

# BBM 413

## Fundamentals of Image Processing

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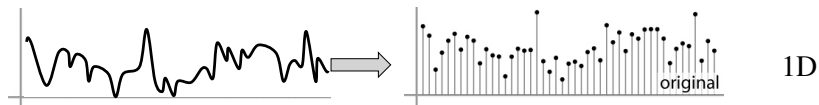
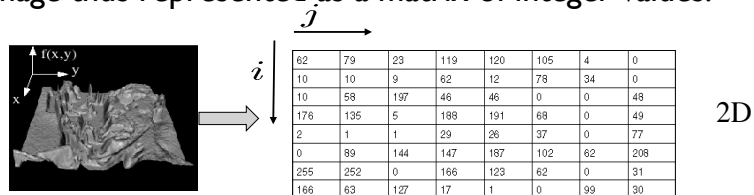
### Point Operations Histogram Processing

### Today's topics

- Point operations
- Histogram processing

### Digital images

- Sample the 2D space on a regular grid
- Quantize each sample (round to nearest integer)
- Image thus represented as a matrix of integer values.



Slide credit: K. Grauman, S. Seitz

### Image Transformations

- $g(x,y) = T[f(x,y)]$

$g(x,y)$ : output image

$f(x,y)$ : input image

$T$ : transformation function

1. Point operations: operations on single pixels
2. Spatial filtering: operations considering pixel neighborhoods
3. Global methods: operations considering whole image

## Point Operations

- Smallest possible neighborhood is of size  $1 \times 1$
- Process each point independently of the others
- Output image  $g$  depends only on the value of  $f$  at a single point  $(x,y)$
- Map each pixel's value to a new value
- Transformation function  $T$  remaps the sample's value:

$$s = T(r)$$

where

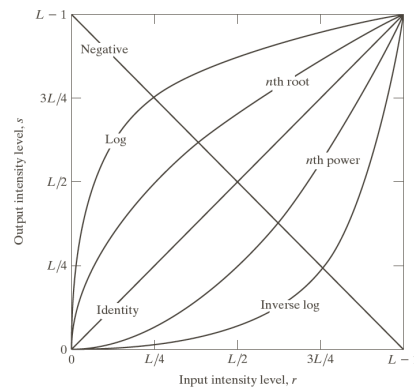
- $r$  is the value at the point in question
- $s$  is the new value in the processed result
- $T$  is a *intensity transformation function*

## Point operations

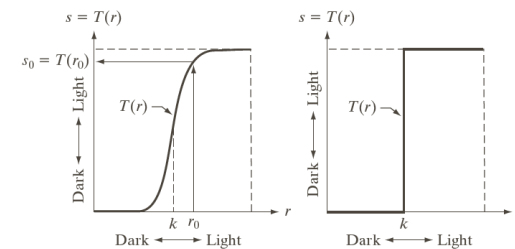
- Is mapping one color space to another (e.g. RGB2HSV) a point operation?
- Is image arithmetic a point operation?
- Is performing geometric transformations a point operation?
  - Rotation
  - Translation
  - Scale change
  - etc.

## Sample intensity transformation functions

- Image negatives
- Log transformations
  - Compresses the dynamic range of images
- Power-law transformations
  - Gamma correction



## Point Processing Examples

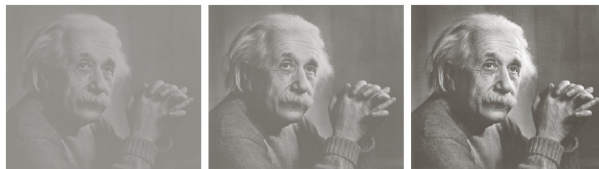


produces an image of higher contrast than the original by darkening the intensity levels below  $k$  and brightening intensities above  $k$

produces a binary (two-intensity level) image

## Dynamic range

- Dynamic range  $R_d = I_{\max} / I_{\min}$ , or  $(I_{\max} + k) / (I_{\min} + k)$ 
  - determines the degree of image contrast that can be achieved
  - a major factor in image quality
- Ballpark values
  - Desktop display in typical conditions: 20:1
  - Photographic print: 30:1
  - High dynamic range display: 10,000:1



