w = weights for orientation and spatial bins



$w \cdot x > 0$

Train with a linear classifier (perceptron, logistic regression, SVMs...)

Source: Deva Ramanan

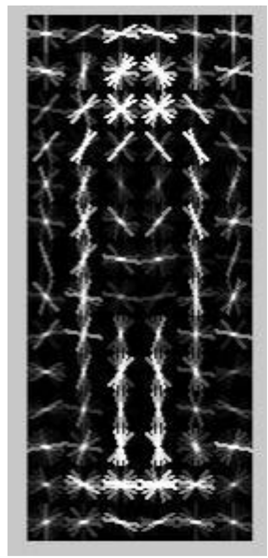
How to interpret positive and negative weights?

$$w \cdot x > 0$$

$$(w_{pos} - w_{neg}) \cdot x > 0$$

$$w_{pos} \cdot x > w_{neg} \cdot x$$

Pedestrian template



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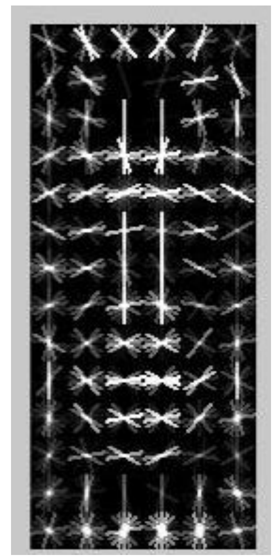


Pedestrian background template

w_{pos}, w_{neg} = weighted average of positive, negative support vectors

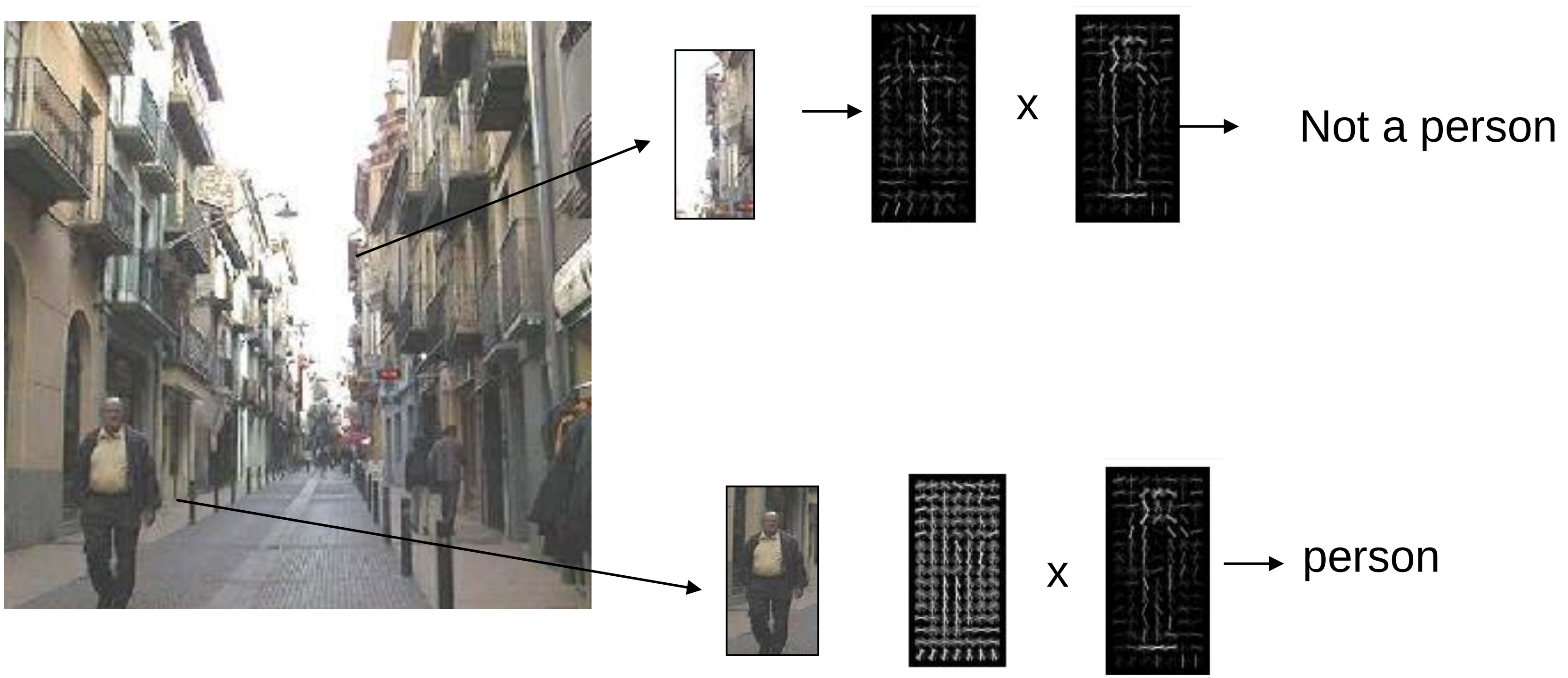
Right approach is to compete pedestrian, pillar, doorway... models

