

# BBM 413

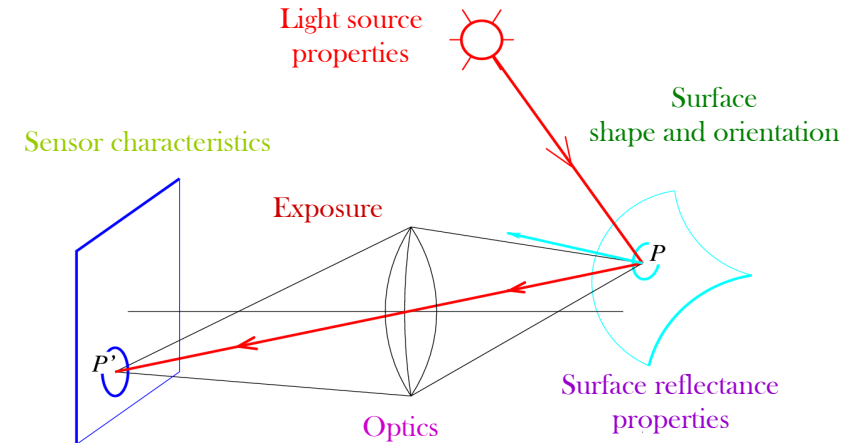
## Fundamentals of Image Processing

Erkut Erdem  
Dept. of Computer Engineering  
Hacettepe University

### Color Perception and Color Spaces

### Review - image formation

- What determines the brightness of an image pixel?



Slide credit: L. Fei-Fei

### Review - digital camera

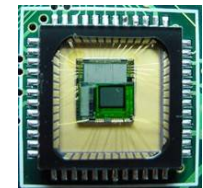
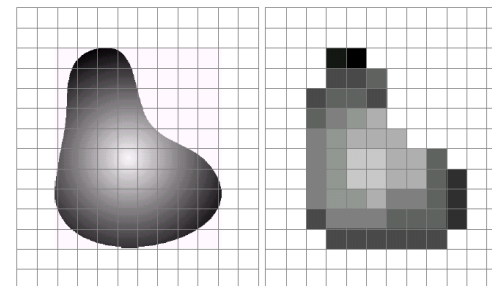


A digital camera replaces film with a sensor array

- Each cell in the array is light-sensitive diode that converts photons to electrons
- <http://electronics.howstuffworks.com/digital-camera.htm>

Slide credit: S. Seitz

### Review – digital images

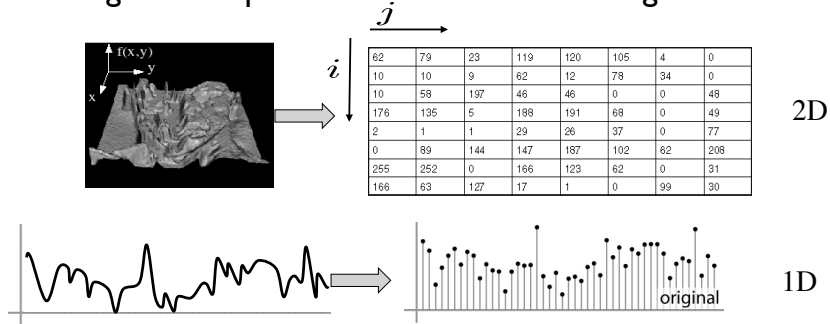


**FIGURE 2.17** (a) Continuous image projected onto a sensor array. (b) Result of image sampling and quantization.

Slide credit: D. Hoiem

## Review - digital images

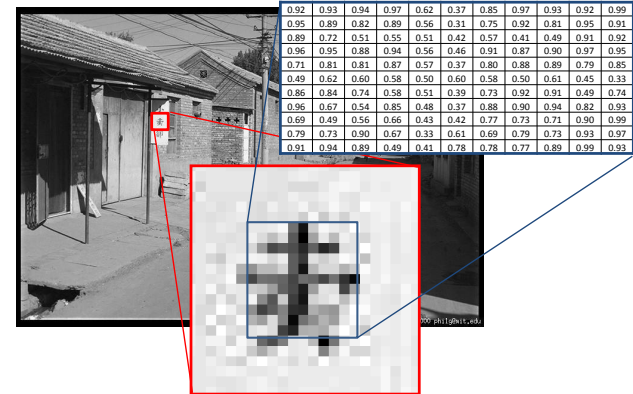
- Sample the 2D space on a regular grid
- Quantize each sample (round to nearest integer)
- Image thus represented as a matrix of integer values.



Slide credit: K. Grauman, S. Seitz

## Review – image representation

- **Digital image:** 2D discrete function  $f$
- **Pixel:** Smallest element of an image  $f(x,y)$



Slide credit: M. J. Black

## Outline

- Perception of color and light
- Color spaces

## Why does a visual system need color?



<http://www.hobbyline.com/gr/pll/pll5019.jpg>

Slide credit: W. Freeman

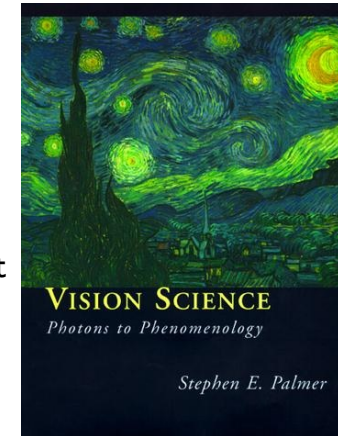
## Why does a visual system need color? (an incomplete list...)

- To tell what food is edible.
- To distinguish material changes from shading changes.
- To group parts of one object together in a scene.
- To find people's skin.
- Check whether a person's appearance looks normal/healthy.

Slide credit: W. Freeman

## What is color?

- Color is the result of interaction between physical light in the environment and our visual system
- Color is a psychological property of our visual experiences when we look at objects and lights, *not* a physical property of those objects or lights (S. Palmer, *Vision Science: Photons to Phenomenology*)



Slide credit: A. Efros

## #thedress

- What is the color of the dress?
- blue and black
- white and gold
- blue and brown
- What #thedress tell about our color perception?



<http://nyti.ms/186m3wE>

## #thedress

- Let's take averages



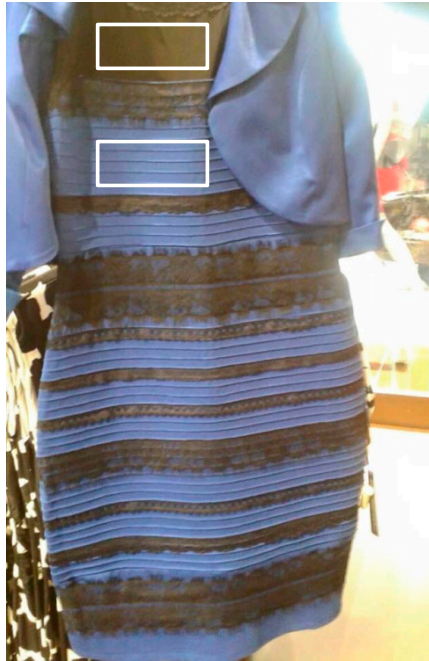
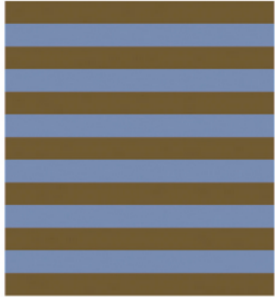
two pieces of the dress      averages      basic pattern



<http://nyti.ms/186m3wE>

## #thedress

- The dress in the photograph



<http://nyti.ms/186m3wE>

## #thedress

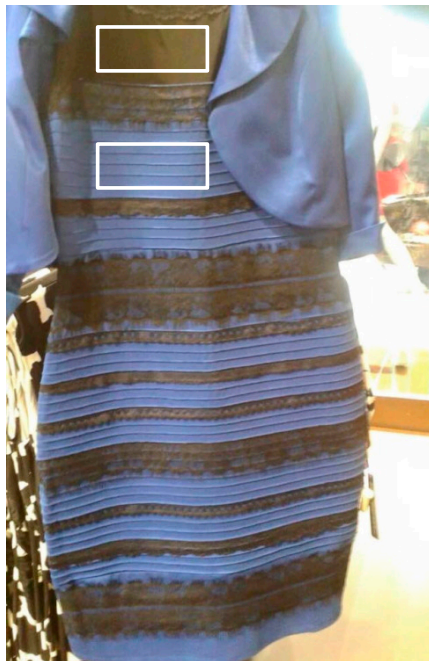
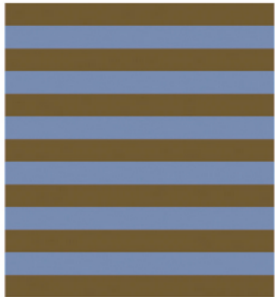
- Consider the dress is in shadow.