low contrast

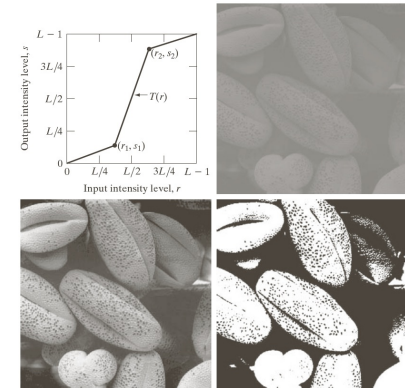
medium contrast

high contrast

Slide credit: S. Marschner

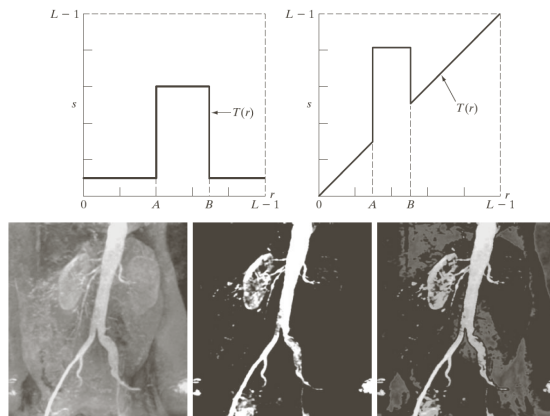
## Point Operations: Contrast stretching and Thresholding

- Contrast stretching: produces an image of higher contrast than the original
- Thresholding: produces a binary (two-intensity level) image



## Point Operations: Intensity-level Slicing

- highlights a certain range of intensities



## Intensity encoding in images

- Recall that the pixel values determine how bright that pixel is.
- Bigger numbers are (usually) brighter
- Transfer function*: function that maps input pixel value to luminance of displayed image

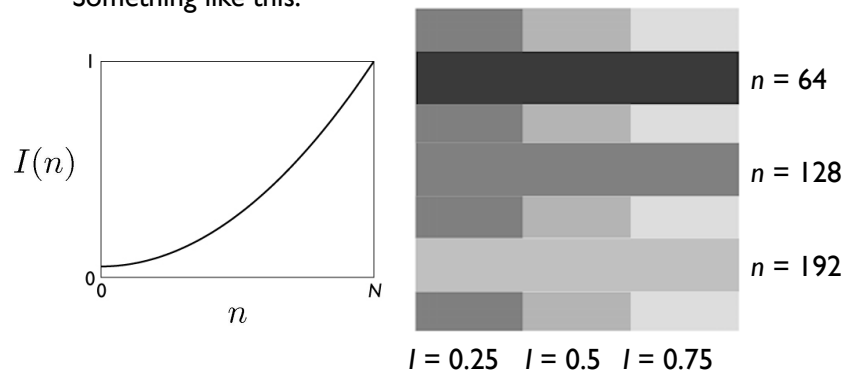
$$I = f(n) \quad f : [0, N] \rightarrow [I_{\min}, I_{\max}]$$

- What determines this function?
  - physical constraints of device or medium
  - desired visual characteristics

adapted from: S. Marschner

## What this projector does?

- Something like this:



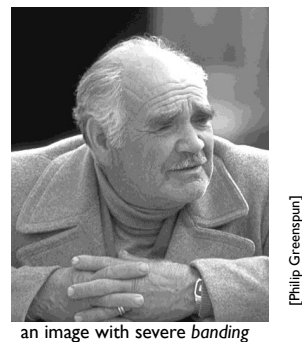
adapted from: S. Marschner

## Constraints on transfer function

- Maximum displayable intensity,  $I_{\max}$ 
  - how much power can be channeled into a pixel?
    - LCD: backlight intensity, transmission efficiency (<10%)
    - projector: lamp power, efficiency of imager and optics
- Minimum displayable intensity,  $I_{\min}$ 
  - light emitted by the display in its “off” state
    - e.g. stray electron flux in CRT, polarizer quality in LCD
- Viewing flare,  $k$ : light reflected by the display
  - very important factor determining image contrast in practice
    - 5% of  $I_{\max}$  is typical in a normal office environment [sRGB spec]
    - much effort to make very black CRT and LCD screens
    - all-black decor in movie theaters

## Transfer function shape

- Desirable property: the change from one pixel value to the next highest pixel value should not produce a visible contrast
  - otherwise smooth areas of images will show visible bands
- What contrasts are visible?
  - rule of thumb: under good conditions we can notice a 2% change in intensity
  - therefore we generally need smaller quantization steps in the darker tones than in the lighter tones
  - most efficient quantization is logarithmic



