

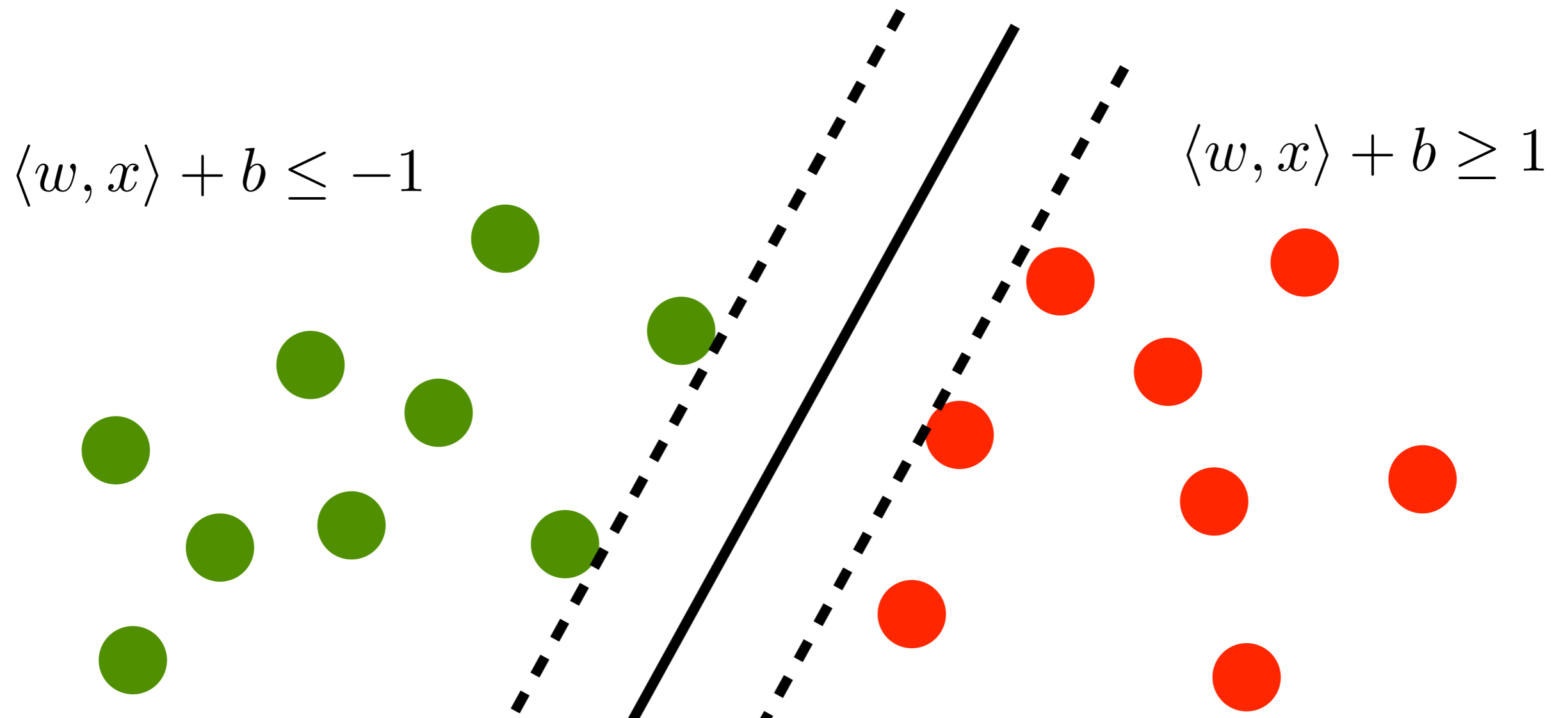
# AIN311

## Fundamentals of Machine Learning

### Lecture 16: Soft Margin Classification Multi-class SVMs Kernels



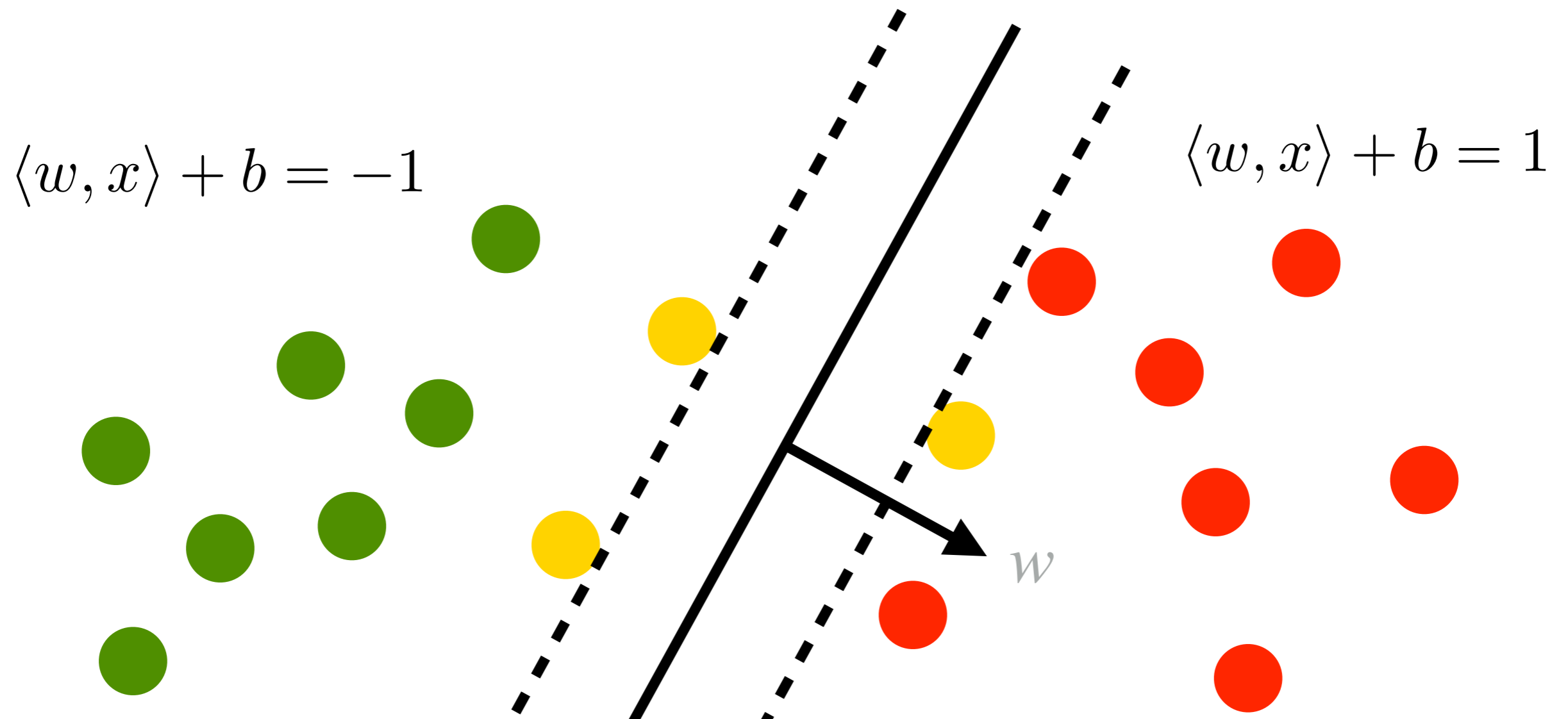
# Last time... Support Vector Machines



linear function

$$f(x) = \langle w, x \rangle + b$$

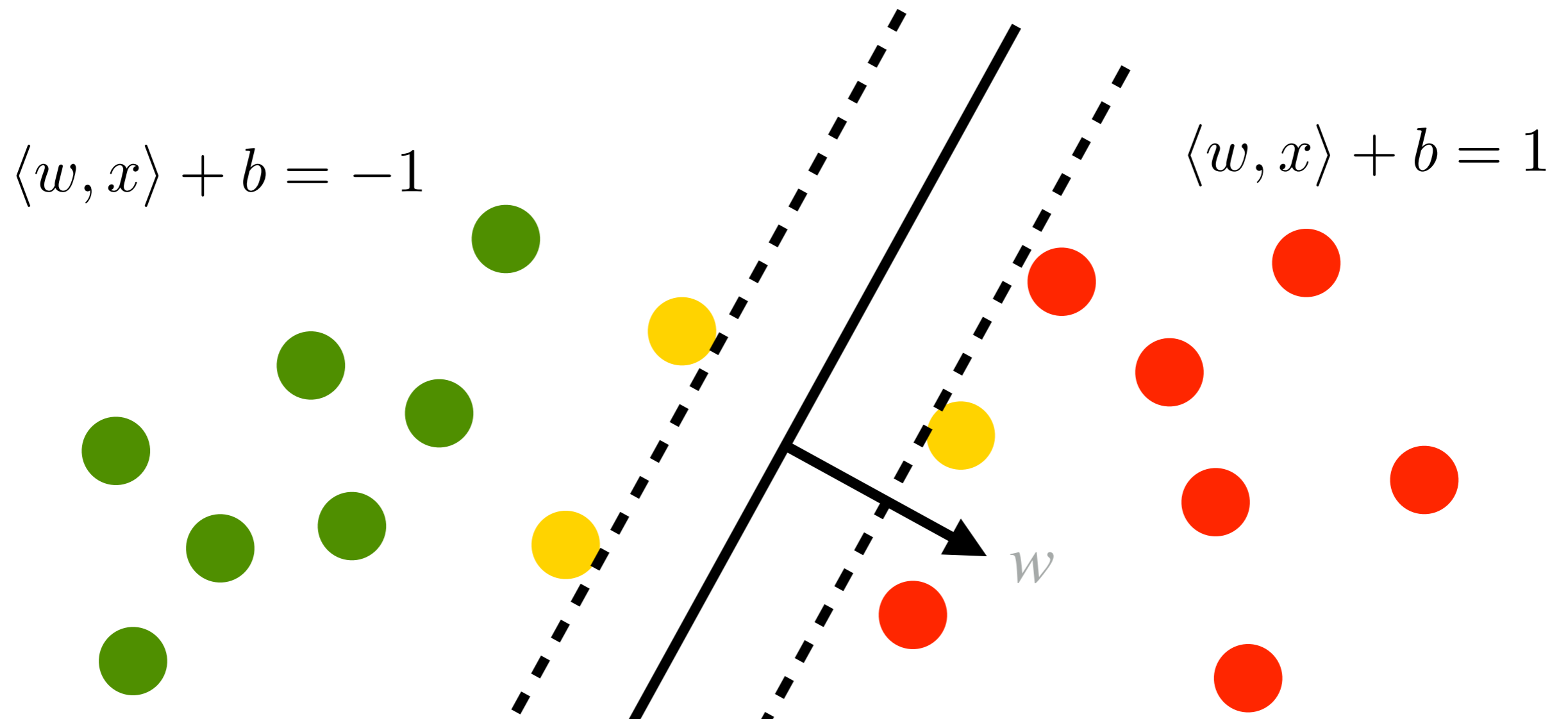
# Last time... Support Vector Machines



optimization problem

$$\text{maximize}_{w,b} \frac{1}{\|w\|} \text{ subject to } y_i [\langle x_i, w \rangle + b] \geq 1$$

# Last time... Support Vector Machines

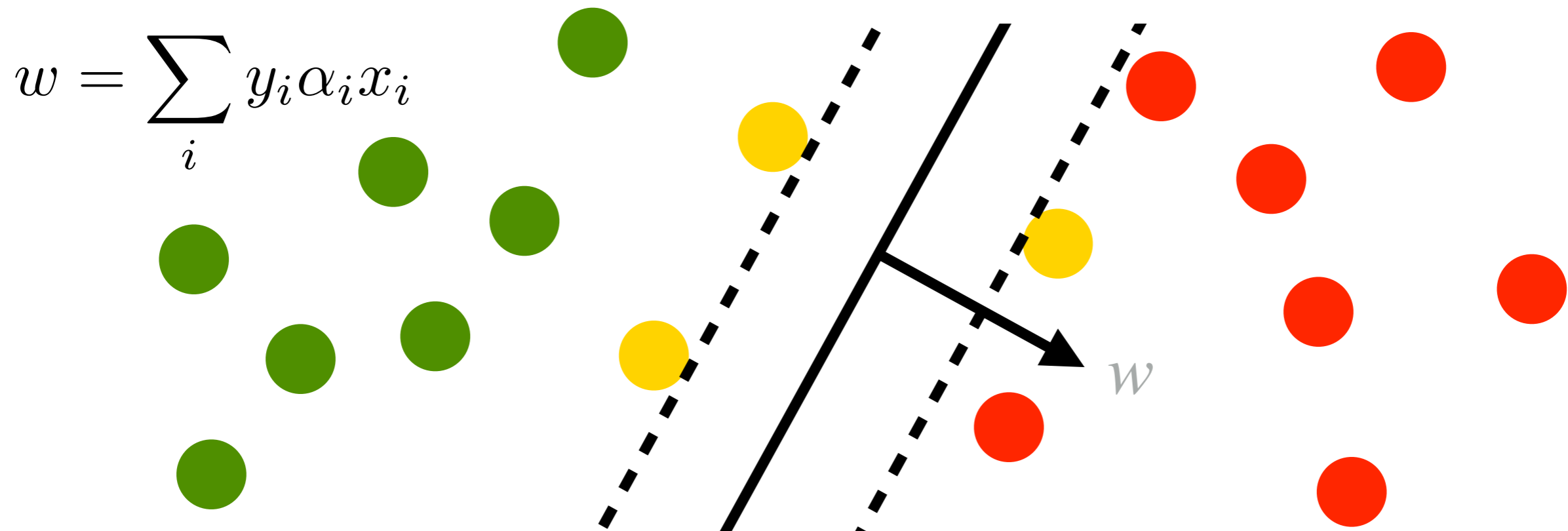


optimization problem

$$\text{minimize}_{w,b} \frac{1}{2} \|w\|^2 \quad \text{subject to } y_i [\langle x_i, w \rangle + b] \geq 1$$

# Last time... Support Vector Machines

$$\text{minimize}_{w,b} \frac{1}{2} \|w\|^2 \quad \text{subject to } y_i [\langle x_i, w \rangle + b] \geq 1$$

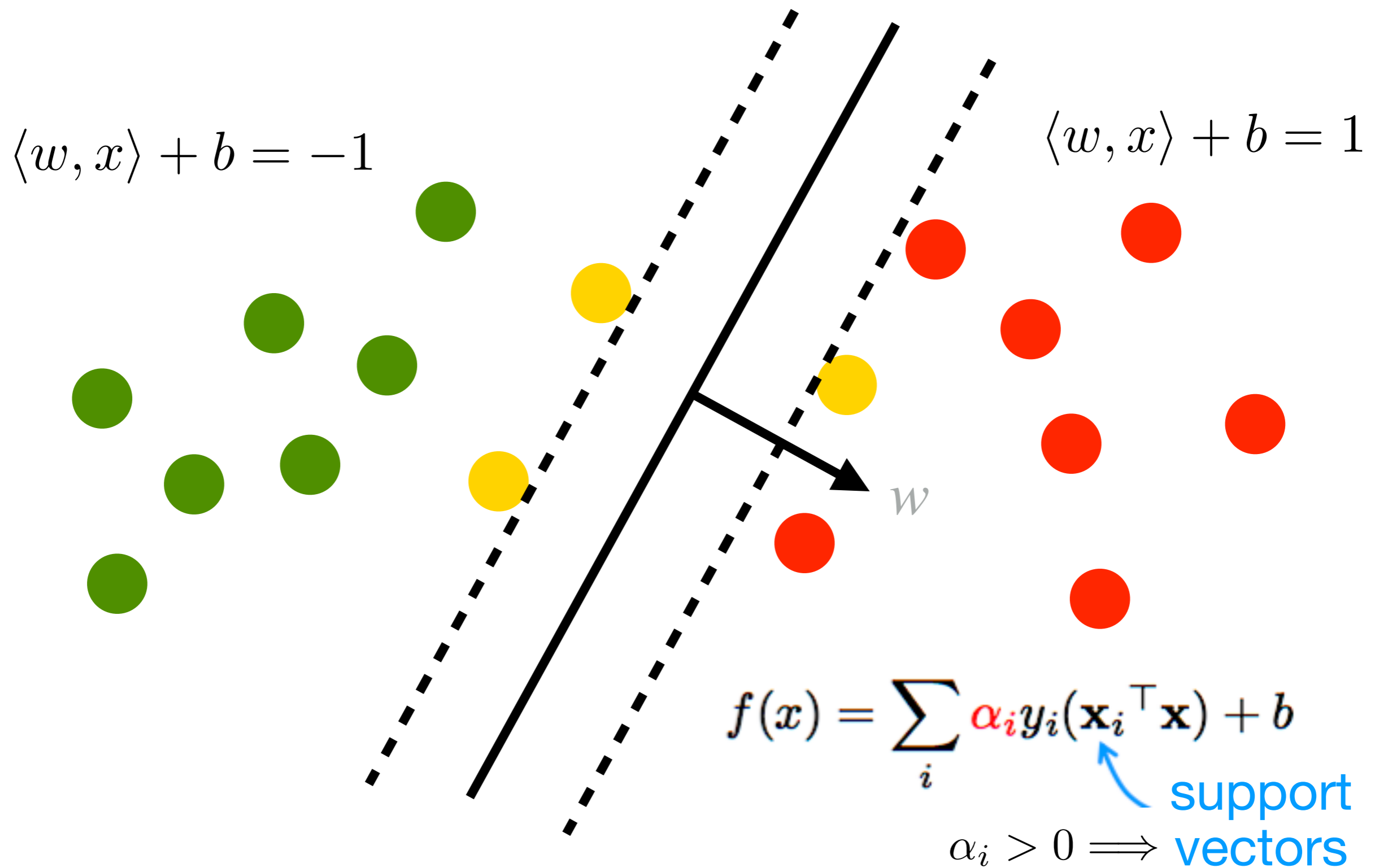


$$w = \sum_i y_i \alpha_i x_i$$

$$\text{maximize}_{\alpha} - \frac{1}{2} \sum_{i,j} \alpha_i \alpha_j y_i y_j \langle x_i, x_j \rangle + \sum_i \alpha_i$$

$$\text{subject to } \sum \alpha_i y_i = 0 \text{ and } \alpha_i \geq 0$$

# Last time... Large Margin Classifier



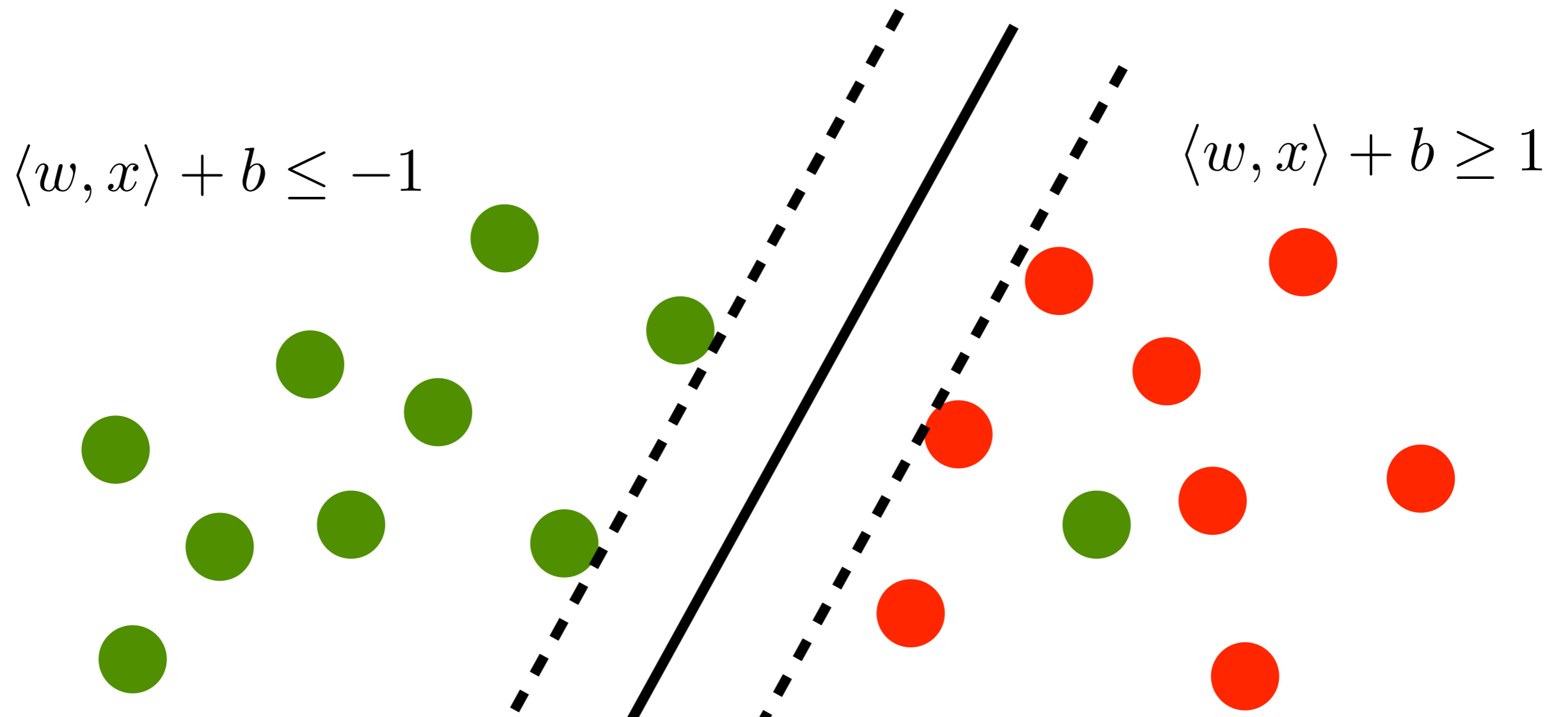
# Today

- Soft margin classification
- Multi-class classification
- Introduction to kernels

# Soft Margin Classification



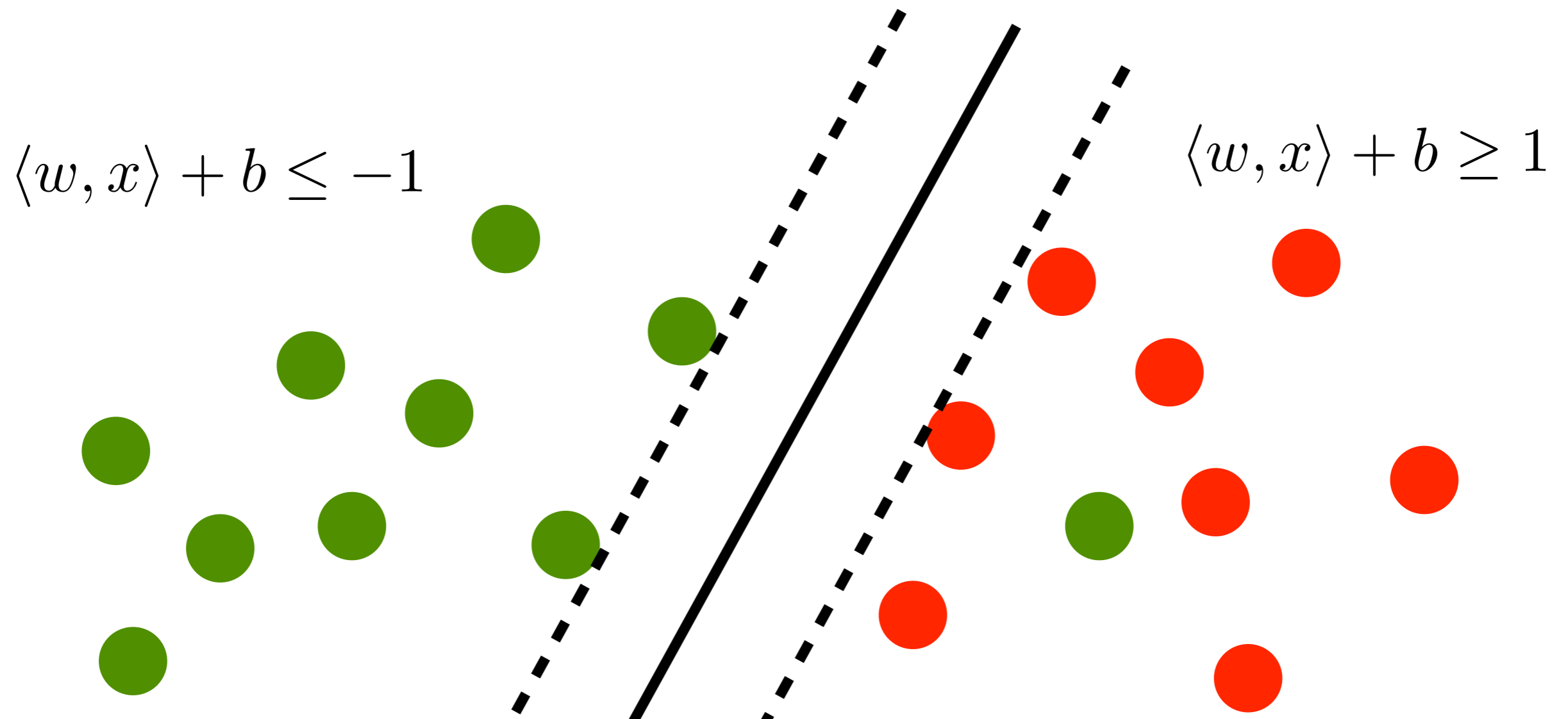
# Large Margin Classifier



linear function  
 $f(x) = \langle w, x \rangle + b$

linear separator  
is impossible

# Large Margin Classifier

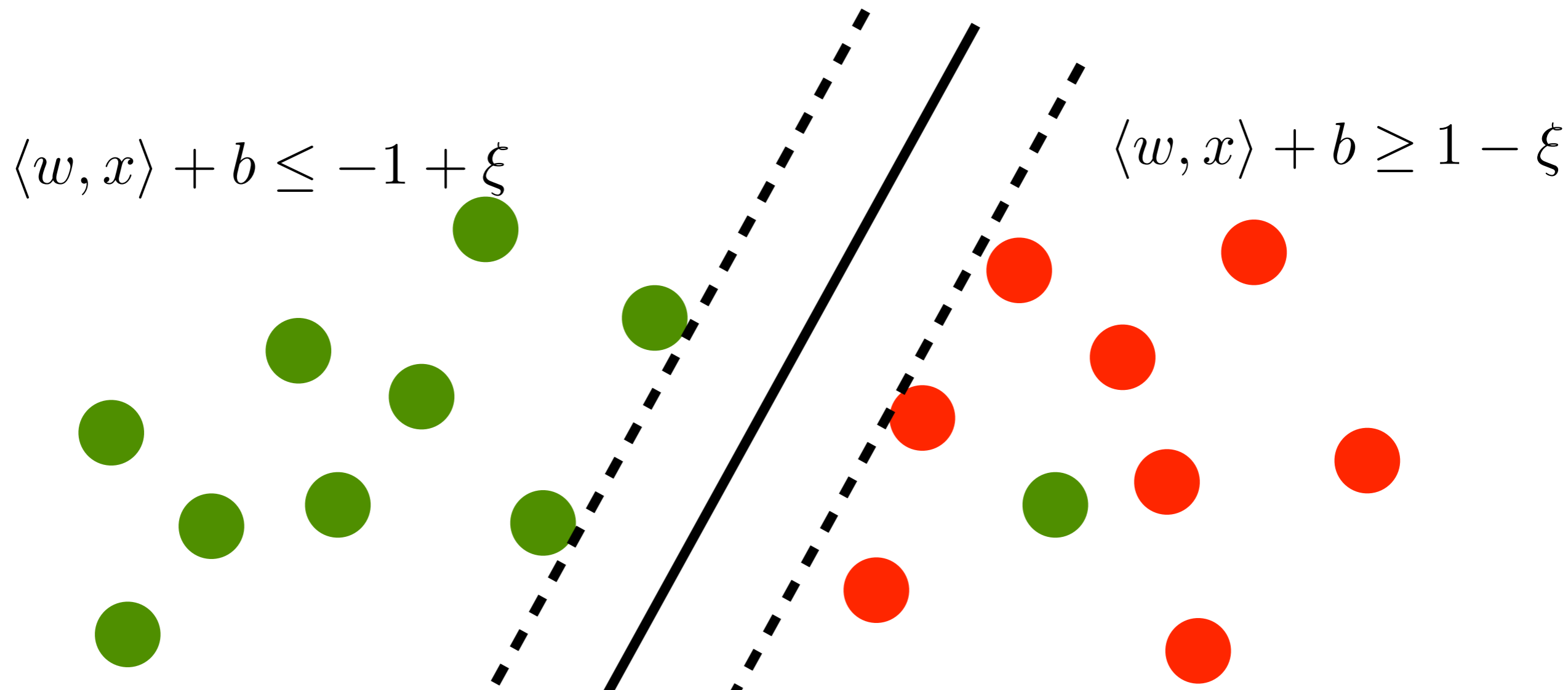


minimum error separator  
is impossible

Theorem (Minsky & Papert)

Finding the minimum error separating hyperplane is NP hard

# Adding Slack Variables



Convex optimization problem

minimize amount  
of slack

# Convex Programs for Dummies

- Primal optimization problem

$$\underset{x}{\text{minimize}} f(x) \text{ subject to } c_i(x) \leq 0$$

- Lagrange function

$$L(x, \alpha) = f(x) + \sum_i \alpha_i c_i(x)$$

- First order optimality conditions in  $x$

$$\partial_x L(x, \alpha) = \partial_x f(x) + \sum_i \alpha_i \partial_x c_i(x) = 0$$

- Solve for  $x$  and plug it back into  $L$

$$\underset{\alpha}{\text{maximize}} L(x(\alpha), \alpha)$$

(keep explicit constraints)

# Adding Slack Variables

- Hard margin problem

$$\underset{w,b}{\text{minimize}} \frac{1}{2} \|w\|^2 \quad \text{subject to } y_i [\langle w, x_i \rangle + b] \geq 1$$

- With slack variables

$$\underset{w,b}{\text{minimize}} \frac{1}{2} \|w\|^2 + C \sum_i \xi_i$$

$$\text{subject to } y_i [\langle w, x_i \rangle + b] \geq 1 - \xi_i \text{ and } \xi_i \geq 0$$

**Problem is always feasible. Proof:**

$w = 0$  and  $b = 0$  and  $\xi_i = 1$  (also yields upper bound)

# Dual Problem

- Primal optimization problem

$$\underset{w, b}{\text{minimize}} \quad \frac{1}{2} \|w\|^2 + C \sum_i \xi_i$$

subject to  $y_i [\langle w, x_i \rangle + b] \geq 1 - \xi_i$  and  $\xi_i \geq 0$

- Lagrange function

$$L(w, b, \alpha) = \frac{1}{2} \|w\|^2 + C \sum_i \xi_i - \sum_i \alpha_i [y_i [\langle x_i, w \rangle + b] + \xi_i - 1] - \sum_i \eta_i \xi_i$$

Optimality in  $w, b, \xi$  is at saddle point with  $\alpha, \eta$

- Derivatives in  $w, b, \xi$  need to vanish

# Dual Problem

- Lagrange function

$$L(w, b, \alpha) = \frac{1}{2} \|w\|^2 + C \sum_i \xi_i - \sum_i \alpha_i [y_i [\langle x_i, w \rangle + b] + \xi_i - 1] - \sum_i \eta_i \xi_i$$

