CMP717

Image Processing

Introduction to Deep Learning

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What is deep learning?

Y. LeCun, Y. Bengio, G. Hinton, "**Deep Learning**", Nature, Vol. 521, 28 May 2015

"Deep learning allows computational models that are composed of **multiple processing layers to learn representations of data with multiple levels of abstraction.**"

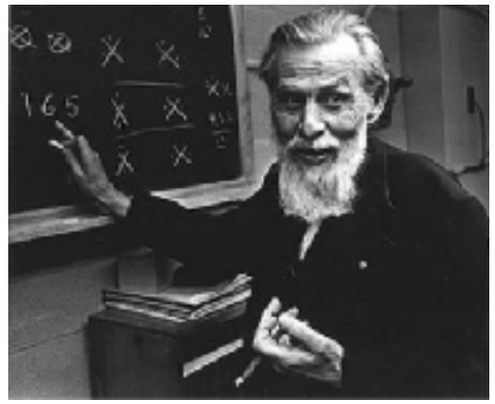
– Yann LeCun, Yoshua Bengio and Geoff Hinton

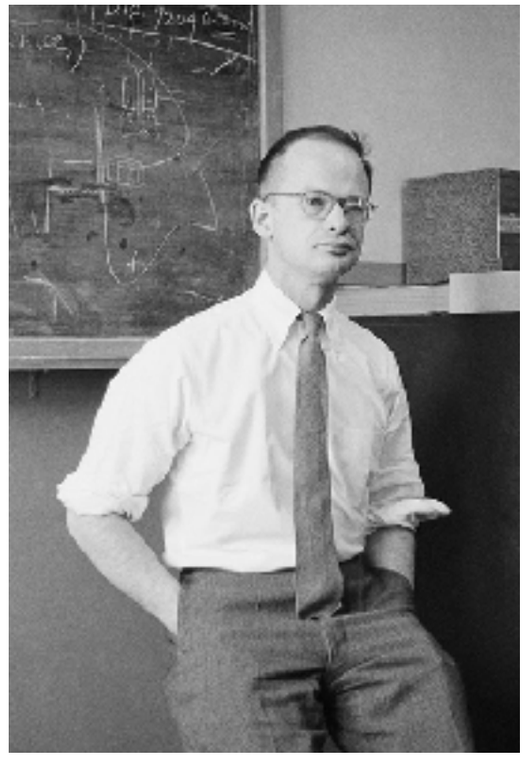
1943 – 2006:

A Prehistory of Deep Learning

1943: Warren McCulloch and Walter Pitts

- First computational model
- Neurons as logic gates (AND, OR, NOT)
- A neuron model that sums binary inputs and outputs 1 if the sum exceeds a certain threshold value, and otherwise outputs 0



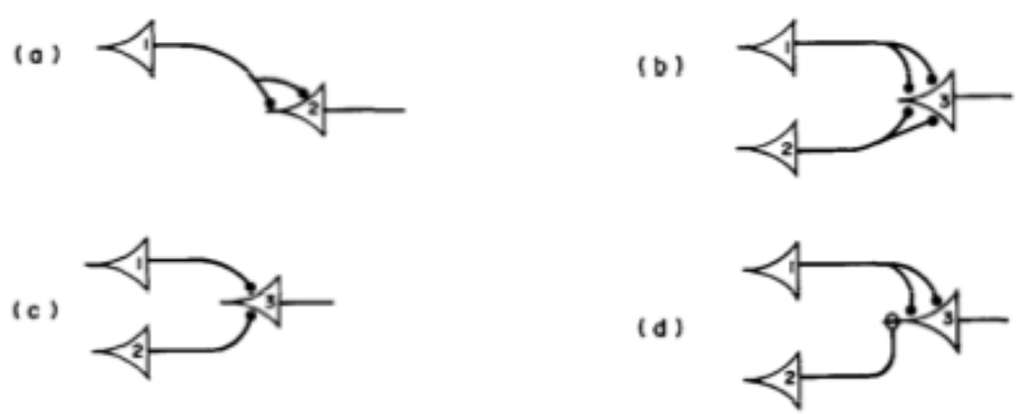


A LOGICAL CALCULUS OF THE IDEAS IMMANENT IN NERVOUS ACTIVITY*

WARREN S. MCCULLOCH AND WALTER PITTS
University of Illinois, College of Medicine,
Department of Psychiatry at the Illinois Neuropsychiatric Institute,
University of Chicago, Chicago, U.S.A.