Slide credit: S. Marschner

## How many levels are needed?

- Depends on dynamic range
  - 2% steps are most efficient:
$$0 \mapsto I_{\min}; 1 \mapsto 1.02I_{\min}; 2 \mapsto (1.02)^2 I_{\min}; \dots$$
  - log 1.02 is about 1/120, so 120 steps per decade of dynamic range
    - 240 for desktop display
    - 360 to print to film
    - 480 to drive HDR display
- If we want to use linear quantization (equal steps)
  - one step must be < 2% (1/50) of  $I_{\min}$
  - need to get from  $\sim 0$  to  $I_{\min} \cdot R_d$  so need about  $50 R_d$  levels
    - 1500 for a print; 5000 for desktop display; 500,000 for HDR display
- Moral: 8 bits is just barely enough for low-end applications
  - but only if we are careful about quantization

Slide credit: S. Marschner

## Intensity quantization in practice

- Option 1: linear quantization  $I(n) = (n/N) I_{\max}$ 
  - pro: simple, convenient, amenable to arithmetic
  - con: requires more steps (wastes memory)
  - need 12 bits for any useful purpose; more than 16 for HDR
- Option 2: power-law quantization  $I(n) = (n/N)^\gamma I_{\max}$ 
  - pro: fairly simple, approximates ideal exponential quantization
  - con: need to linearize before doing pixel arithmetic
  - con: need to agree on exponent
  - 8 bits are OK for many applications; 12 for more critical ones
- Option 2: floating-point quantization  $I(x) = (x/w) I_{\max}$ 
  - pro: close to exponential; no parameters; amenable to arithmetic
  - con: definitely takes more than 8 bits
  - 16-bit “half precision” format is becoming popular

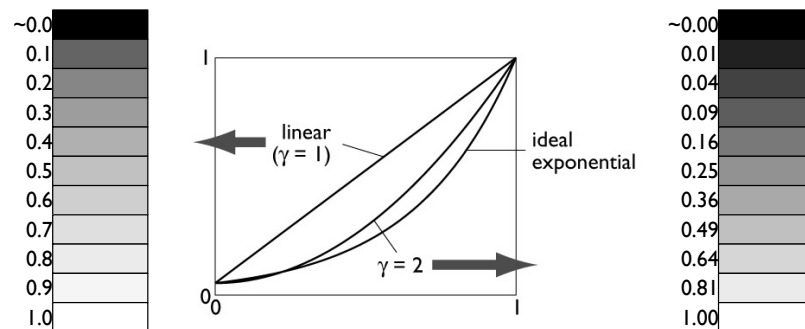
Slide credit: S. Marschner

## Why gamma?

- Power-law quantization, or *gamma correction* is most popular
- Original reason: CRTs are like that
  - intensity on screen is proportional to (roughly) voltage<sup>2</sup>
- Continuing reason: inertia + memory savings
  - inertia: gamma correction is close enough to logarithmic that there's no sense in changing
  - memory: gamma correction makes 8 bits per pixel an acceptable option

Slide credit: S. Marschner

## Gamma quantization



- Close enough to ideal perceptually uniform exponential

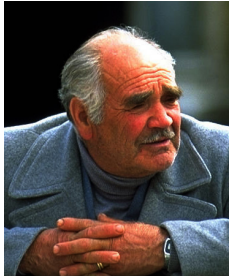
Slide credit: S. Marschner

## Gamma correction

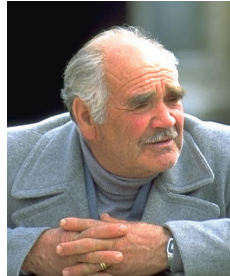
- Sometimes (often, in graphics) we have computed intensities  $a$  that we want to display linearly
- In the case of an ideal monitor with zero black level,
 
$$I(n) = (n/N)^\gamma$$
 (where  $N = 2^n - 1$  in  $n$  bits). Solving for  $n$ :
 
$$n = N a^{\frac{1}{\gamma}}$$
- This is the “gamma correction” recipe that has to be applied when computed values are converted to 8 bits for output
  - failing to do this (implicitly assuming gamma = 1) results in dark, oversaturated images

Slide credit: S. Marschner

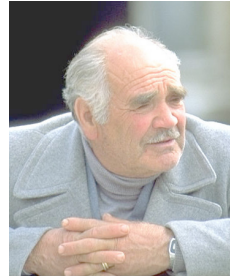
## Gamma correction



corrected for  
 $\gamma$  lower than  
display



OK



corrected for  
 $\gamma$  higher than  
display

[Philip Greenspun]

Slide credit: S. Marschner

## Instagram Filters

- How do they make those Instagram filters?