- Derivatives in  $w$ ,  $b$  need to vanish

$$\partial_w L(w, b, \xi, \alpha, \eta) = w - \sum_i \alpha_i y_i x_i = 0$$

$$\partial_b L(w, b, \xi, \alpha, \eta) = \sum_i \alpha_i y_i = 0$$

$$\partial_{\xi_i} L(w, b, \xi, \alpha, \eta) = C - \alpha_i - \eta_i = 0$$

- Plugging terms back into  $L$  yields

$$\text{maximize}_{\alpha} - \frac{1}{2} \sum_{i,j} \alpha_i \alpha_j y_i y_j \langle x_i, x_j \rangle + \sum_i \alpha_i$$

$$\text{subject to } \sum_i \alpha_i y_i = 0 \text{ and } \alpha_i \in [0, C]$$

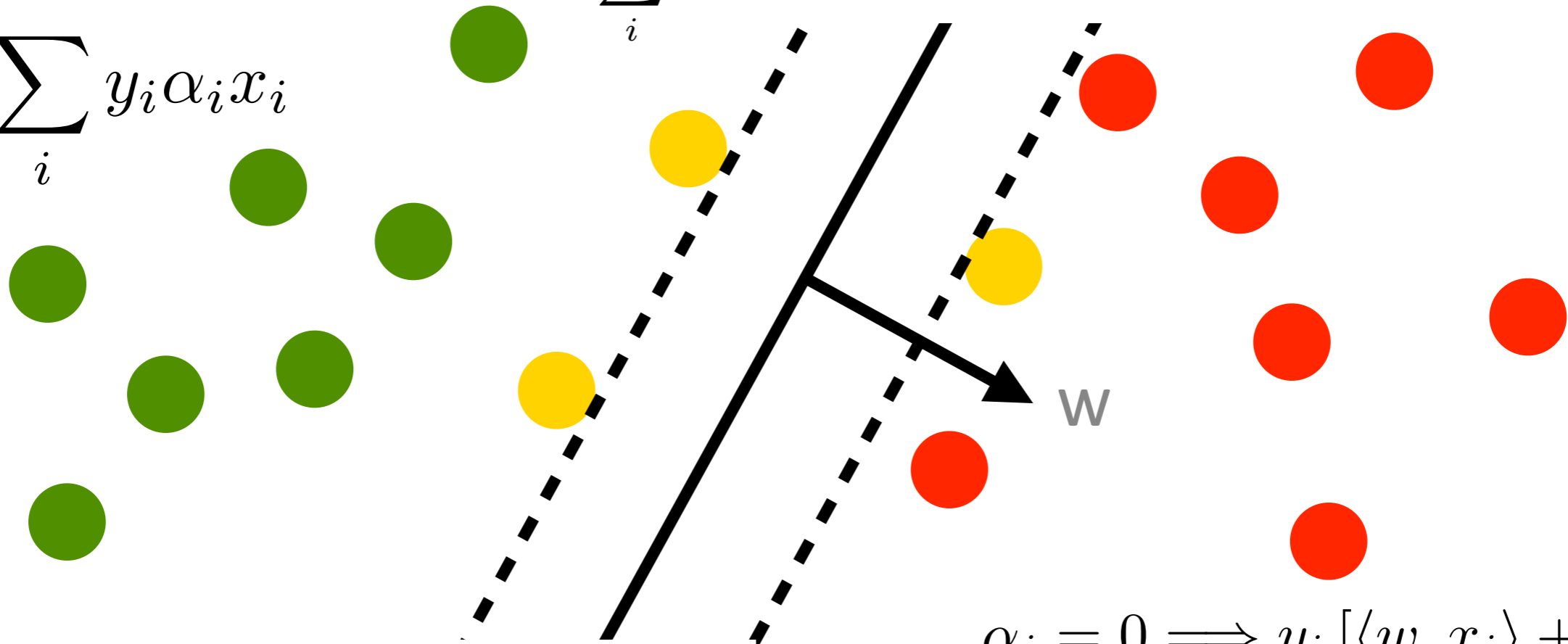
bound  
influence

# Karush Kuhn Tucker Conditions

$$\text{maximize}_{\alpha} -\frac{1}{2} \sum_{i,j} \alpha_i \alpha_j y_i y_j \langle x_i, x_j \rangle + \sum_i \alpha_i$$

$$\text{subject to } \sum_i \alpha_i y_i = 0 \text{ and } \alpha_i \in [0, C]$$

$$w = \sum_i y_i \alpha_i x_i$$



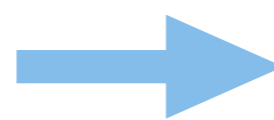
$$\alpha_i = 0 \implies y_i [\langle w, x_i \rangle + b] \geq 1$$

$$0 < \alpha_i < C \implies y_i [\langle w, x_i \rangle + b] = 1$$

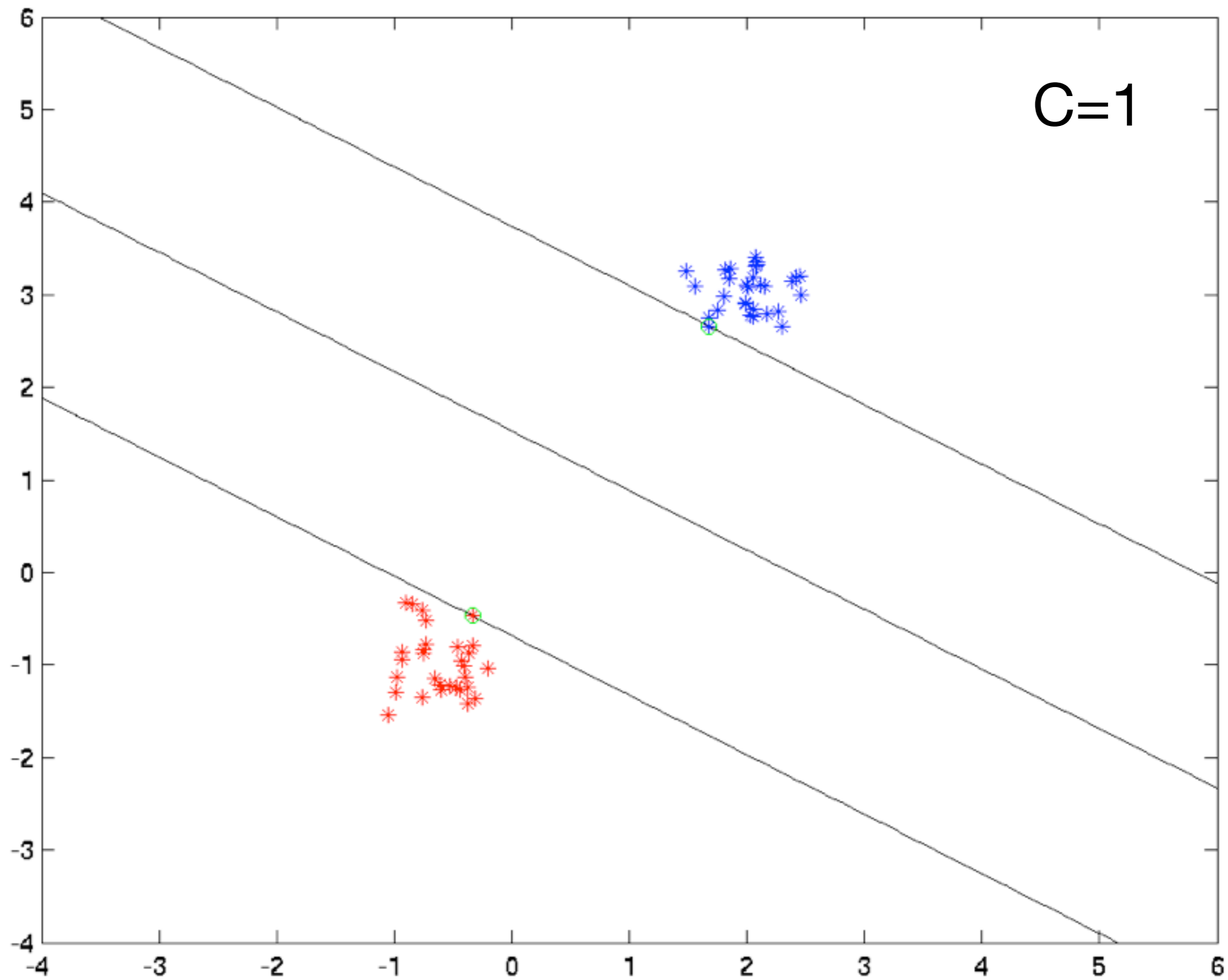
$$\alpha_i = C \implies y_i [\langle w, x_i \rangle + b] \leq 1$$

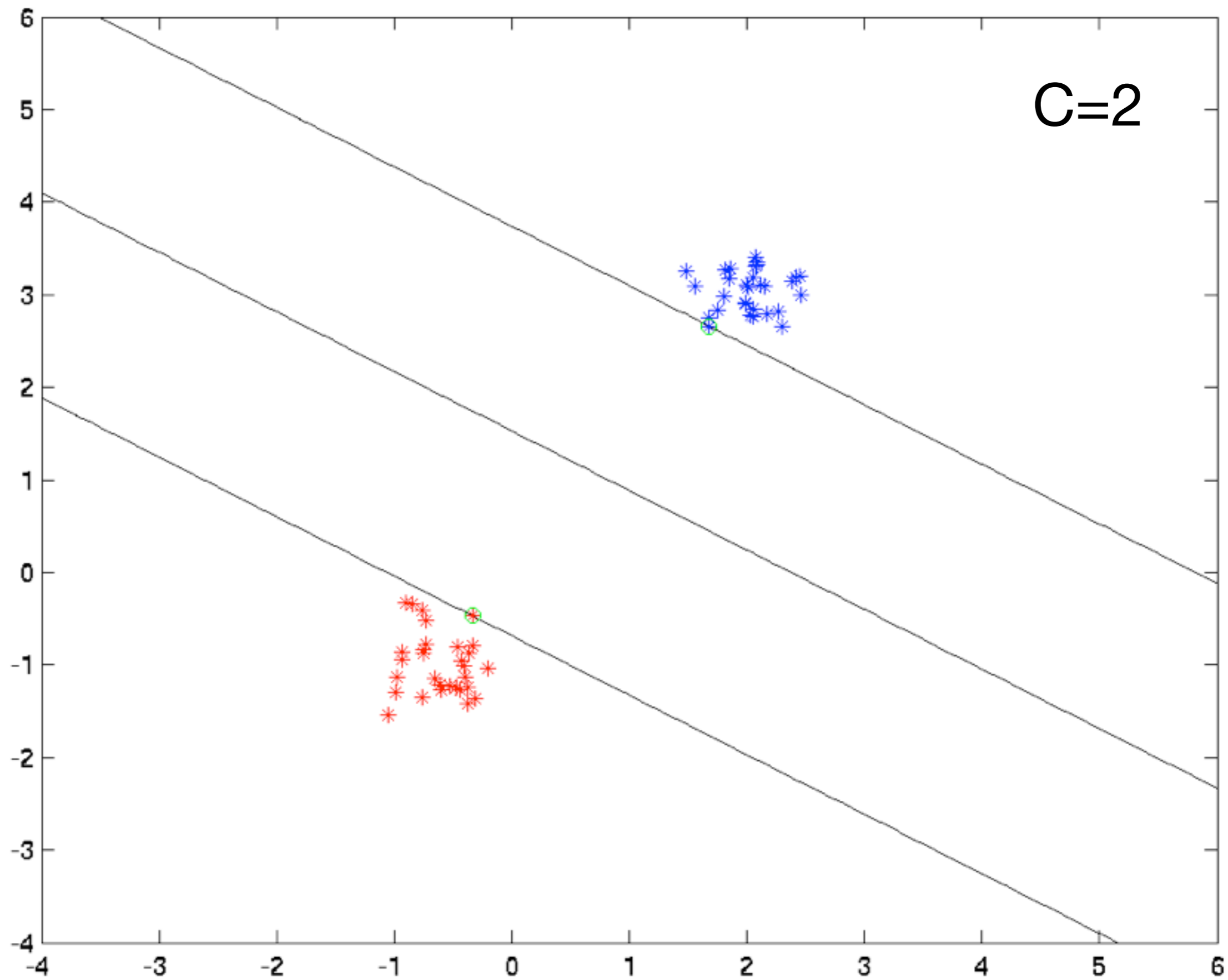
$$\alpha_i [y_i [\langle w, x_i \rangle + b] + \xi_i - 1] = 0$$