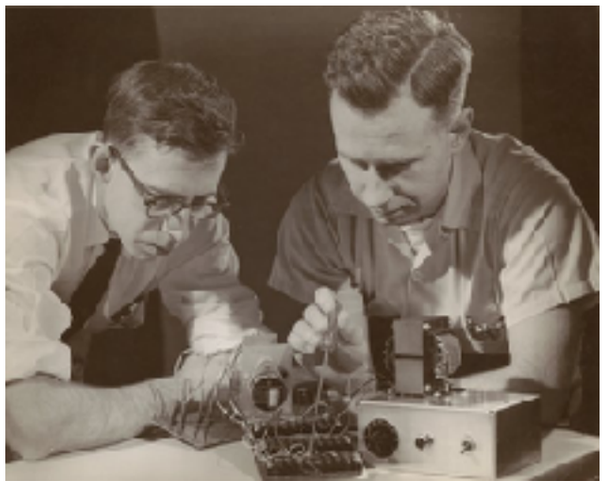
1. Introduction. Theoretical neurophysiology rests on certain cardinal assumptions. The nervous system is a net of neurons, each having a soma and an axon. Their junctions, or synapses, are always between the axon of one neuron and the soma of another. At any instant a neuron has some threshold, which excitation must exceed to initiate an impulse. This, except for the fact and the time of its occurrence, is determined by the neuron, not by the excitation. From the point of excitation the impulse is propagated to all parts of the neuron. The velocity along the axon varies directly with its diameter, from $<1\ ms^{-1}$ in thin axons, which are usually short, to $>150\ ms^{-1}$ in thick axons, which are usually long. The time for axonal conduction is consequently of little importance in determining the time of arrival of impulses at points unequally remote from the same source. Excitation across synapses occurs predominantly from axonal terminations to somata. It is still a moot point whether this depends upon irreducibly synaptic or merely upon prevalent anatomical configurations. To suppose the latter requires no hypothesis ad hoc and explains known exceptions, but any assumption as to cause is compatible with the calculus to come. No case is known in which excitation through a single synapse has elicited a nervous impulse in any neuron, whereas any neuron may be excited by impulses arriving at a sufficient number of neighboring synapses within the period of latent addition, which lasts <0.25 ms. Observed temporal summation of impulses at greater intervals

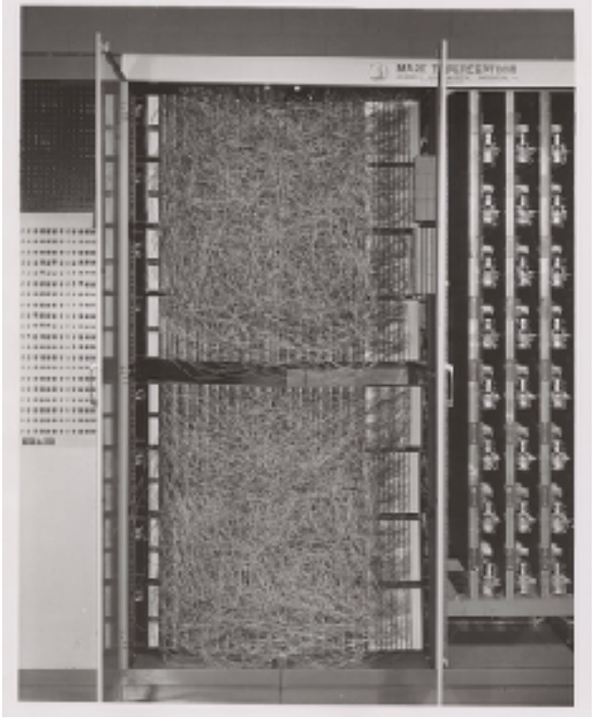
* Reprinted from the Bulletin of Mathematical Biophysics, Vol 5, pp. 115-133 (1943).