<http://nyti.ms/186m3wE>

## #thedress

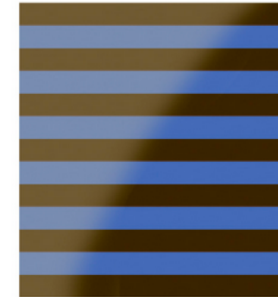
- The dress in the photograph



<http://nyti.ms/186m3wE>

## #thedress

- Consider the dress is in bright light.

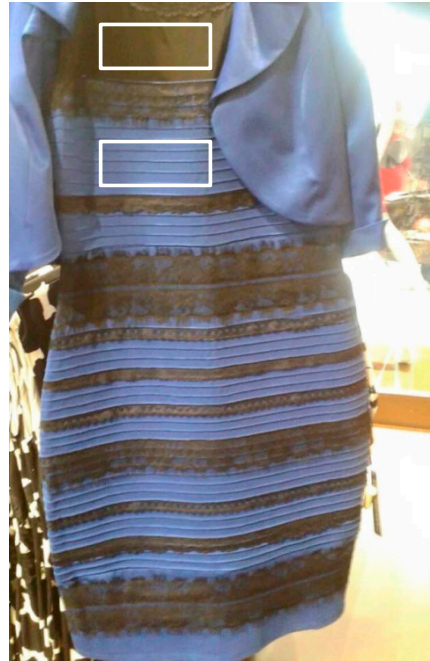


<http://nyti.ms/186m3wE>

- Your brain perceives the dress as a darker blue and black

## #thedress

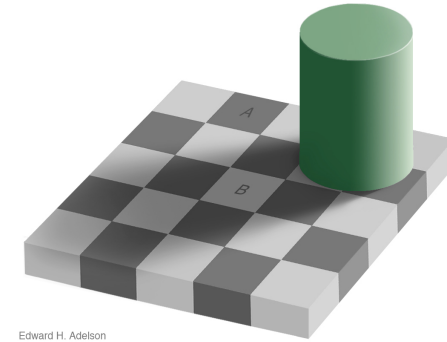
- Answer:



- The dress is actually blue and black.

<http://nyti.ms/186m3wE>

## Brightness perception

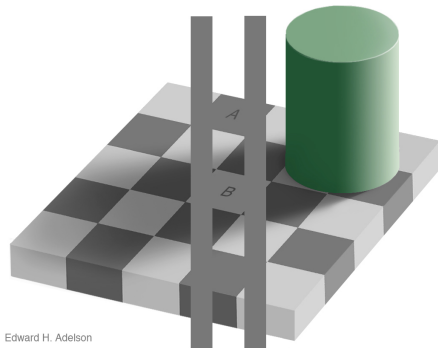


Edward H. Adelson

Edward Adelson

[http://web.mit.edu/persci/people/adelson/illusions\\_demos.html](http://web.mit.edu/persci/people/adelson/illusions_demos.html)

## Brightness perception

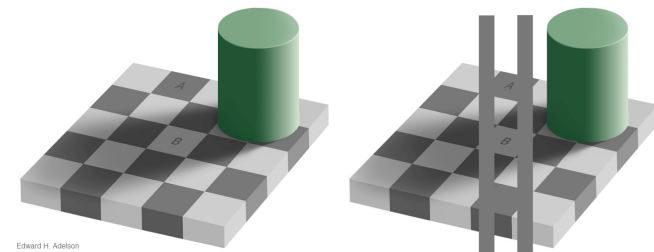


Edward H. Adelson

Edward Adelson

[http://web.mit.edu/persci/people/adelson/illusions\\_demos.html](http://web.mit.edu/persci/people/adelson/illusions_demos.html)

## Brightness perception



Edward H. Adelson

Edward Adelson

[http://web.mit.edu/persci/people/adelson/illusions\\_demos.html](http://web.mit.edu/persci/people/adelson/illusions_demos.html)

## Brightness perception



21

## Land's Experiment (1959)



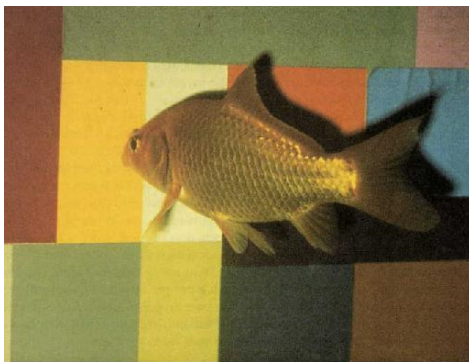
- Cover all patches except a blue rectangle
- Make it look gray by changing illumination
- Uncover the other patches

Color Constancy

We filter out illumination variations

Slide credit: S. Narasimhan

## Color Constancy in Gold Fish

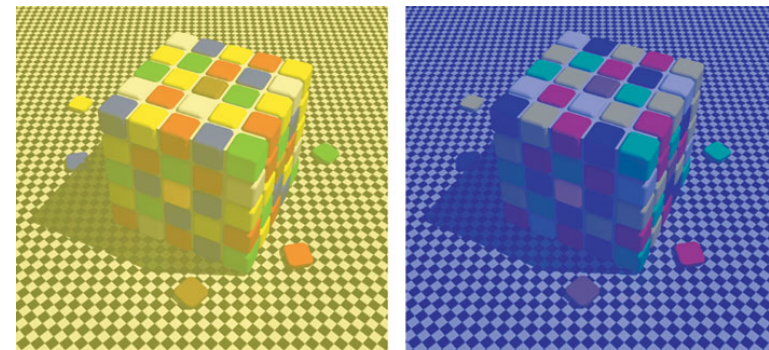


In David Ingle's experiment, a goldfish has been trained to swim to a patch of a given color for a reward—a piece of liver. It swims to the green patch regardless of the exact setting of the three projectors' intensities. The behavior is strikingly similar to the perceptual result in humans.

<http://neuro.med.harvard.edu/site/dh/b45.htm>

Slide credit: S. Narasimhan

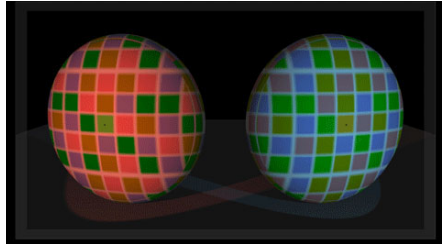
## Color Cube Illusion



Content © 2008 R.Beau Lotto

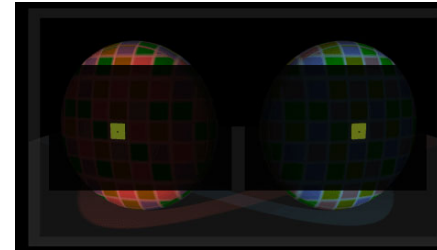
<http://www.lottolab.org/articles/illusionsoflight.asp>

## Color perception



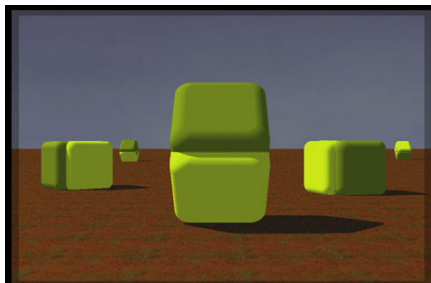
Content © 2008 R.Beau Lotto  
<http://www.lottolab.org/articles/illusionsoflight.asp>