Background class is hard to model - easier to penalize particular vertical edges

Source: Deva Ramanan

Histograms of oriented gradients

Dalal & Trigs, 2006



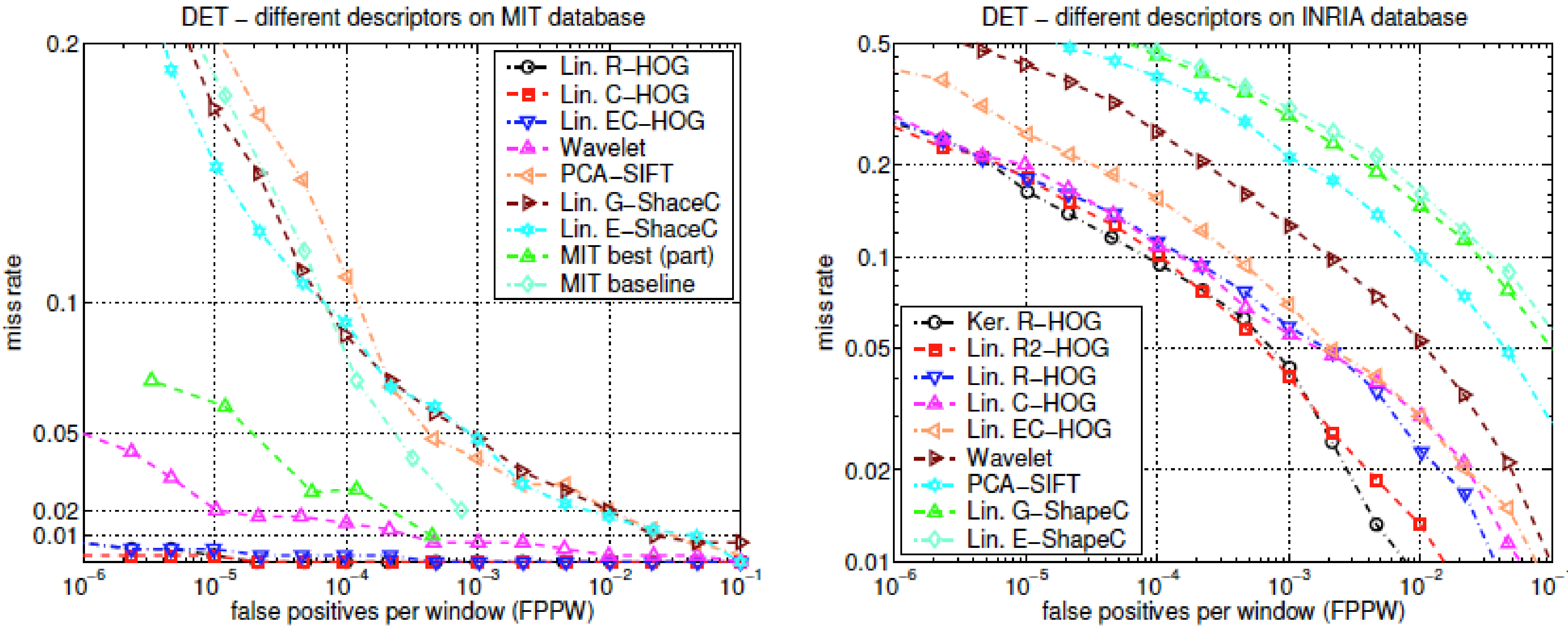


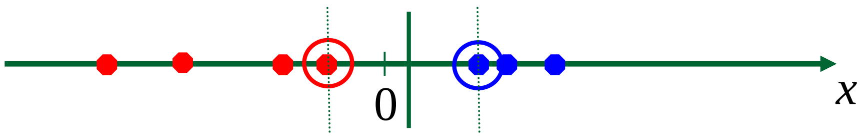
Figure 3. The performance of selected detectors on (left) MIT and (right) INRIA data sets. See the text for details.

Questions

- What if the features are not 2d?
- **What if the data is not linearly separable?**
- What if we have more than just two categories?