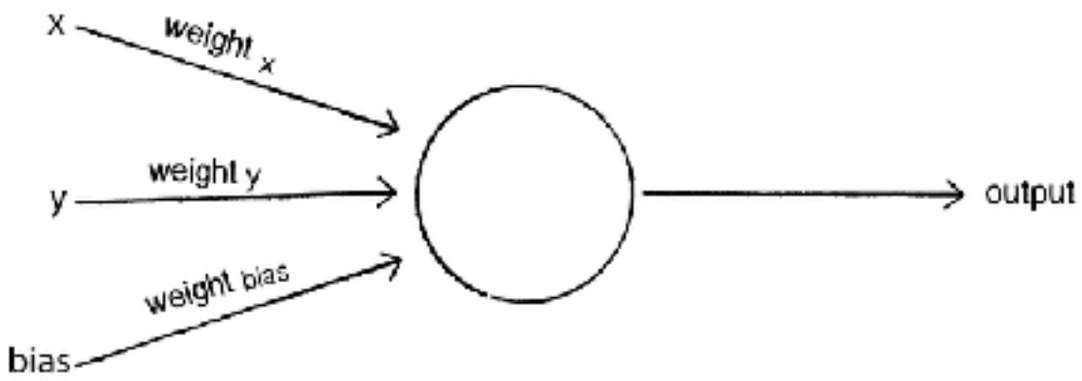


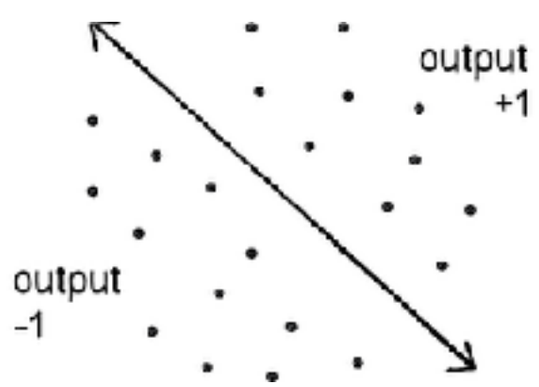
1958: Frank Rosenblatt's Perceptron

- A computational model of a **single neuron**
- Solves a **binary classification problem**
- Simple training algorithm
- Built using specialized hardware







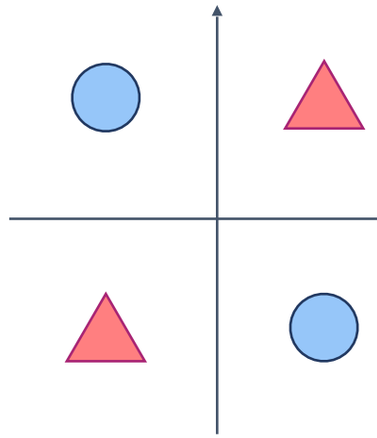


F. Rosenblatt, "The perceptron: A probabilistic model for information storage and organization in the brain", Psychological Review, Vol. 65, 1958

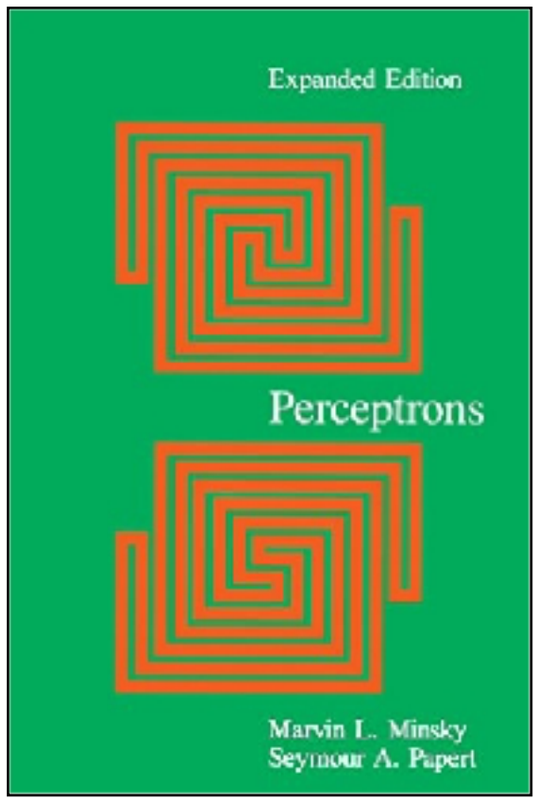
1969: Marvin Minsky and Seymour Papert

"No machine can learn to recognize X unless it possesses, at least potentially, some scheme for representing X." (p. xiii)

- Perceptrons can only represent linearly separable functions.
  - such as **XOR** Problem