## Color perception



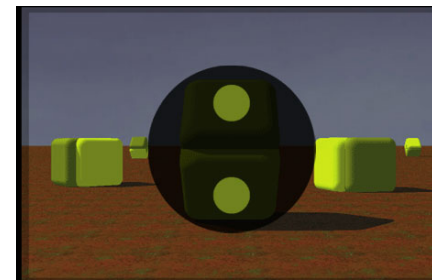
Content © 2008 R.Beau Lotto  
<http://www.lottolab.org/articles/illusionsoflight.asp>

## Color perception



Content © 2008 R.Beau Lotto  
<http://www.lottolab.org/articles/illusionsoflight.asp>

## Color perception



Content © 2008 R.Beau Lotto  
<http://www.lottolab.org/articles/illusionsoflight.asp>

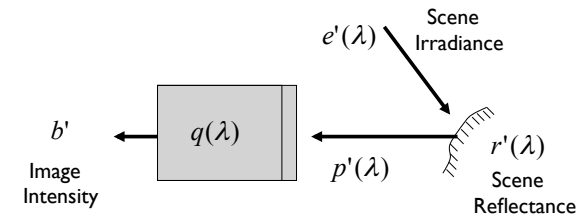
## Reading Assignment #2

- Watch Beau Lotto's TED talk on "Optical illusions show how we see" [link available on course webpage]
- Prepare a 1-page summary of the talk
- Due on 22<sup>nd</sup> of October



**TED** Ideas worth spreading

## Image Brightness (Intensity)



- Monochromatic Light : ( $\lambda = \lambda_i$ )

$$b'(x, y) = r'(x, y) e'(x, y) \quad q(\lambda_i) = 1$$

NOTE: The analysis can be applied to COLORED LIGHT using FILTERS

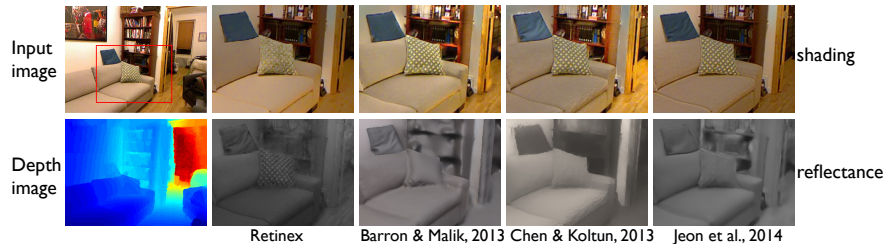
Slide credit: S. Narasimhan

## Recovering Lightness

- Image Intensity:  $b'(x, y) = r'(x, y) e'(x, y)$  **An illposed problem!**

Can we recover  $e'$  and  $r'$  from  $b'$  ?

- Retinex theory, Land and McCann, 1971
- use constraints (or priors) on shading and reflectance
- employ additional information (multiple images, depth maps, etc.)



Slide credit: S. Narasimhan

## Color and light

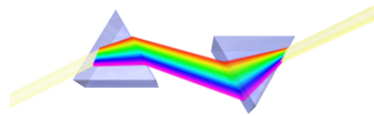
- **Color of light** arriving at camera depends on
  - Spectral reflectance of the surface light is leaving
  - Spectral radiance of light falling on that patch
- **Color perceived** depends on
  - Physics of light
  - Visual system receptors
  - Brain processing, environment
- Color is a phenomenon of human perception; it is **not** a universal property of light

Slide credit: K. Grauman, S. Marschner



# Color

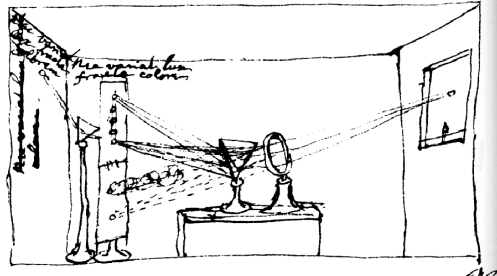
White light: composed of about equal energy in all wavelengths of the visible spectrum



Color



Newton 1665

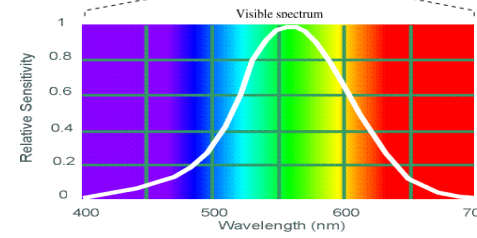
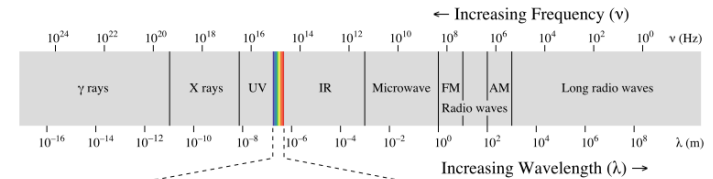


4.1 NEWTON'S SUMMARY DRAWING of his experiments with light. Using a point source of light and a prism, Newton separated sunlight into its fundamental components. By reconverging the rays, he also showed that the decomposition is reversible.  
From Foundations of Vision, by Brian Wandell, Sinauer Assoc., 1995

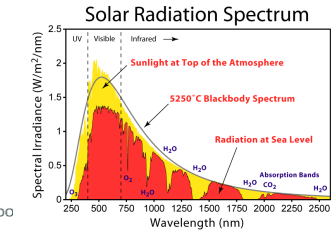
Slide credit: B. Freeman, A. Torralba, K. Grauman

# Electromagnetic spectrum

- Light is electromagnetic radiation
  - exists as oscillations of different frequency (or, wavelength)



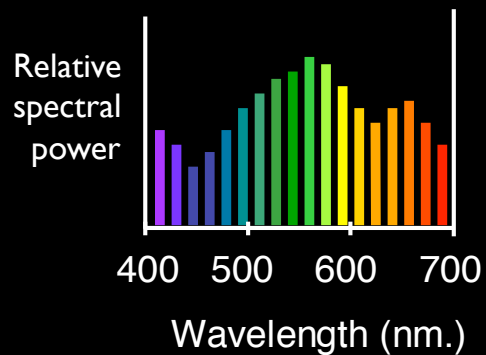
Human Luminance Sensitivity Function



Slide credit: A. Efros

# The Physics of light

Any source of light can be completely described physically by its spectrum: the amount of energy emitted (per time unit) at each wavelength 400 - 700 nm.