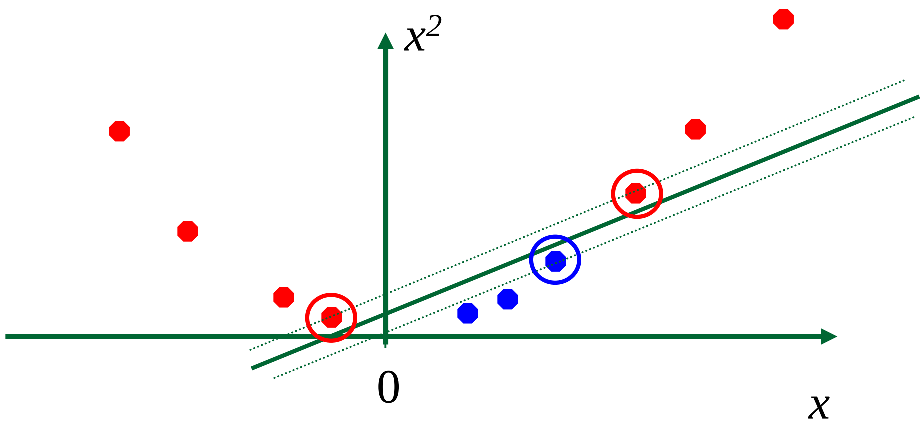
Non-linear SVMs

- Datasets that are linearly separable with some noise work out great:



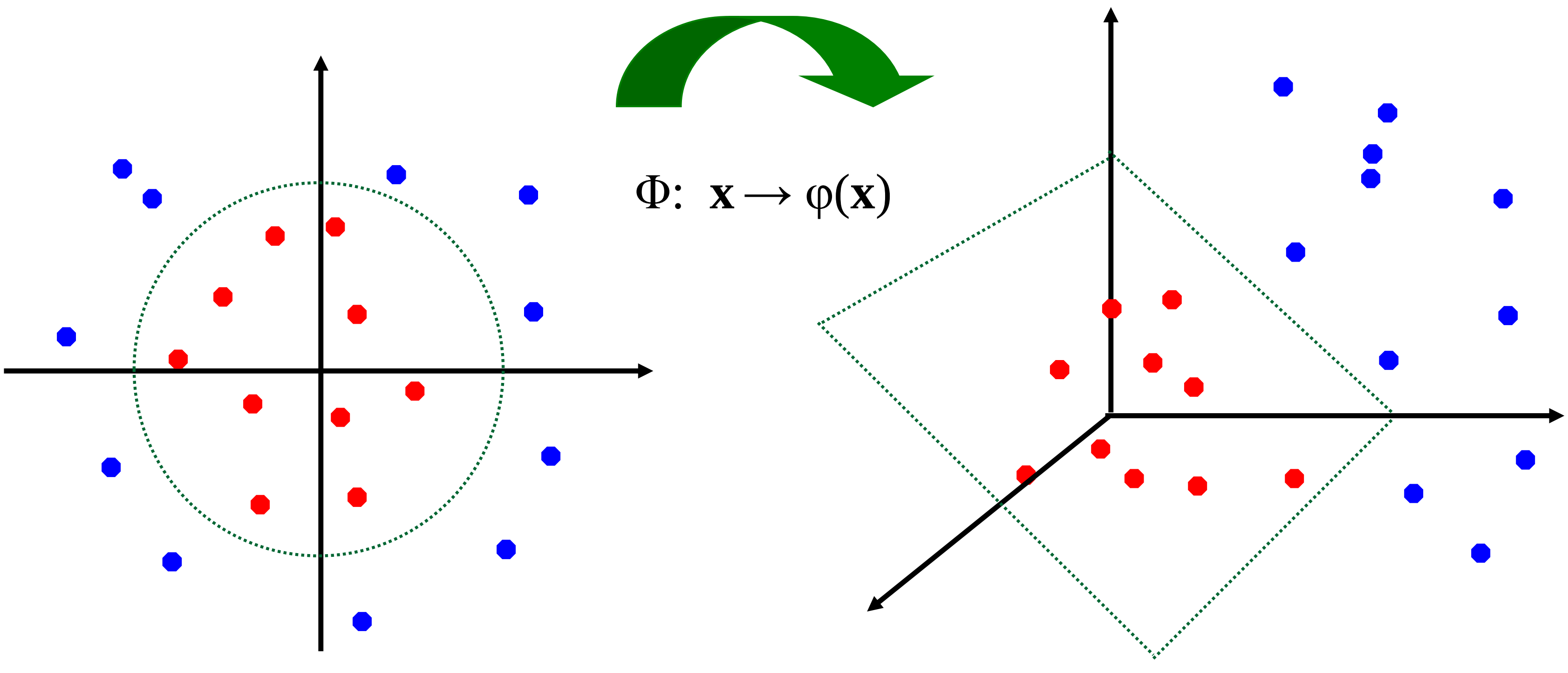
- But what are we going to do if the dataset is just too hard?

- How about… mapping data to a higher-dimensional space:



Non-linear SVMs: feature spaces

- General idea: the original input space can be mapped to some higher-dimensional feature space where the training set is separable:



Slide from Andrew Moore's tutorial: http://www.autonlab.org/tutorials/svm.html

The "Kernel Trick"

- The linear classifier relies on dot product between vectors $K(x_i,x_j)=x_i^T x_j$

- If every data point is mapped into high-dimensional space via some transformation Φ: $x \rightarrow \phi(x)$, the dot product becomes:

$$K(x_i,x_j)= \phi(x_i)^T\phi(x_j)$$

- A *kernel function* is similarity function that corresponds to an inner product in some expanded feature space.