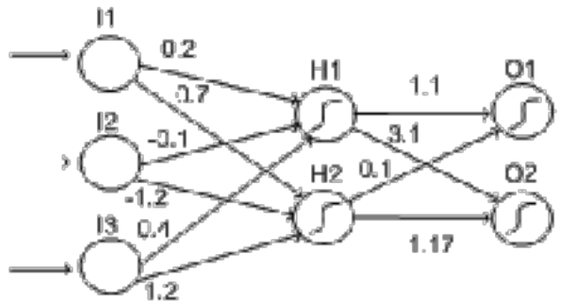


- Wrongly attributed as the reason behind the **AI winter**, a period of reduced funding and interest in AI research



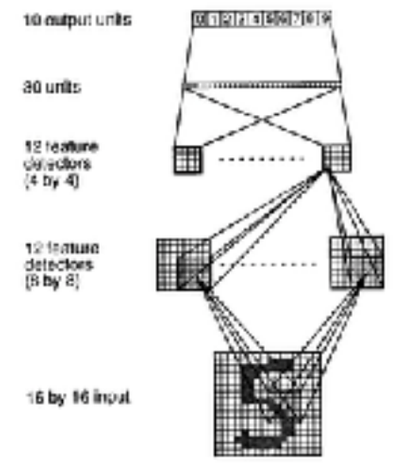
1990s

- **Multi-layer perceptrons** can theoretically learn any function (Cybenko, 1989; Hornik, 1991)

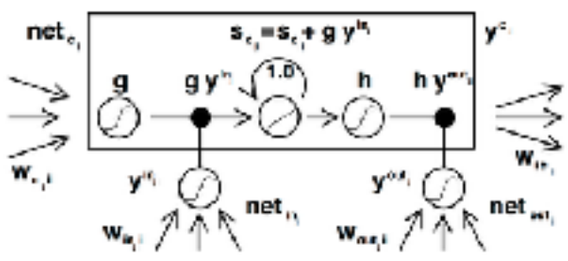



Backpropagation Through Time: What It Does and How to Do It

- Training multi-layer perceptrons
  - **Back-propagation** (Rumelhart, Hinton, Williams, 1986)
  - **Back-propagation through time** (BPTT) (Werbos, 1988)



- New neural architectures
  - **Convolutional neural nets** (LeCun et al., 1989)
  - **Long-short term memory networks** (LSTM) (Schmidhuber, 1997)



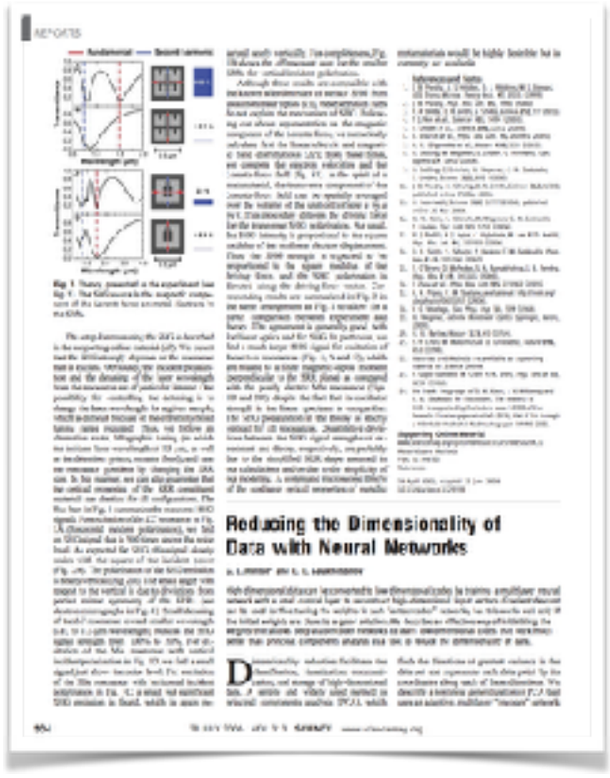
Why it failed then

- Too many parameters to learn from few labeled examples.
- “I know my features are better for this task”.
- Non-convex optimization? No, thanks.
- Black-box model, no interpretability.

- Very slow and inefficient
- Overshadowed by the success of SVMs (Cortes and Vapnik, 1995)

A major breakthrough in 2006

2006 Breakthrough: Hinton and Salakhutdinov



Reducing the Dimensionality of Data with Neural Networks

G. E. Hinton* and R. R. Salakhutdinov

High-dimensional data can be converted to low-dimensional codes by training a multilayer neural network with a small central layer to reconstruct high-dimensional input vectors. Gradient descent can be used for fine-tuning the weights in such "autoencoder" networks, but this works well only if the initial weights are close to a good solution. We describe an effective way of initializing the weights that allows deep autoencoder networks to learn low-dimensional codes that work much better than principal components analysis as a tool to reduce the dimensionality of data.

