Secret Sharing (Threshold) Schemes

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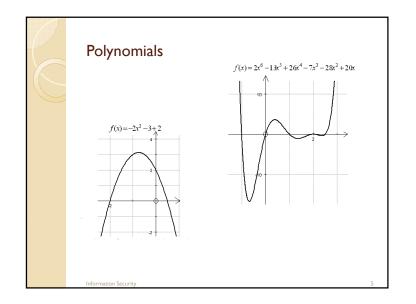
Secret Sharing in Digital World

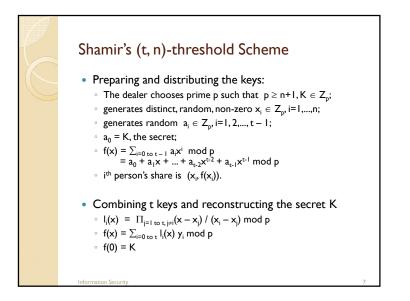
- How would you distribute a secret among n parties, such that only t or more of them together can reconstruct it.
 - Answer: A (t, n)-threshold scheme
 - Create n keys
 - Reveal the secret by using t of the keys
- Some applications:
- Storage of sensitive cryptographic keys
- Command & control of nuclear weapons

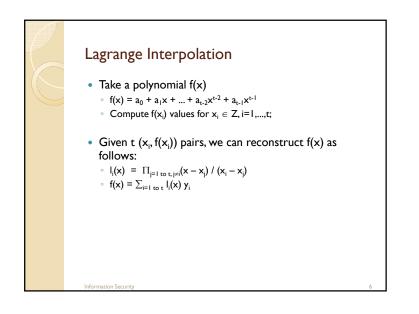
Secret Sharing in Real World • A bank safe can be protected with a combination of locks, keys.

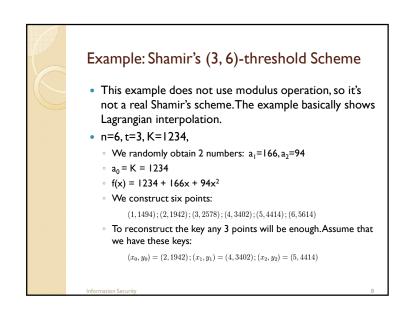
A Secret Sharing Scheme Example: An (n, n)-threshold scheme: To share a k-bit secret, the dealer D generates n − 1 random k-bit numbers (shares) y₁ where i = 1, 2,..., n − 1, y_n = K ⊕ y₁ ⊕ y₂ ⊕ ... ⊕ y_{n-1}, gives the share y₁ to party P_i. This is a "perfect" SSS: A coalition of less than t can not obtain information about the secret. Q: How to generalize to arbitrary (t, n)?

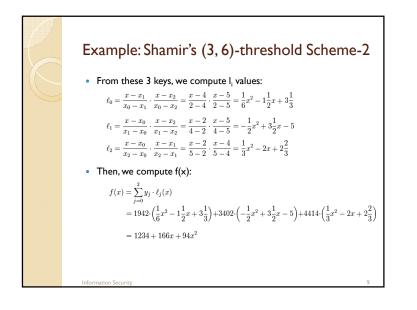
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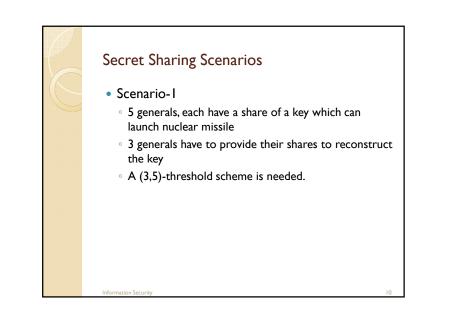












Secret Sharing Scenarios

• Scenario-2

- A bank branch with 10 bank tellers and a manager
- 7 tellers or the manager with 4 tellers can open the safe
- How do you define the threshold schemes?
- (7,13)-threshold scheme: I key for tellers, 3 keys for manager
- (7,10)-threshold scheme (1 key for each teller)
 (4,10)-threshold scheme (1 key for each teller) and (2,2)-threshold scheme (1 key for manager, the other key comes from (4,10) scheme)

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