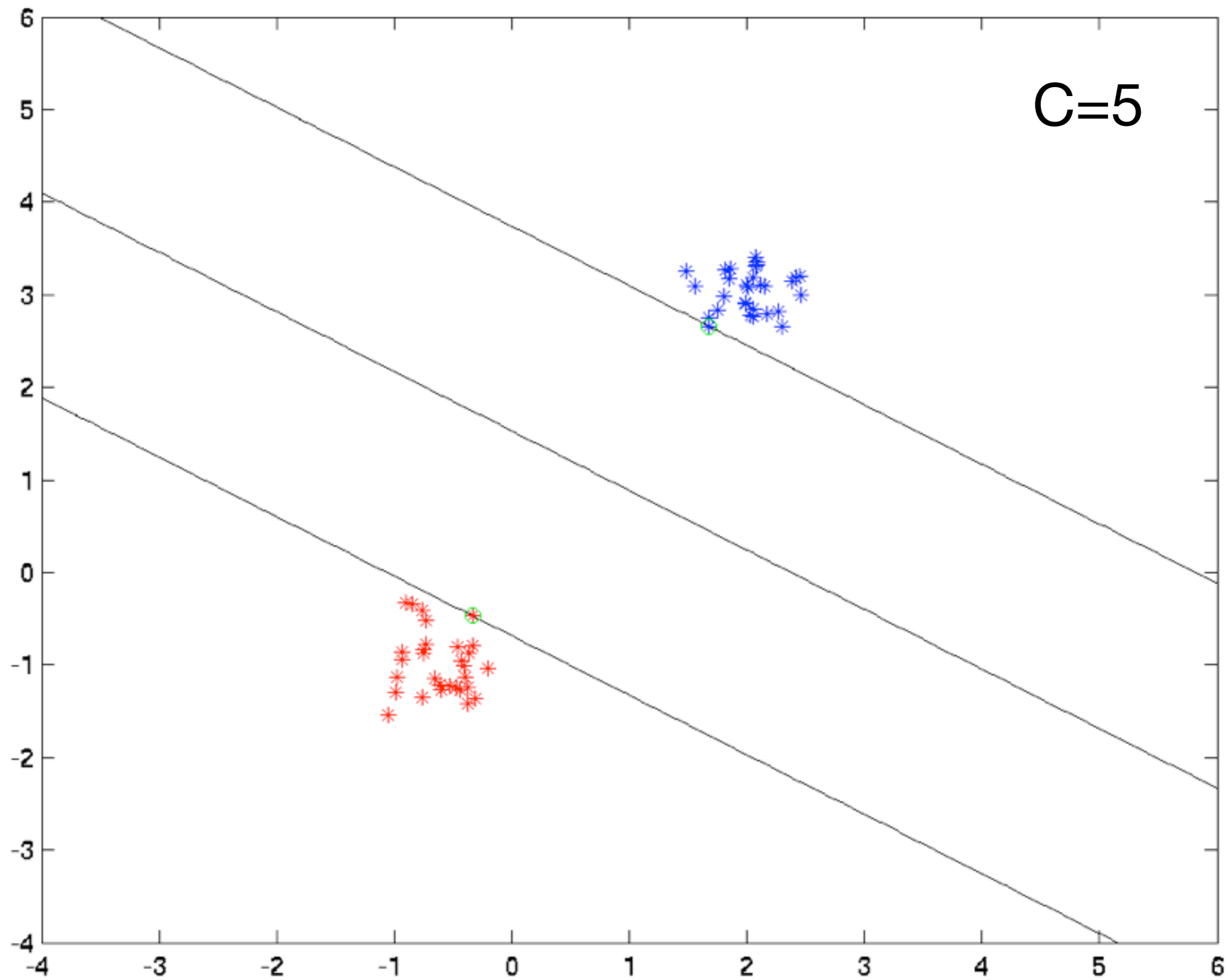
$$\eta_i \xi_i = 0$$

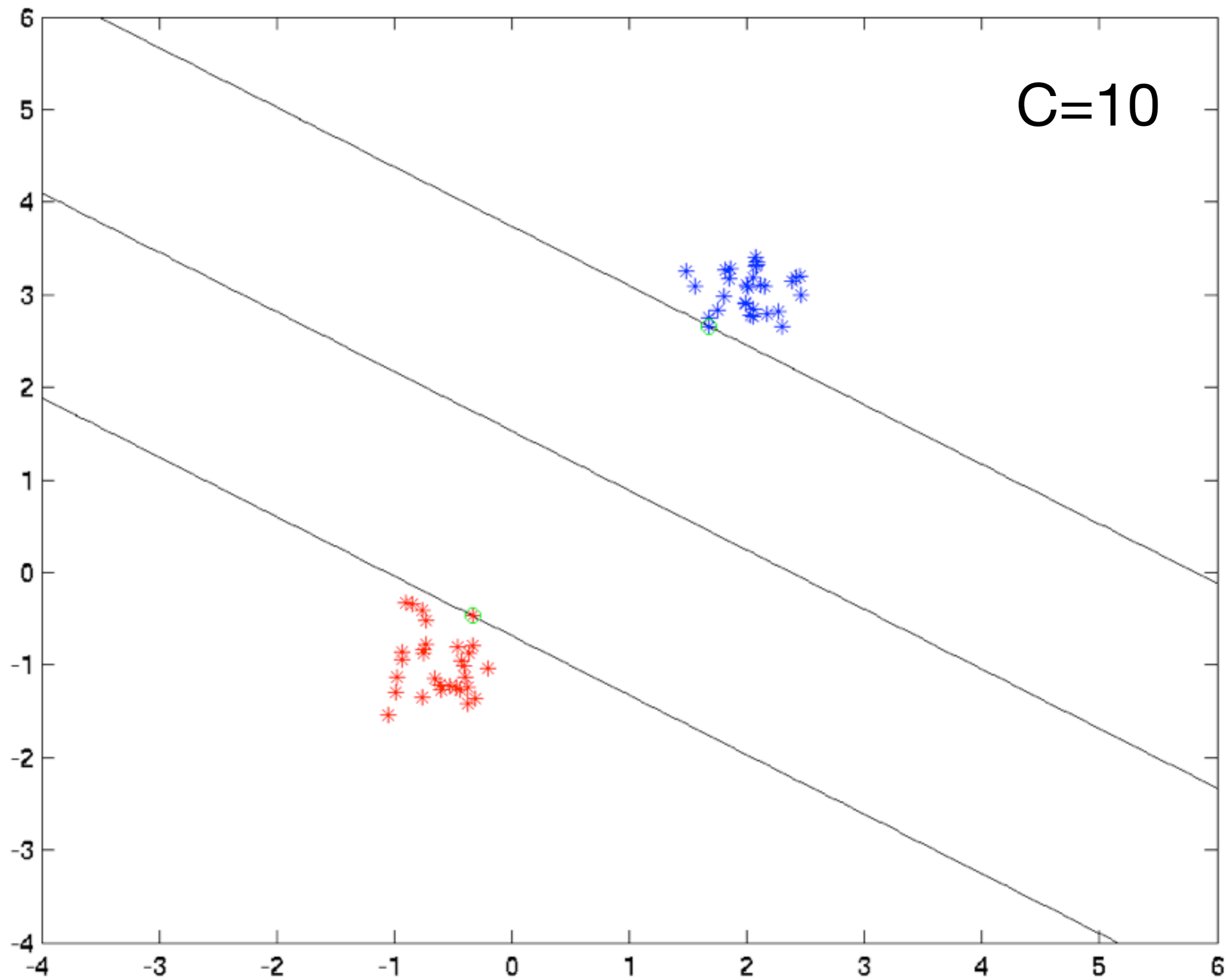


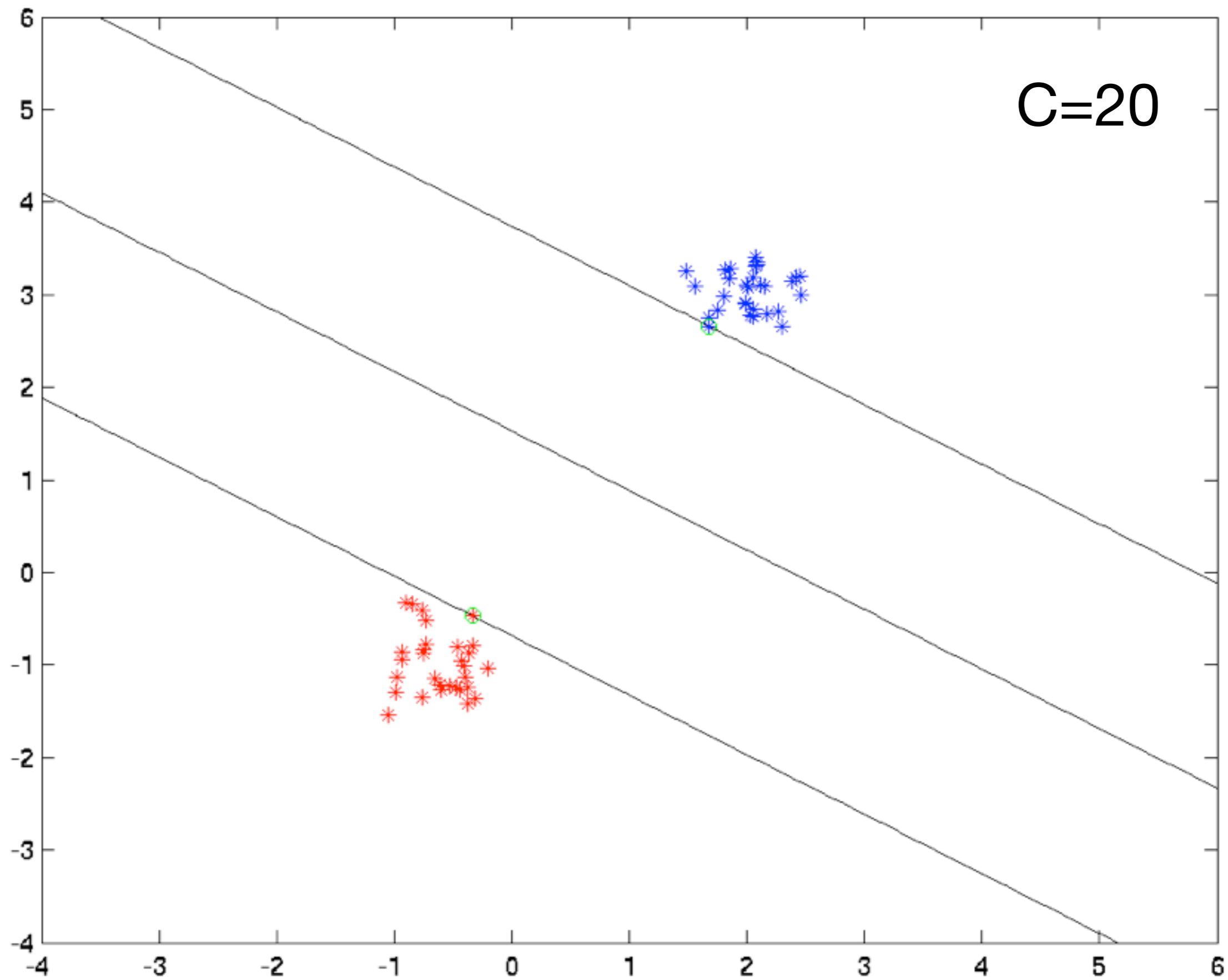


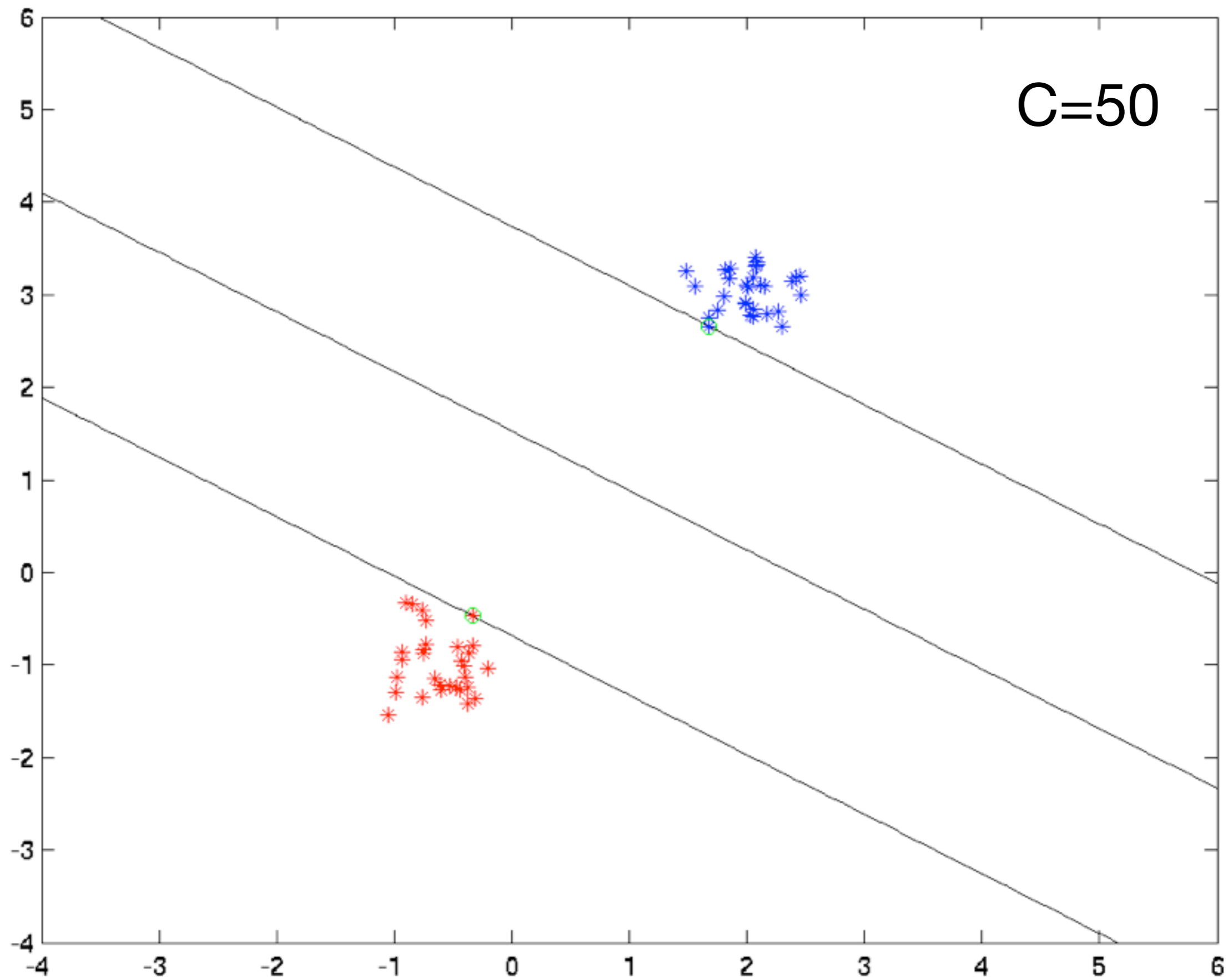


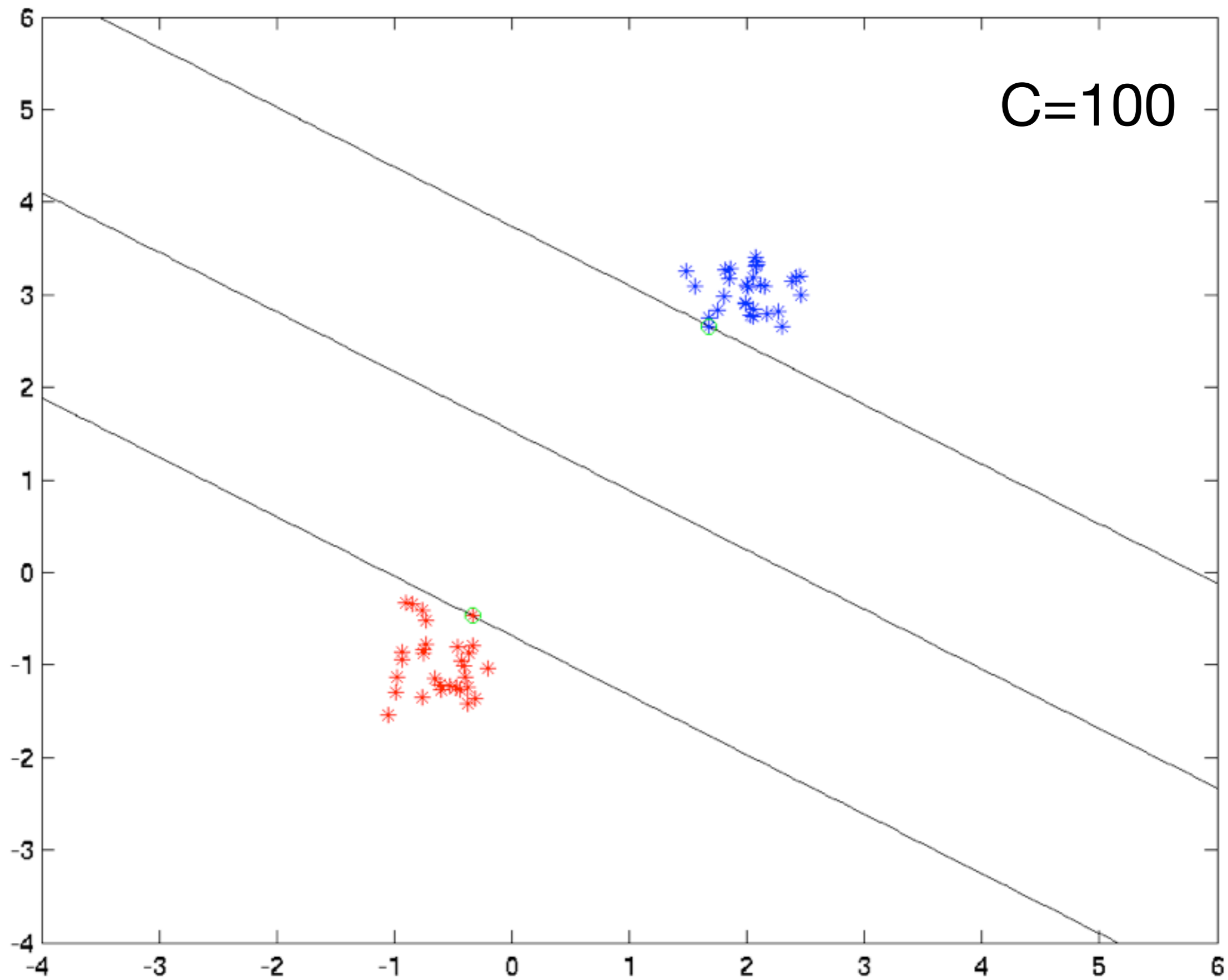


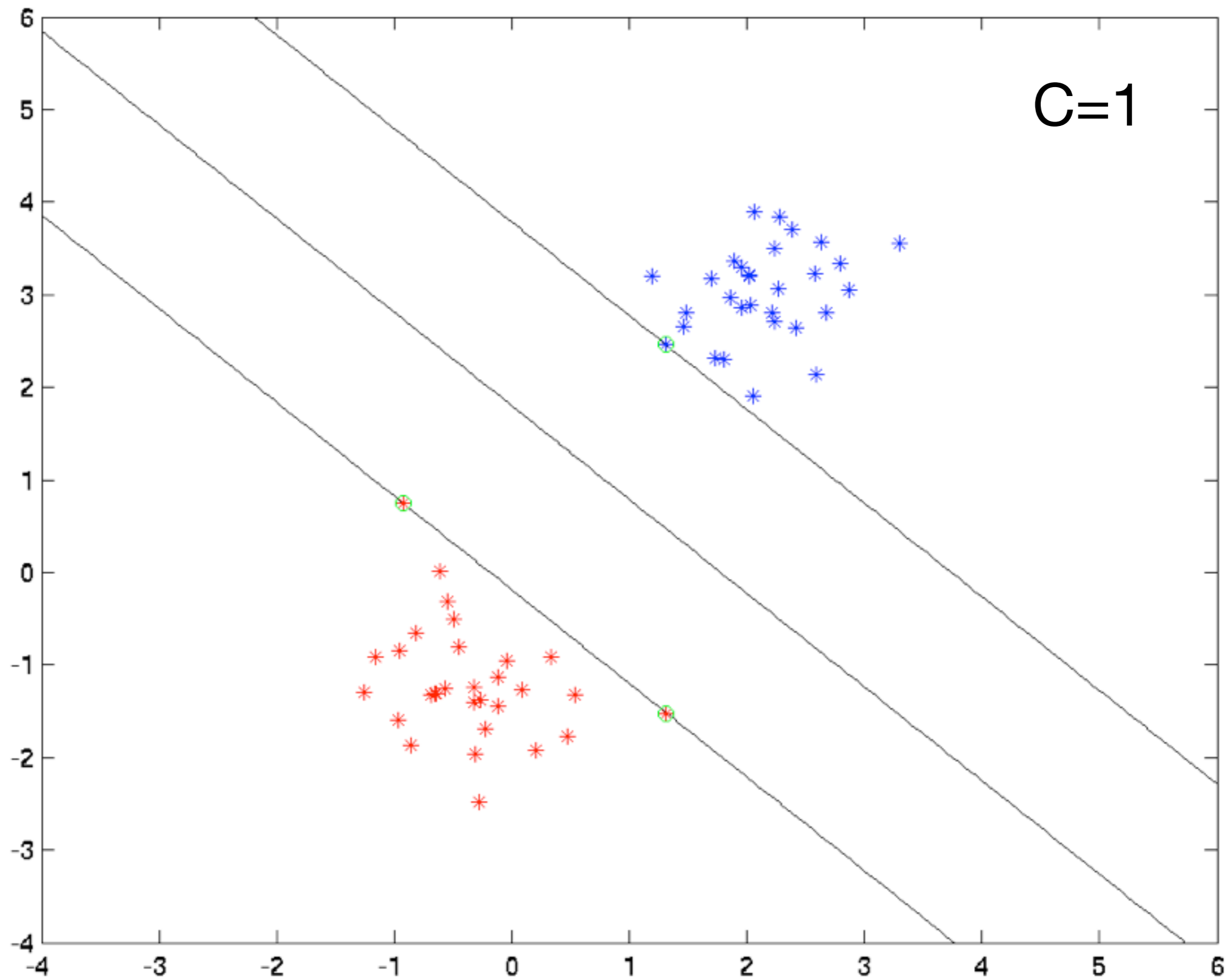




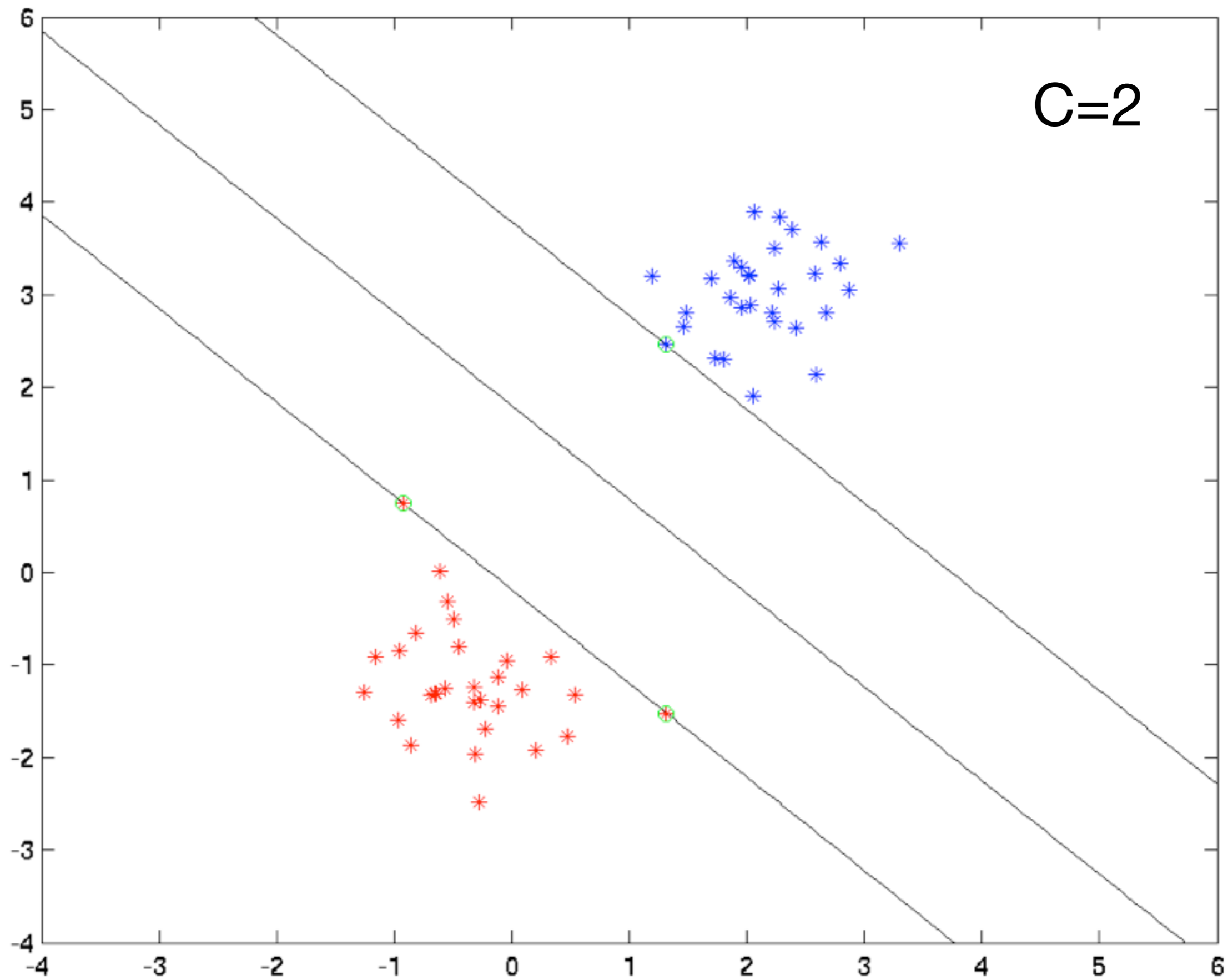


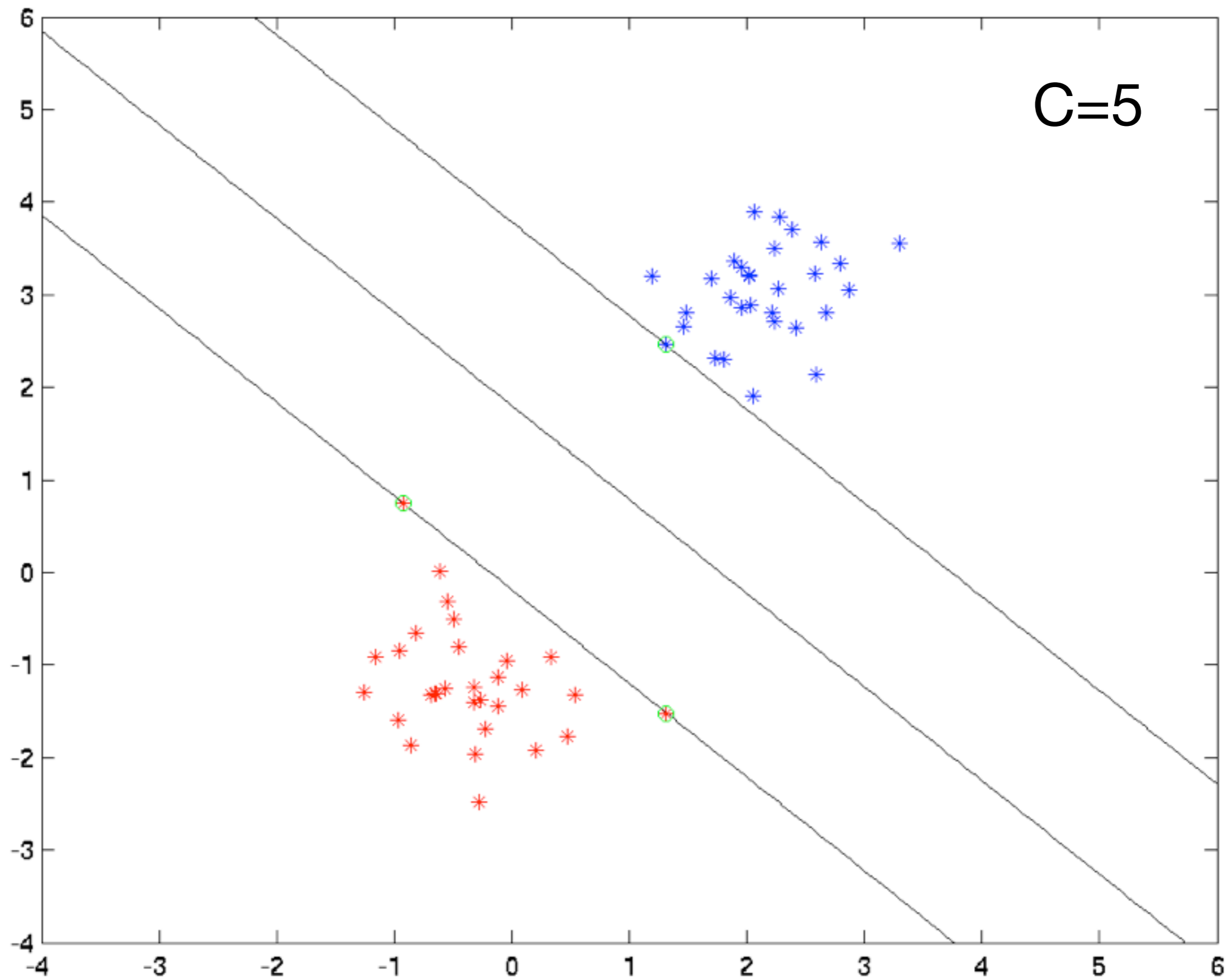


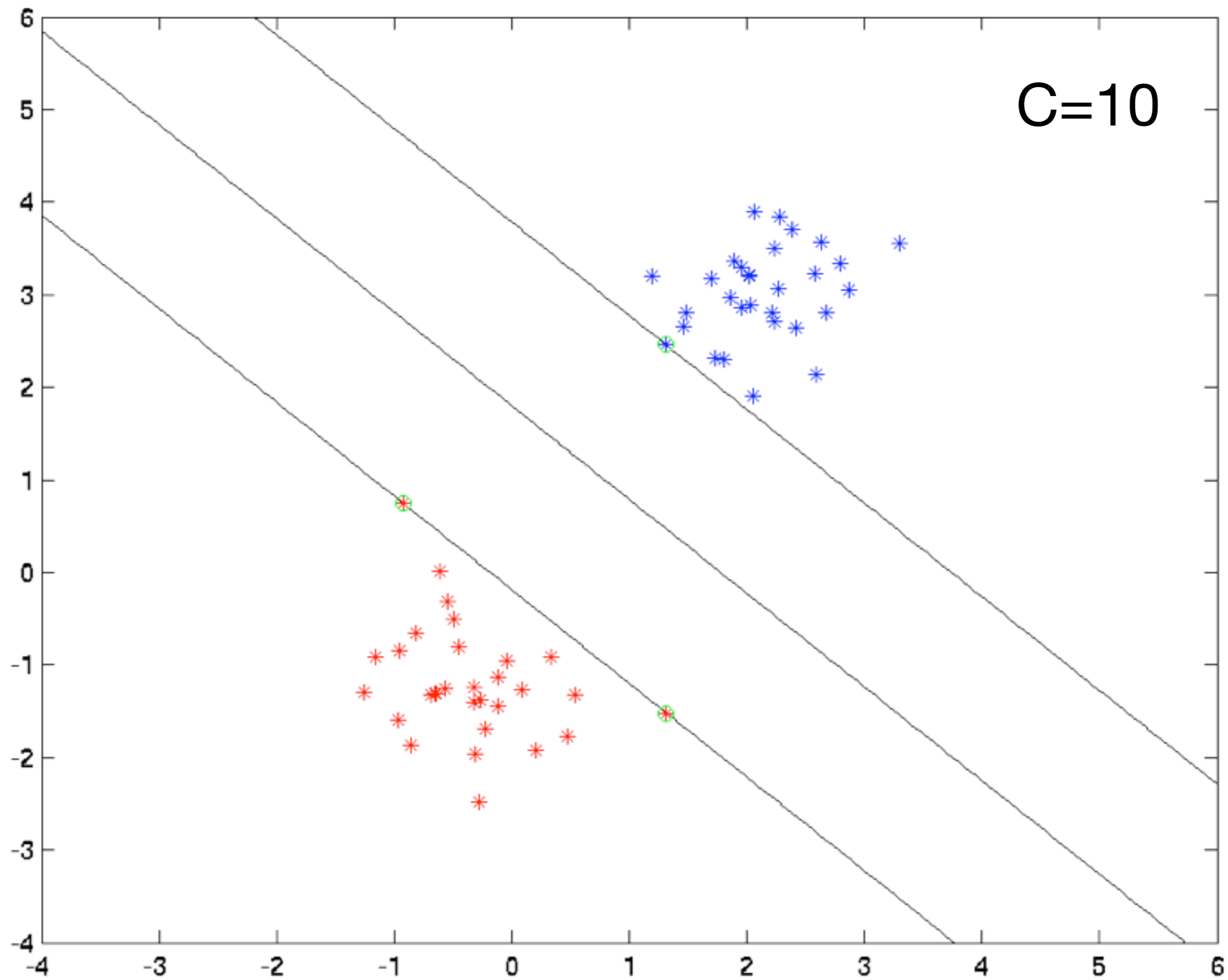


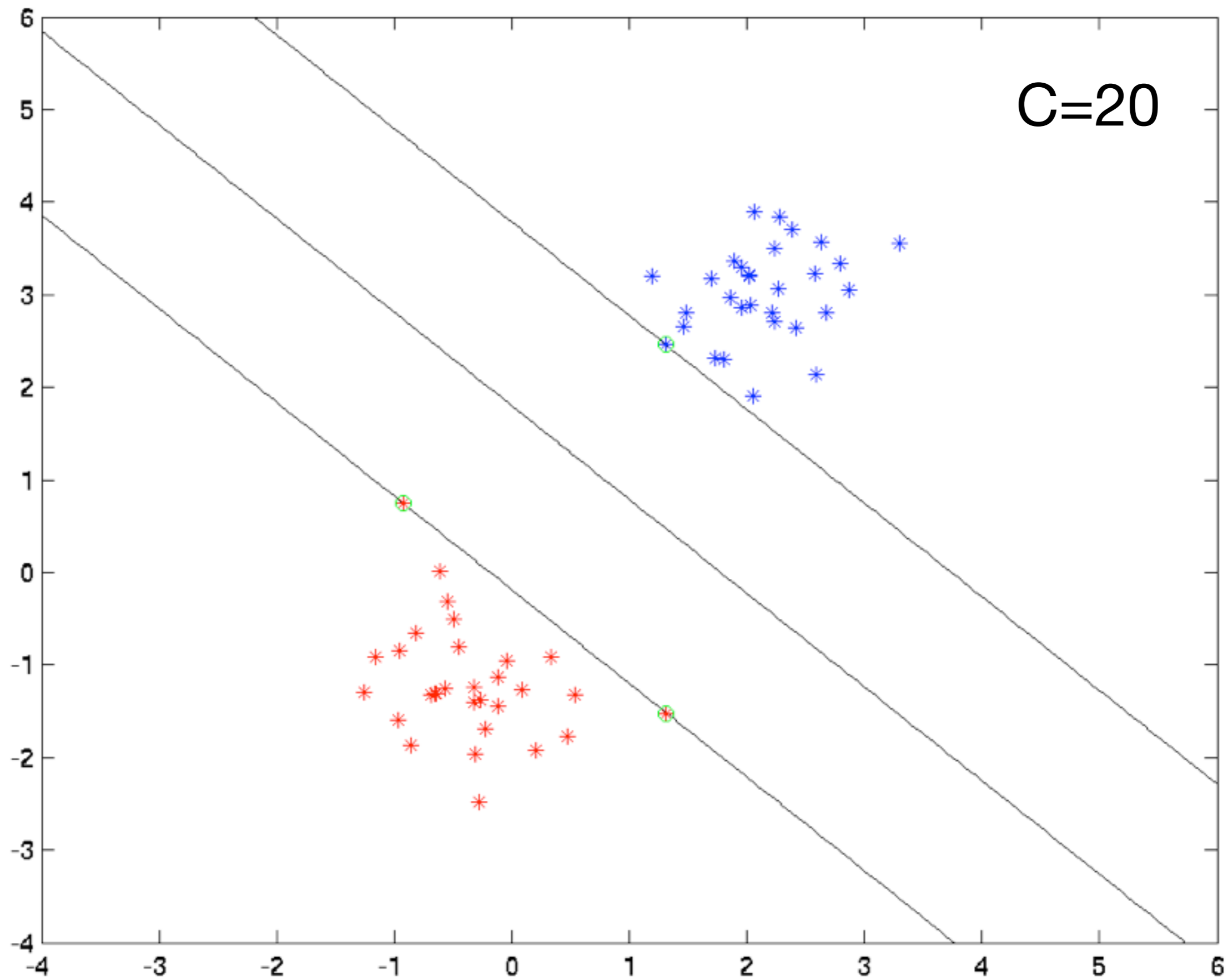


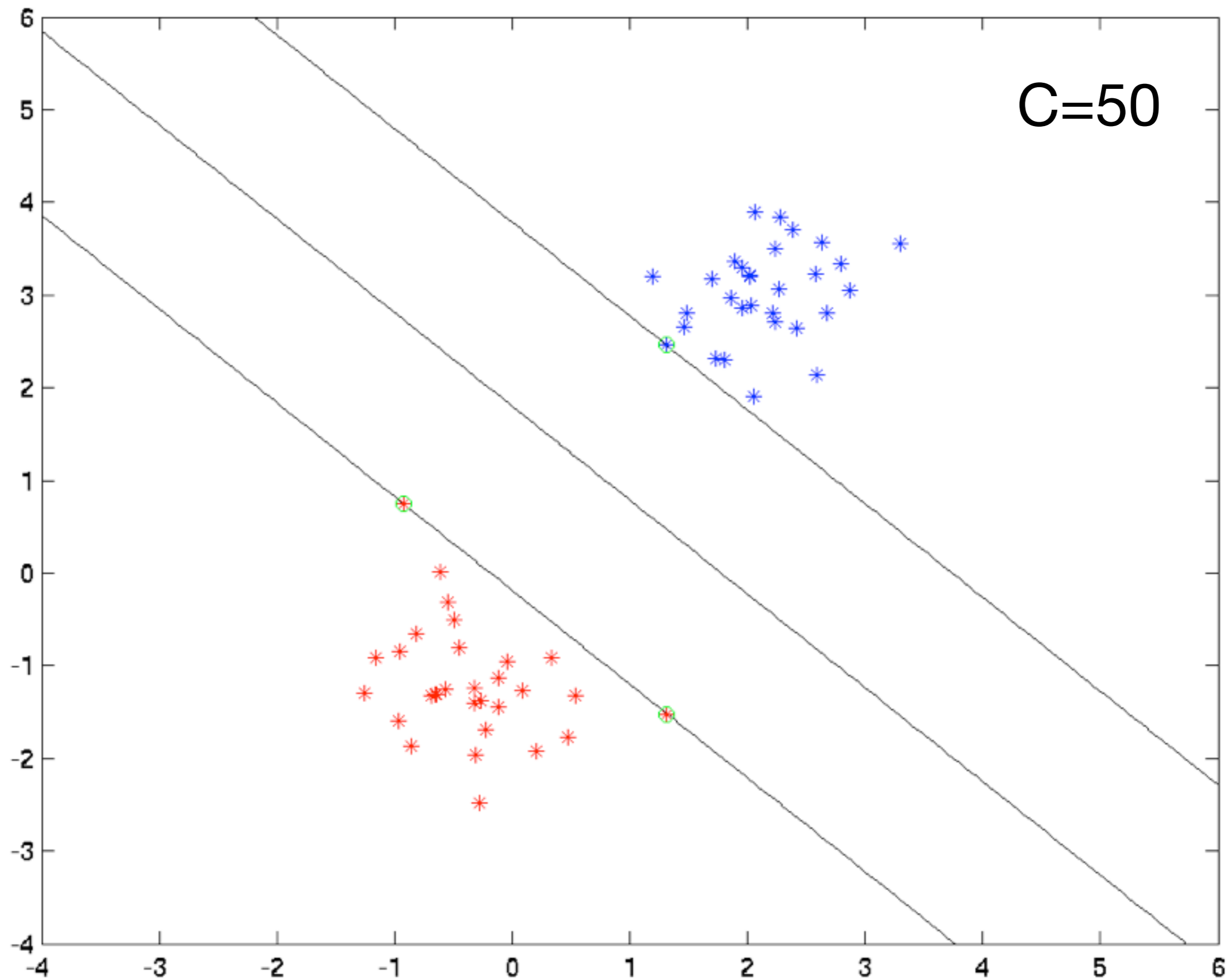


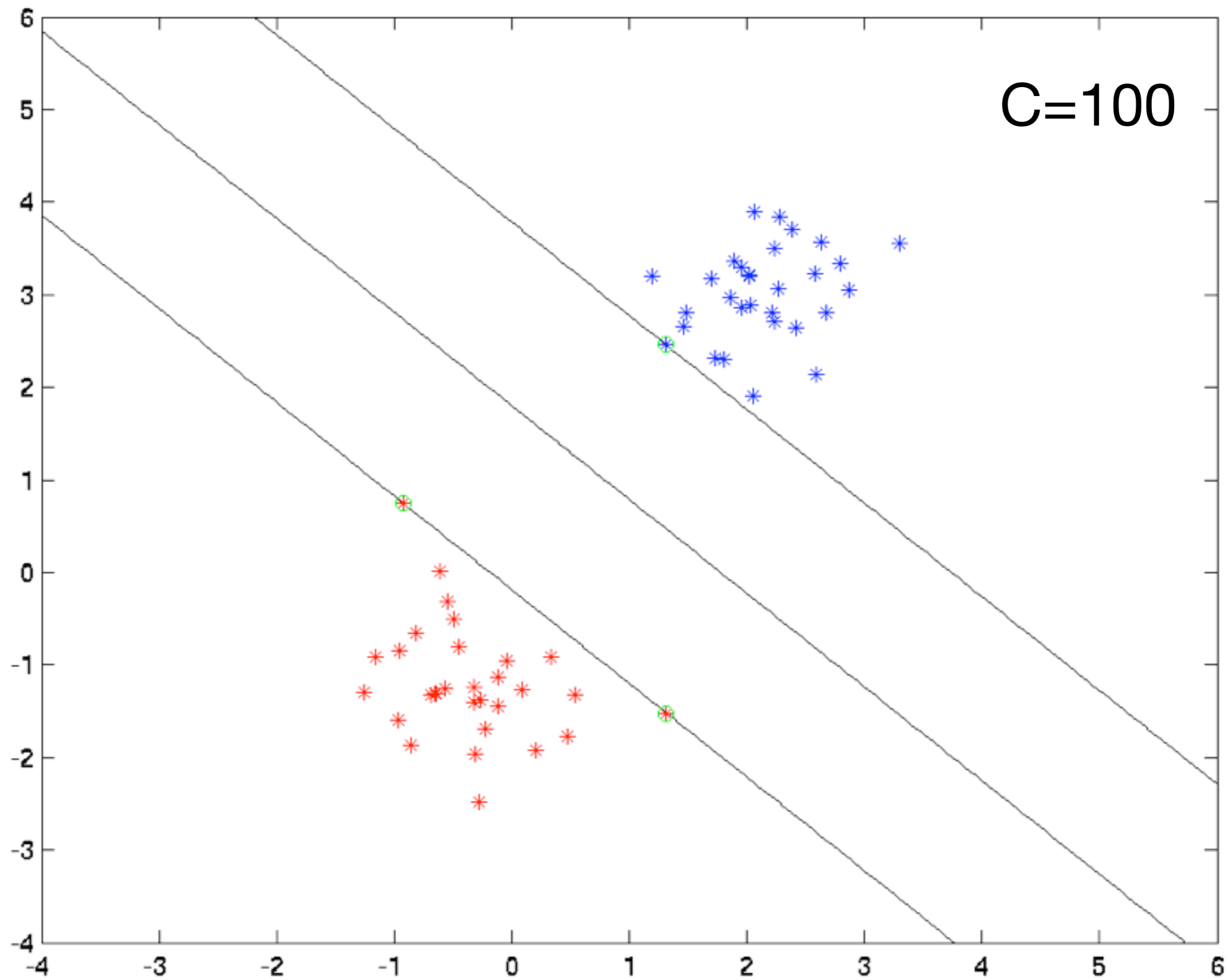


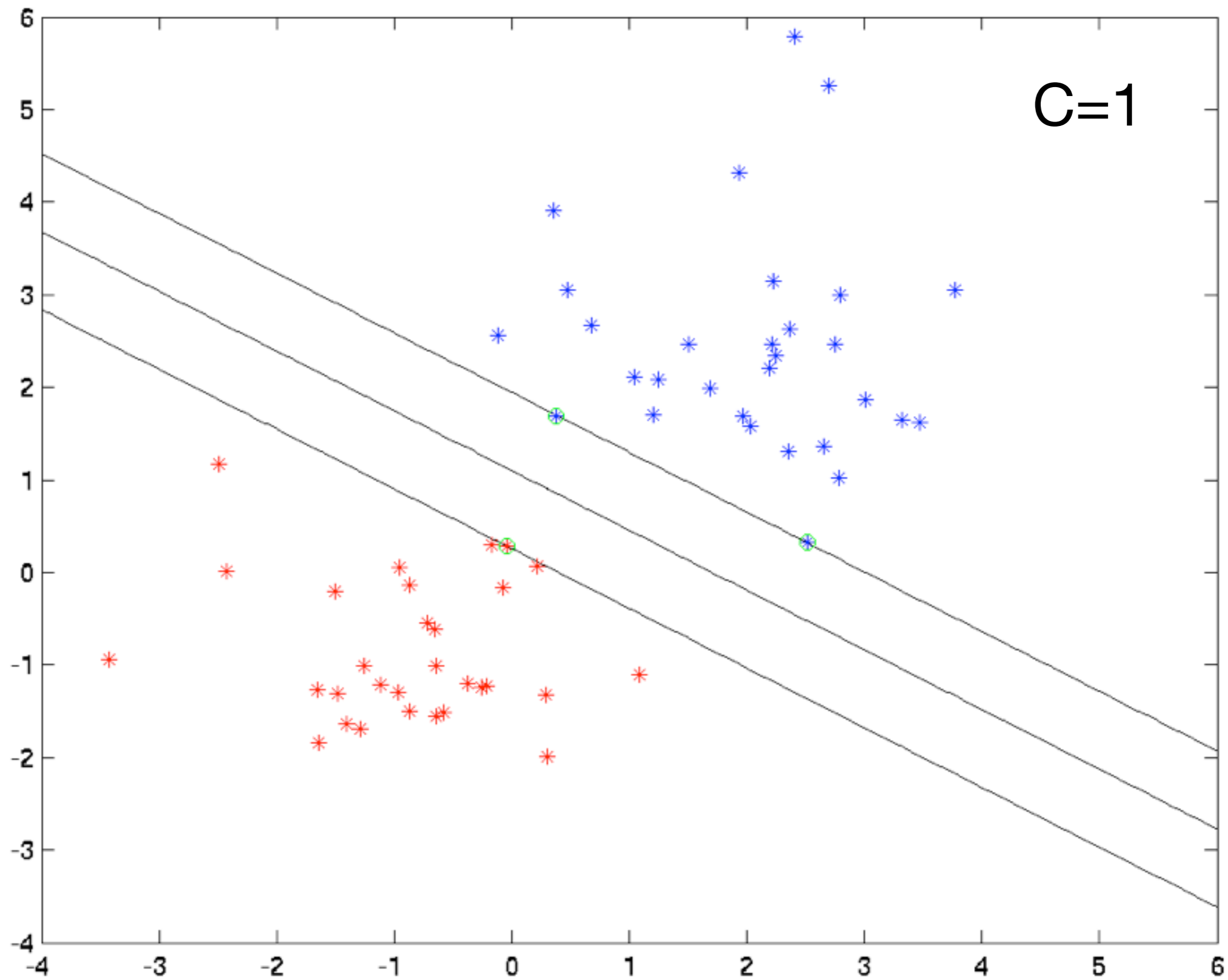


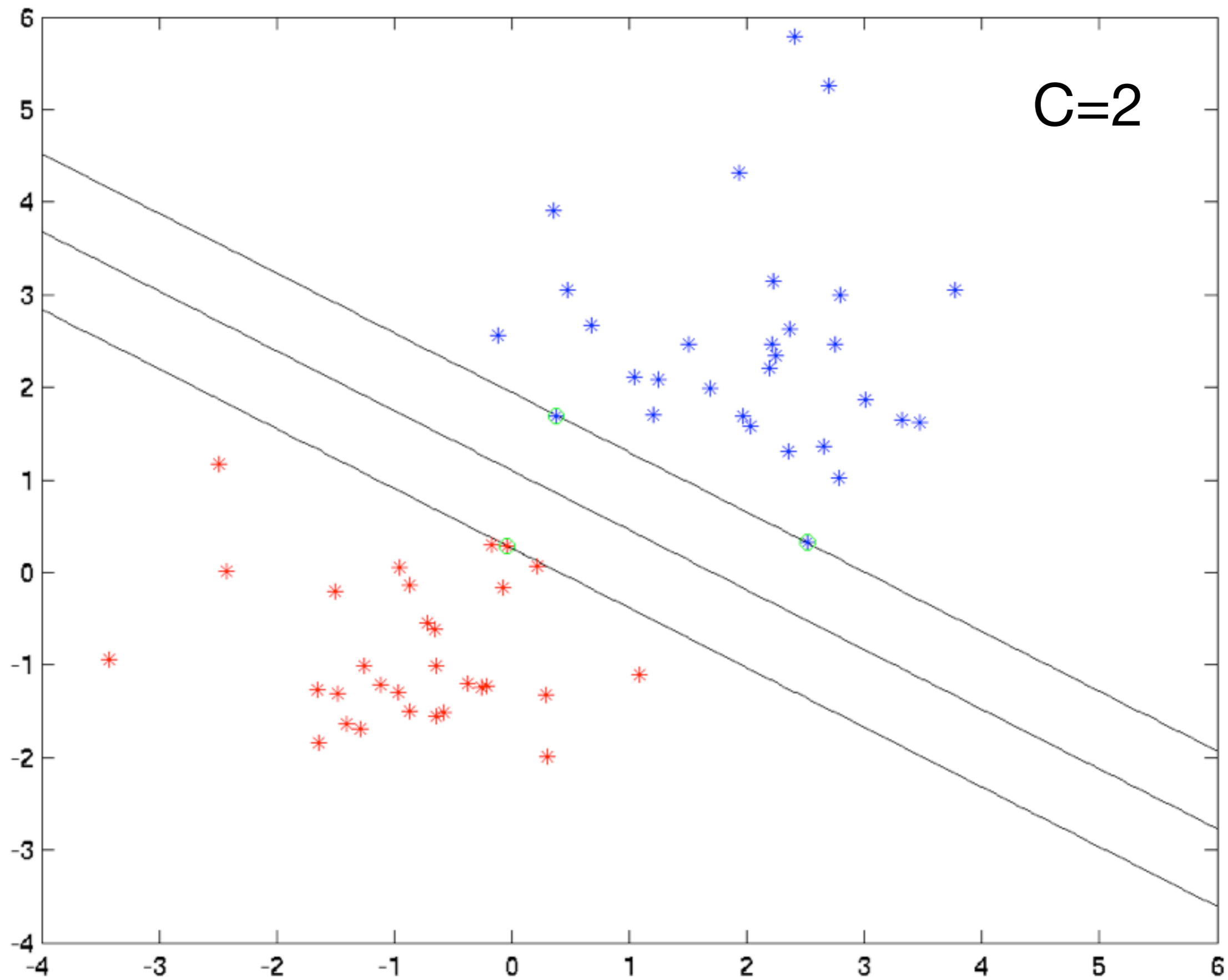




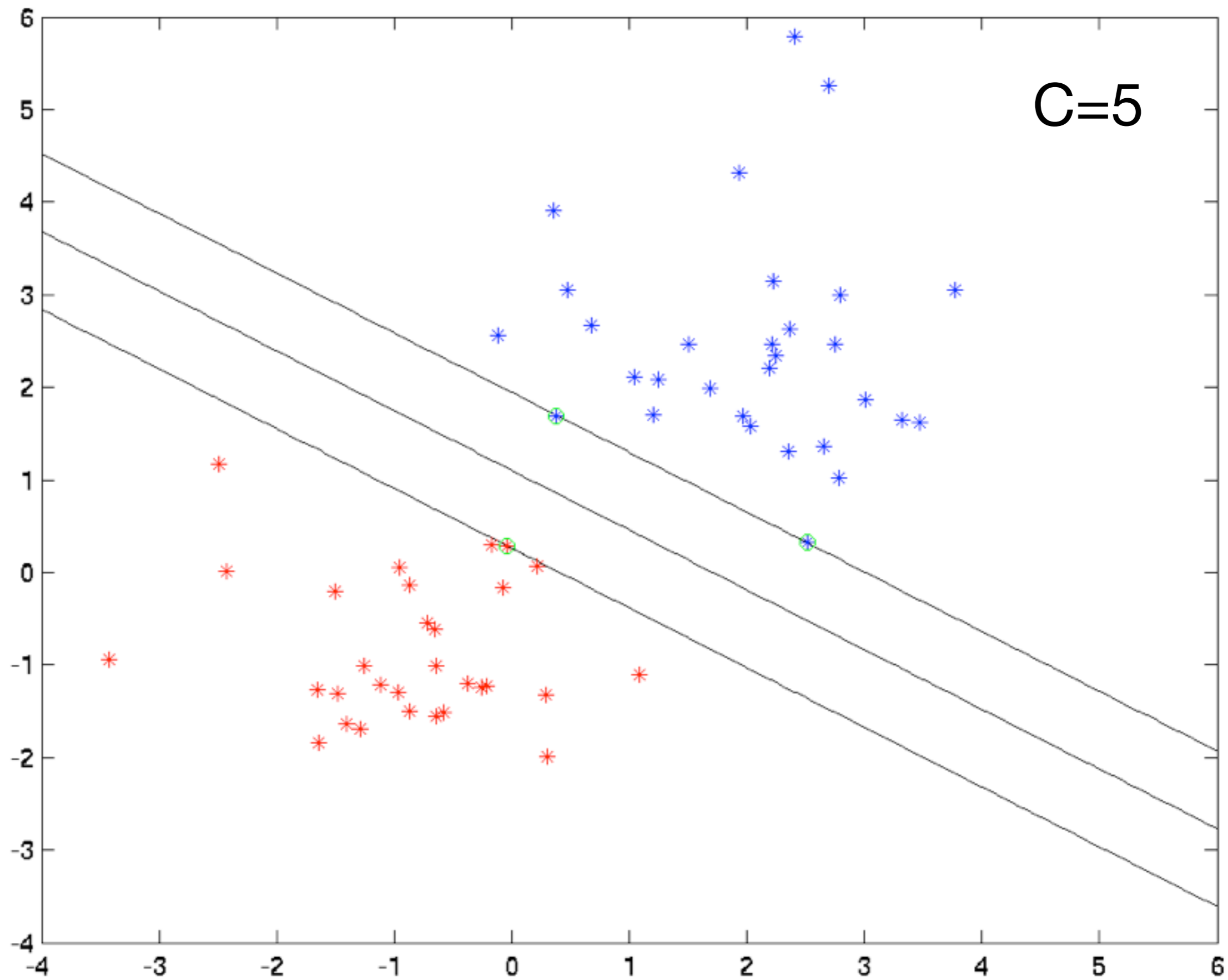


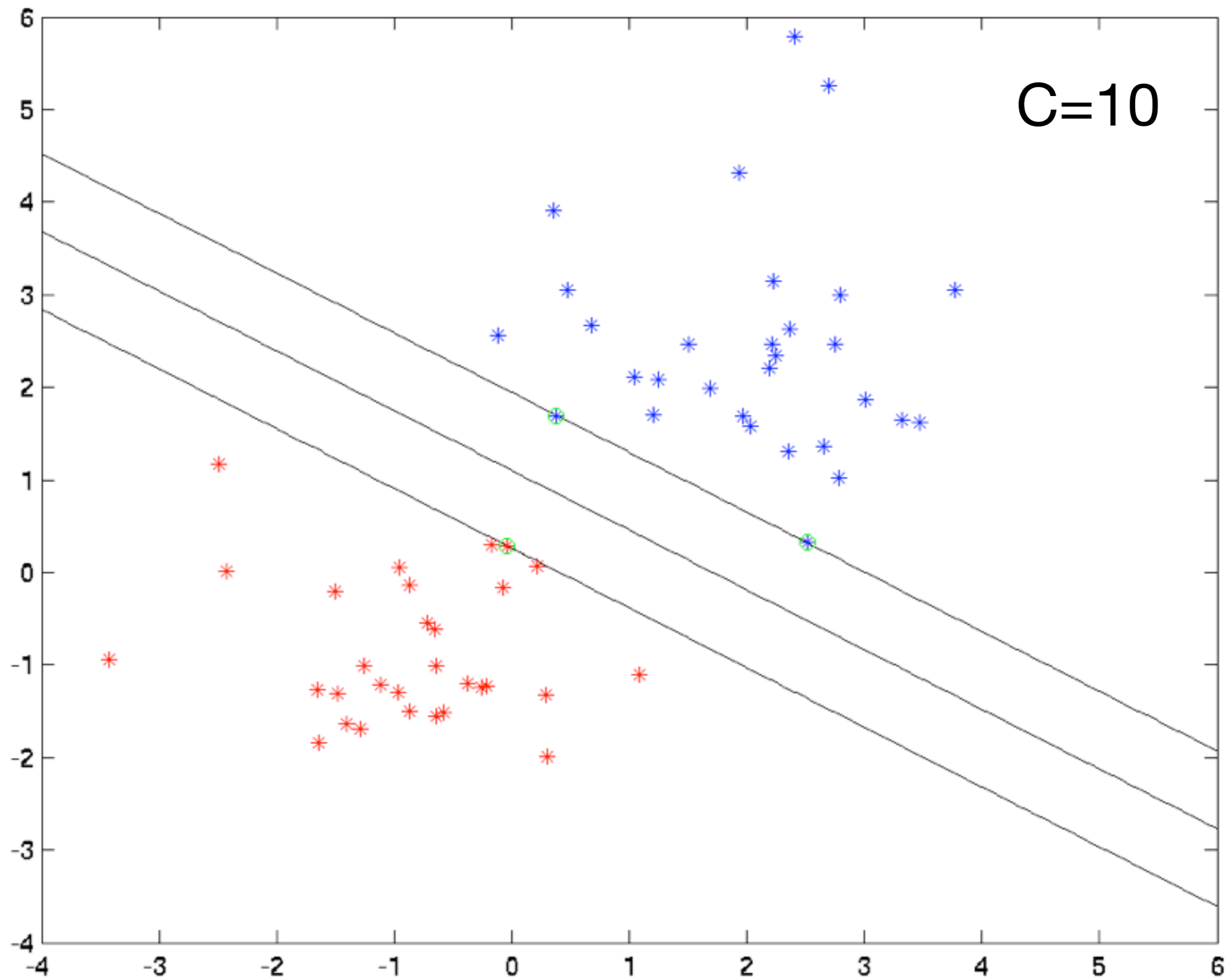