- The first solution to the **vanishing gradient problem**.
- Build the model in a layer-by-layer fashion using unsupervised learning
  - The features in early layers are already initialized or "pretrained" with some suitable features (weights).
  - Pretrained features in early layers only need to be adjusted slightly during supervised learning to achieve good results.

G. E. Hinton and R. R. Salakhutdinov, "**Reducing the dimensionality of data with neural networks**", Science, Vol. 313, 28 July 2006.

The 2012 revolution

ImageNet Challenge

- IMAGENET Large Scale Visual Recognition Challenge (ILSVRC)
  - **1.2M** training images with **1K** categories
  - Measure top-5 classification error

Output
Scale
T-shirt
Steel drum
Drumstick
Mud turtle

✔

Output
Scale
T-shirt
Giant panda
Drumstick
Mud turtle

✗

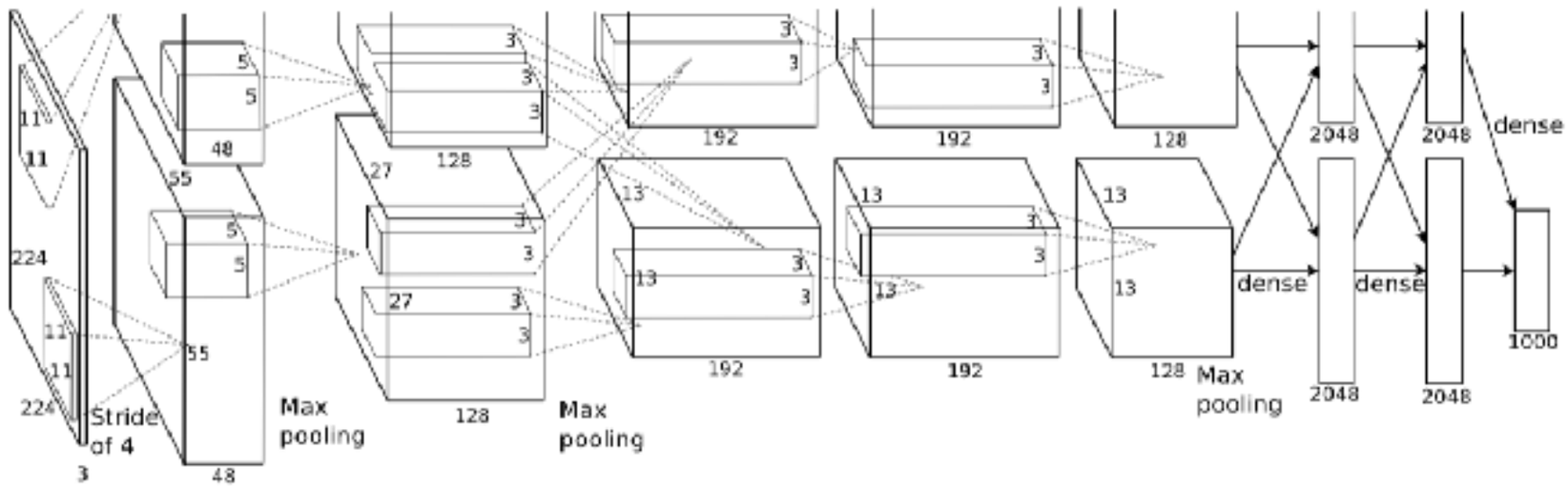
Image classification

J. Deng, Wei Dong, R. Socher, L.-J. Li, K. Li and L. Fei-Fei , **"ImageNet: A Large-Scale Hierarchical Image Database"**, CVPR 2009.
O. Russakovsky et al., **"ImageNet Large Scale Visual Recognition Challenge"**, Int. J. Comput. Vis.,, Vol. 115, Issue 3, pp 211-252, 2015.