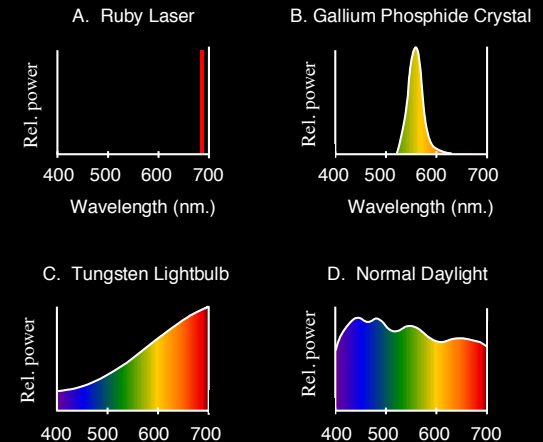


Slide credit: A. Efros

© Stephen E. Palmer, 2002

# The Physics of light

Some examples of the spectra of light sources

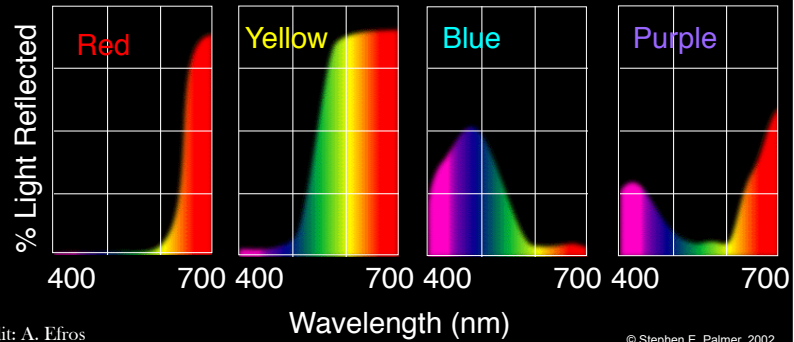


Slide credit: A. Efros

© Stephen E. Palmer, 2002

# The Physics of light

Some examples of the reflectance spectra of surfaces

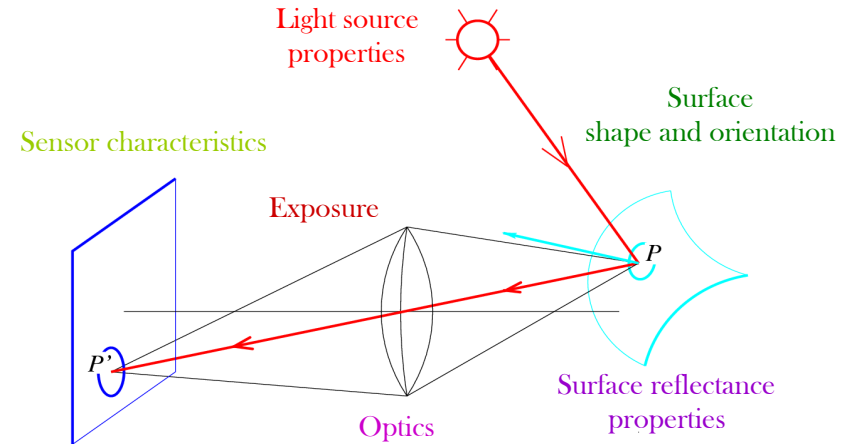


Slide credit: A. Efros

© Stephen E. Palmer, 2002

# Image formation

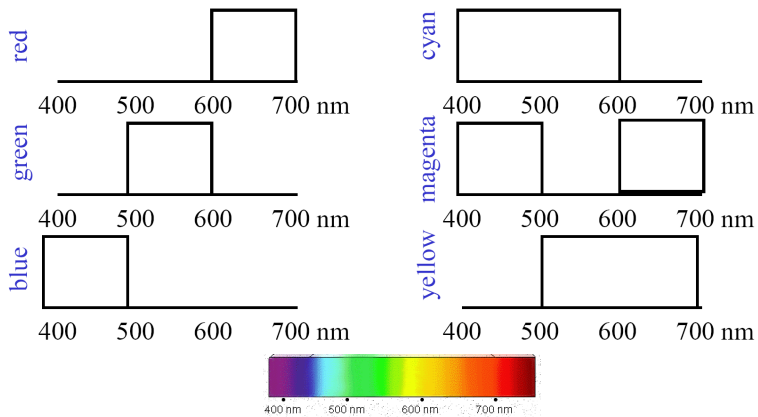
- What determines the brightness of an image pixel?



Slide credit: L. Fei-Fei

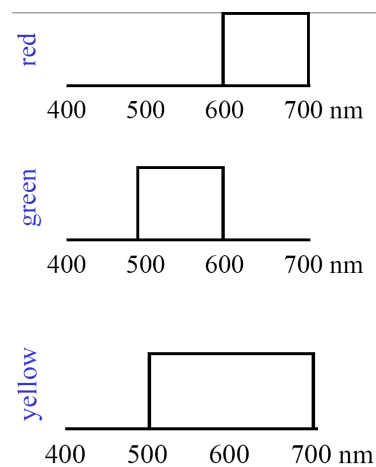
# Color mixing

Cartoon spectra for color names:

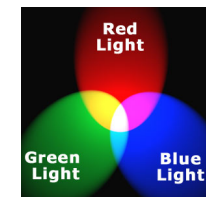


Credit: W. Freeman

# Additive color mixing



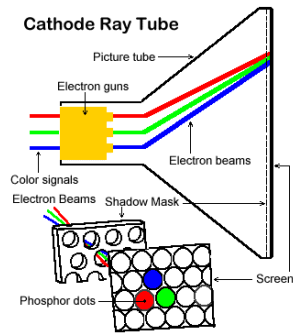
Colors combine by *adding* color spectra



Light *adds* to black.

Credit: W. Freeman

## Examples of additive color systems



CRT phosphors

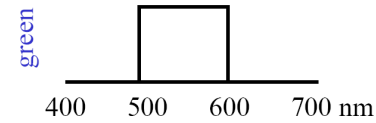
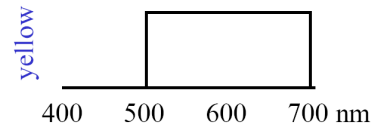
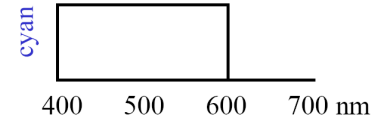


multiple projectors

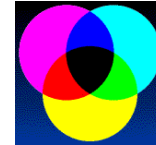
Slide credit: K. Grauman

<http://www.jegsworks.com>  
<http://www.crtprojectors.co.uk/>

## Subtractive color mixing



Colors combine by *multiplying* color spectra.



Pigments *remove* color from incident light (white).

Credit: W. Freeman

## Examples of subtractive color systems

- Printing on paper
- Crayons
- Photographic film

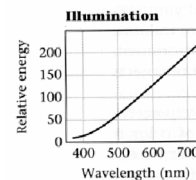


Slide credit: K. Grauman

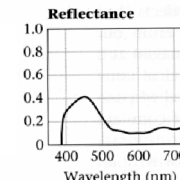
## Interaction of light and surfaces



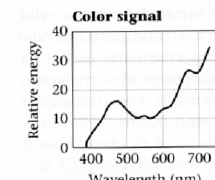
- Reflected color is the result of interaction of light source spectrum with surface reflectance



• \*

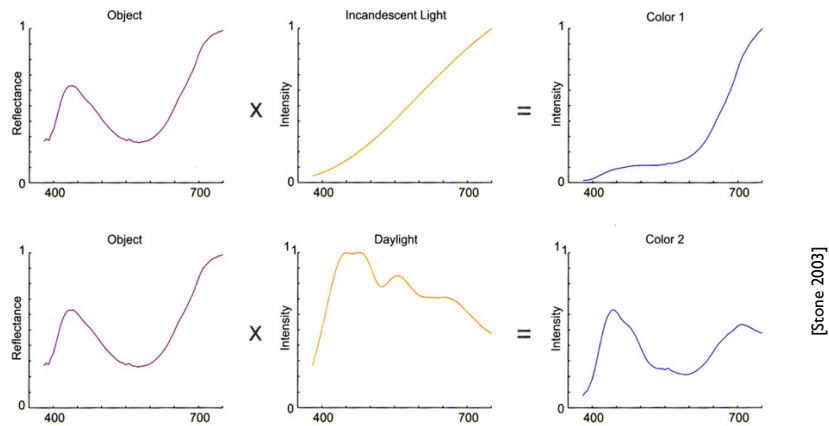


=



Slide credit: A. Efros

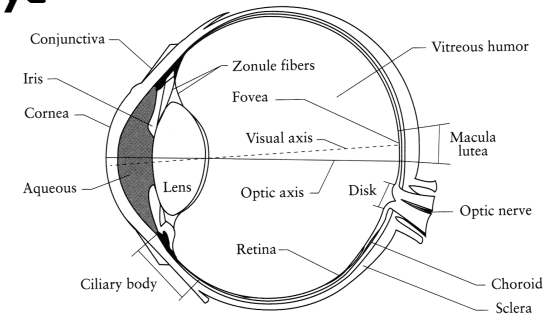
## Reflection from colored surface



[Stone 2003]