Slide from Andrew Moore's tutorial: http://www.autonlab.org/tutorials/svm.html

Example

2-dimensional vectors $\mathrm{x}=[x_1 \;\; x_2]$;

let $K(\mathrm{x_i},\mathrm{x_j})=(1 + \mathrm{x_i}^T\mathrm{x_j})^2$

Need to show that $K(\mathrm{x_i},\mathrm{x_j})= \varphi(\mathrm{x_i})^T\varphi(\mathrm{x_j})$:

$$K(\mathrm{x_i},\mathrm{x_j})=(1 + \mathrm{x_i}^T\mathrm{x_j})^2,$$

$$= 1+ x_{i1}^2x_{j1}^2 + 2\, x_{i1}x_{j1}\, x_{i2}x_{j2}+ x_{i2}^2x_{j2}^2 + 2x_{i1}x_{j1} + 2x_{i2}x_{j2}$$

$$= [1 \;\; x_{i1}^2 \;\; \sqrt{2}\, x_{i1}x_{i2} \;\; x_{i2}^2 \;\; \sqrt{2}x_{i1} \;\; \sqrt{2}x_{i2}]^T$$

$$[1 \;\; x_{j1}^2 \;\; \sqrt{2}\, x_{j1}x_{j2} \;\; x_{j2}^2 \;\; \sqrt{2}x_{j1} \;\; \sqrt{2}x_{j2}]$$

$$= \varphi(\mathrm{x_i})^T\varphi(\mathrm{x_j}),$$

where $\varphi(\mathrm{x}) = [1 \;\; x_1^2 \;\; \sqrt{2}\, x_1x_2 \;\; x_2^2 \;\; \sqrt{2}x_1 \;\; \sqrt{2}x_2]$

from Andrew Moore's tutorial: http://www.autonlab.org/tutorials/svm.html

Nonlinear SVMs

- *The kernel trick*: instead of explicitly computing the lifting transformation $\boldsymbol{\varphi}(\mathbf{x})$, define a kernel function K such that

$$K(\mathbf{x}_i,\mathbf{x}_j) = \boldsymbol{\varphi}(\mathbf{x}_i) \cdot \boldsymbol{\varphi}(\mathbf{x}_j)$$

- This gives a nonlinear decision boundary in the original feature space:

$$\sum_i \alpha_i y_i K(\mathbf{x}_i, \mathbf{x}) + b$$

Examples of kernel functions

- Linear:

$$K(x_i, x_j) = x_i^T x_j$$

- Gaussian RBF:

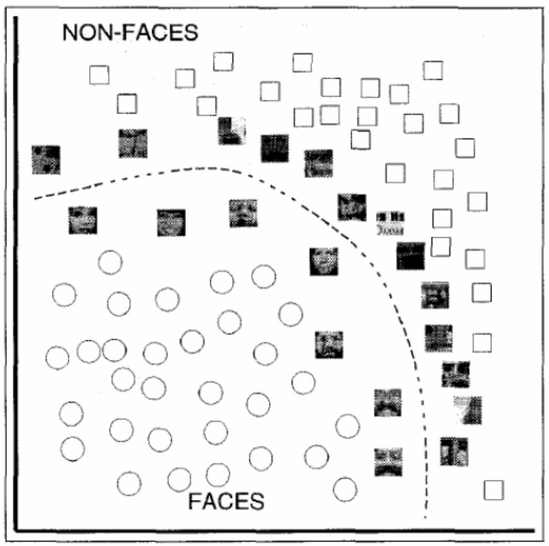
$$K(x_i, x_j) = \exp\left(-\frac{\left\| x_i - x_j \right\|^2}{2\sigma^2}\right)$$

- Histogram intersection:

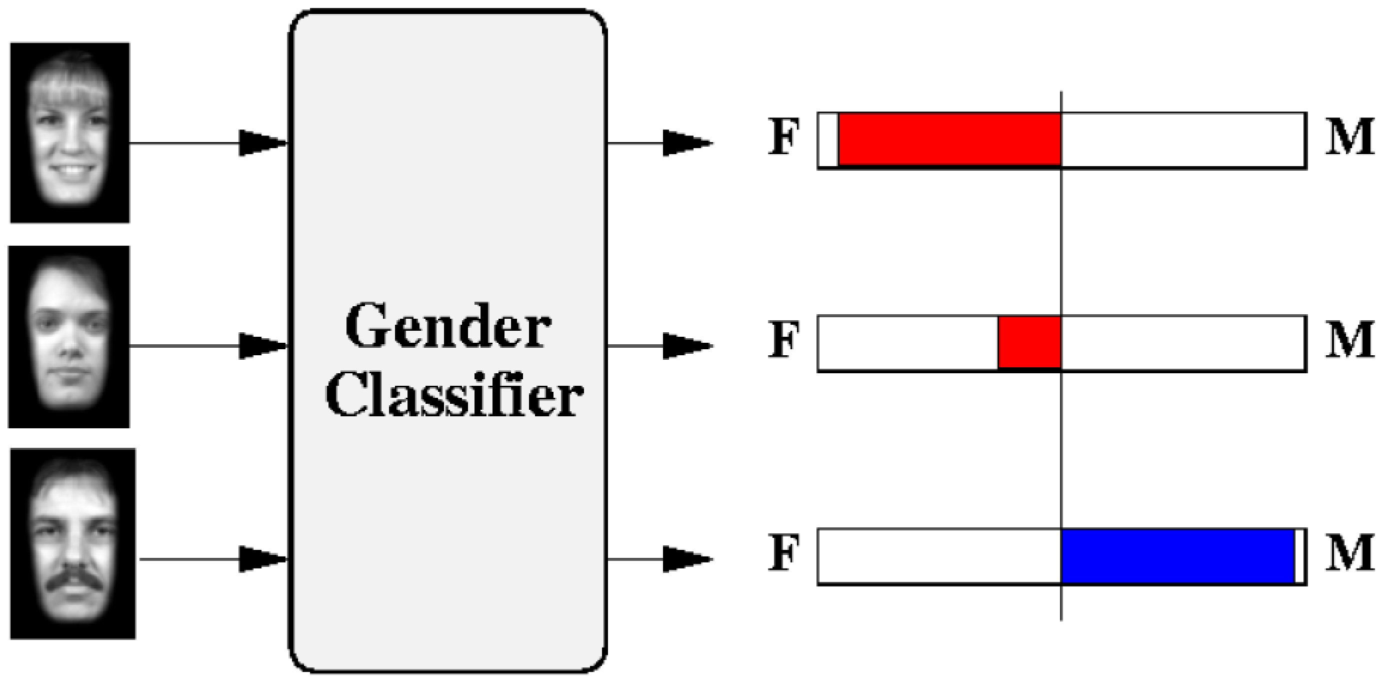
$$K(x_i, x_j) = \sum_k \min(x_i(k), x_j(k))$$

SVMs for recognition

1. Define your representation for each example.
2. Select a kernel function.
3. Compute pairwise kernel values between labeled examples
4. Use this “kernel matrix” to solve for SVM support vectors & weights.
5. To classify a new example: compute kernel values between new input and support vectors, apply weights, check sign of output.