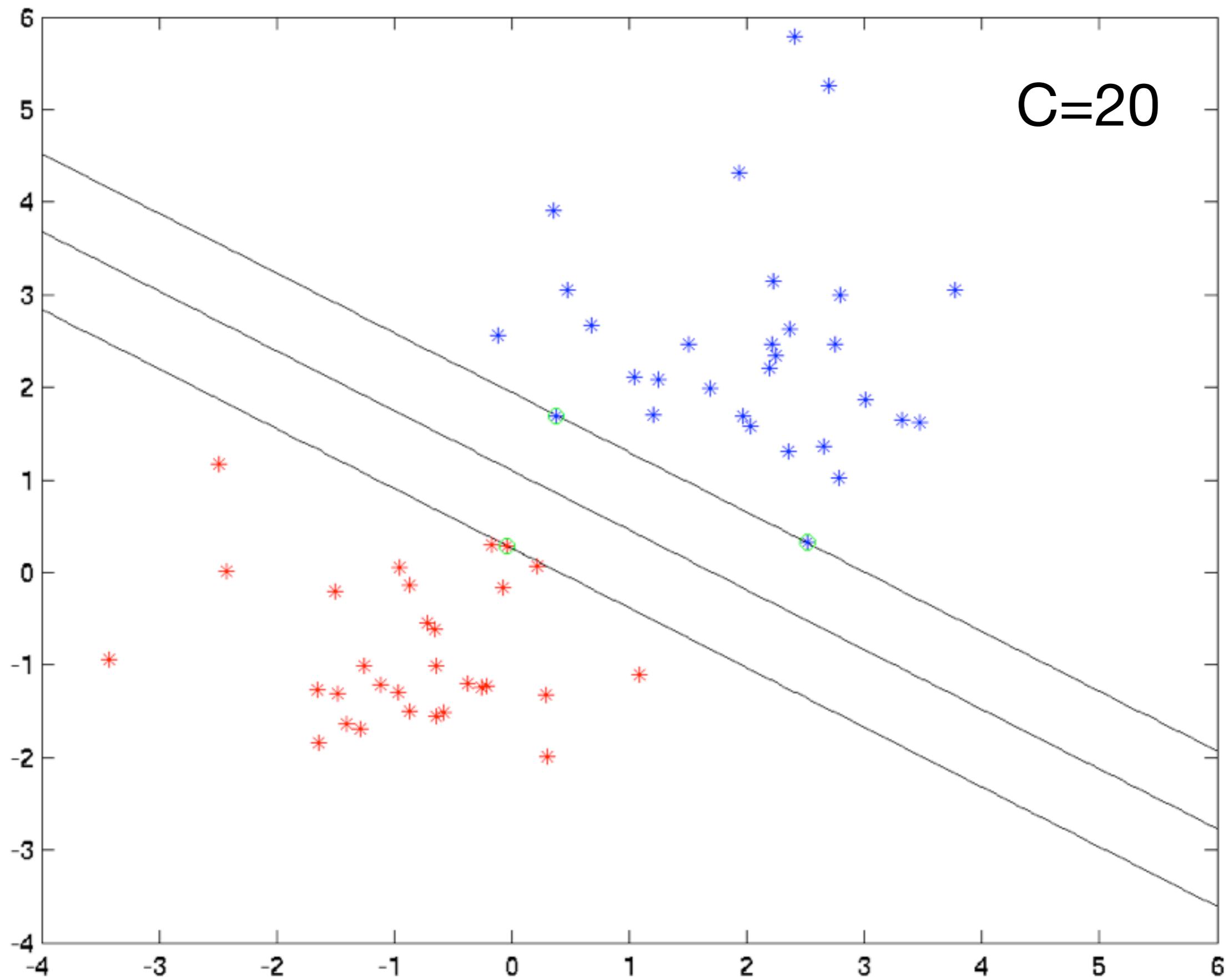


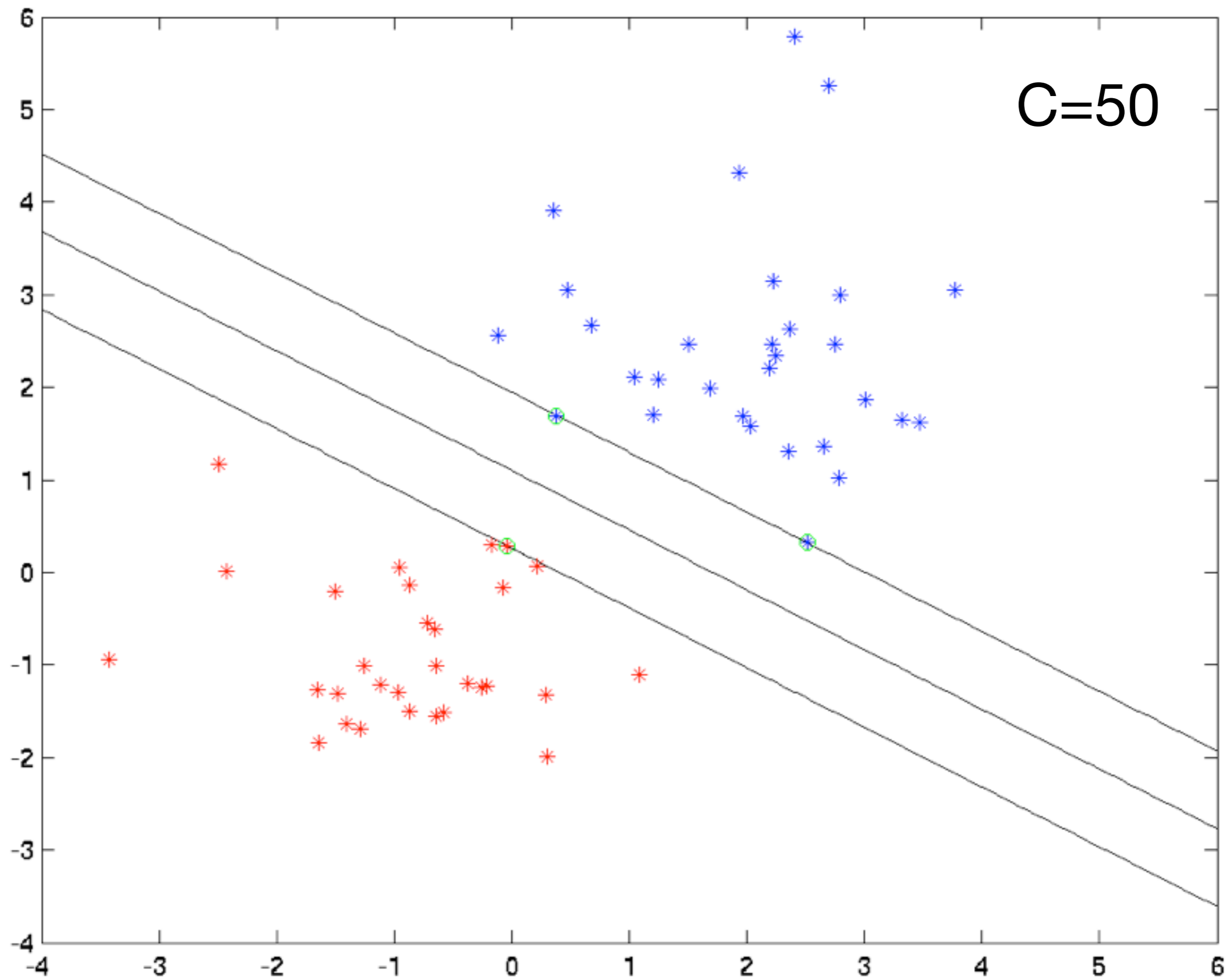


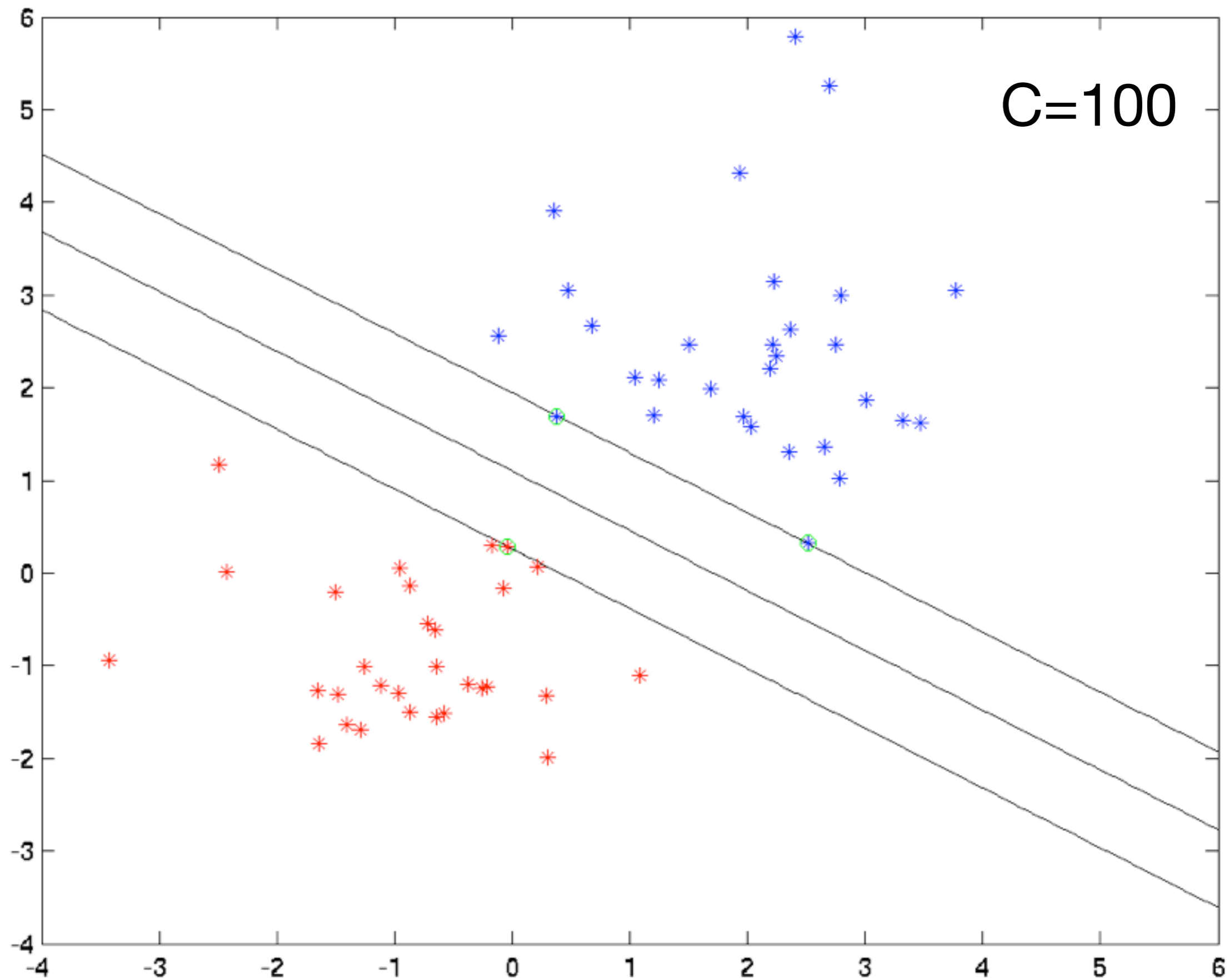


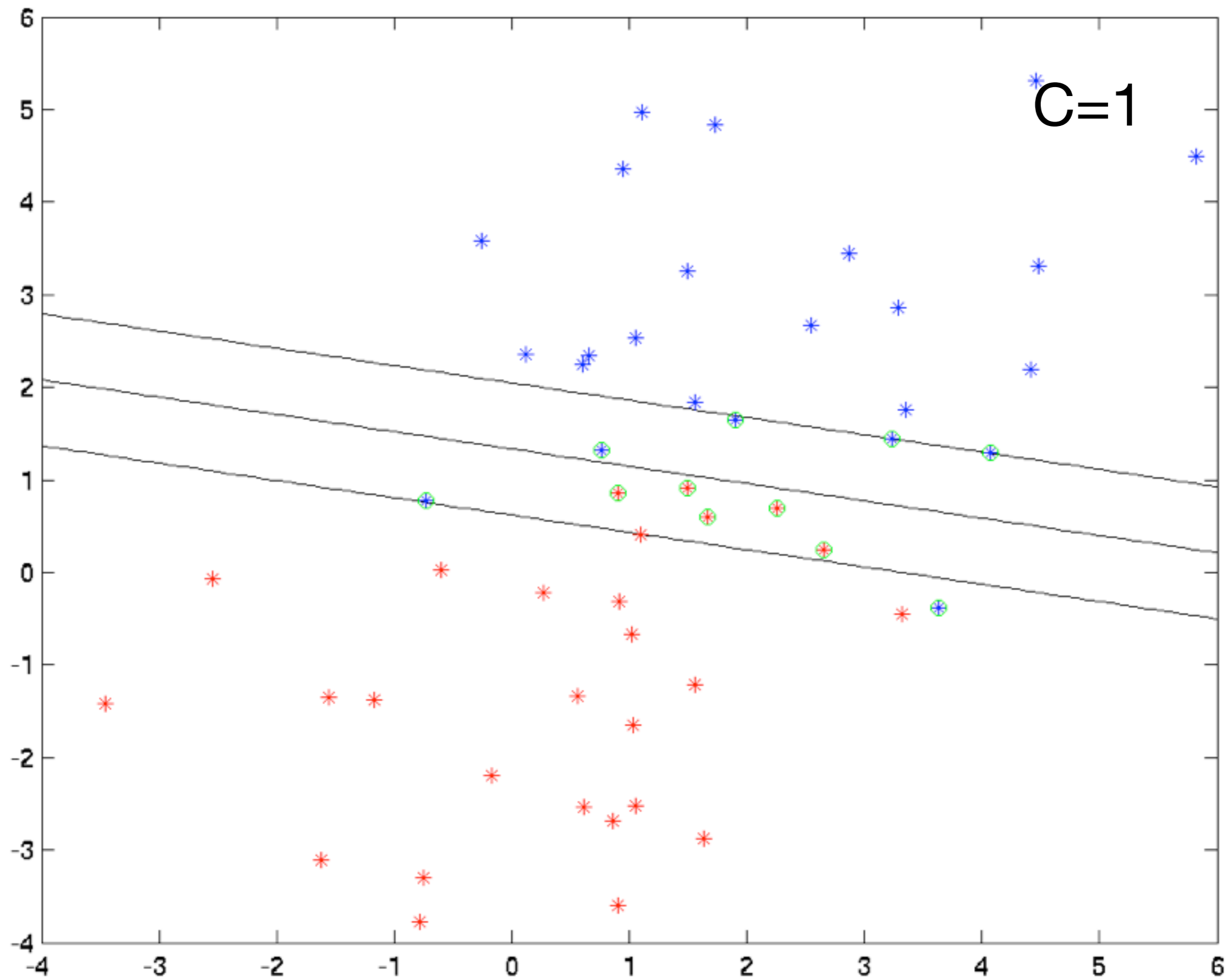


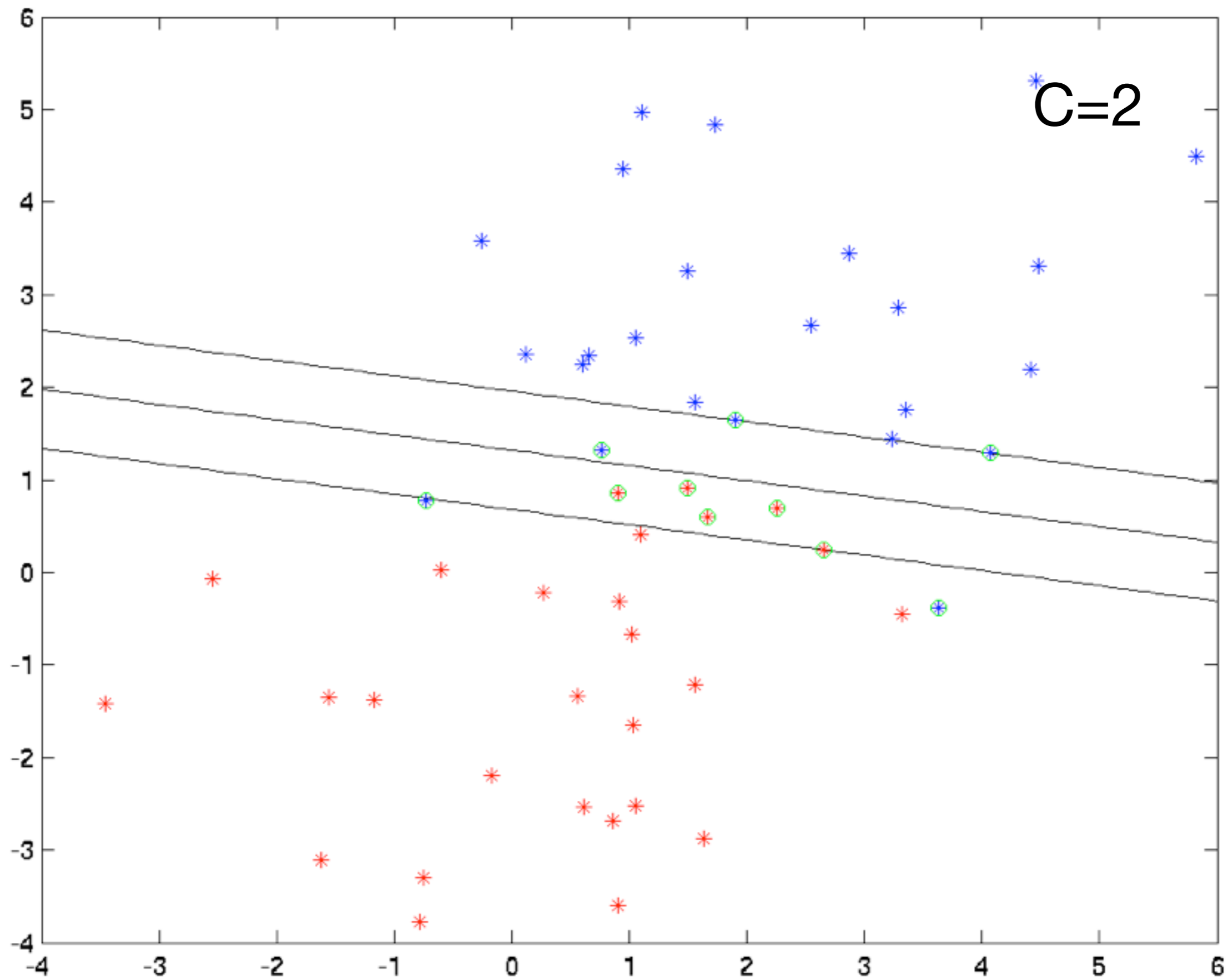


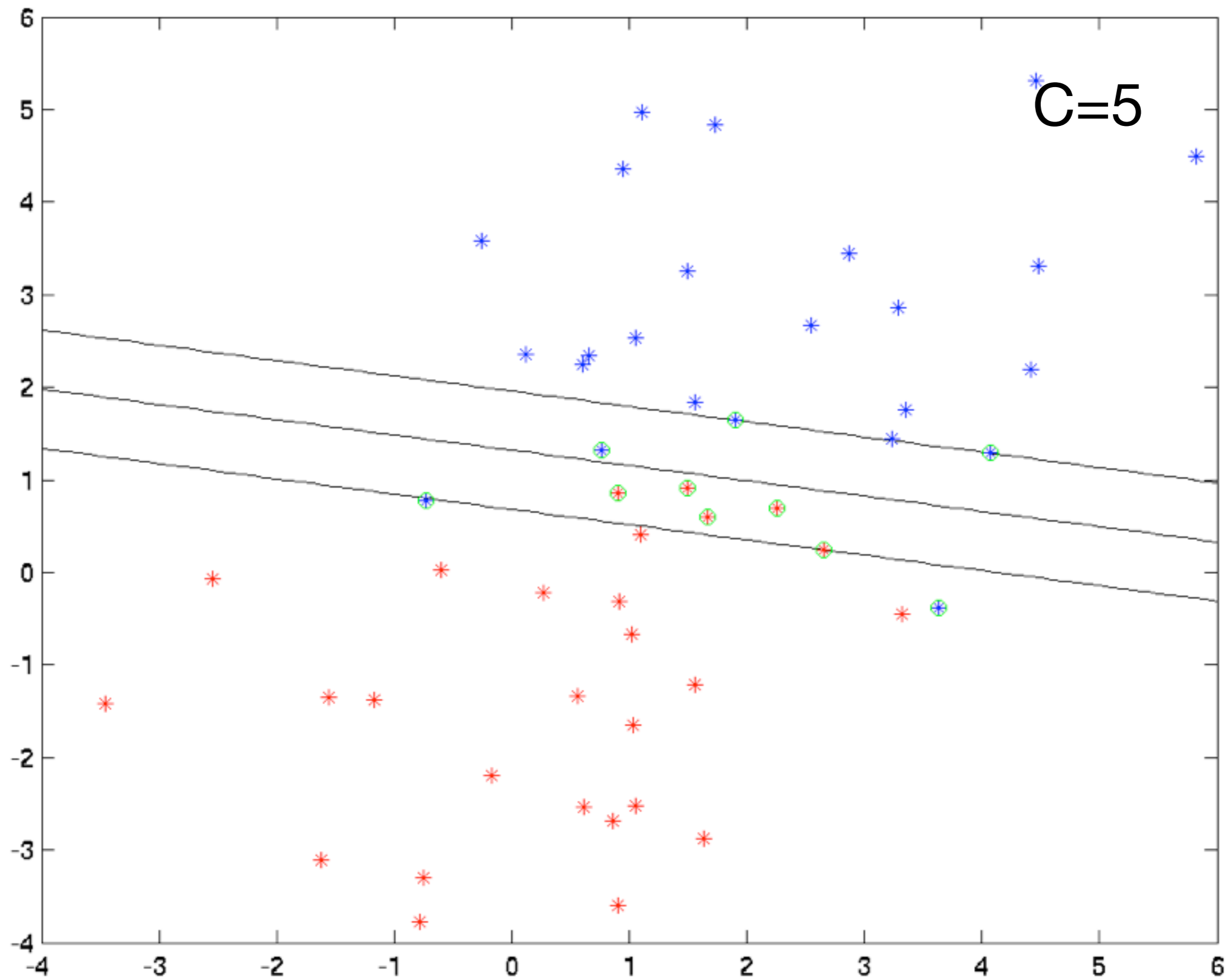






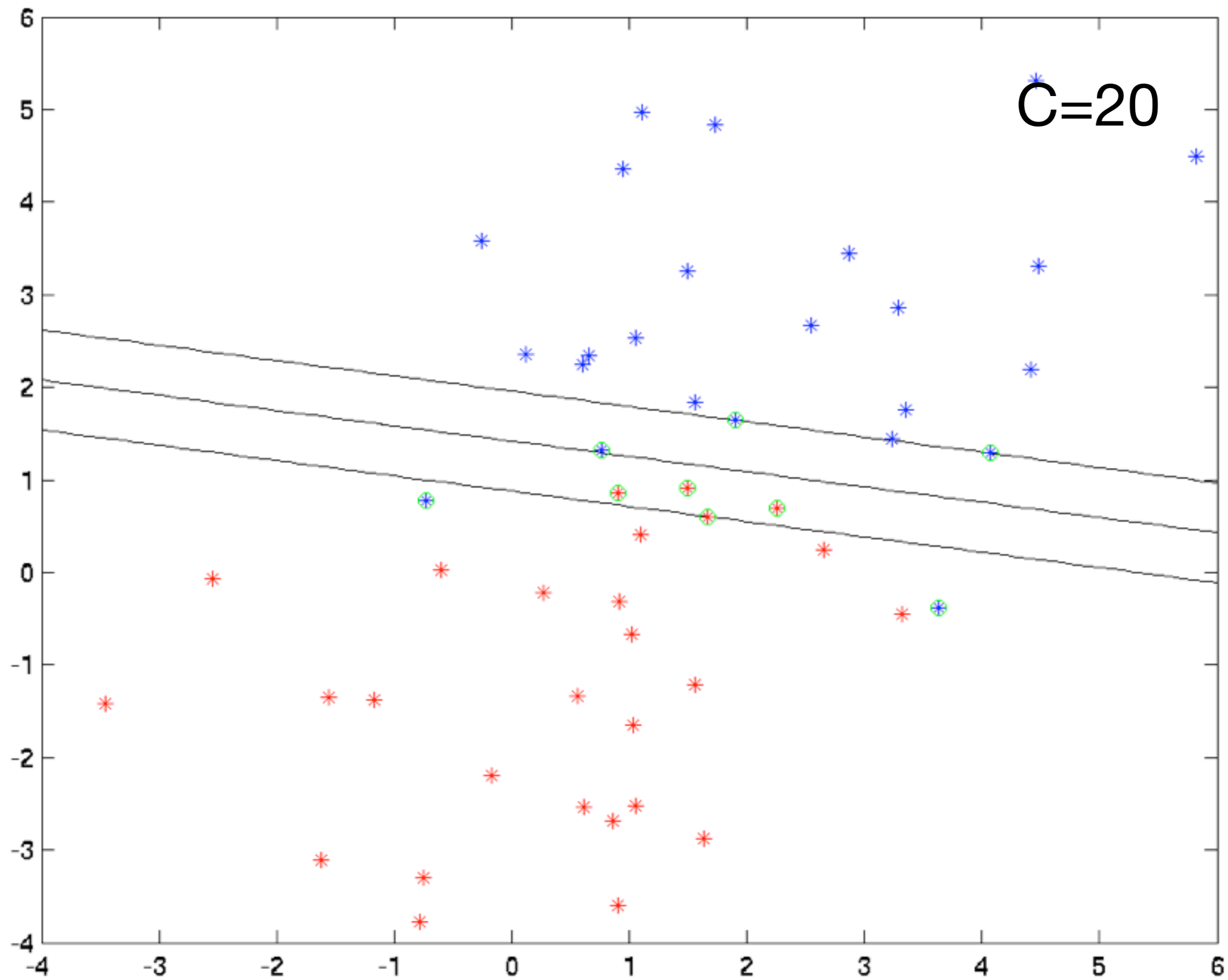


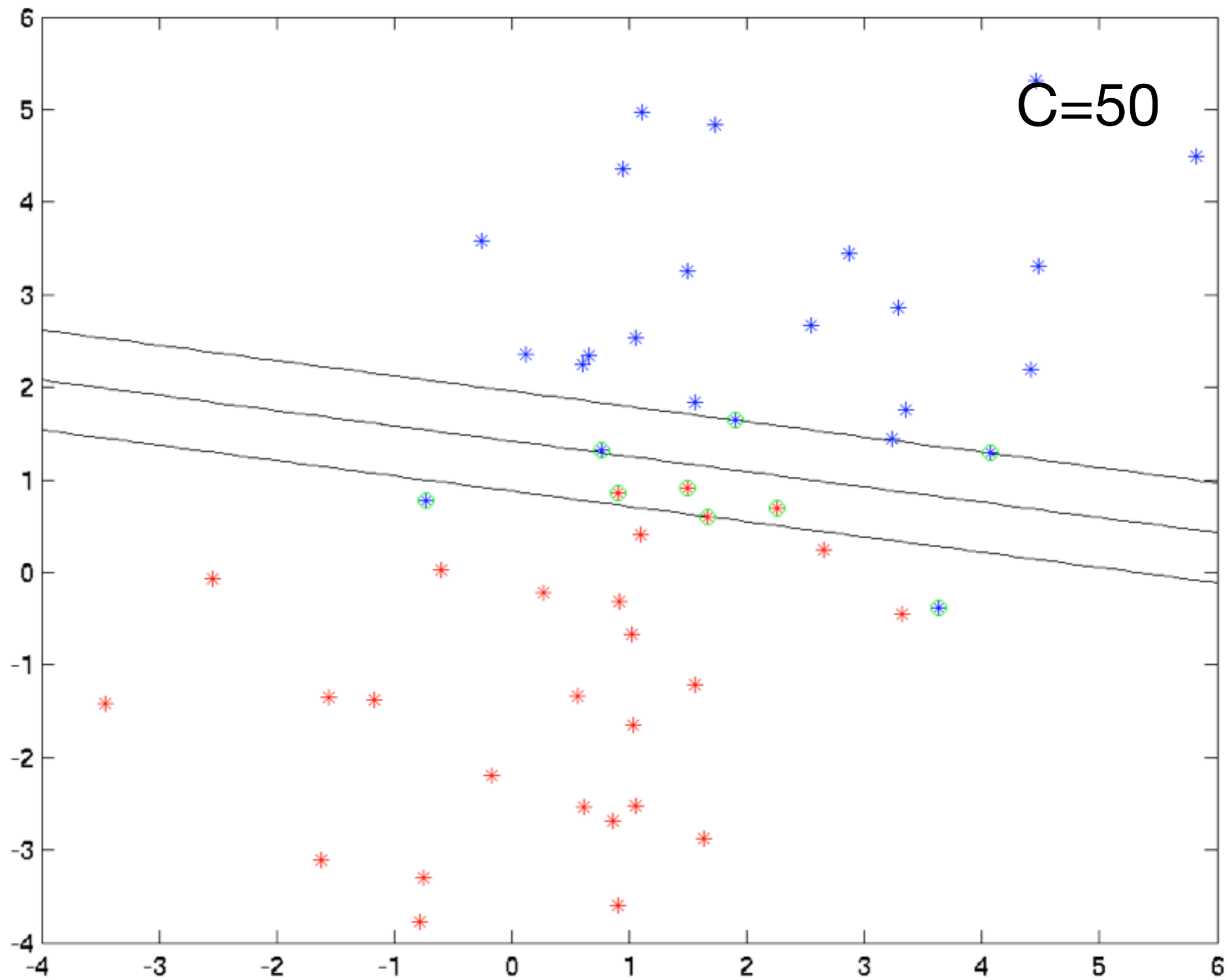


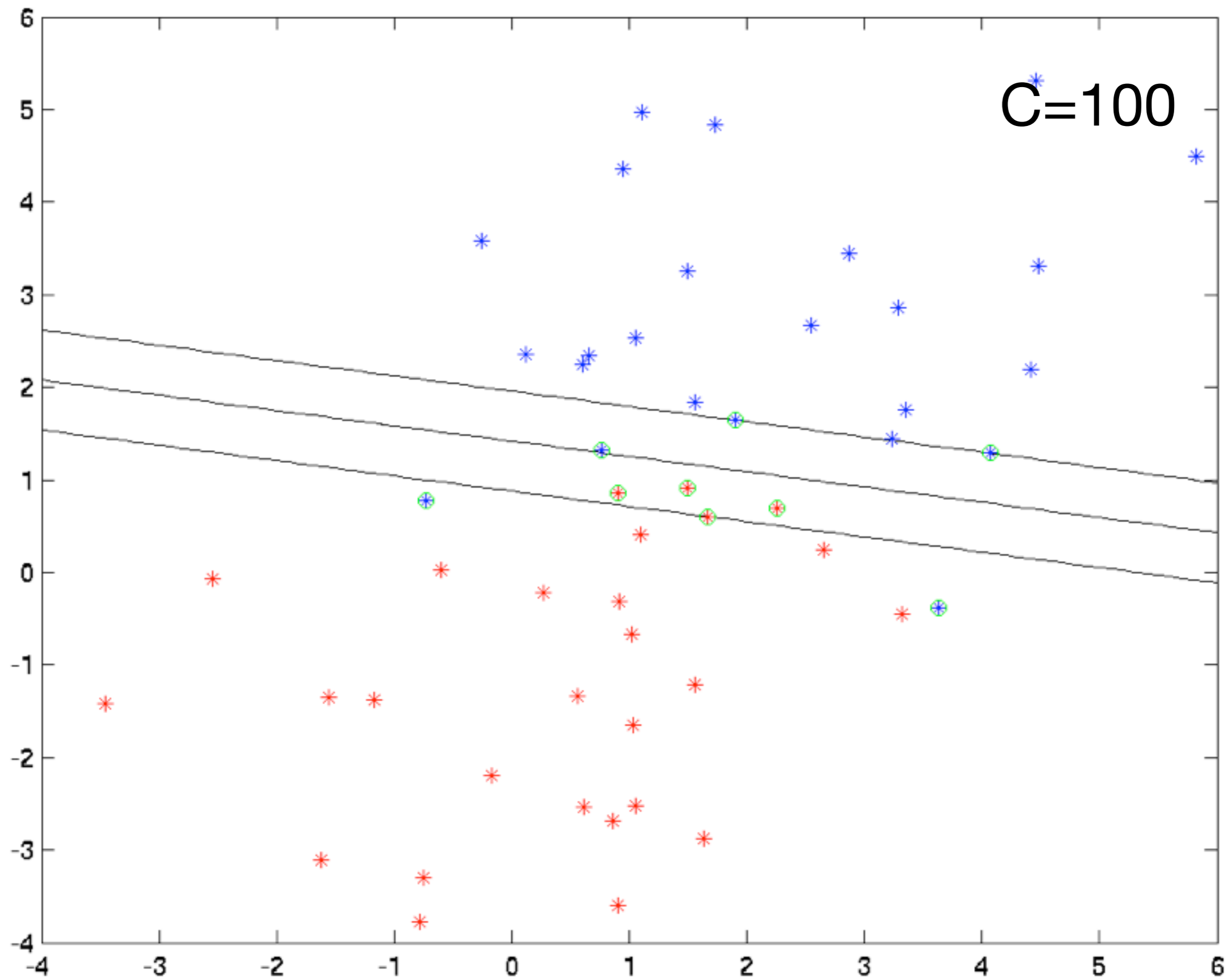












# Solving the optimization problem

- Dual problem

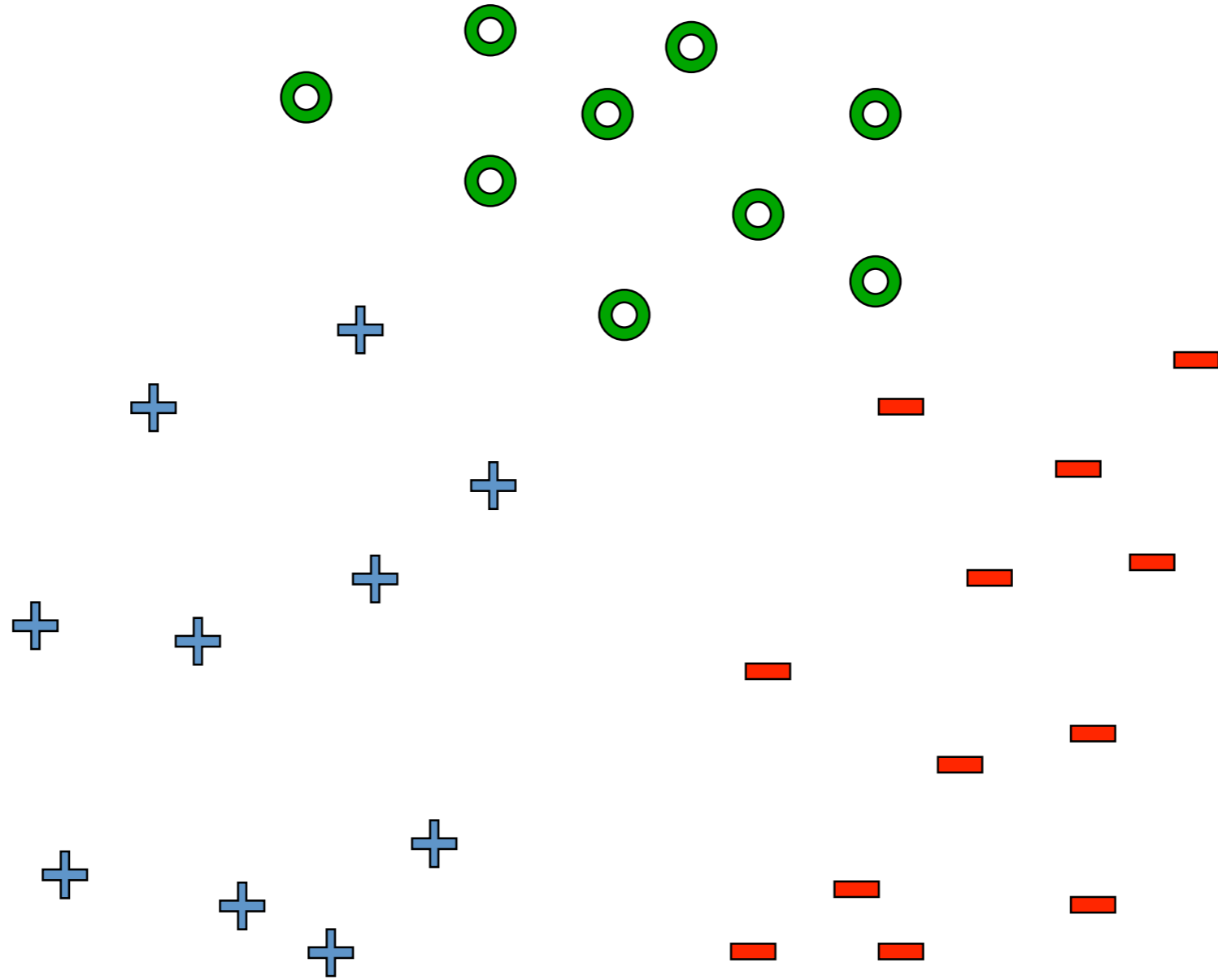
$$\underset{\alpha}{\text{maximize}} \quad -\frac{1}{2} \sum_{i,j} \alpha_i \alpha_j y_i y_j \langle x_i, x_j \rangle + \sum_i \alpha_i$$

$$\text{subject to} \quad \sum_i \alpha_i y_i = 0 \text{ and } \alpha_i \in [0, C]$$