Slide credit: S. Marschner

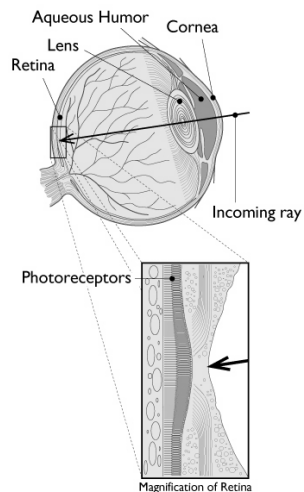
## The Eye



- **Iris** - colored annulus with radial muscles
- **Pupil** - the hole (aperture) whose size is controlled by the iris
- **Lens** - changes shape by using ciliary muscles (to focus on objects at different distances)
- **Retina** - photoreceptor cells

Slide credit: S. Seitz

## The eye as a measurement device

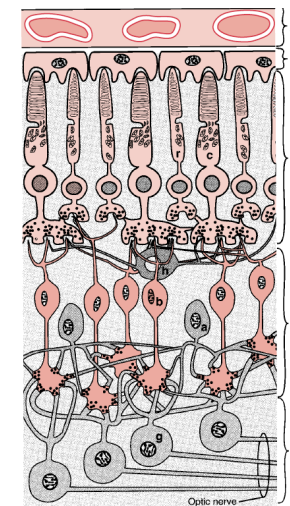


[Greger et al. 1995]

- We can model the low-level behavior of the eye by thinking of it as a light-measuring machine
  - its optics are much like a camera
  - its detection mechanism is also much like a camera
- Light is measured by the *photoreceptors* in the retina
  - they respond to visible light
  - different types respond to different wavelengths
- **The human eye is a camera!**

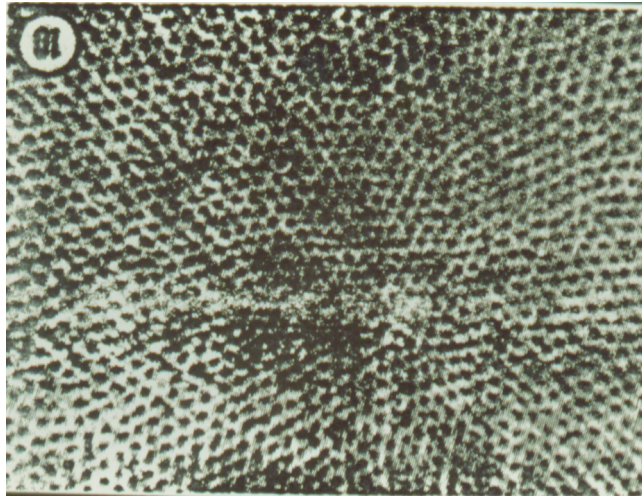
Slide credit: S. Marschner

## Layers of the retina



Slide credit: S. Ullman

## Receptors Density - Fovea



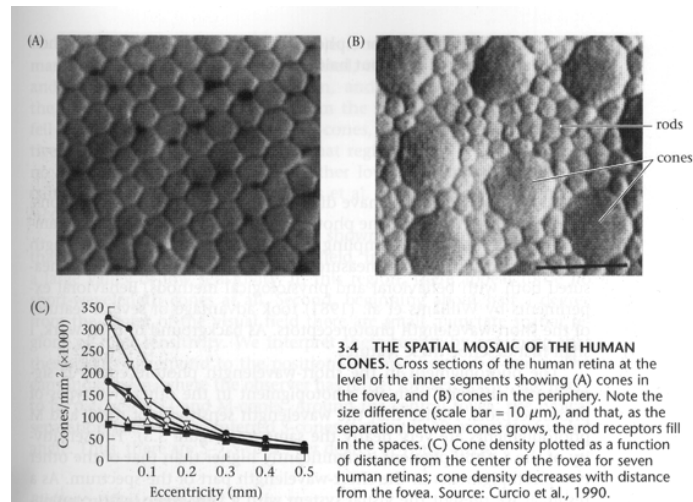
Slide credit: S. Ullman

## Receptors Density - Fovea

64	66	76	85	99	100	101	101	106	112	117	118	105	77	57	50	51	43	52	55	62
65	69	76	84	97	89	93	107	121	121	121	122	125	101	71	43	45	41	52	52	68
66	72	78	83	91	86	91	102	108	104	106	113	136	118	86	43	49	47	60	55	64
73	79	83	85	94	93	90	83	79	79	85	92	124	124	108	62	58	43	57	57	64
78	84	86	86	69	71	68	68	86	108	115	109	117	135	139	93	73	37	49	58	70
75	75	73	77	75	80	62	84	90	94	98	102	102	110	114	100	80	58	51	51	51
77	72	73	83	84	91	80	77	71	70	73	80	80	87	99	103	93	67	53	50	51
74	66	69	88	98	101	95	65	56	55	55	60	64	70	93	114	112	82	56	47	53
64	59	66	86	108	103	98	54	52	57	54	54	67	77	103	124	125	96	64	46	53
56	57	66	83	112	108	104	59	55	60	59	60	78	94	115	125	121	98	68	43	46
56	58	66	80	114	121	117	85	71	67	69	76	87	101	116	117	112	94	68	43	46
61	57	61	77	111	125	119	114	98	87	87	94	97	102	111	113	108	90	65	43	44
63	52	54	73	103	117	107	126	119	108	103	104	106	103	108	115	112	91	65	48	42
66	63	58	63	94	115	120	108	102	104	106	108	105	108	107	105	105	97	72	47	41
68	65	58	61	86	108	115	106	102	103	103	104	98	99	97	97	103	101	81	57	43
72	68	62	64	78	102	111	105	101	101	101	103	99	98	96	97	104	104	86	63	48
74	71	64	64	69	93	104	99	94	93	96	101	99	101	102	103	108	106	90	69	53

Slide credit: S. Ullman

## Human Photoreceptors

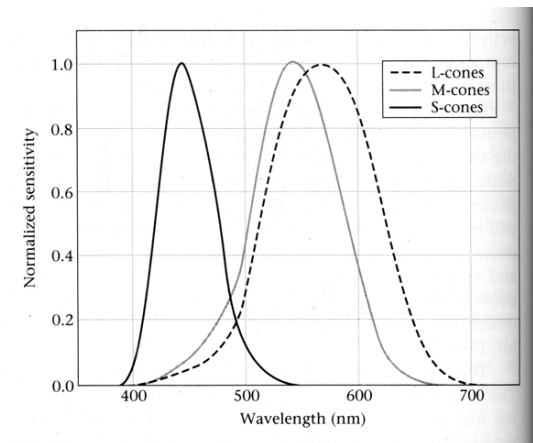


Images: Foundations of Vision, by Brian Wandell, Sinauer Assoc., 1995

Slide Credit: B. Freeman and A. Torralba

## Human eye photoreceptor spectral sensitivities

**3.3 SPECTRAL SENSITIVITIES OF THE L-, M-, AND S-CONES** in the human eye. The measurements are based on a light source at the cornea, so that the wavelength loss due to the cornea, lens, and other inert pigments of the eye plays a role in determining the sensitivity. Source: Stockman and MacLeod, 1993.