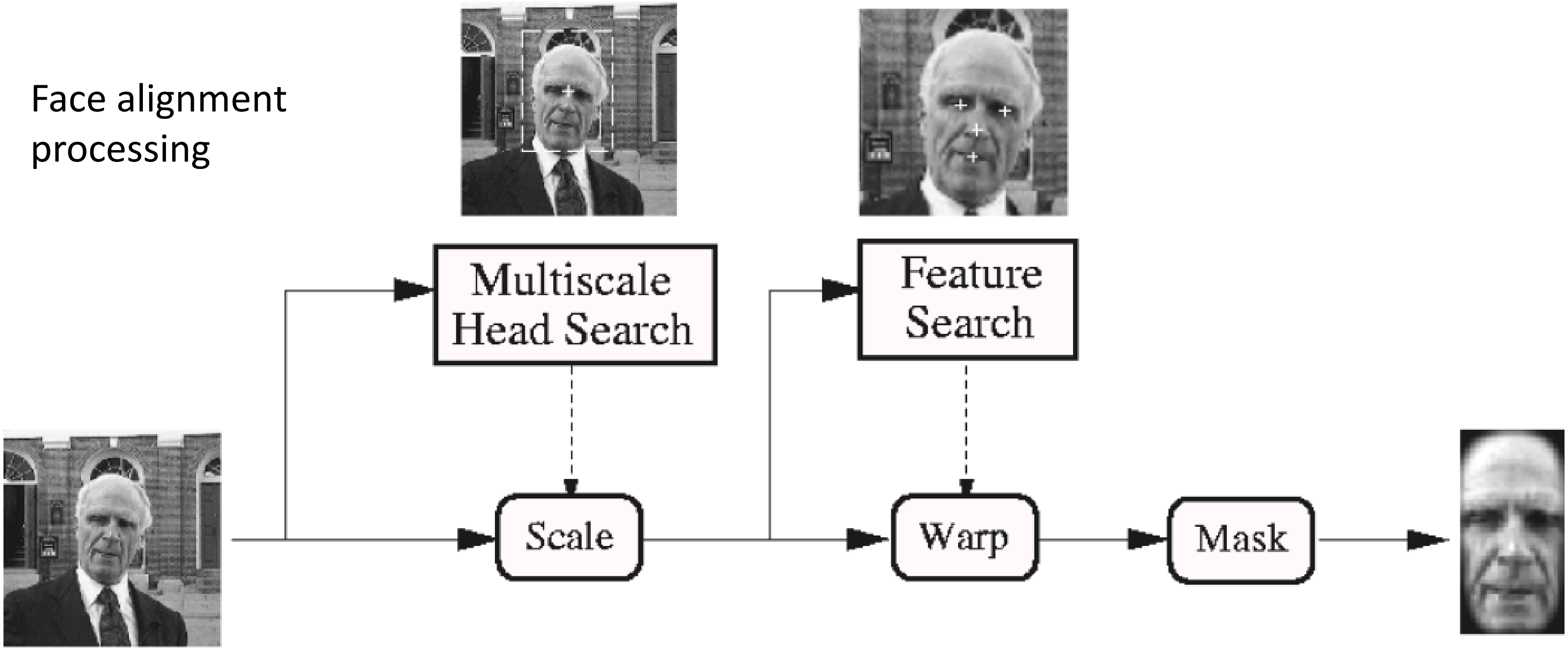
Example: learning gender with SVMs



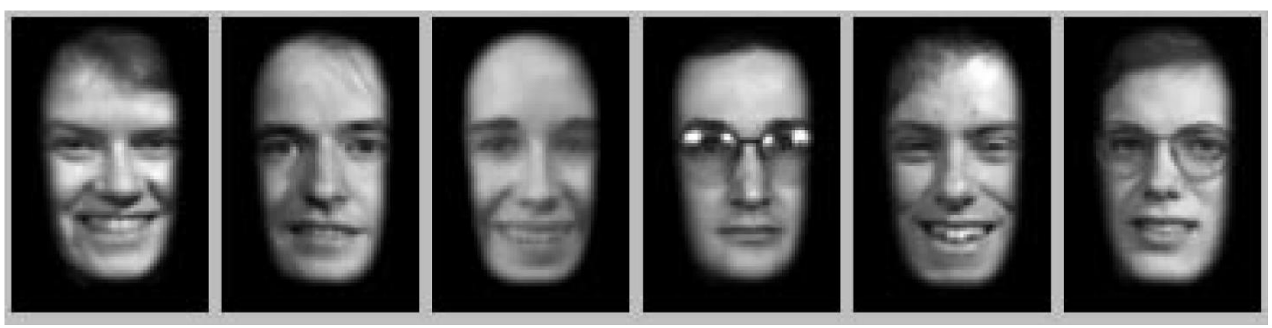
Moghaddam and Yang, Learning Gender with Support Faces, TPAMI 2002.

Moghaddam and Yang, Face & Gesture 2000.

Face alignment processing



Processed faces



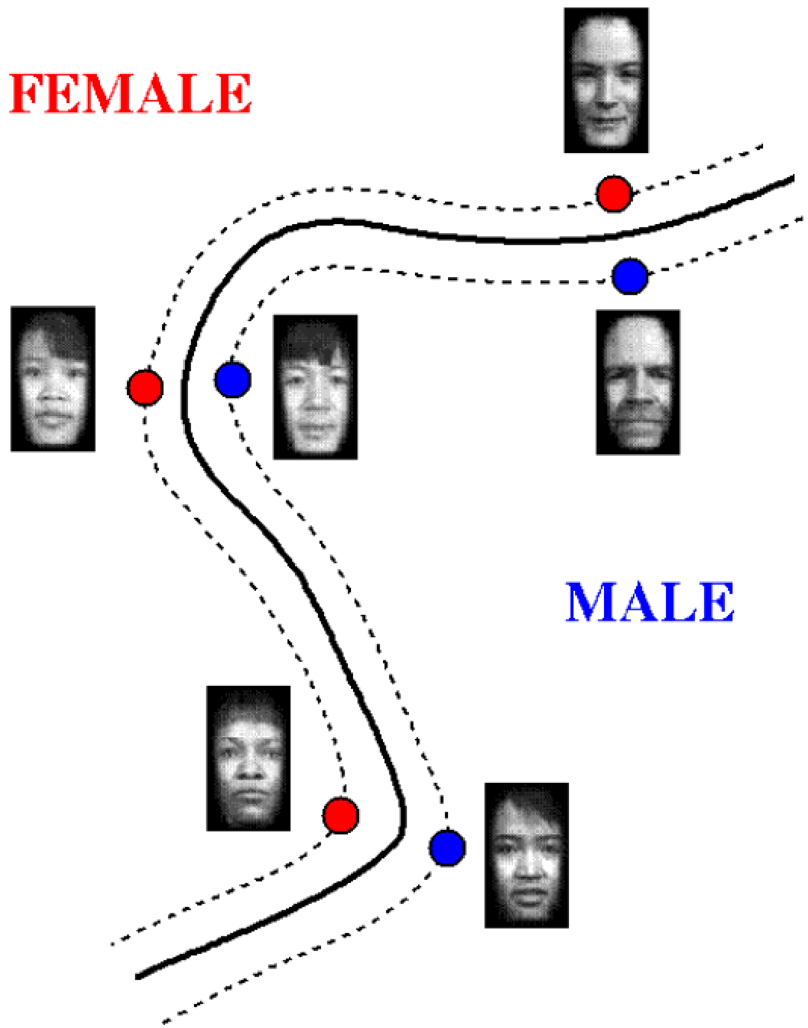
Moghaddam and Yang, Learning Gender with Support Faces, TPAMI 2002.