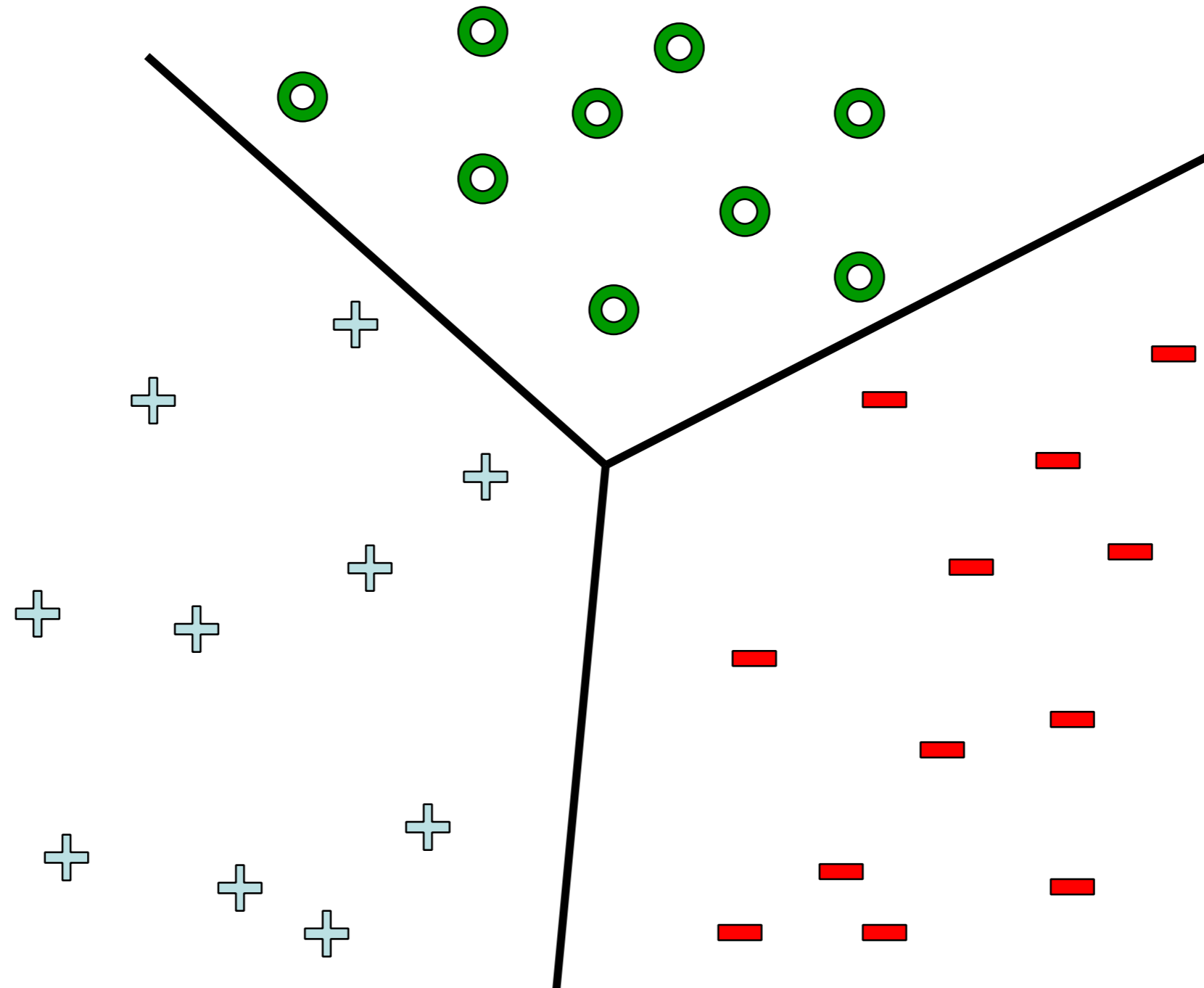
- If problem is small enough (1000s of variables) we can use off-the-shelf solver (CVXOPT, CPLEX, OOQP, LOQO)
- For larger problem use fact that only SVs matter and solve in blocks (active set method).

# Multi-class classification

# Multi-class classification

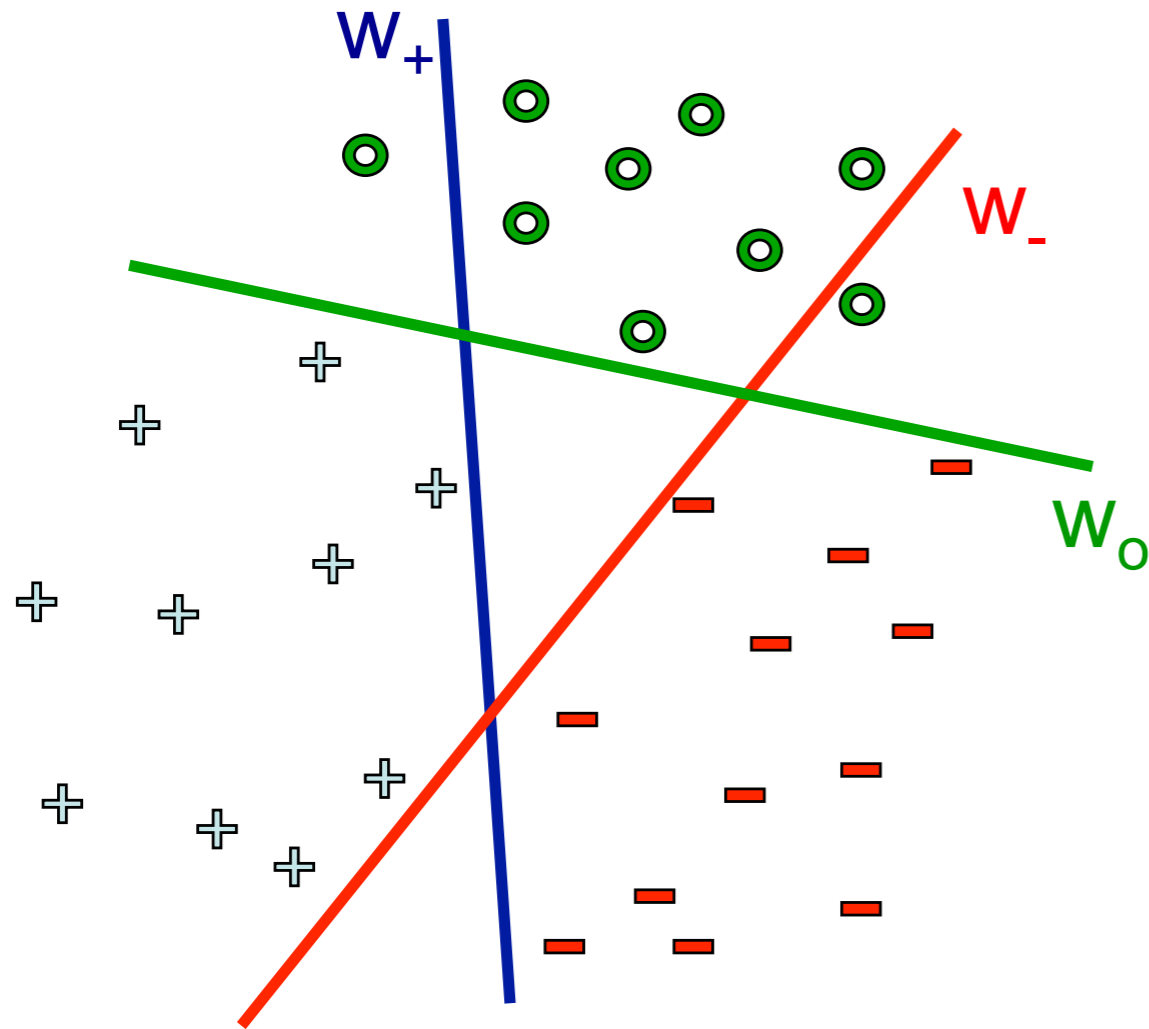


# Multi-class classification





# One versus all classification



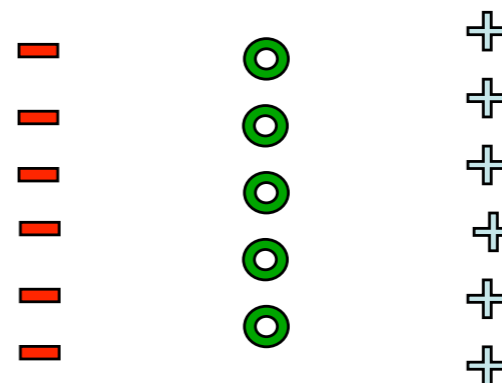
- Learn 3 classifiers:
  - - vs. {0,+}, weights  $w_-$
  - + vs. {0,-}, weights  $w_+$
  - 0 vs. {+,-}, weights  $w_0$

- Predict label using:

$$\hat{y} \leftarrow \arg \max_k w_k \cdot x + b_k$$

- Any problems?

- Could we learn this dataset?

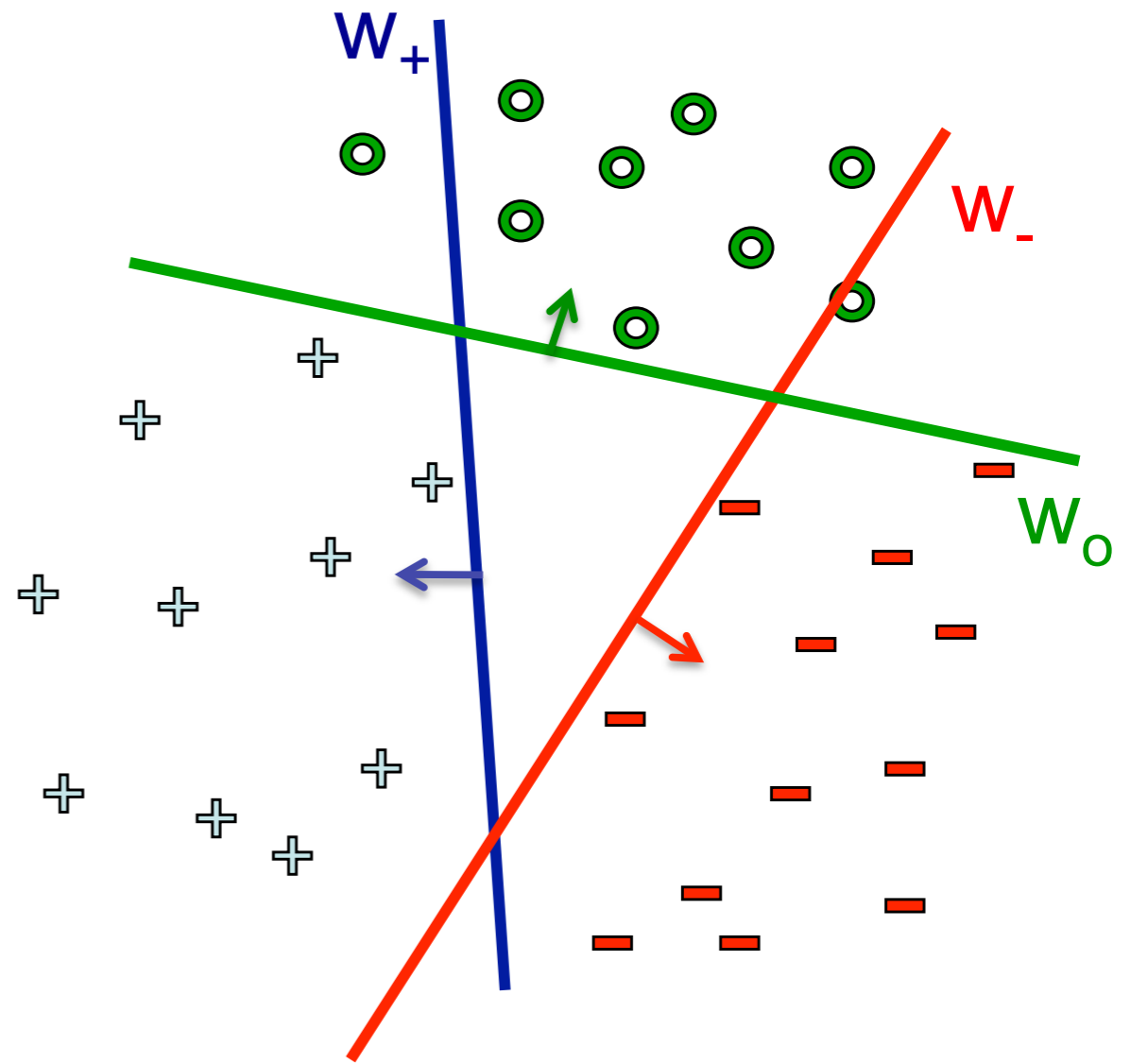


# Multi-class SVM

- Simultaneously learn 3 sets of weights:
- How do we guarantee the correct labels?
- Need new constraints!

The “score” of the correct class must be better than the “score” of wrong classes:

$$w^{(y_j)} \cdot x_j + b^{(y_j)} > w^{(y)} \cdot x_j + b^{(y)} \quad \forall j, y \neq y_j$$



# Multi-class SVM

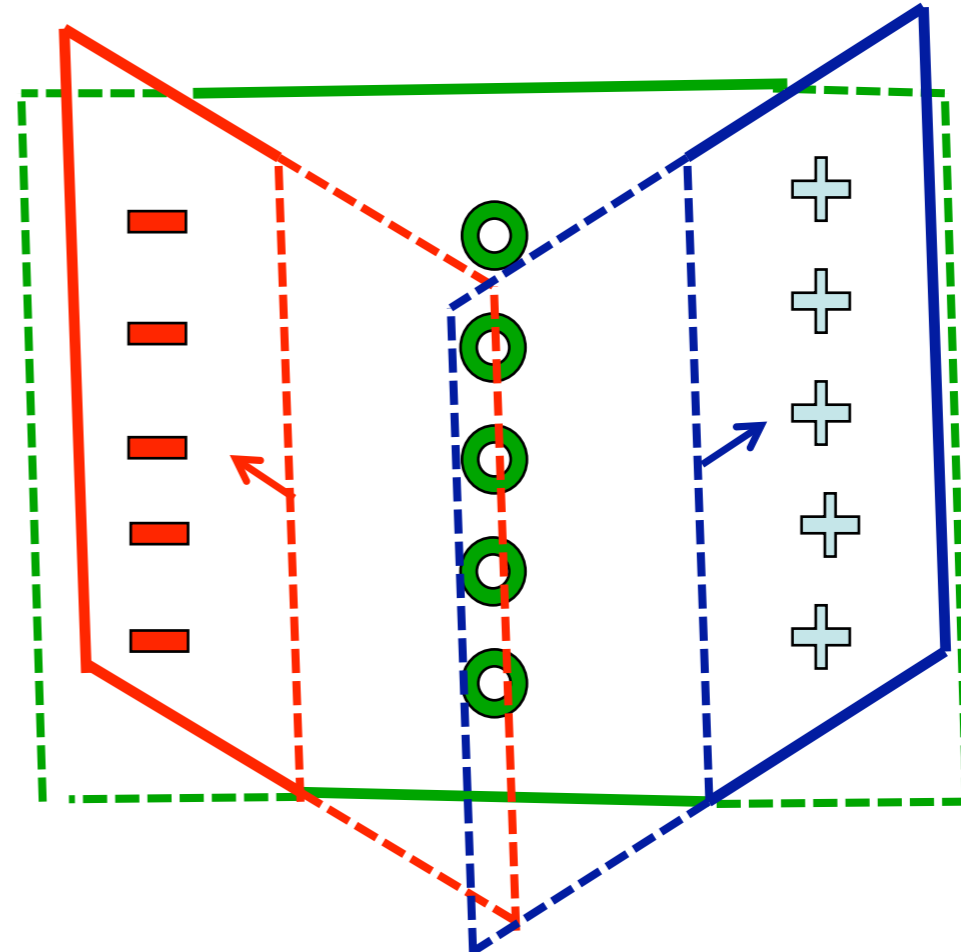
- As for the SVM, we introduce slack variables and maximize margin:

$$\begin{aligned} \text{minimize}_{\mathbf{w}, b} \quad & \sum_y \mathbf{w}^{(y)} \cdot \mathbf{w}^{(y)} + C \sum_j \xi_j \\ \mathbf{w}^{(y_j)} \cdot \mathbf{x}_j + b^{(y_j)} \geq & \mathbf{w}^{(y')} \cdot \mathbf{x}_j + b^{(y')} + 1 - \xi_j, \quad \forall y' \neq y_j, \quad \forall j \\ & \xi_j \geq 0, \quad \forall j \end{aligned}$$

To predict, we use:

$$\hat{y} \leftarrow \arg \max_k w_k \cdot x + b_k$$

Now can we learn it? →

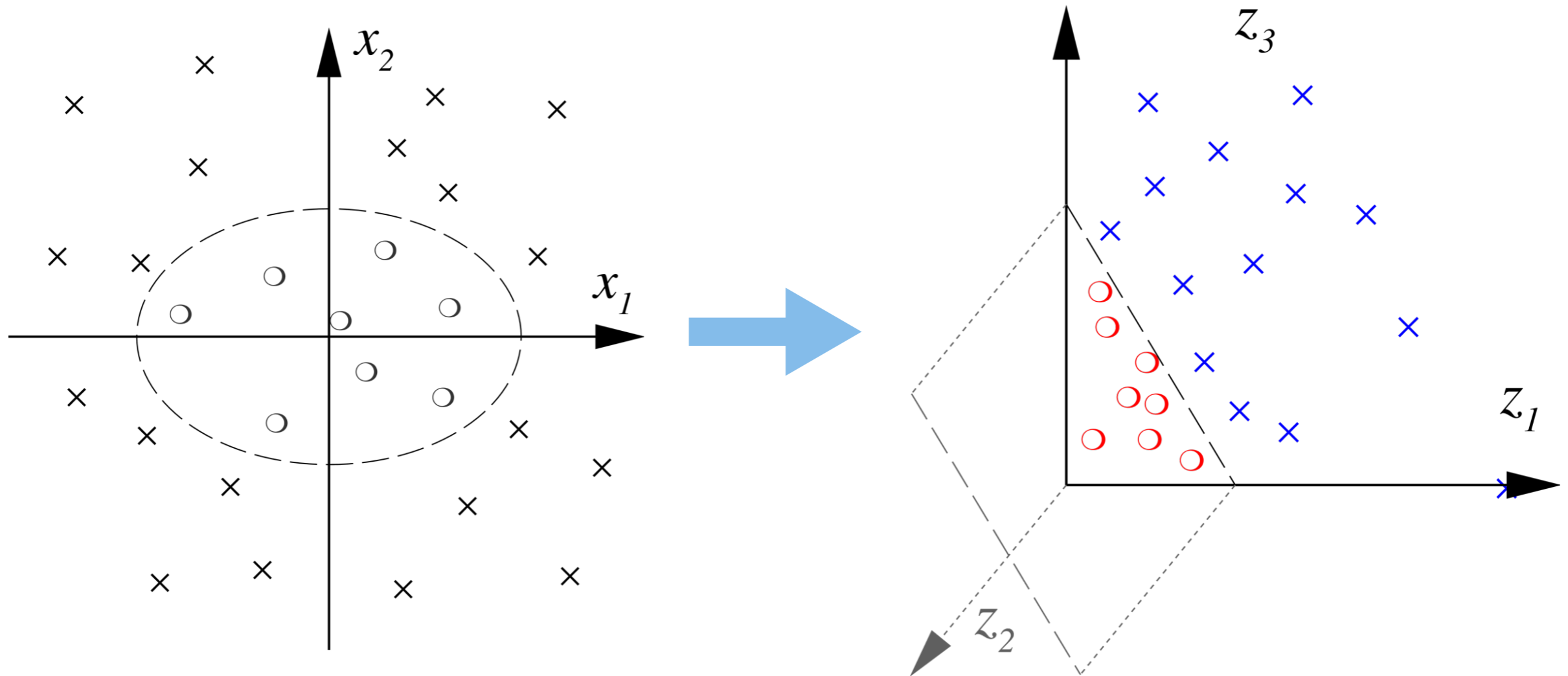


# Kernels

# Non-linear features

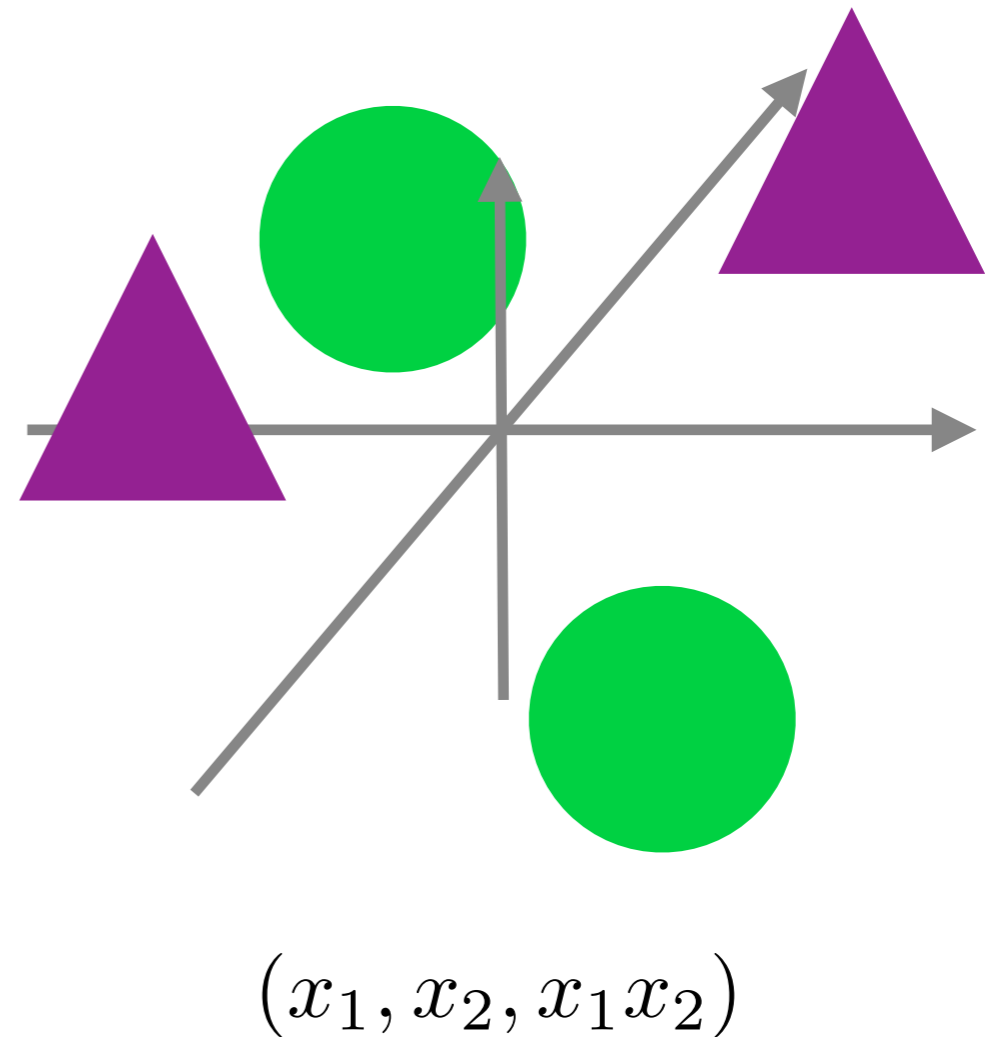
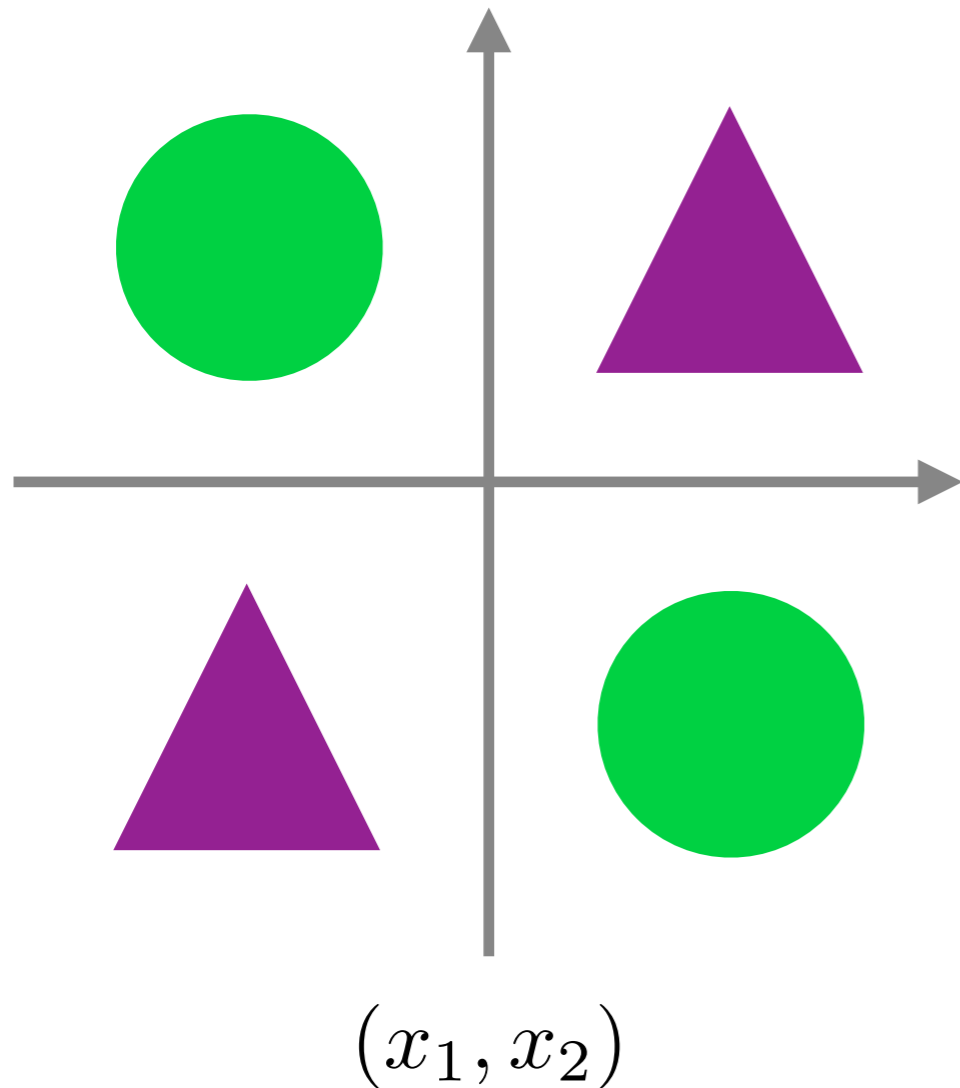
- Regression  
We got nonlinear functions by preprocessing
- Perceptron
  - Map data into feature space  $x \rightarrow \phi(x)$
  - Solve problem in this space
  - Query replace  $\langle x, x' \rangle$  by  $\langle \phi(x), \phi(x') \rangle$  for code
- Feature Perceptron
  - Solution in span of  $\phi(x_i)$

# Non-linear features



- Separating surfaces are  
Circles, hyperbolae, parabolae

# Solving XOR



- XOR not linearly separable
- Mapping into 3 dimensions makes it easily solvable

# Quadratic Features

## Quadratic Features in $\mathbb{R}^2$

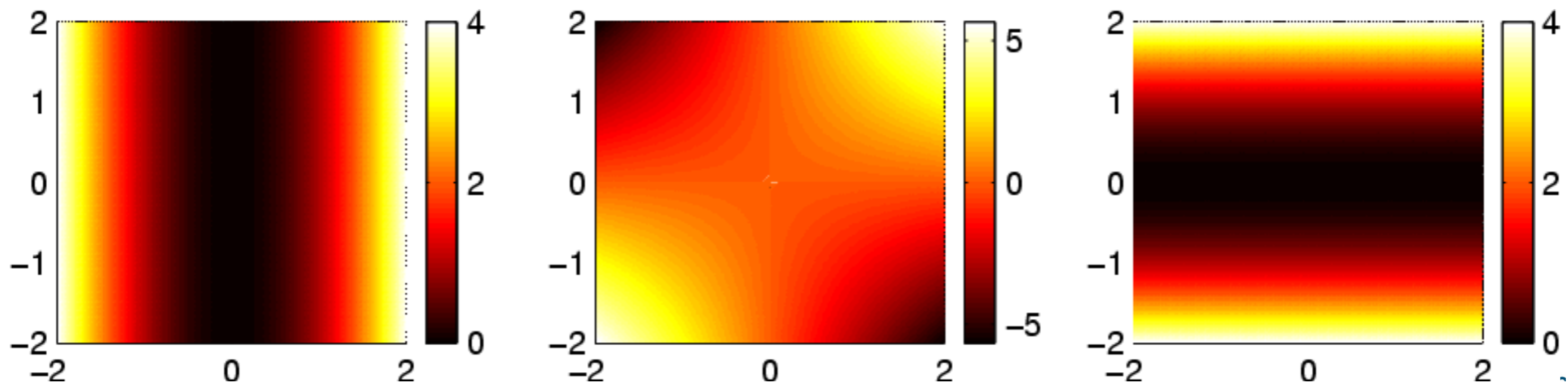
$$\Phi(x) := \left( x_1^2, \sqrt{2}x_1x_2, x_2^2 \right)$$

## Dot Product

$$\begin{aligned} \langle \Phi(x), \Phi(x') \rangle &= \left\langle \left( x_1^2, \sqrt{2}x_1x_2, x_2^2 \right), \left( x_1'^2, \sqrt{2}x_1'x_2', x_2'^2 \right) \right\rangle \\ &= \langle x, x' \rangle^2. \end{aligned}$$

## Insight

Trick works for any polynomials of order via  $\langle x, x' \rangle^d$ .





# SVM with a polynomial Kernel visualization

Created by:  
Udi Aharoni

# Computational Efficiency

## Problem

- Extracting features can sometimes be very costly.
- Example: second order features in 1000 dimensions. This leads to  $5 \cdot 10^5$  numbers. For higher order polynomial features much worse.

## Solution

Don't compute the features, try to compute dot products implicitly. For some features this works ...

## Definition

A kernel function  $k : \mathcal{X} \times \mathcal{X} \rightarrow \mathbb{R}$  is a symmetric function in its arguments for which the following property holds

$$k(x, x') = \langle \Phi(x), \Phi(x') \rangle \text{ for some feature map } \Phi.$$

If  $k(x, x')$  is much cheaper to compute than  $\Phi(x)$  ...

# Recap: The Perceptron

**initialize**  $w = 0$  and  $b = 0$

**repeat**

**if**  $y_i [\langle w, x_i \rangle + b] \leq 0$  **then**

$w \leftarrow w + y_i x_i$  and  $b \leftarrow b + y_i$

**end if**

**until** all classified correctly

- Nothing happens if classified correctly

- Weight vector is linear combination  $w = \sum_{i \in I} y_i x_i$

- Classifier is linear combination of inner products  $f(x) = \sum_{i \in I} y_i \langle x_i, x \rangle + b$

# Recap: The Perceptron on features

initialize  $w, b = 0$

repeat

Pick  $(x_i, y_i)$  from data

if  $y_i(w \cdot \Phi(x_i) + b) \leq 0$  then

$$w' = w + y_i \Phi(x_i)$$

$$b' = b + y_i$$

until  $y_i(w \cdot \Phi(x_i) + b) > 0$  for all  $i$

- Nothing happens if classified correctly
- Weight vector is linear combination  $w = \sum_{i \in I} y_i \phi(x_i)$
- Classifier is linear combination of inner products  $f(x) = \sum_{i \in I} y_i \langle \phi(x_i), \phi(x) \rangle + b$

# The Kernel Perceptron

initialize  $f = 0$

repeat

Pick  $(x_i, y_i)$  from data

if  $y_i f(x_i) \leq 0$  then

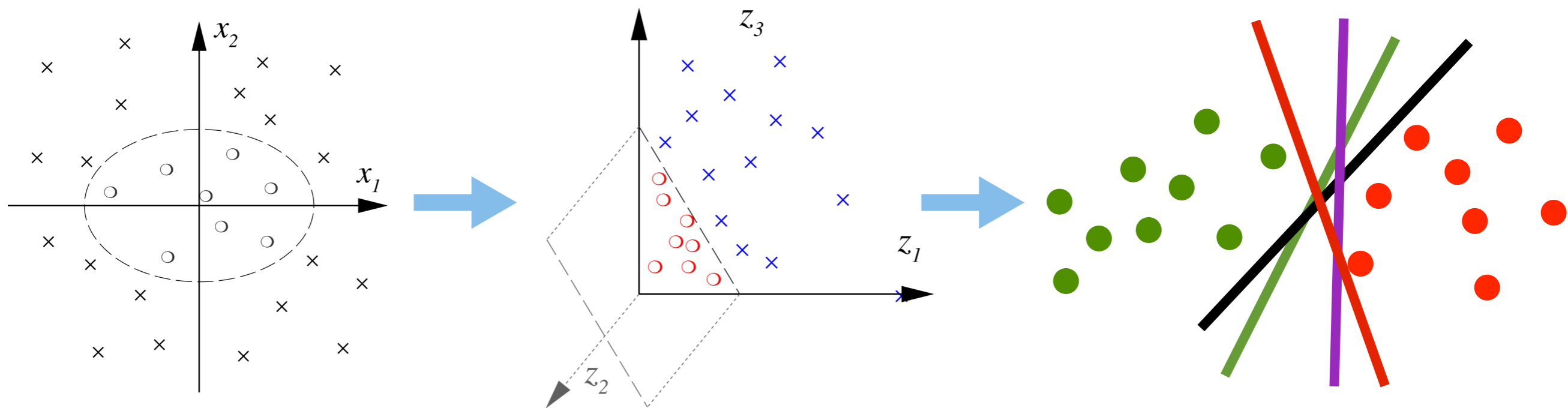
$$f(\cdot) \leftarrow f(\cdot) + y_i k(x_i, \cdot) + y_i$$

until  $y_i f(x_i) > 0$  for all  $i$

- Nothing happens if classified correctly
- Weight vector is linear combination  $w = \sum_{i \in I} y_i \phi(x_i)$
- Classifier is linear combination of inner products

$$f(x) = \sum_{i \in I} y_i \langle \phi(x_i), \phi(x) \rangle + b = \sum_{i \in I} y_i k(x_i, x) + b$$

# Processing Pipeline



- Original data
- Data in feature space (implicit)
- Solve in feature space using kernels

# Polynomial Kernels

## Idea

- We want to extend  $k(x, x') = \langle x, x' \rangle^2$  to

$$k(x, x') = (\langle x, x' \rangle + c)^d \text{ where } c > 0 \text{ and } d \in \mathbb{N}.$$

- Prove that such a kernel corresponds to a dot product.