Images: Foundations of Vision, by Brian Wandell, Sinauer Assoc., 1995

Slide Credit: B. Freeman and A. Torralba

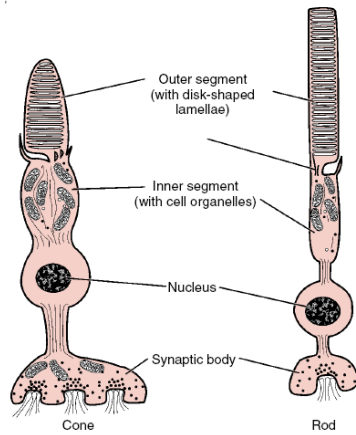
## Two types of light-sensitive receptors

### Cones

cone-shaped  
less sensitive  
operate in high light  
color vision

### Rods

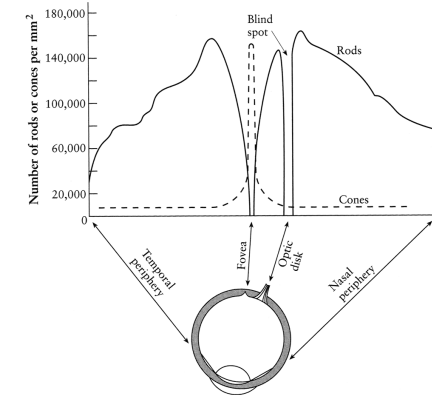
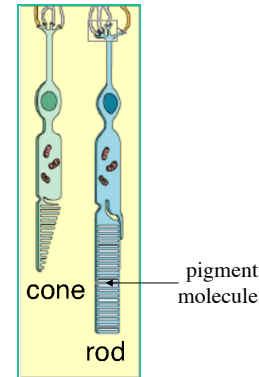
rod-shaped  
highly sensitive  
operate at night  
gray-scale vision



Images by Shimon Ullman

Slide credit: A. Efros

## Rods and cones



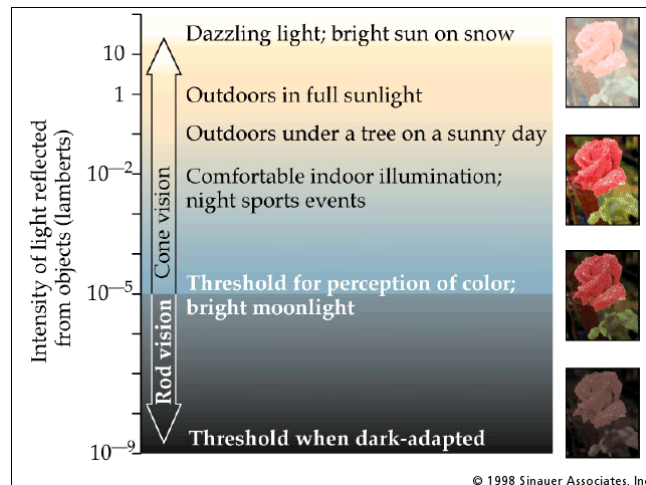
Rods are responsible for intensity, cones for color perception

Rods and cones are non-uniformly distributed on the retina

- Fovea - Small region (1 or 2°) at the center of the visual field containing the highest density of cones (and no rods)

Slide credit: S. Seitz

## Rod / Cone sensitivity

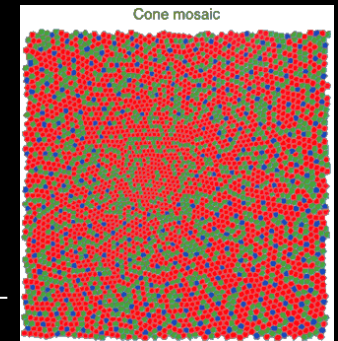
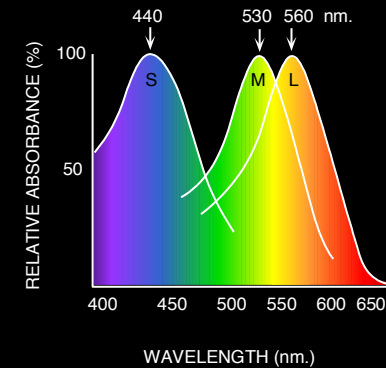


© 1998 Sinauer Associates, Inc.

Slide credit: A. Efros

## Physiology of Color Vision

### Three kinds of cones:

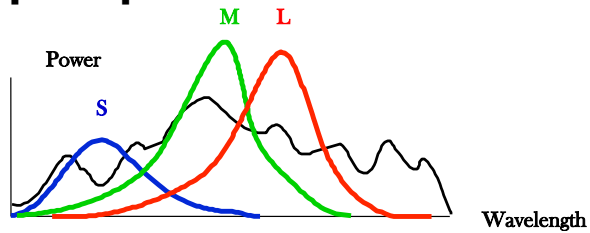


- Ratio of L to M to S cones: approx. 10:5:1
- Almost no S cones in the center of the fovea

Slide credit: A. Efros

© Stephen E. Palmer, 2002

## Color perception



Rods and cones act as filters on the spectrum

- To get the output of a filter, multiply its response curve by the spectrum, integrate over all wavelengths
  - Each cone yields one number

Q: How can we represent an entire spectrum with 3 numbers?

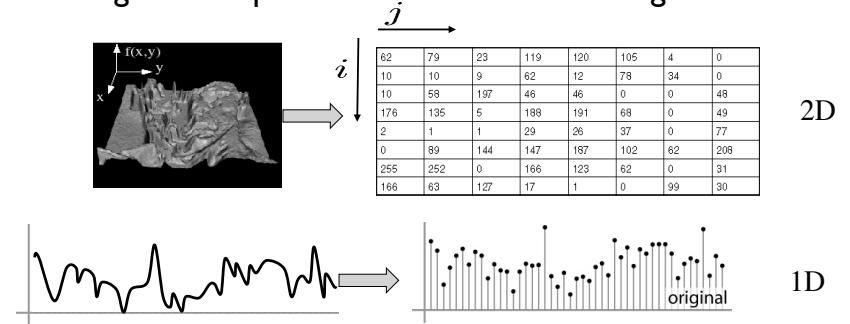
A: We can't! Most of the information is lost.

- As a result, two different spectra may appear indistinguishable

Slide credit: S. Seitz

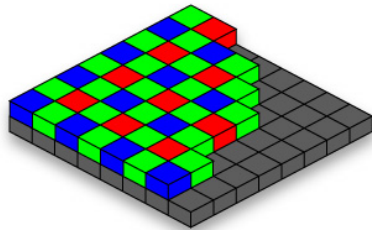
## Digital images

- Sample the 2D space on a regular grid
- Quantize each sample (round to nearest integer)
- Image thus represented as a matrix of integer values.

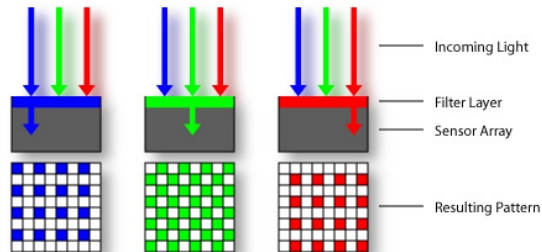


Slide credit: K. Grauman, S. Seitz

## Color Images: Bayer Grid



- Estimate RGB at 'G' cells from neighboring values



Slide credit: S. Seitz

<http://www.cooldictionary.com/words/Bayer-filter.wikipedia>

## Digital color images

Color images, RGB color space



R



G



B

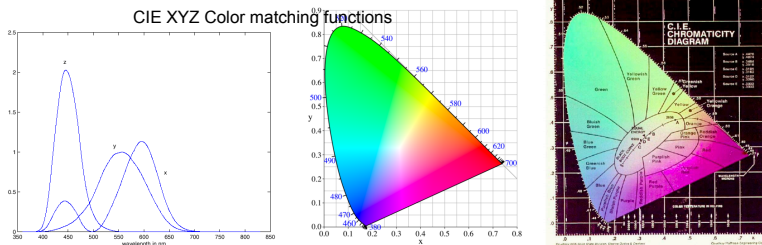
Slide credit: K. Grauman





## Color spaces: CIE XYZ

- Standardized by CIE (*Commission Internationale de l'Éclairage*, the standards organization for color science)
- Based on three “imaginary” primaries **X**, **Y**, and **Z**
  - imaginary = only realizable by spectra that are negative at some wavelengths
  - separates out luminance: **X**, **Z** have zero luminance, so **Y** tells you the luminance by itself



Slide credit: K. Grauman, S. Marschner

## Color spaces: CIE XYZ

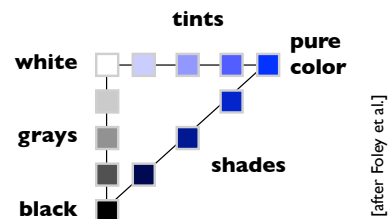
- Standardized by CIE (*Commission Internationale de l'Éclairage*, the standards organization for color science)
- Based on three “imaginary” primaries **X**, **Y**, and **Z**
  - imaginary = only realizable by spectra that are negative at some wavelengths
  - separates out luminance: **X**, **Z** have zero luminance, so **Y** tells you the luminance by itself

$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \frac{1}{0.17697} \begin{bmatrix} 0.49 & 0.31 & 0.20 \\ 0.17697 & 0.81240 & 0.01063 \\ 0.00 & 0.01 & 0.99 \end{bmatrix} \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$

Slide credit: K. Grauman, S. Marschner

## Perceptually organized color spaces

- Artists often refer to colors as *tints*, *shades*, and *tones* of pure pigments
  - tint: mixture with white
  - shade: mixture with black
  - tones: mixture with black and white
  - gray: no color at all (aka. neutral)
- This seems intuitive
  - tints and shades are inherently related to the pure color
    - “same” color but lighter, darker, paler, etc.