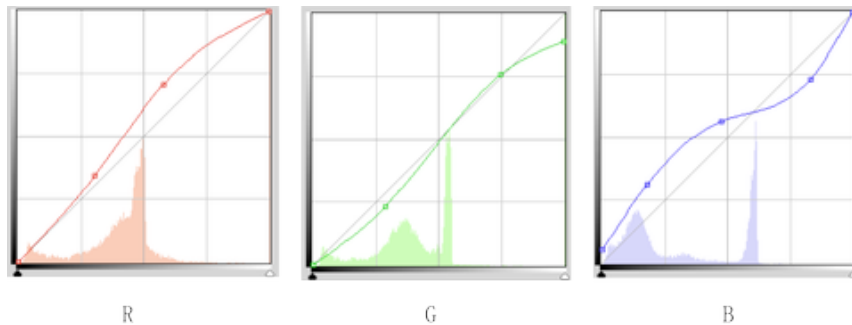


"It's really a combination of a bunch of different methods. In some cases we draw on top of images, in others we do pixel math. It really depends on the effect we're going for." --- Kevin Systrom, co-founder of Instagram

Source: C. Dyer

## Example Instagram Steps

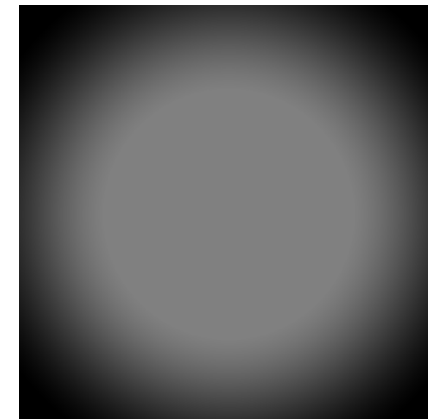
1. Perform an independent RGB color point transformation on the original image to increase contrast or make a color cast



Source: C. Dyer

## Example Instagram Steps

2. Overlay a circle background image to create a vignette effect



Source: C. Dyer

## Example Instagram Steps

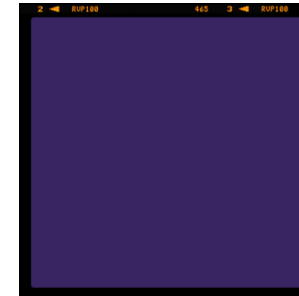
3. Overlay a background image as decorative grain



Source: C. Dyer

## Example Instagram Steps

4. Add a border or frame



Source: C. Dyer

## Result



Javascript library for creating  
Instagram-like effects, see:  
<http://alexmic.net/filrr/>

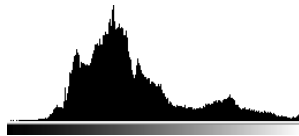
Source: C. Dyer

## Today's topics

- Point operations
- Histogram processing

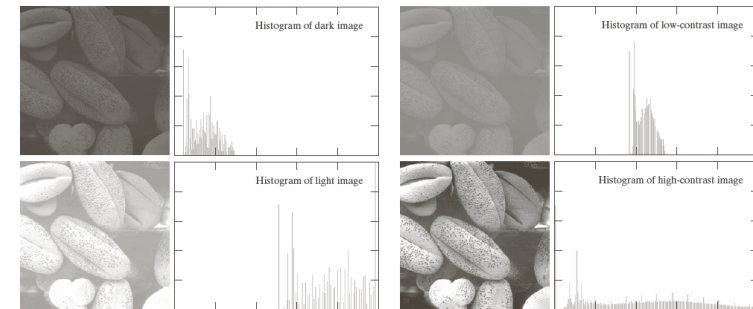
## Histogram

- Histogram: a discrete function  $h(r)$  which counts the number of pixels in the image having intensity  $r$
- If  $h(r)$  is normalized, it measures the probability of occurrence of intensity level  $r$  in an image



- What histograms say about images? **A descriptor for visual information**
- What they don't?
  - No spatial information