Learning gender with SVMs

- Training examples:
  - 1044 males
  - 713 females
- Experiment with various kernels, select Gaussian RBF

$$K(\mathbf{x_i}, \mathbf{x_j}) = \exp\left(-\frac{\left\|\mathbf{x_i} - \mathbf{x_j}\right\|^2}{2\sigma^2}\right)$$

Support Faces



Moghaddam and Yang, Learning Gender with Support Faces, TPAMI 2002.

Classifier Performance

Classifier	Error Rate		
	Overall	Male	Female
SVM with RBF kernel	**3.38%**	**2.05%**	**4.79%**
SVM with cubic polynomial kernel	**4.88%**	**4.21%**	**5.59%**
Large Ensemble of RBF	5.54%	4.59%	6.55%
Classical RBF	7.79%	6.89%	8.75%
Quadratic classifier	10.63%	9.44%	11.88%
Fisher linear discriminant	13.03%	12.31%	13.78%
Nearest neighbor	27.16%	26.53%	28.04%
Linear classifier	58.95%	58.47%	59.45%

Moghaddam and Yang, Learning Gender with Support Faces, TPAMI 2002.

Gender perception experiment: How well can humans do?

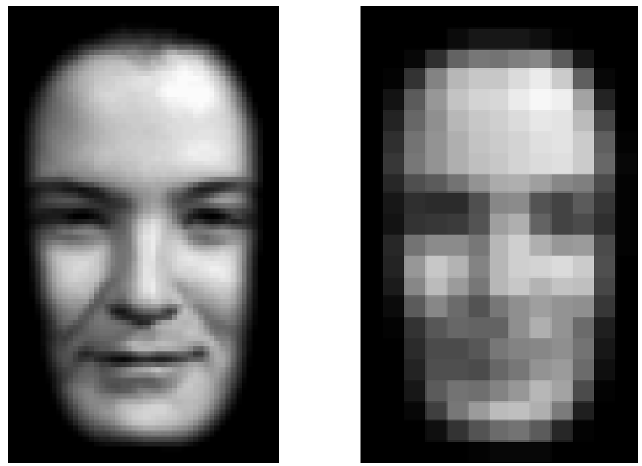
- Subjects:
  - 30 people (22 male, 8 female)
  - Ages mid-20’s to mid-40’s
- Test data:
  - 254 face images (6 males, 4 females)
  - Low res and high res versions
- Task:
  - Classify as male or female, forced choice
  - No time limit

Moghaddam and Yang, Face & Gesture 2000.

Gender perception experiment: How well can humans do?

Stimuli →

84 x 48   21 x 12



N = 4032   N = 252

Results →

High-Res	Low-Res
6.54%	30.7%
Error	Error

$\sigma = 3.7\%$

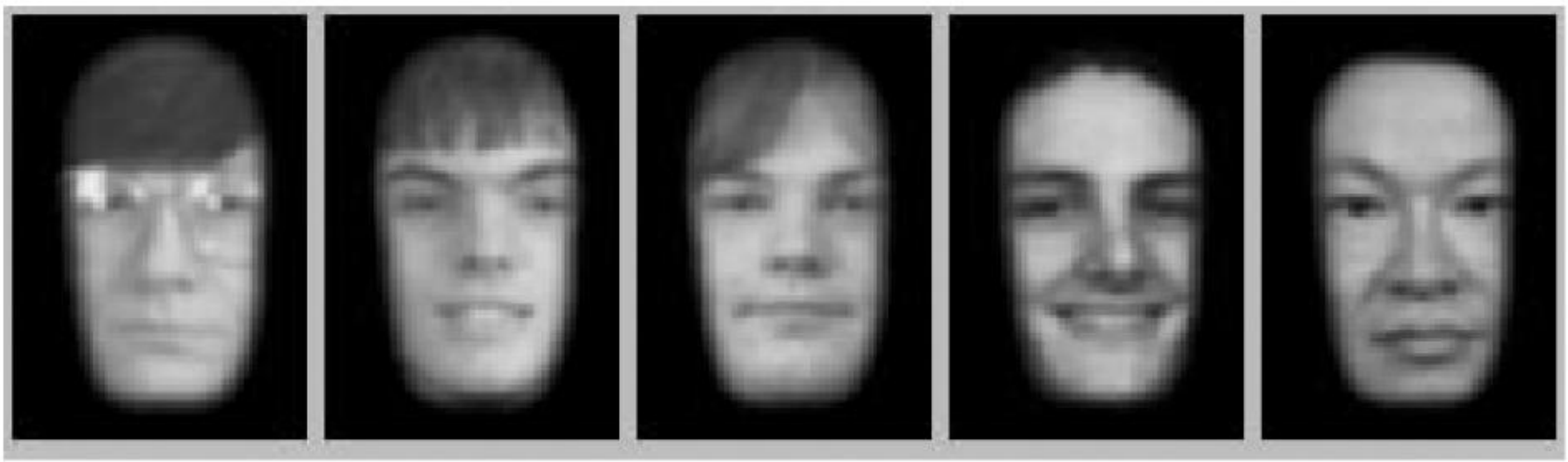
Moghaddam and Yang, Face & Gesture 2000.