## Proof strategy

Simple and straightforward: compute the explicit sum given by the kernel, i.e.

$$k(x, x') = (\langle x, x' \rangle + c)^d = \sum_{i=0}^d \binom{d}{i} (\langle x, x' \rangle)^i c^{d-i}$$

Individual terms  $(\langle x, x' \rangle)^i$  are dot products for some  $\Phi_i(x)$ .

# Kernel Conditions

## Computability

We have to be able to compute  $k(x, x')$  efficiently (much cheaper than dot products themselves).

## “Nice and Useful” Functions

The features themselves have to be useful for the learning problem at hand. Quite often this means smooth functions.

## Symmetry

Obviously  $k(x, x') = k(x', x)$  due to the symmetry of the dot product  $\langle \Phi(x), \Phi(x') \rangle = \langle \Phi(x'), \Phi(x) \rangle$ .

## Dot Product in Feature Space

Is there always a  $\Phi$  such that  $k$  really is a dot product?



# Mercer's Theorem

## The Theorem

For any symmetric function  $k : \mathcal{X} \times \mathcal{X} \rightarrow \mathbb{R}$  which is square integrable in  $\mathcal{X} \times \mathcal{X}$  and which satisfies

$$\int_{\mathcal{X} \times \mathcal{X}} k(x, x') f(x) f(x') dx dx' \geq 0 \text{ for all } f \in L_2(\mathcal{X})$$

there exist  $\phi_i : \mathcal{X} \rightarrow \mathbb{R}$  and numbers  $\lambda_i \geq 0$  where

$$k(x, x') = \sum_i \lambda_i \phi_i(x) \phi_i(x') \text{ for all } x, x' \in \mathcal{X}.$$

## Interpretation

Double integral is the continuous version of a vector-matrix-vector multiplication. For positive semidefinite matrices we have

$$\sum \sum k(x_i, x_j) \alpha_i \alpha_j \geq 0$$

# Properties

## Distance in Feature Space

Distance between points in feature space via

$$\begin{aligned}d(x, x')^2 &:= \|\Phi(x) - \Phi(x')\|^2 \\ &= \langle \Phi(x), \Phi(x) \rangle - 2\langle \Phi(x), \Phi(x') \rangle + \langle \Phi(x'), \Phi(x') \rangle \\ &= k(x, x) + k(x', x') - 2k(x, x')\end{aligned}$$

## Kernel Matrix

To compare observations we compute dot products, so we study the matrix  $K$  given by

$$K_{ij} = \langle \Phi(x_i), \Phi(x_j) \rangle = k(x_i, x_j)$$

where  $x_i$  are the training patterns.

## Similarity Measure

The entries  $K_{ij}$  tell us the overlap between  $\Phi(x_i)$  and  $\Phi(x_j)$ , so  $k(x_i, x_j)$  is a similarity measure.

# Properties

## $K$ is Positive Semidefinite

Claim:  $\alpha^\top K \alpha \geq 0$  for all  $\alpha \in \mathbb{R}^m$  and all kernel matrices  $K \in \mathbb{R}^{m \times m}$ . Proof:

$$\begin{aligned} \sum_{i,j}^m \alpha_i \alpha_j K_{ij} &= \sum_{i,j}^m \alpha_i \alpha_j \langle \Phi(x_i), \Phi(x_j) \rangle \\ &= \left\langle \sum_i^m \alpha_i \Phi(x_i), \sum_j^m \alpha_j \Phi(x_j) \right\rangle = \left\| \sum_{i=1}^m \alpha_i \Phi(x_i) \right\|^2 \end{aligned}$$

## Kernel Expansion

If  $w$  is given by a linear combination of  $\Phi(x_i)$  we get

$$\langle w, \Phi(x) \rangle = \left\langle \sum_{i=1}^m \alpha_i \Phi(x_i), \Phi(x) \right\rangle = \sum_{i=1}^m \alpha_i k(x_i, x).$$

# Examples

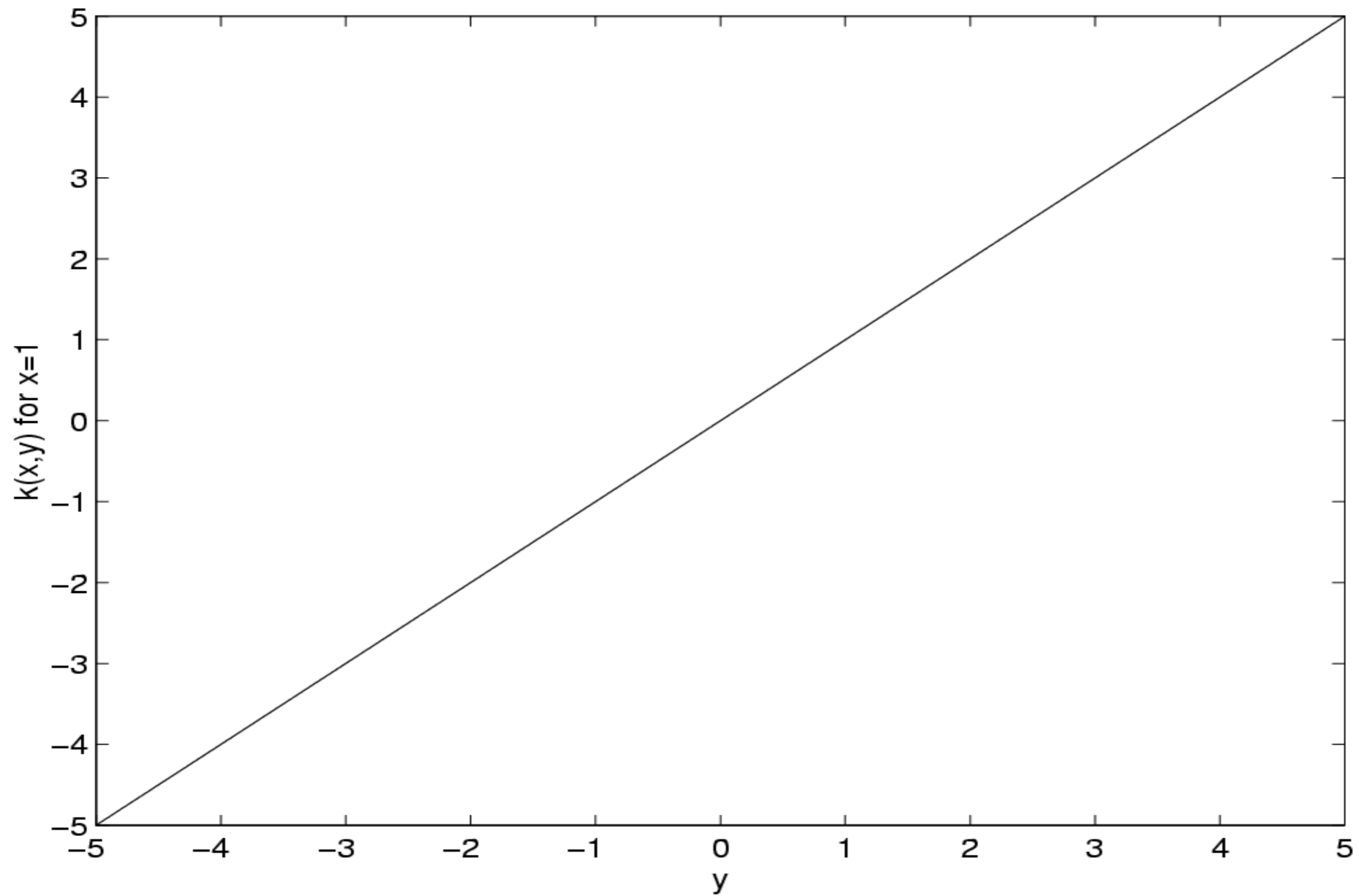
## Examples of kernels $k(x, x')$

Linear	$\langle x, x' \rangle$
Laplacian RBF	$\exp(-\lambda \ x - x'\ )$
Gaussian RBF	$\exp(-\lambda \ x - x'\ ^2)$
Polynomial	$(\langle x, x' \rangle + c)^d, c \geq 0, d \in \mathbb{N}$
B-Spline	$B_{2n+1}(x - x')$
Cond. Expectation	$\mathbf{E}_c[p(x c)p(x' c)]$

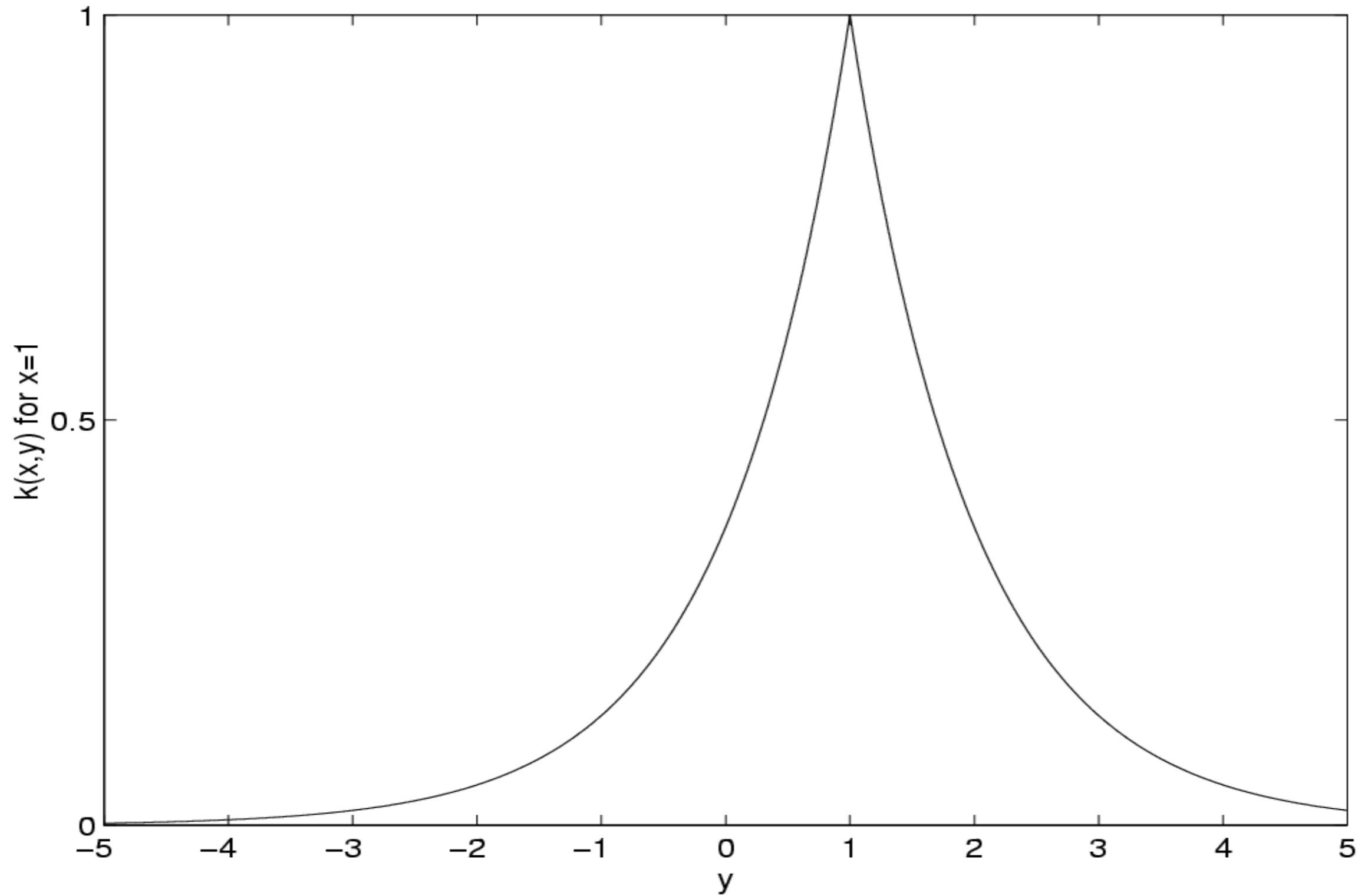
## Simple trick for checking Mercer's condition

Compute the Fourier transform of the kernel and check that it is nonnegative.

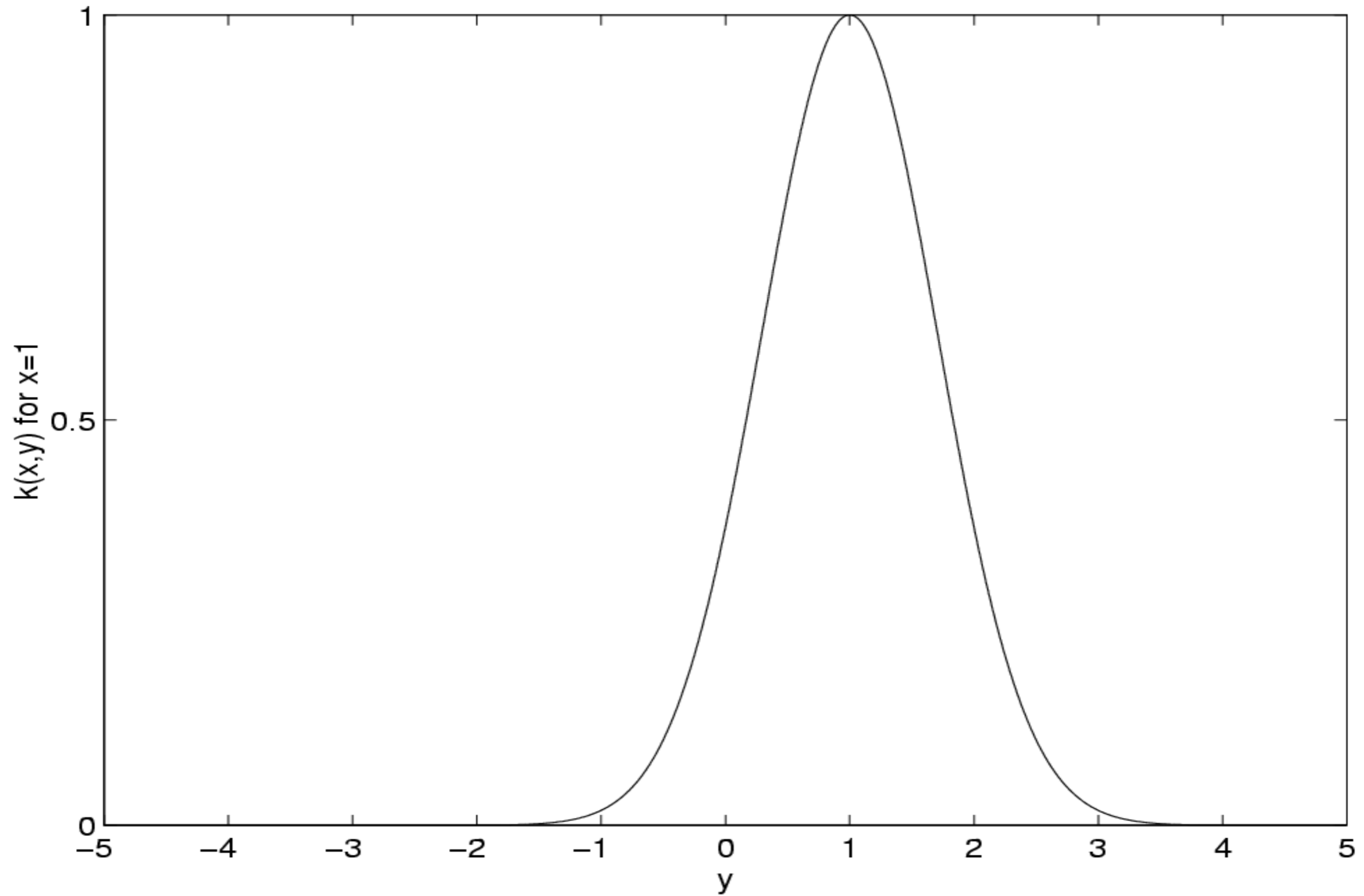
# Linear Kernel



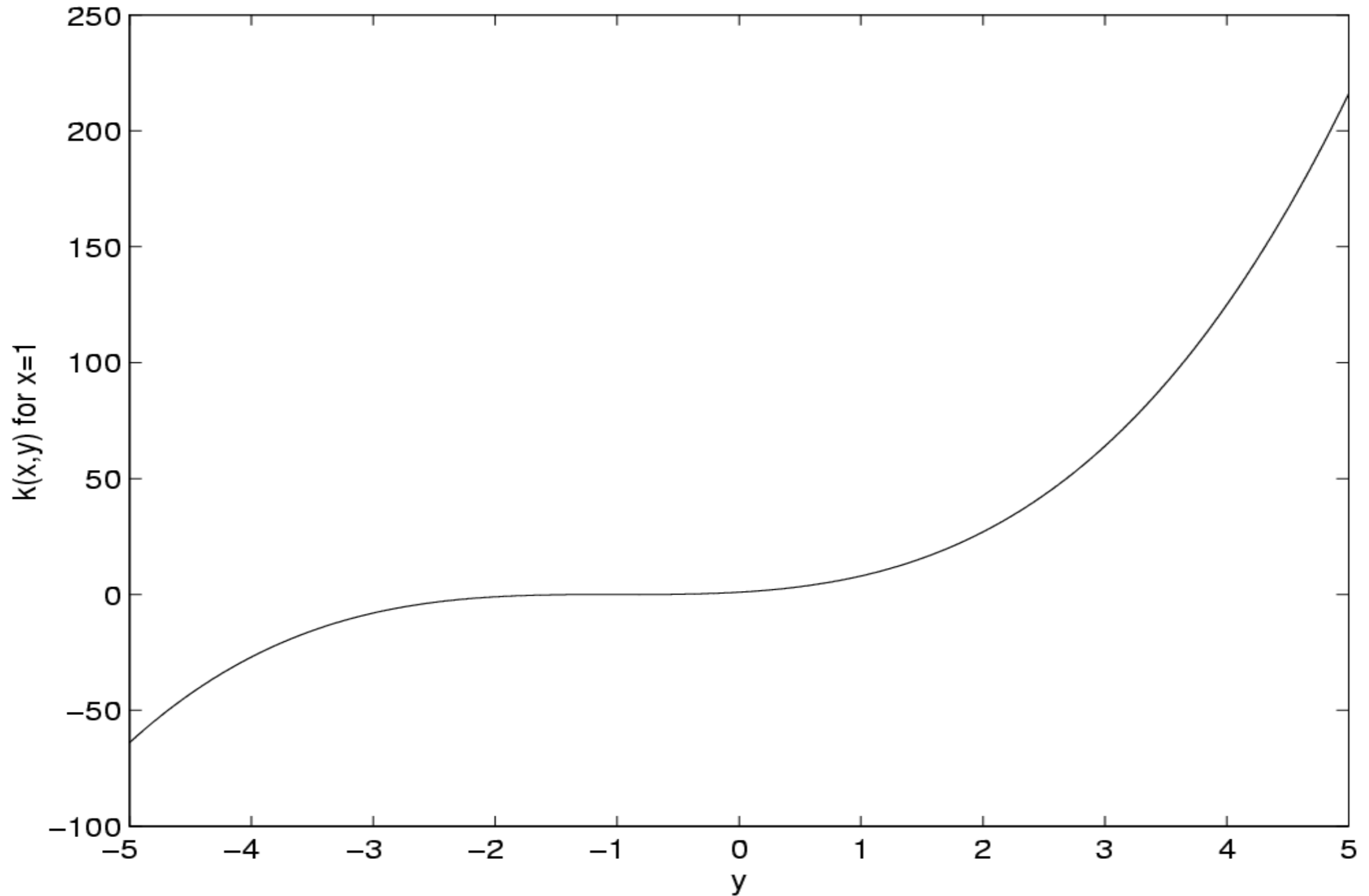
# Laplacian Kernel



# Gaussian Kernel

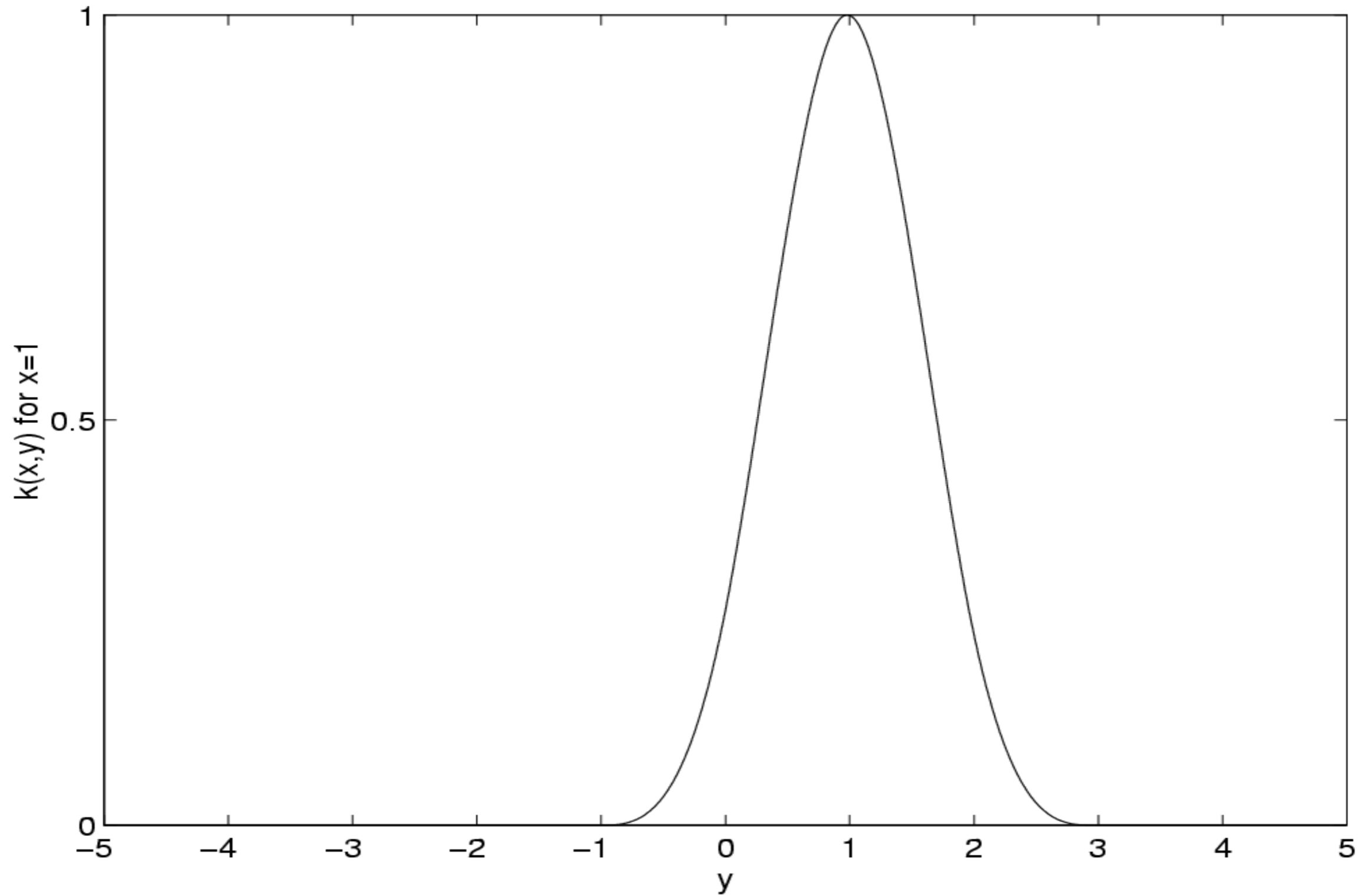


# Polynomial of order 3





# B<sub>3</sub> Spline Kernel



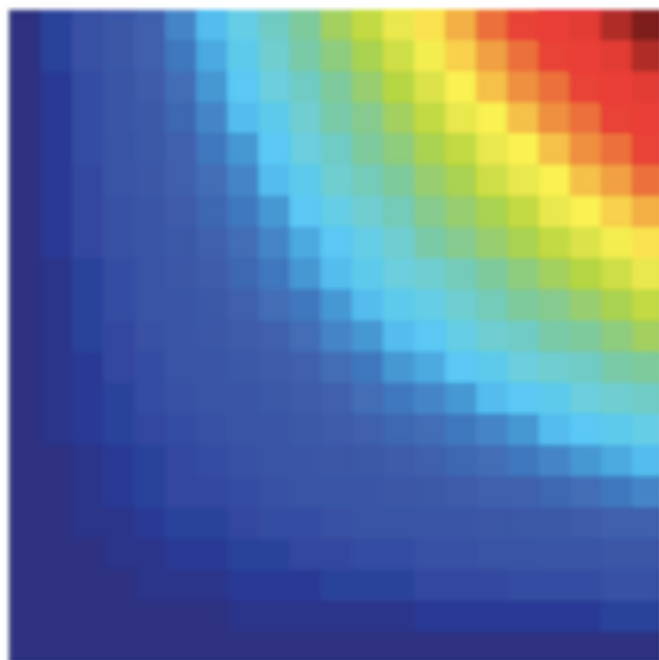
# Kernels in Computer Vision

- Features  $x$  = histogram (of color, texture, etc)
- Common Kernels
  - Intersection Kernel
  - Chi-square Kernel

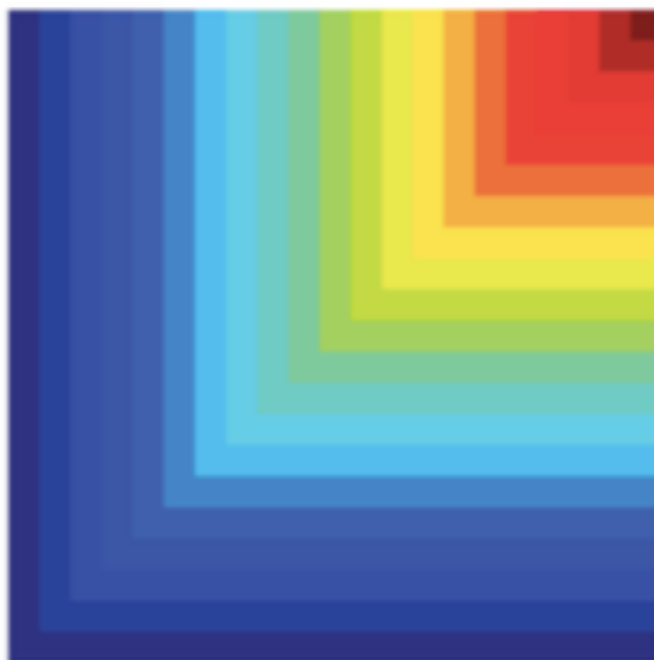
$$K_{\text{intersect}}(\mathbf{u}, \mathbf{v}) = \sum_i \min(u_i, v_i)$$

$$K_{\chi^2}(\mathbf{u}, \mathbf{v}) = \sum_i \frac{2u_i v_i}{u_i + v_i}$$

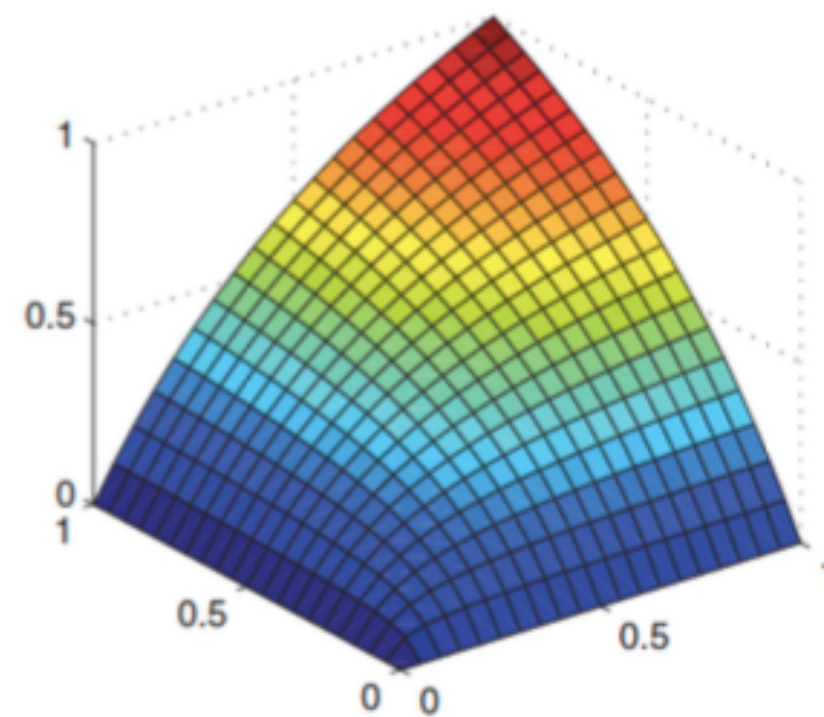
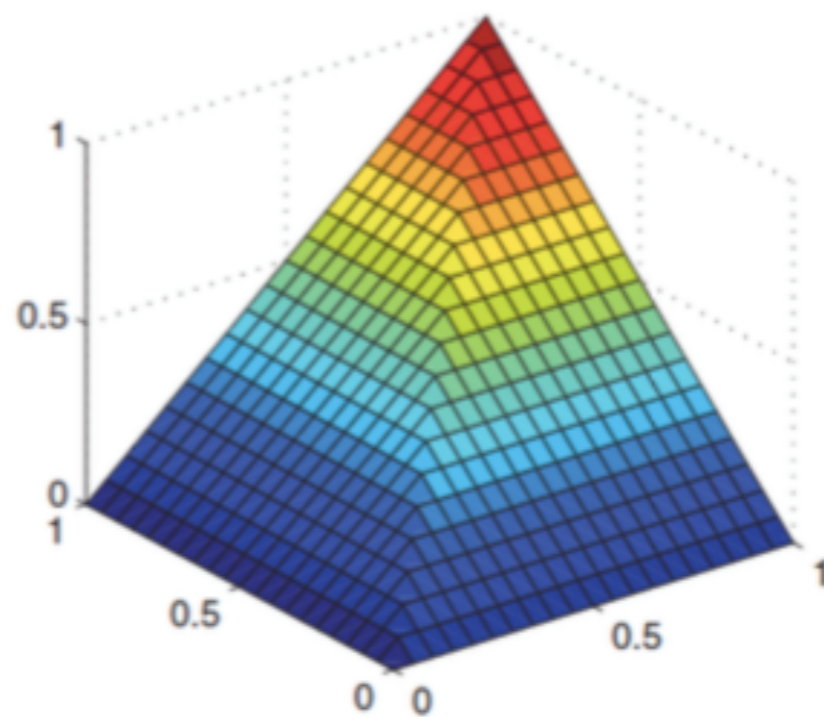
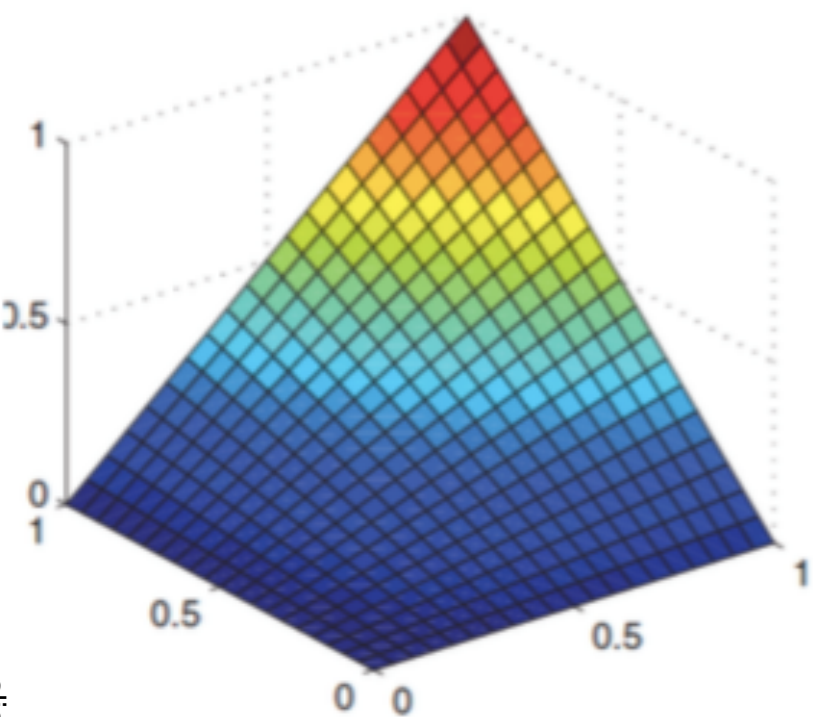
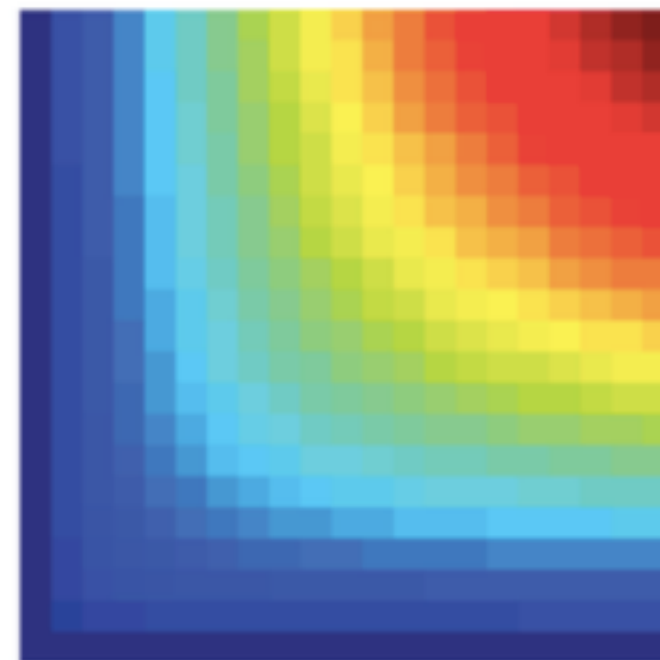
$$K_{\text{linear}}(x,y) = xy$$