## Images and histograms

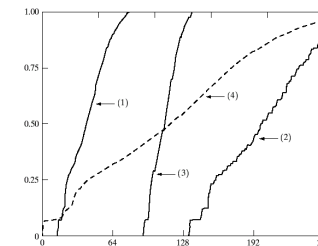
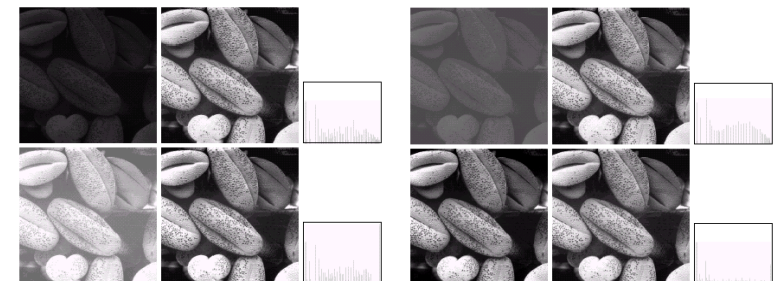


- How do histograms change when
  - we adjust brightness? **shifts the histogram horizontally**
  - we adjust contrast? **stretches or shrinks the histogram horizontally**

## Histogram equalization

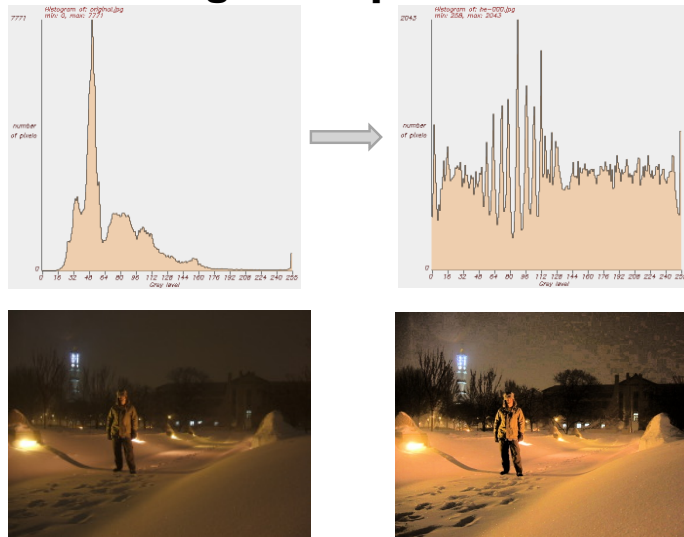
- A good quality image has a nearly uniform distribution of intensity levels. Why?
- Every intensity level is equally likely to occur in an image
- *Histogram equalization*: Transform an image so that it has a uniform distribution
  - create a lookup table defining the transformation

## Histogram equalization examples





## Histogram Equalization



Source: C. Dyer

## Histogram as a probability density function

- Recall that a normalized histogram measures the probability of occurrence of an intensity level  $r$  in an image
- We can normalize a histogram by dividing the intensity counts by the area

$$p(r) = \frac{h(r)}{\text{Area}}$$

## Histogram equalization: Continuous domain

- Define a transformation function of the form

$$s = T(r) = (L-1) \underbrace{\int_0^r p(w) dw}_{\text{cumulative distribution function}}$$

where

- $r$  is the input intensity level
- $s$  is the output intensity level
- $p$  is the normalized histogram of the input signal
- $L$  is the desired number of intensity levels

(Continuous) output signal has a uniform distribution!

## Histogram equalization: Discrete domain

- Define the following transformation function for an  $M \times N$  image

$$s_k = T(r_k) = (L-1) \sum_{j=0}^k \frac{n_j}{MN} = \frac{(L-1)}{MN} \sum_{j=0}^k n_j$$

for  $k = 0, \dots, L-1$

where

- $r_k$  is the input intensity level
- $s_k$  is the output intensity level
- $n_j$  is the number of pixels having intensity value  $j$  in the input image
- $L$  is the number of intensity levels

(Discrete) output signal has a nearly uniform distribution!

## Histogram Specification

- Given an input image  $f$  and a specific histogram  $p_2(r)$ , transform the image so that it has the specified histogram
- How to perform histogram specification?
- Histogram equalization produces a (nearly) uniform output histogram
- Use histogram equalization as an intermediate step

## Histogram Specification

1. Equalize the histogram of the input image

$$T_1(r) = (L-1) \int_0^r p_1(w) dw$$

2. Histogram equalize the desired output histogram

$$T_2(r) = (L-1) \int_0^r p_2(w) dw$$

3. Histogram specification can be carried out by the following point operation:

$$s = T(r) = T_2^{-1}(T_1(r))$$