Slide credit: S. Marschner

## Perceptual dimensions of color

- Hue
  - the “kind” of color, regardless of attributes
  - colorimetric correlate: dominant wavelength
  - artist’s correlate: the chosen pigment color
- Saturation
  - the “colorfulness”
  - colorimetric correlate: purity
  - artist’s correlate: fraction of paint from the colored tube
- Lightness (or value)
  - the overall amount of light
  - colorimetric correlate: luminance
  - artist’s correlate: tints are lighter, shades are darker

Slide credit: S. Marschner

## Color spaces: HSV

- **Hue, Saturation, Value**
- Nonlinear – reflects topology of colors by coding **hue** as an angle
- Matlab: `hsv2rgb`, `rgb2hsv`.

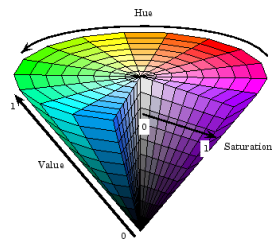
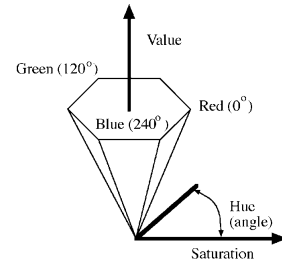


Image from mathworks.com



Slide credit: K. Grauman

## Color spaces: HSV

- **Hue, Saturation, Value**
- Nonlinear – reflects topology of colors by coding **hue** as an angle
- Matlab: `hsv2rgb`, `rgb2hsv`.

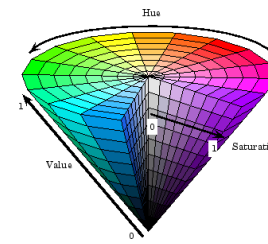


Image from mathworks.com

$$H = \begin{cases} \left( \frac{G' - B'}{MAX - MIN} \right) / 6, & \text{if } R' = MAX \\ 2 + \left( \frac{B' - R'}{MAX - MIN} \right) / 6, & \text{if } G' = MAX \\ 4 + \left( \frac{R' - G'}{MAX - MIN} \right) / 6, & \text{if } B' = MAX \end{cases}$$

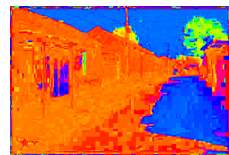
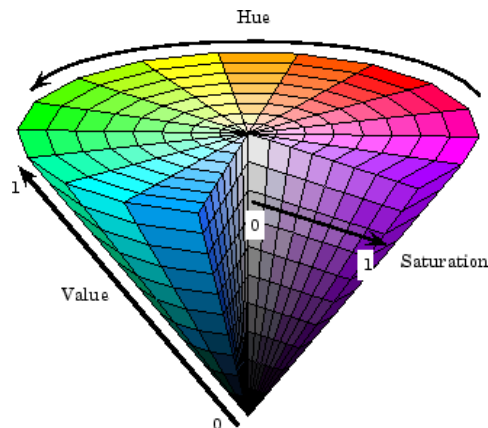
$$S = \frac{MAX - MIN}{MAX}$$

$$V = MAX$$

Slide credit: K. Grauman

## Color spaces: HSV

Intuitive color space



**H**  
(S=1, V=1)



**S**  
(H=1, V=1)

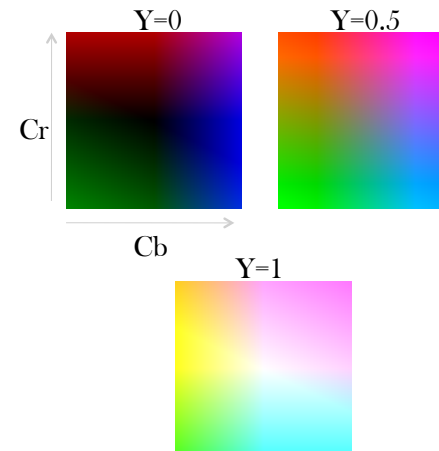


**V**  
(H=1, S=0)

Slide credit: D. Hoiem

## Color spaces: YCbCr

Fast to compute, good for compression, used by TV



**Y**  
(Cb=0.5, Cr=0.5)



**Cb**  
(Y=0.5, Cr=0.5)

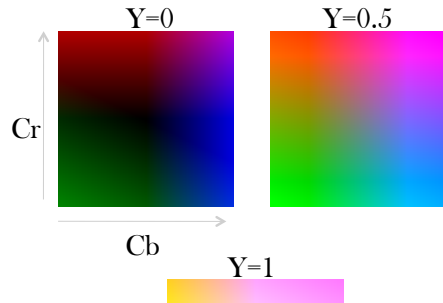


**Cr**  
(Y=0.5, Cb=0.5)

Slide credit: D. Hoiem

## Color spaces: YCbCr

Fast to compute, good for compression, used by TV



**Y**  
(Cb=0.5, Cr=0.5)



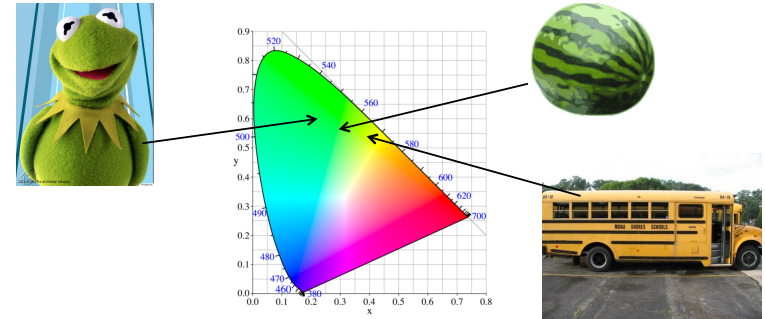
**Cb**  
(Y=0.5, Cr=0.5)

$$\begin{bmatrix} Y' \\ C_b \\ C_r \end{bmatrix} = \begin{bmatrix} 0.299 & 0.587 & 0.114 \\ -0.168736 & -0.331264 & 0.5 \\ 0.5 & -0.418688 & -0.081312 \end{bmatrix} \begin{bmatrix} R' \\ G' \\ B' \end{bmatrix} + \begin{bmatrix} 0 \\ 128 \\ 128 \end{bmatrix}$$

Slide credit: D. Hoiem

## Distances in color space

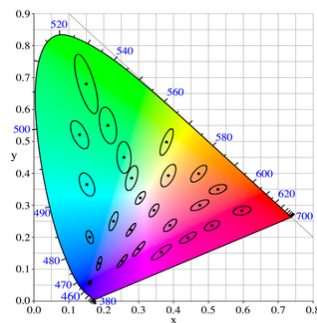
- Are distances between points in a color space perceptually meaningful?



Slide credit: K. Grauman

## Distances in color space

- Not necessarily: CIE XYZ is not a uniform color space, so magnitude of differences in coordinates are poor indicator of color "distance".