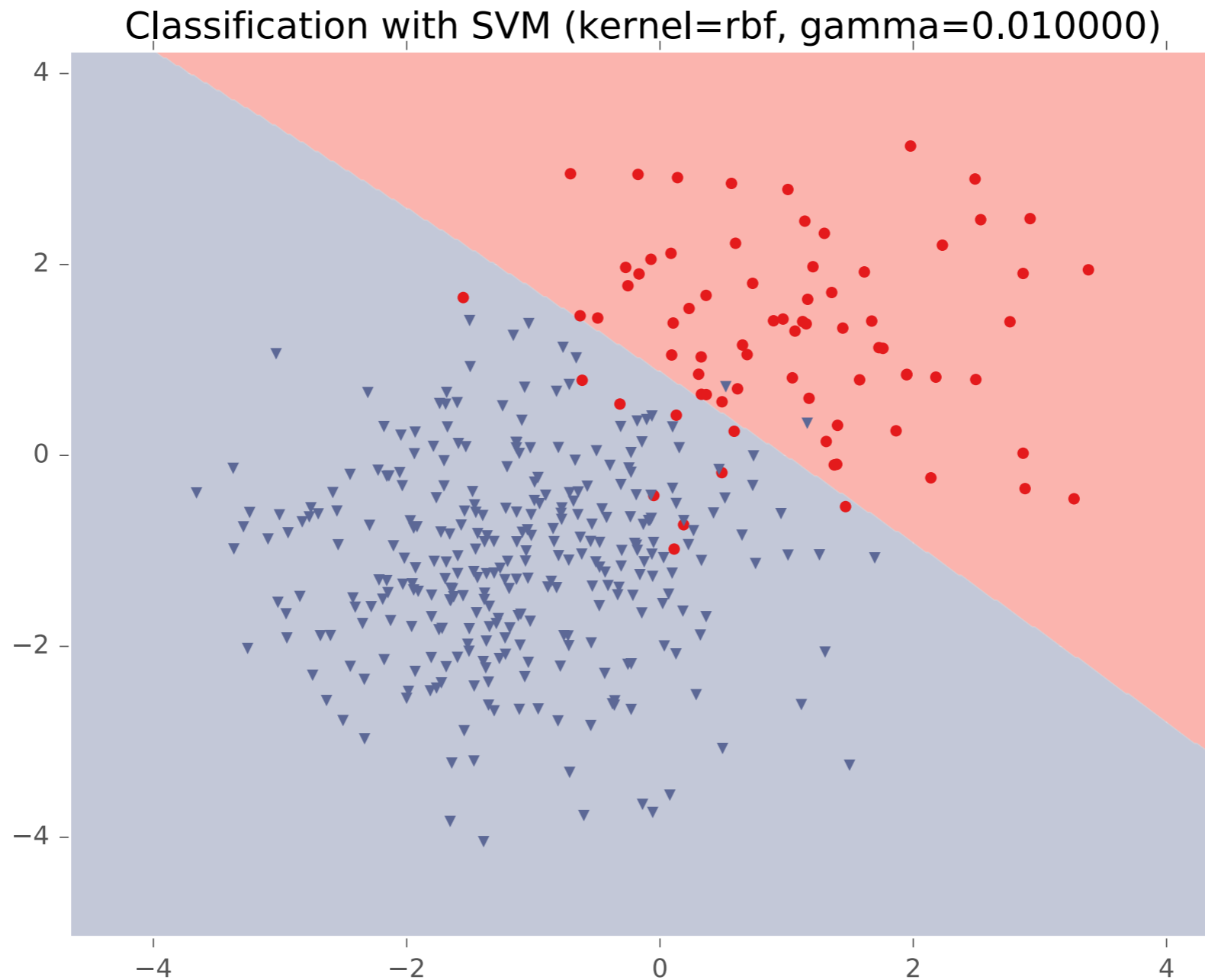
$$K_{\text{min}}(x,y) = \min(x,y)$$



$$K_{\chi^2} = 2xy/(x+y)$$

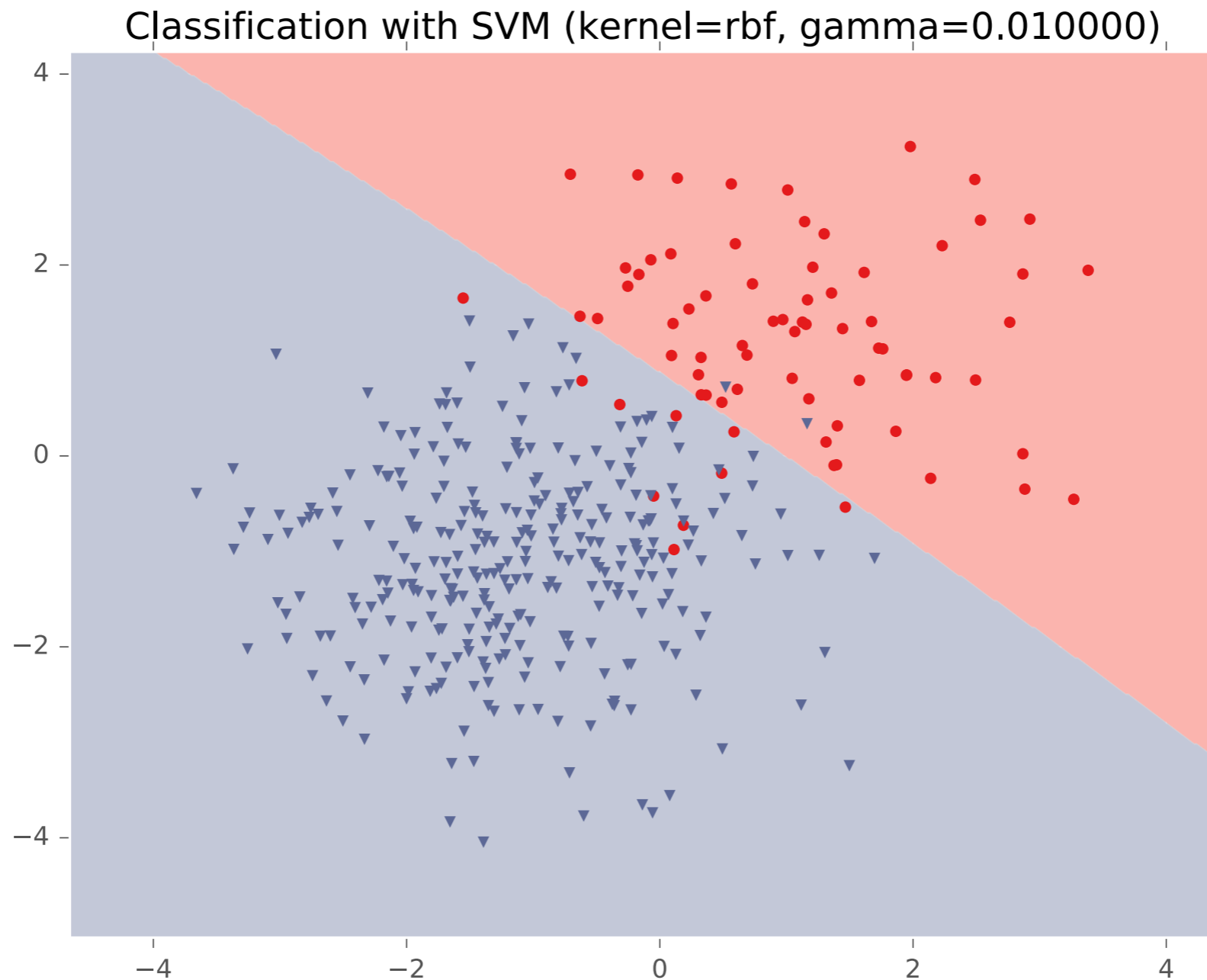


# RBF Kernel Example



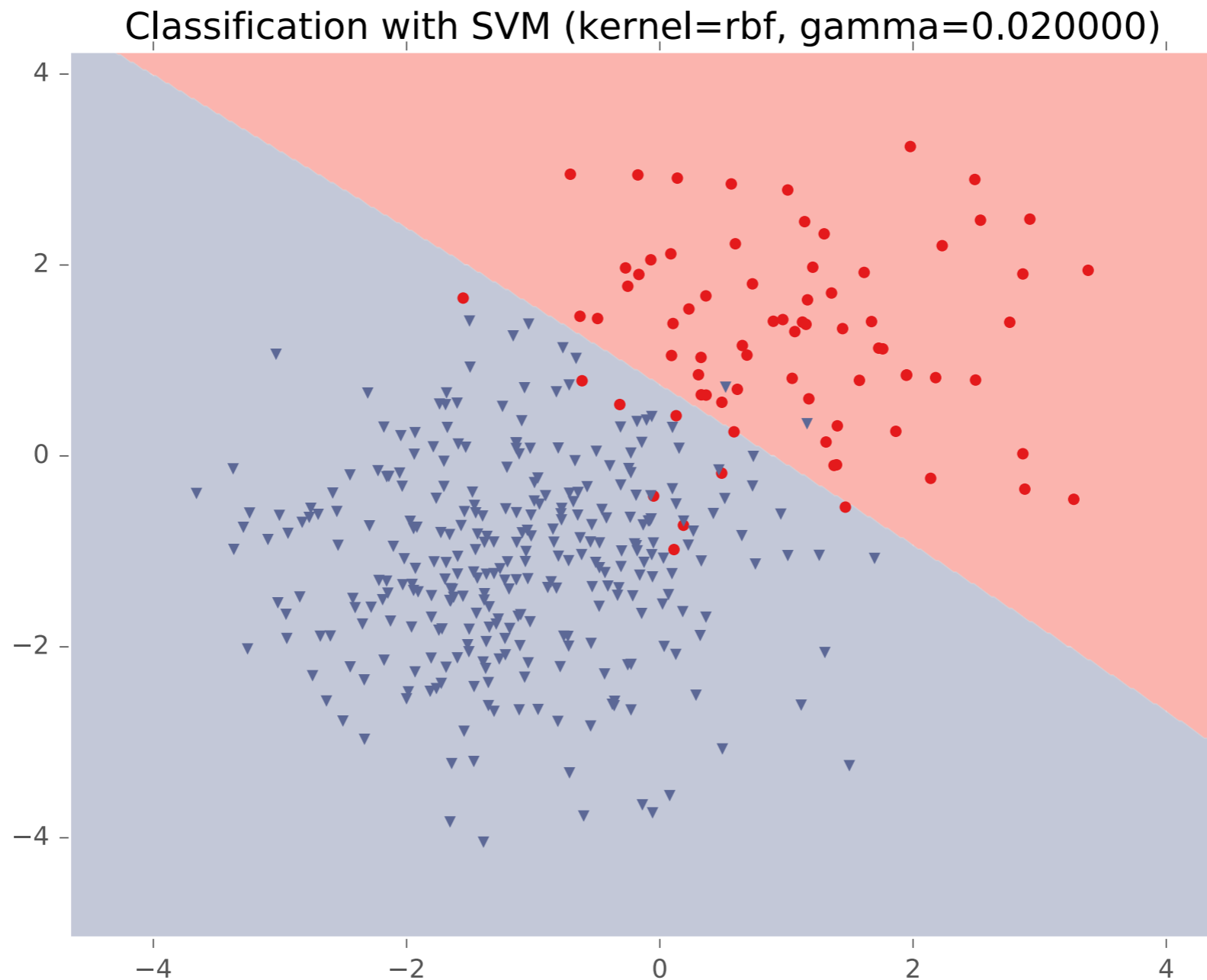
**RBF Kernel:**  $K(\mathbf{x}^{(i)}, \mathbf{x}^{(j)}) = \exp(-\gamma \|\mathbf{x}^{(i)} - \mathbf{x}^{(j)}\|_2^2)$

# RBF Kernel Example



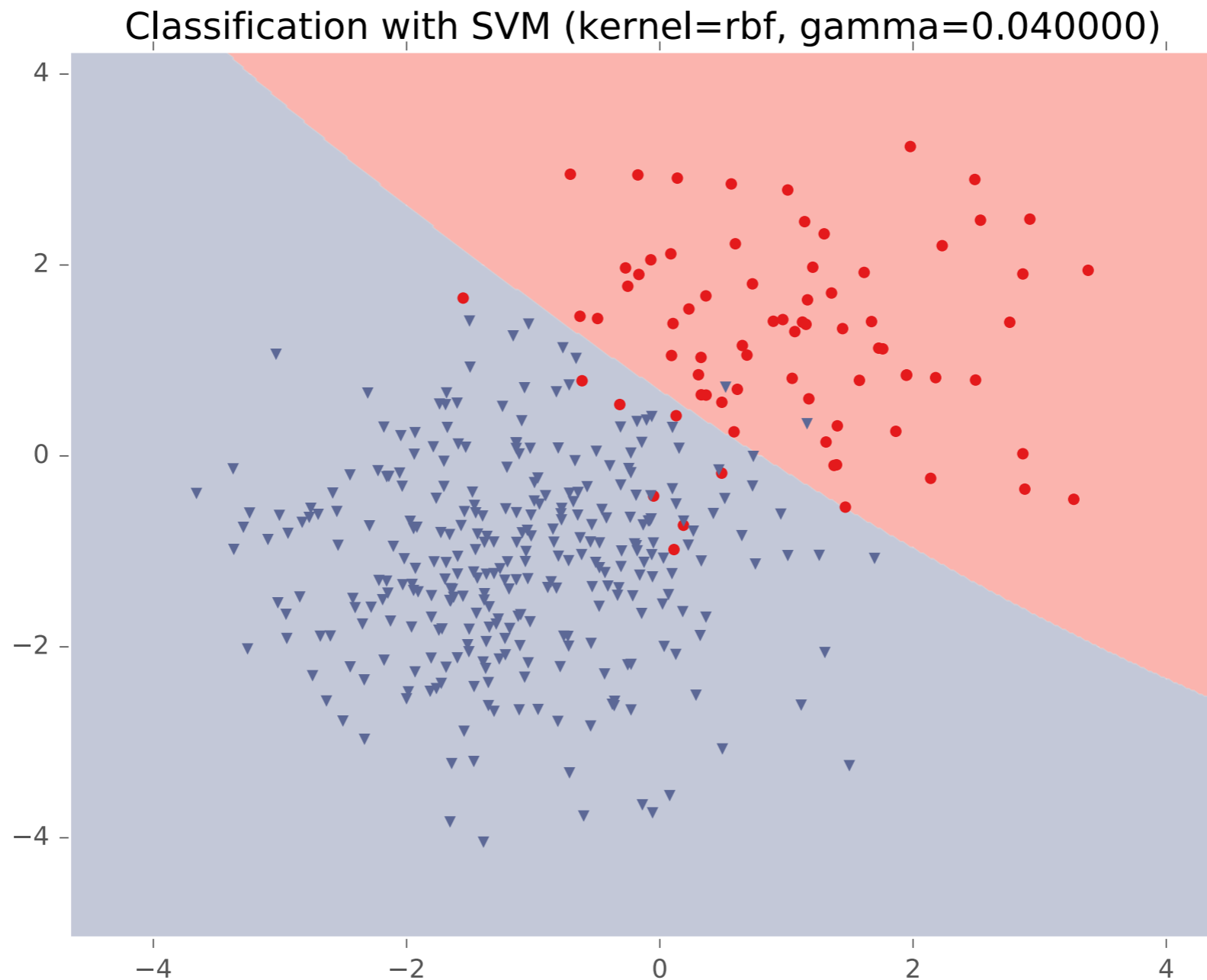
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# RBF Kernel Example



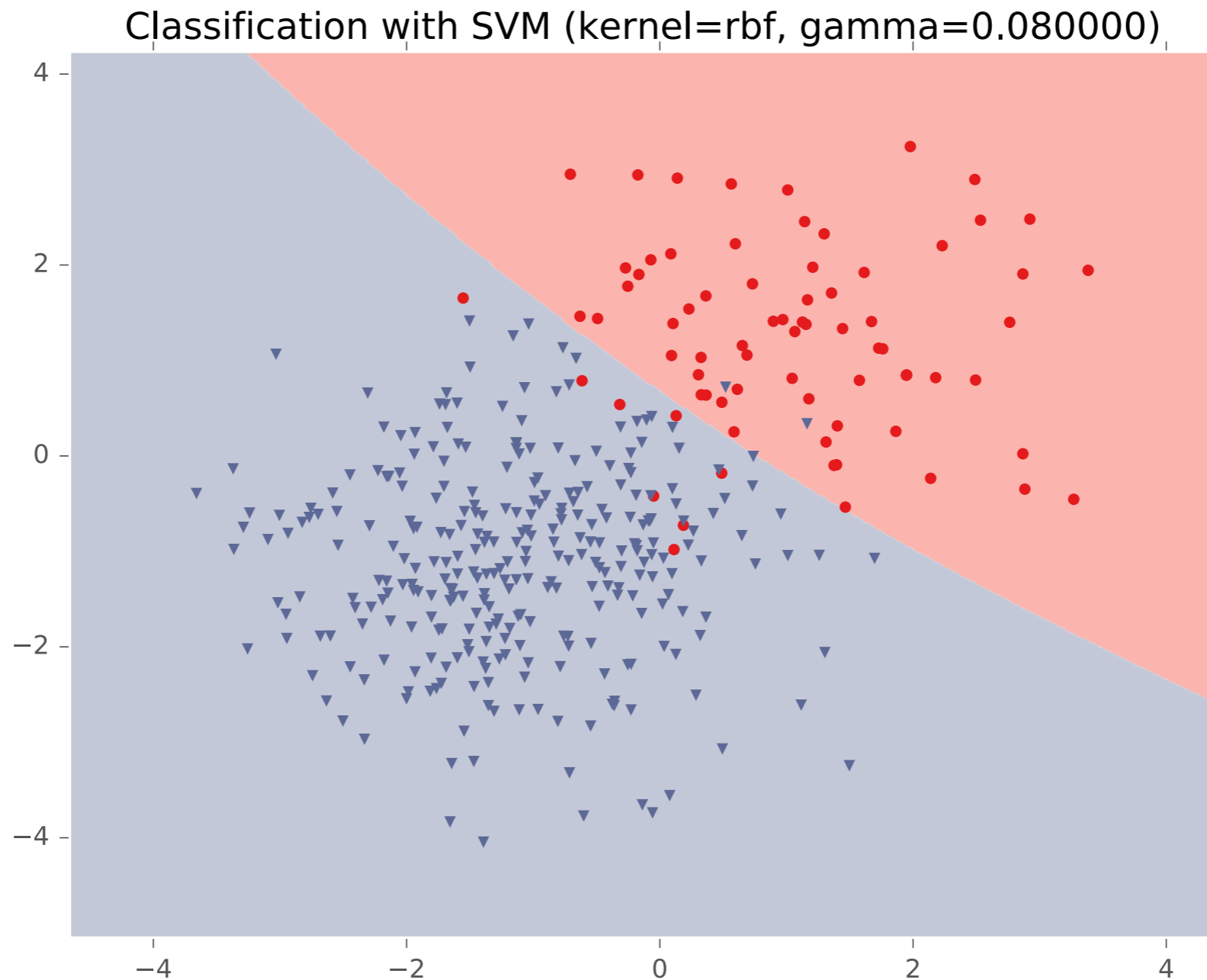
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# RBF Kernel Example



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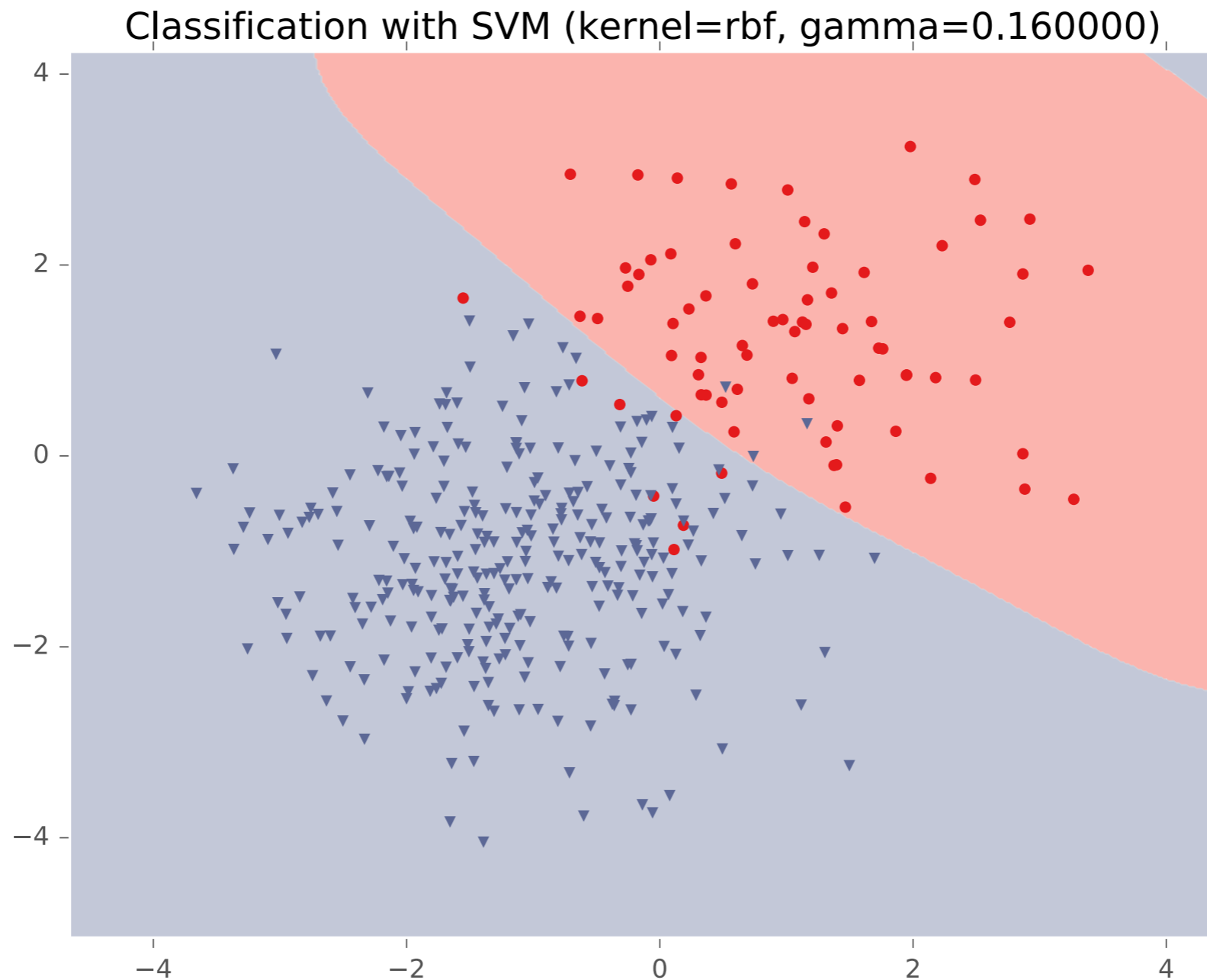
# RBF Kernel Example



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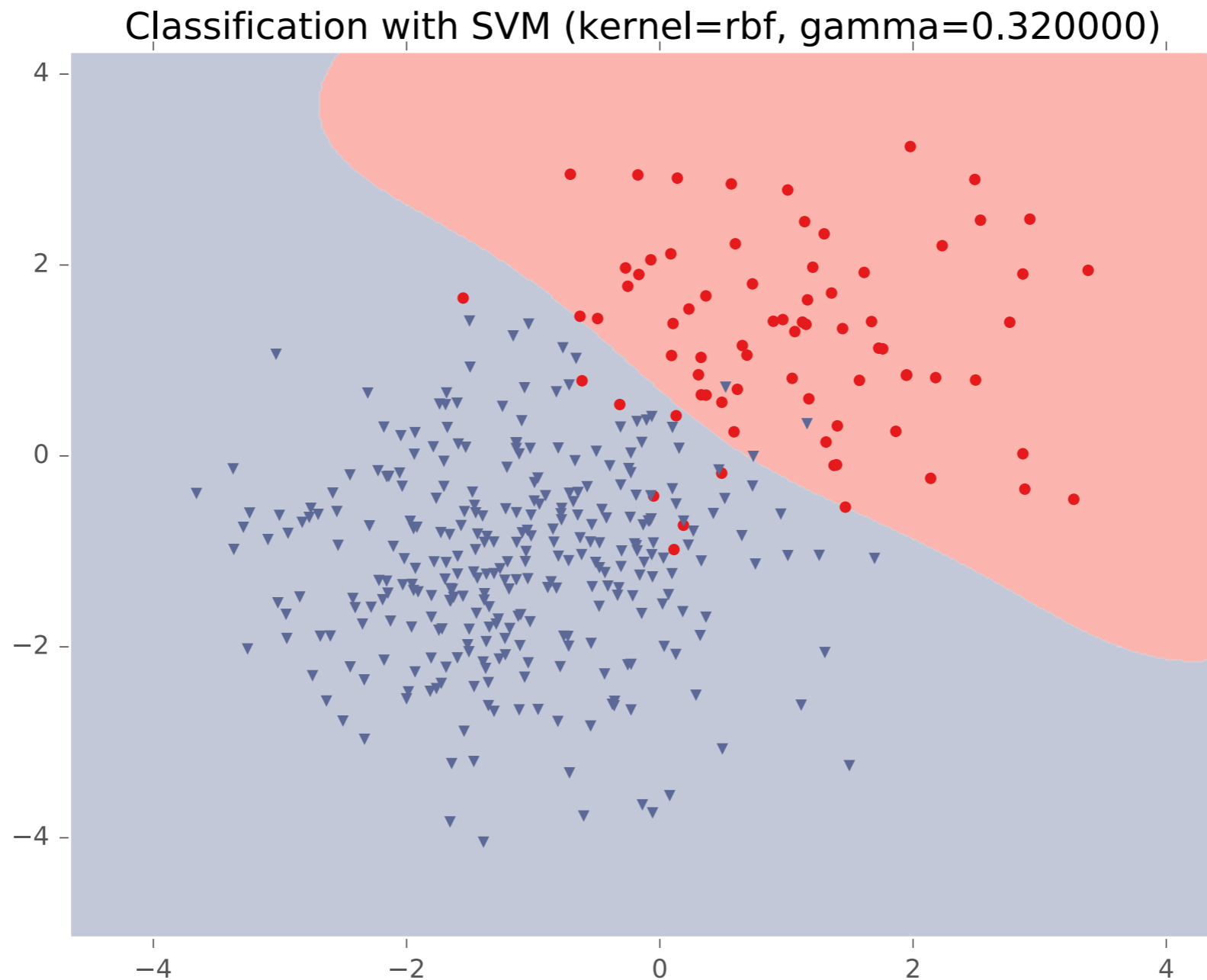


# RBF Kernel Example



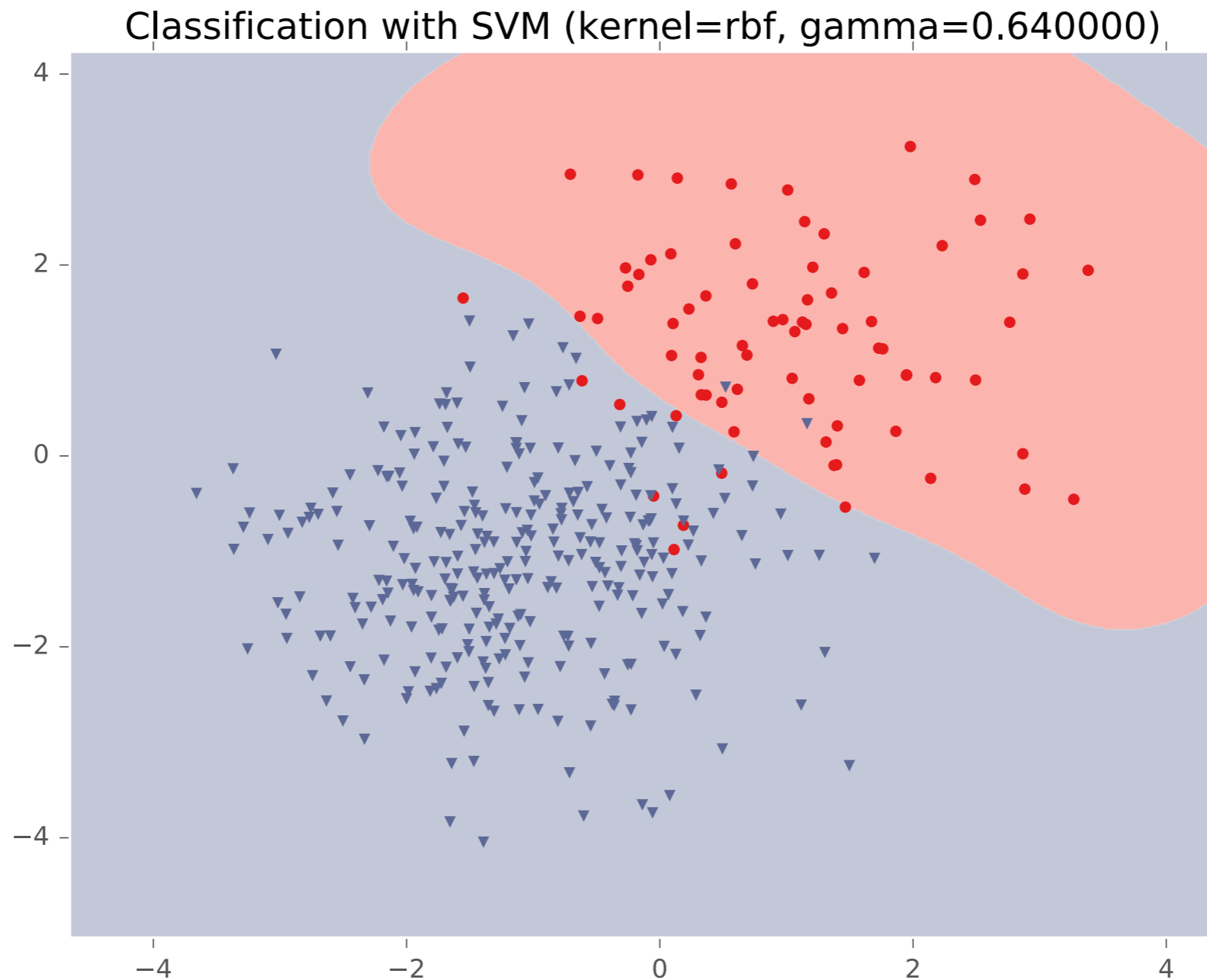
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# RBF Kernel Example



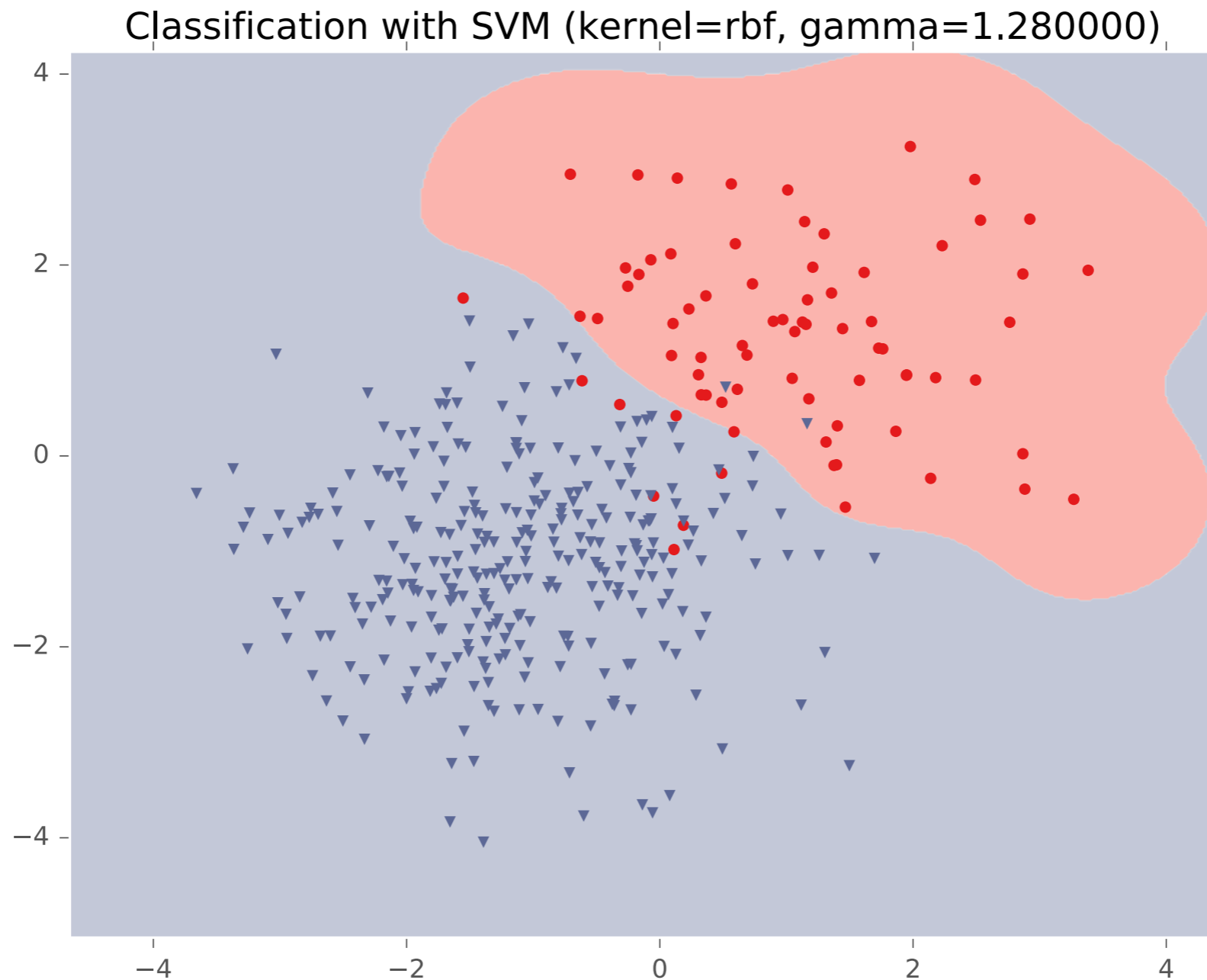
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# RBF Kernel Example