Human vs. Machine

Figure 6. SVM vs. Human performance

- SVMs performed better than any single human test subject, at either resolution

Hardest examples for humans



Top five human misclassifications

Moghaddam and Yang, Face & Gesture 2000.

Questions

- What if the features are not 2d?
- What if the data is not linearly separable?
- **What if we have more than just two categories?**

Multi-class SVMs

- Achieve multi-class classifier by combining a number of binary classifiers
- **One vs. all**
  - Training: learn an SVM for each class vs. the rest
  - Testing: apply each SVM to test example and assign to it the class of the SVM that returns the highest decision value
- **One vs. one**
  - Training: learn an SVM for each pair of classes
  - Testing: each learned SVM "votes" for a class to assign to the test example

SVMs: Pros and cons

- Pros
  - Many publicly available SVM packages: http://www.kernel-machines.org/software
  - http://www.csie.ntu.edu.tw/~cjlin/libsvm/
  - Kernel-based framework is very powerful, flexible
  - Often a sparse set of support vectors – compact at test time
  - Work very well in practice, even with very small training sample sizes
- Cons
  - No “direct” multi-class SVM, must combine two-class SVMs
  - Can be tricky to select best kernel function for a problem
  - Computation, memory
    - During training time, must compute matrix of kernel values for every pair of examples
    - Learning can take a very long time for large-scale problems

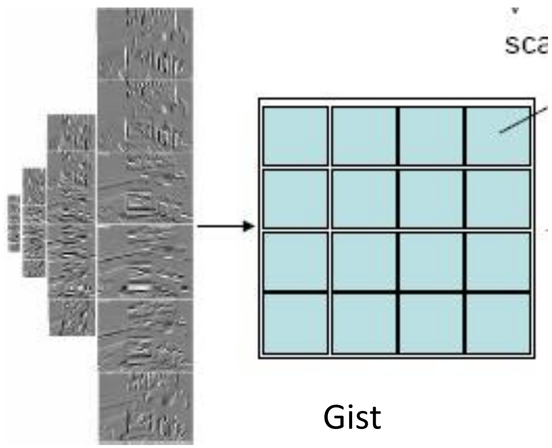
Adapted from Lana Lazebnik

Summary

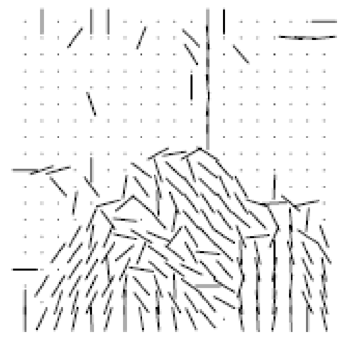
- Discriminative classifiers
  – Boosting
  – Nearest neighbors
  – Support vector machines

- Useful for object recognition when combined with “window-based” or holistic appearance descriptors

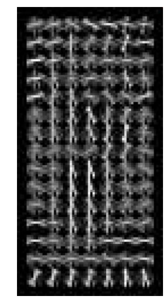
Global window-based appearance representations



Gist



Map of local orientations

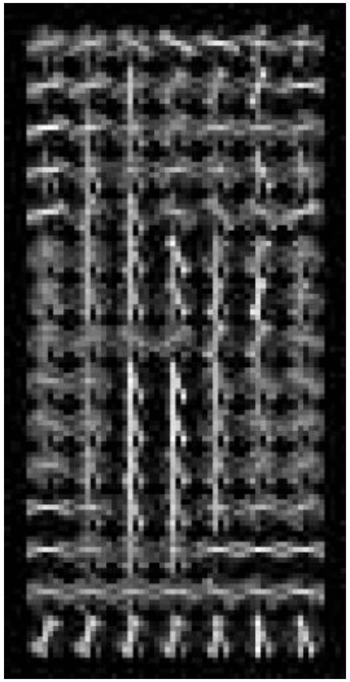


Histograms of oriented gradients

- These examples are truly global; each pixel in the window contributes to the representation.
- Classifier can account for relative relevance…
- *When might this not be ideal?*

Kristen Grauman

Generic category recognition: representation choice



Window-based

Part-based