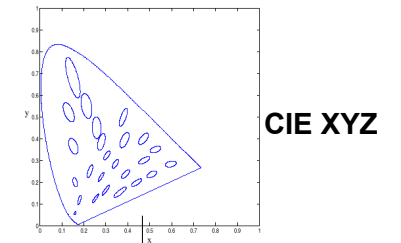


McAdam ellipses:  
Just noticeable differences in color

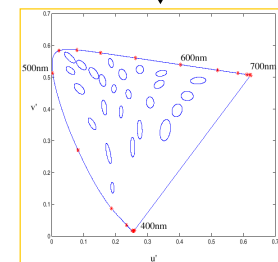
Slide credit: K. Grauman

## Uniform color spaces

- Attempt to correct this limitation by remapping color space so that just-noticeable differences are contained by circles → distances more perceptually meaningful.



**CIE XYZ**



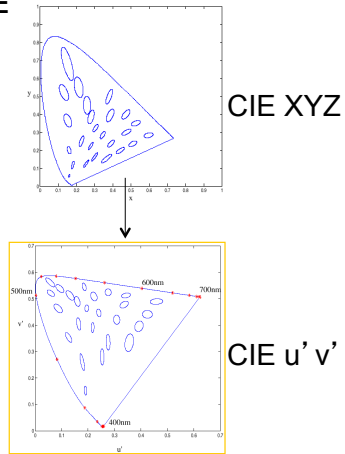
**CIE u'v'**

- Examples:
  - CIE u'v'
  - CIE Lab

Slide credit: K. Grauman

## Perceptually uniform spaces

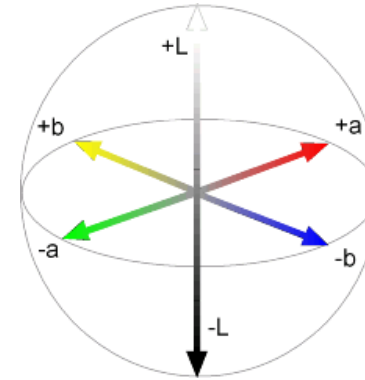
- Two major spaces standardized by CIE
  - designed so that equal differences in coordinates produce equally visible differences in color
  - by remapping color space so that just-noticeable differences are contained by circles → distances more perceptually meaningful.
  - LUV: earlier, simpler space;  $L^*$ ,  $u^*$ ,  $v^*$
  - LAB: more complex but more uniform:  $L^*$ ,  $a^*$ ,  $b^*$
  - both separate luminance from chromaticity
  - including a gamma-like nonlinear component is important



Slide credit: K. Grauman, S. Marschner

## Color spaces: $L^*a^*b^*$

“Perceptually uniform”\* color space



**L**  
(a=0,b=0)



**a**  
(L=65,b=0)



**b**  
(L=65,a=0)

Slide credit: D. Hoiem

## Color spaces: $L^*a^*b^*$

“Perceptually uniform”\* color space



$$L^* = 116f\left(\frac{Y}{Y_n}\right)$$

$$f(t) = \begin{cases} t^{1/3} & t > \delta^3 \\ t/(3\delta^2) + 2\delta/3 & \text{else,} \end{cases}$$

$$a^* = 500 \left[ f\left(\frac{X}{X_n}\right) - f\left(\frac{Y}{Y_n}\right) \right]$$

$$b^* = 200 \left[ f\left(\frac{Y}{Y_n}\right) - f\left(\frac{Z}{Z_n}\right) \right]$$

$(X_n, Y_n, Z_n)$ : measured white point



**L**  
(a=0,b=0)



**a**  
(L=65,b=0)



**b**  
(L=65,a=0)

Slide credit: D. Hoiem

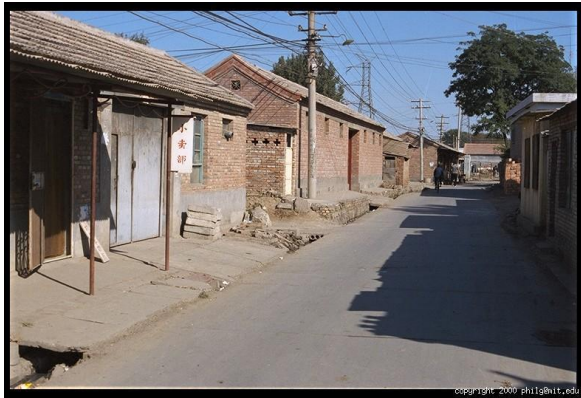
## Most information in intensity



Only intensity shown – constant color

Slide credit: D. Hoiem

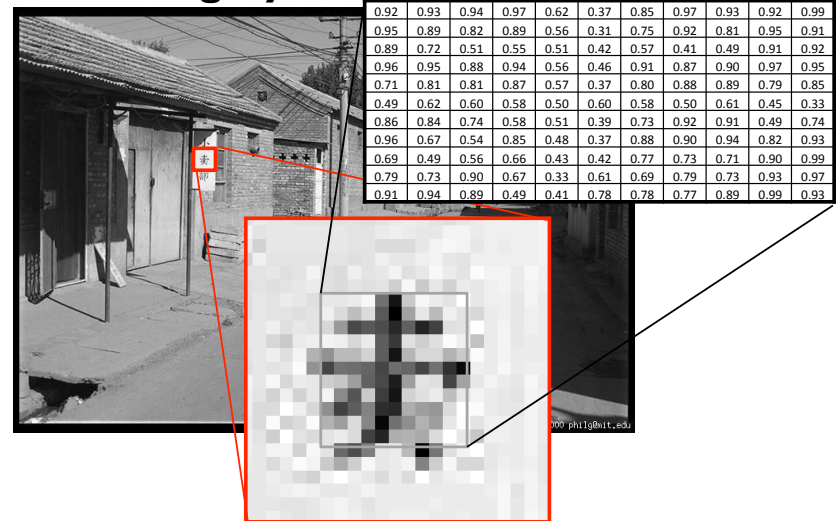
## Most information in intensity



Original image

Slide credit: D. Hoiem

## Back to grayscale intensity



Slide credit: D. Hoiem

## Today

- Perception of color and light
- Color spaces

## Next week

- Point operations
- Histogram processing

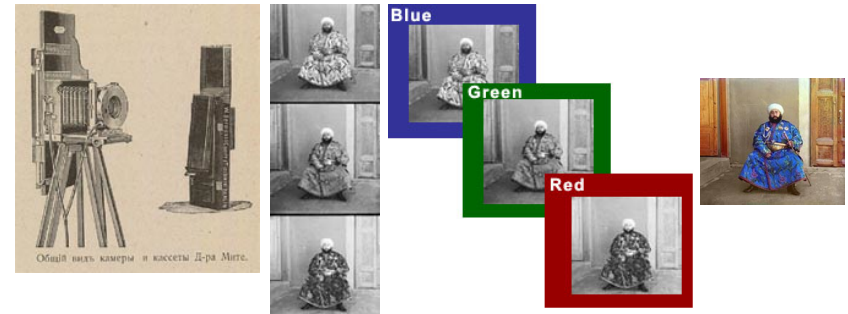
## Your first programming assignment

- Colorizing the Prokudin-Gorskii photo collection
- A Matlab warm-up exercise
- Main steps:
  1. Divide the input image into three equal parts corresponding to RGB channels.
  2. Align the second and the third parts (G and R channels) to the first one (B channel).



## Prokudin-Gorskii's Russia in Color

- Russia circa 1900
- One camera, move the film with filters to get 3 exposures



Images from: <http://www.loc.gov/exhibits/empire/>

Slide credit: F. Durand

## Prokudin-Gorskii's Russia in Color

- Digital restoration



Slide credit: F. Durand



Emir Seyyid Mir Mohammed Alim Khan, the Emir of Bukhara, ca. 1910.



Self-portrait on the Karolitskhali River, ca. 1910.



A metal truss bridge on stone piers, part of the Trans-Siberian Railway, crossing the Kama River near Perm, Ural Mountains Region, ca. 1910.



On the Sim River, a shepherd boy, ca. 1910.



Peasants harvesting hay in 1909. From the album "Views along the Mariinskii Canal and river system, Russian Empire", ca. 1910.