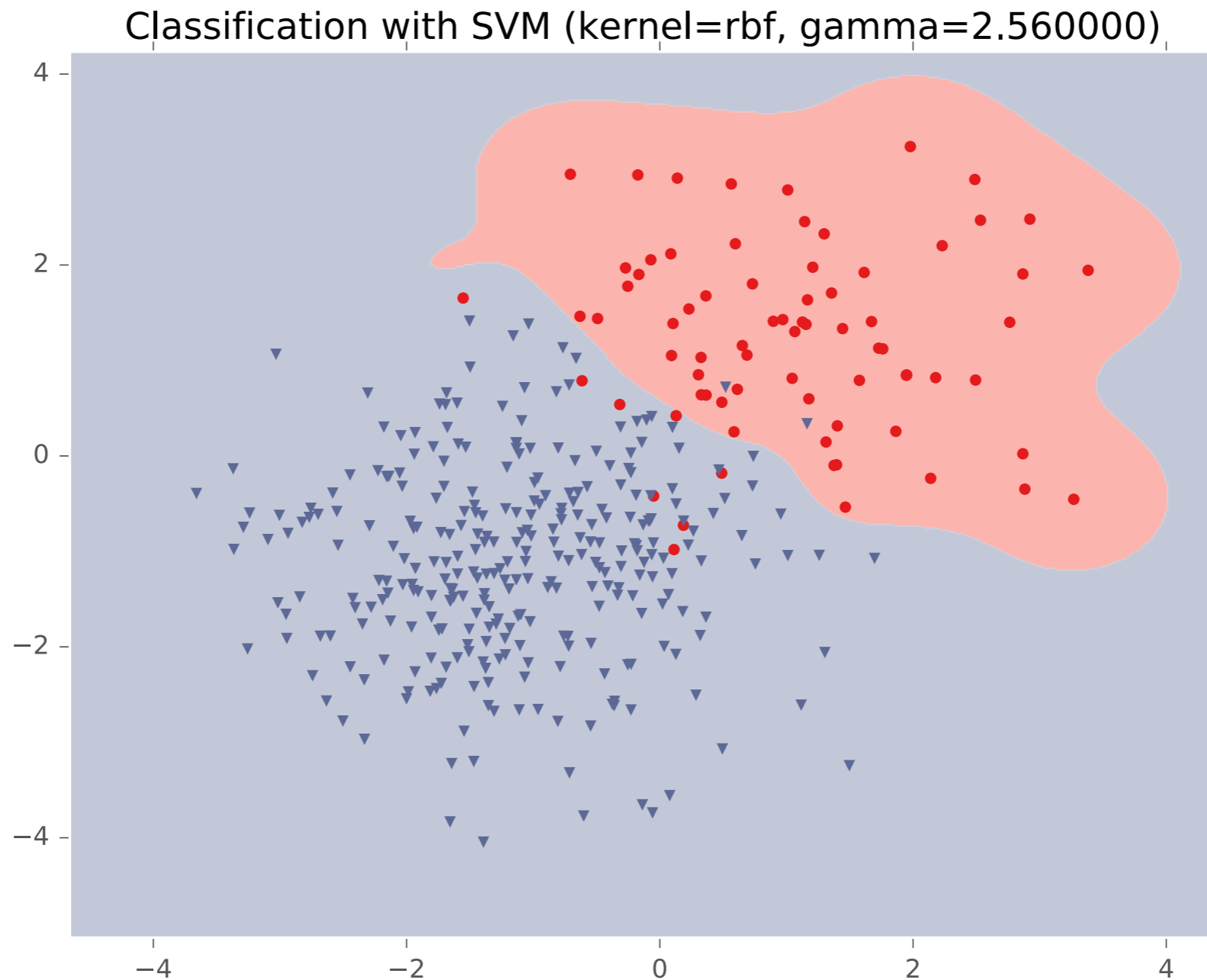
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# RBF Kernel Example



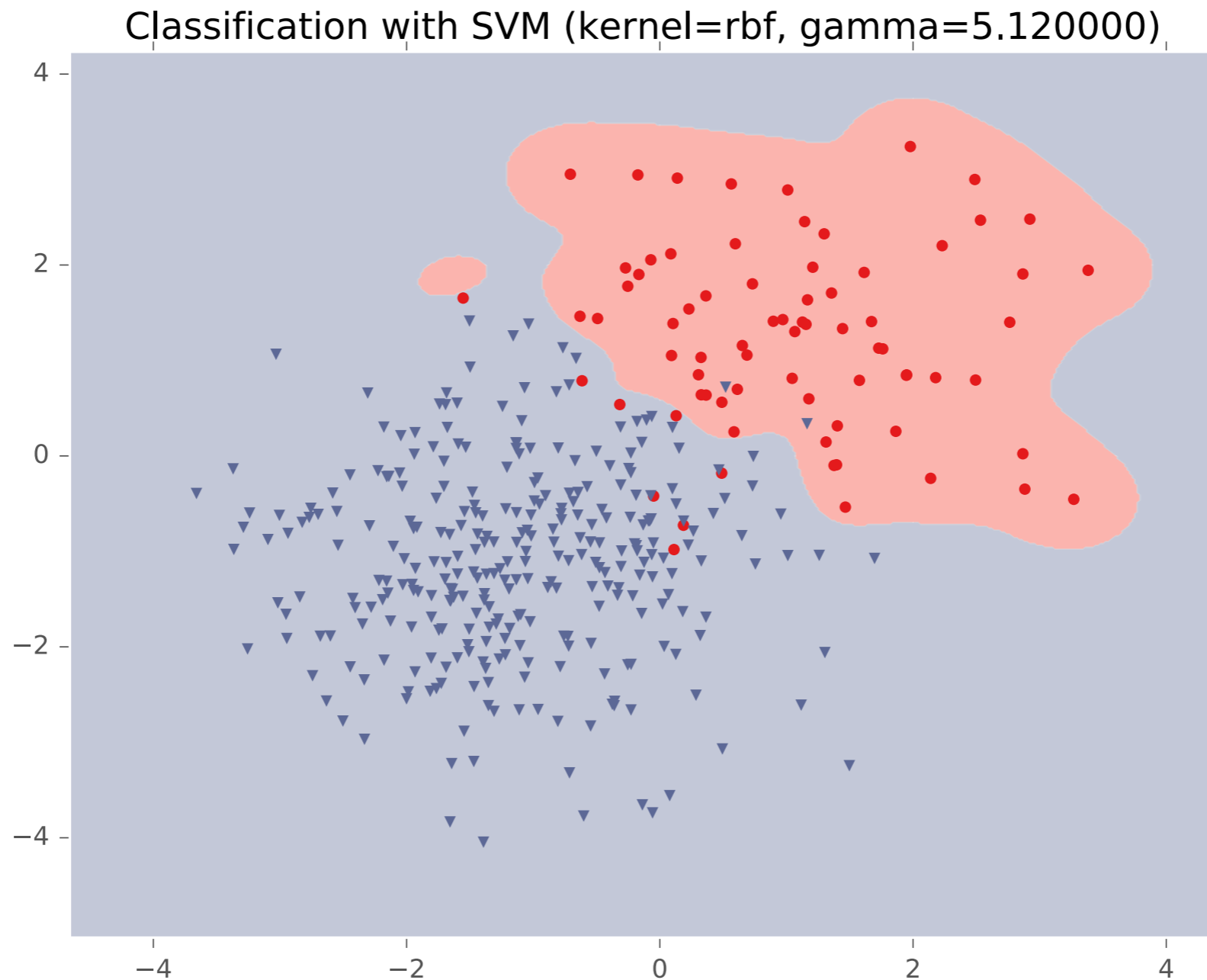
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# RBF Kernel Example



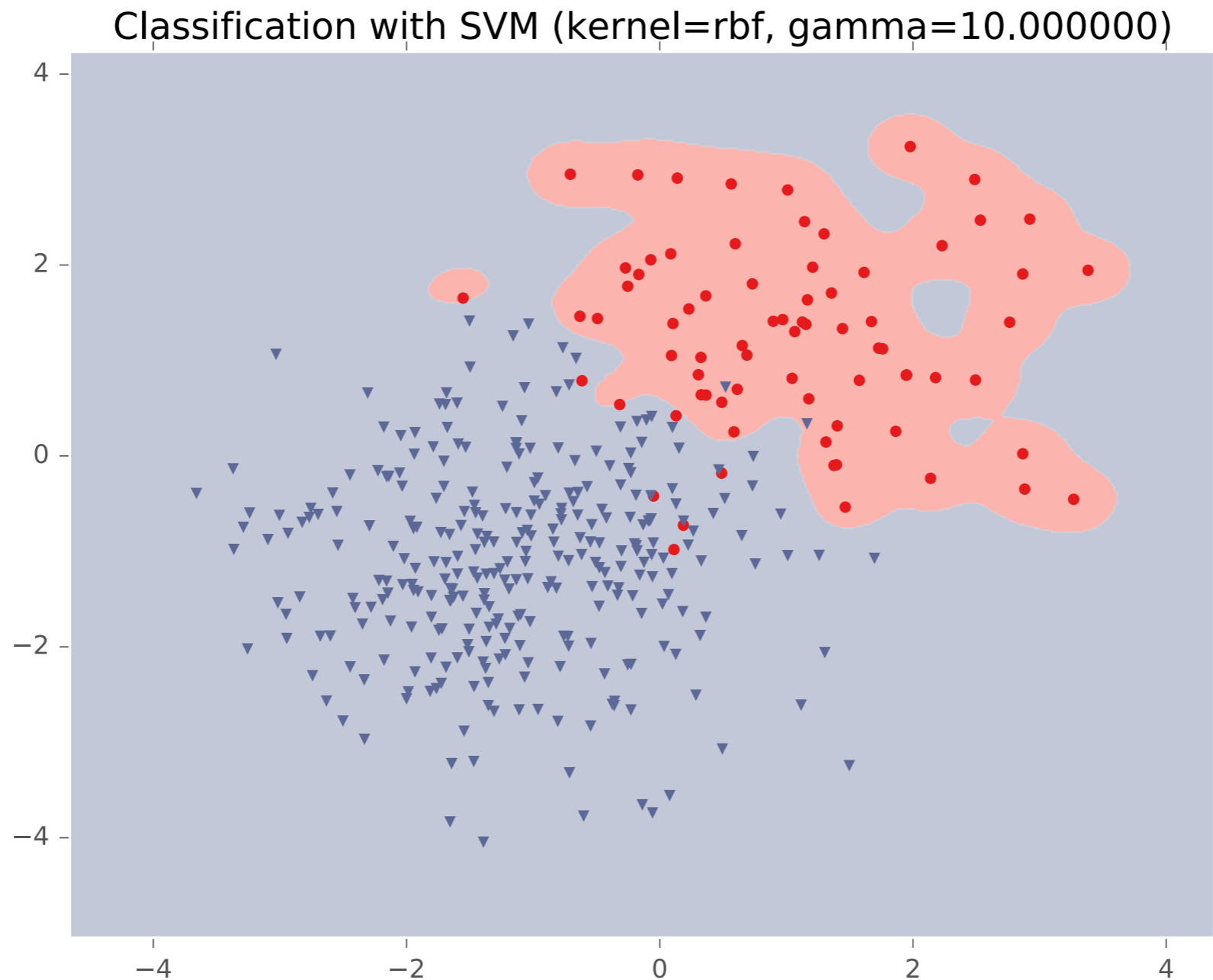
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# RBF Kernel Example



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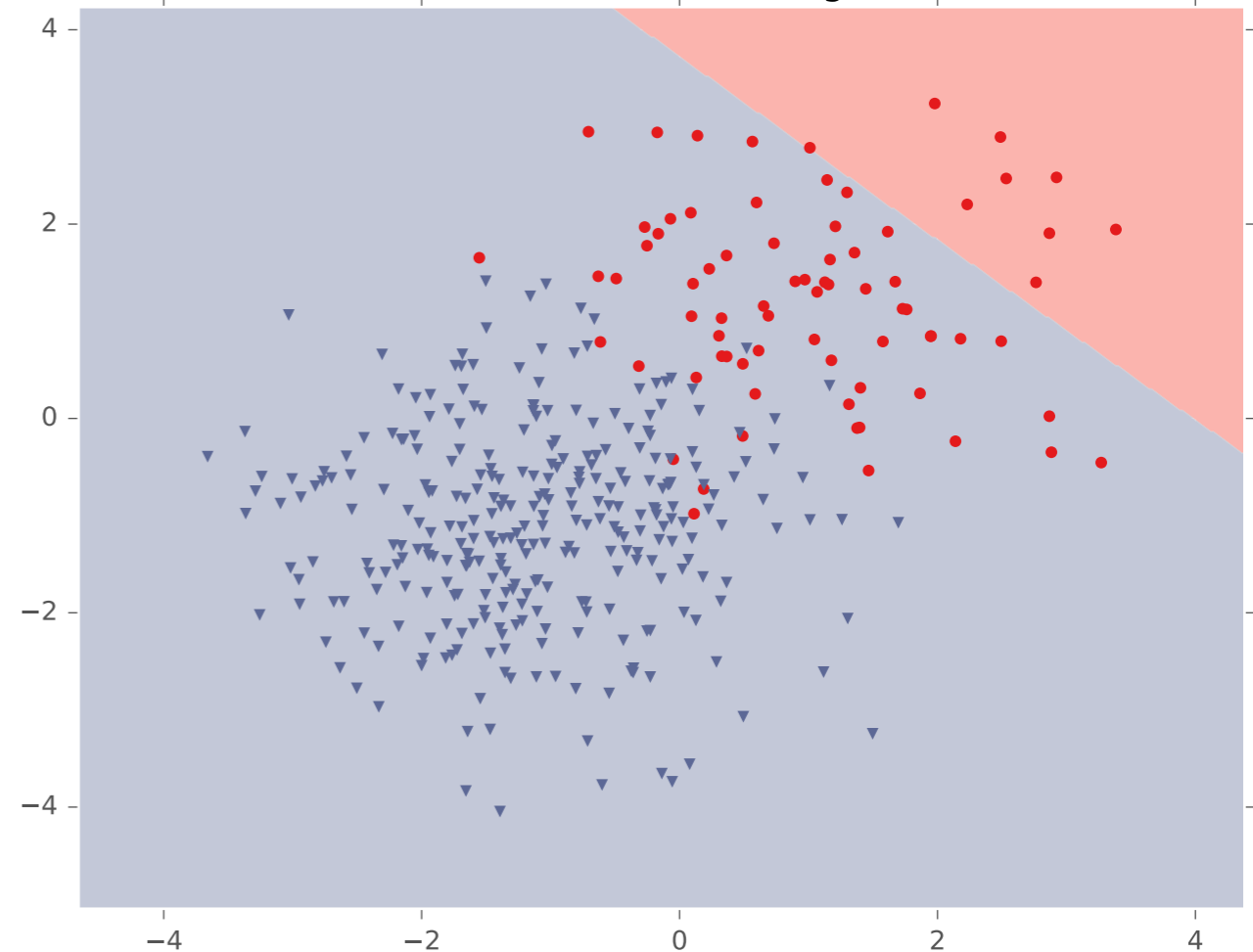
# RBF Kernel Example

## KNN vs. SVM

Classification with KNN (k = 100, weights = 'uniform')



Classification with SVM (kernel=rbf, gamma=0.001000)



**RBF Kernel:**  $K(\mathbf{x}^{(i)}, \mathbf{x}^{(j)}) = \exp(-\gamma \|\mathbf{x}^{(i)} - \mathbf{x}^{(j)}\|_2^2)$



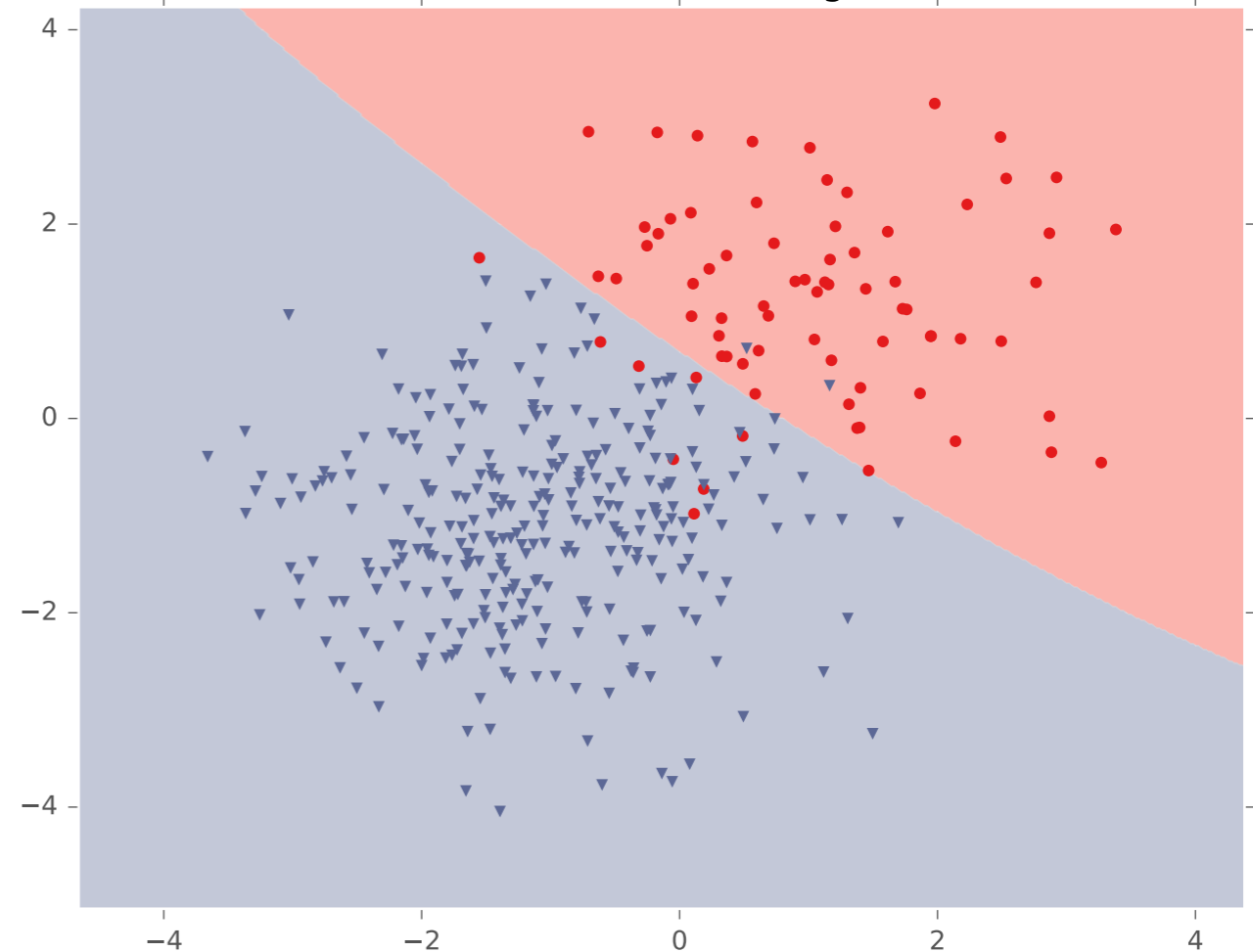
# RBF Kernel Example

## KNN vs. SVM

Classification with KNN (k = 16, weights = 'uniform')



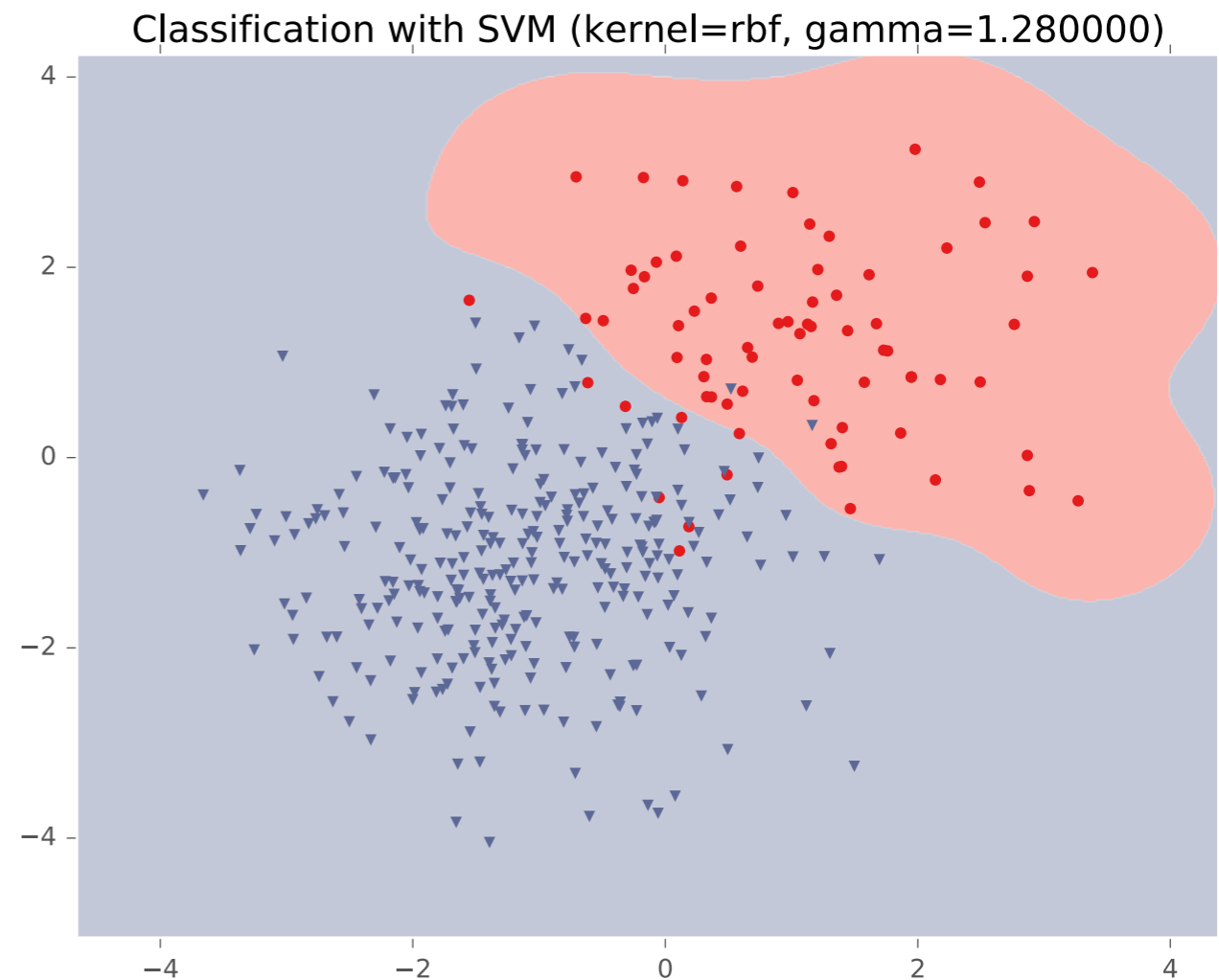
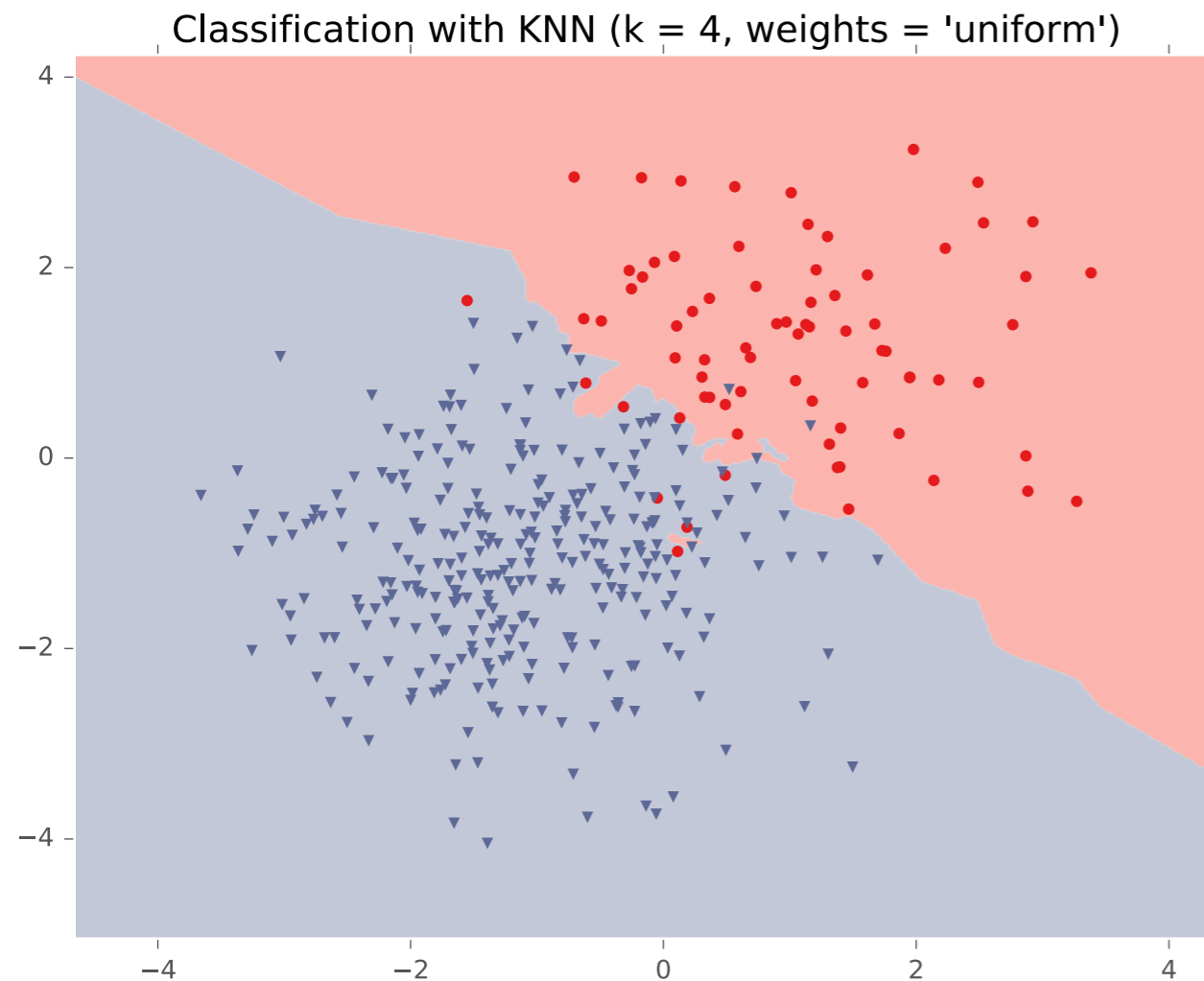
Classification with SVM (kernel=rbf, gamma=0.040000)



**RBF Kernel:**  $K(\mathbf{x}^{(i)}, \mathbf{x}^{(j)}) = \exp(-\gamma \|\mathbf{x}^{(i)} - \mathbf{x}^{(j)}\|_2^2)$

# RBF Kernel Example

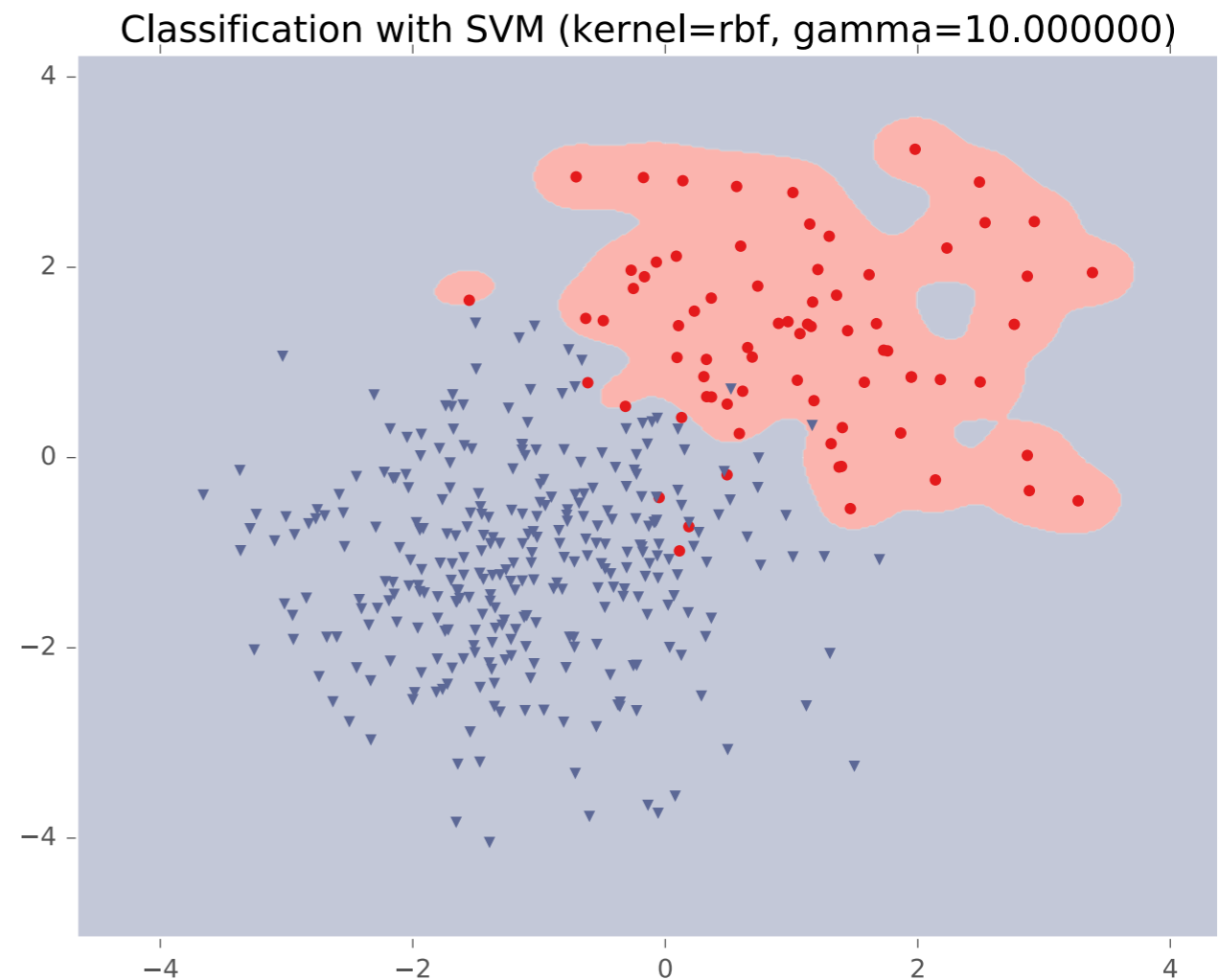
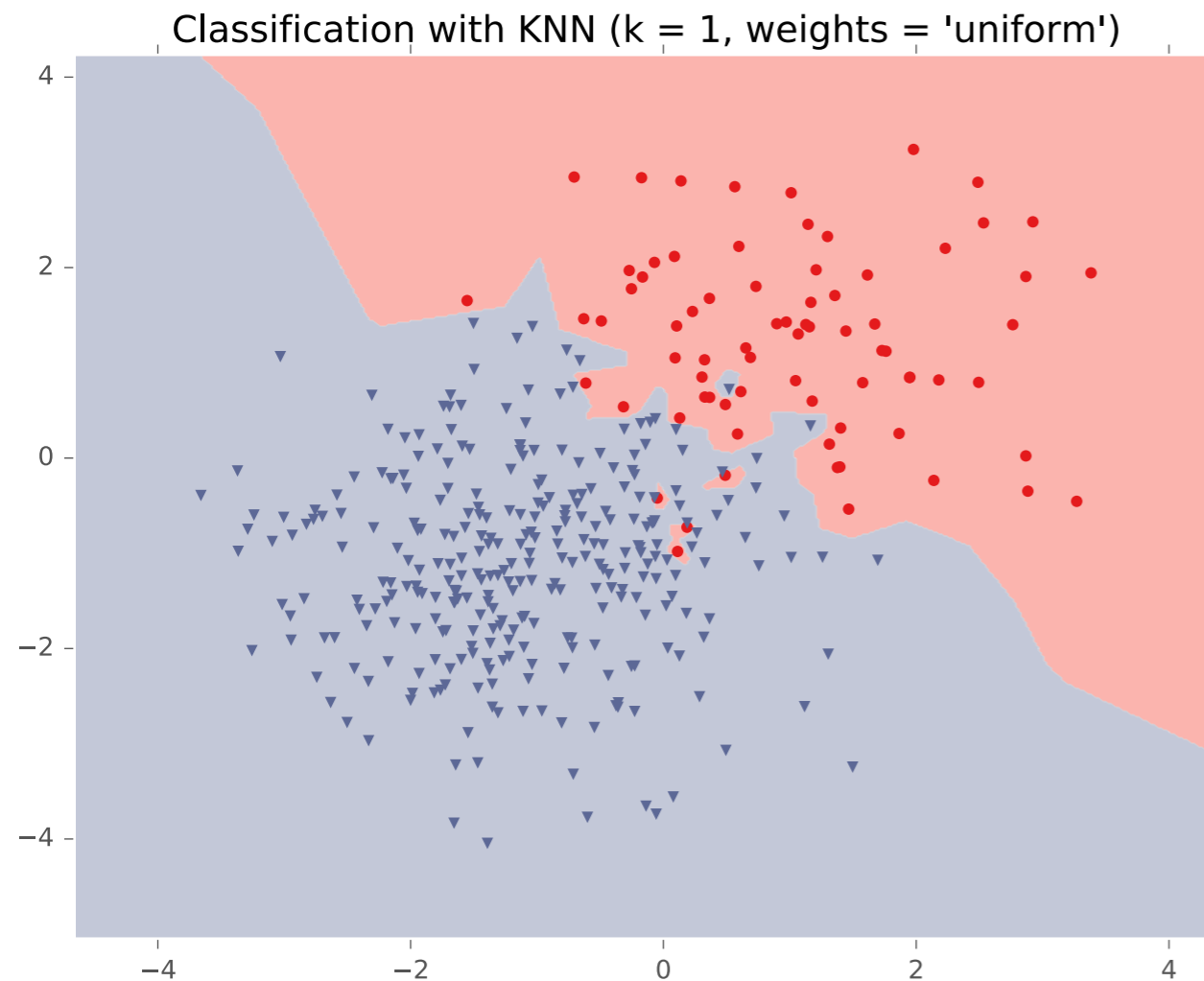
## KNN vs. SVM



**RBF Kernel:**  $K(\mathbf{x}^{(i)}, \mathbf{x}^{(j)}) = \exp(-\gamma \|\mathbf{x}^{(i)} - \mathbf{x}^{(j)}\|_2^2)$

# RBF Kernel Example

## KNN vs. SVM



**RBF Kernel:**  $K(\mathbf{x}^{(i)}, \mathbf{x}^{(j)}) = \exp(-\gamma \|\mathbf{x}^{(i)} - \mathbf{x}^{(j)}\|_2^2)$

# SVM + Kernels: Takeaways

- Maximizing the margin of a linear separator is a **good training criteria**
- Support Vector Machines (SVMs) learn a **max-margin linear classifier**
- The SVM optimization problem can be solved with black-box **Quadratic Programming (QP) solvers**
- Learned decision boundary is defined by its **support vectors**
- Kernel methods allow us to work in a transformed feature space **without explicitly representing that space**
- The **kernel-trick** can be applied to **SVMs**, as well as many other algorithms

**Next Lecture:**  
Kernel Trick for SVMs,  
Support Vector Regression