ILSVRC 2012 Competition

2012 Teams	%Error
Supervision (Toronto)	15.3
ISI (Tokyo)	26.1
VGG (Oxford)	26.9
XRCE/INRIA	27.0
UvA (Amsterdam)	29.6
INRIA/LEAR	33.4

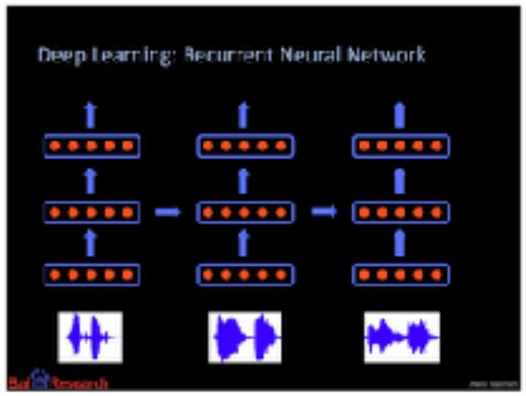
CNN based,
non-CNN based



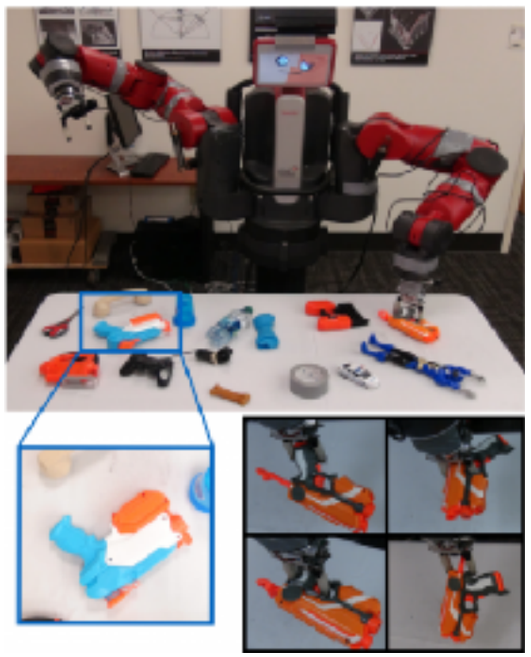
- The success of AlexNet, a deep convolutional network
  - 7 hidden layers (not counting some max pooling layers)
  - 60M parameters
- Combined several tricks
  - ReLU activation function, data augmentation, dropout

2012 – now

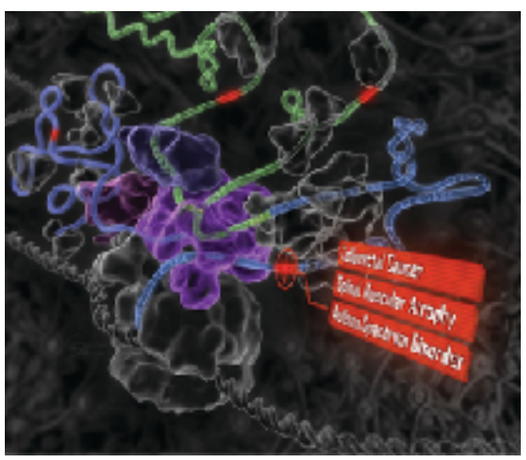
A Cambrian explosion in deep learning



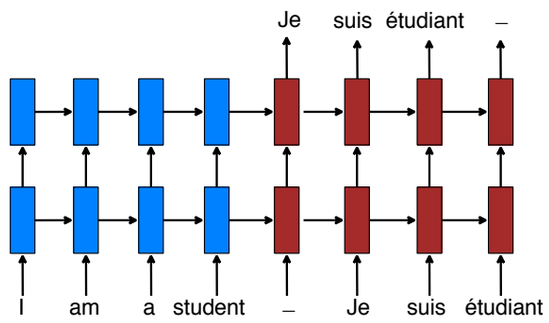
Speech recognition



Robotics



Genomics



Machine Translation

Game Playing

Audio Generation

Self-Driving Cars

Amodei et al., **"Deep Speech 2: End-to-End Speech Recognition in English and Mandarin"**, In CoRR 2015

M.-T. Luong et al., **"Effective Approaches to Attention-based Neural Machine Translation"**, EMNLP 2015

M. Bojarski et al., **"End to End Learning for Self-Driving Cars"**, In CoRR 2016

D. Silver et al., **"Mastering the game of Go with deep neural networks and tree search"**, Nature 529, 2016

L. Pinto and A. Gupta, **"Supersizing Self-supervision: Learning to Grasp from 50K Tries and 700 Robot Hours"** ICRA 2015

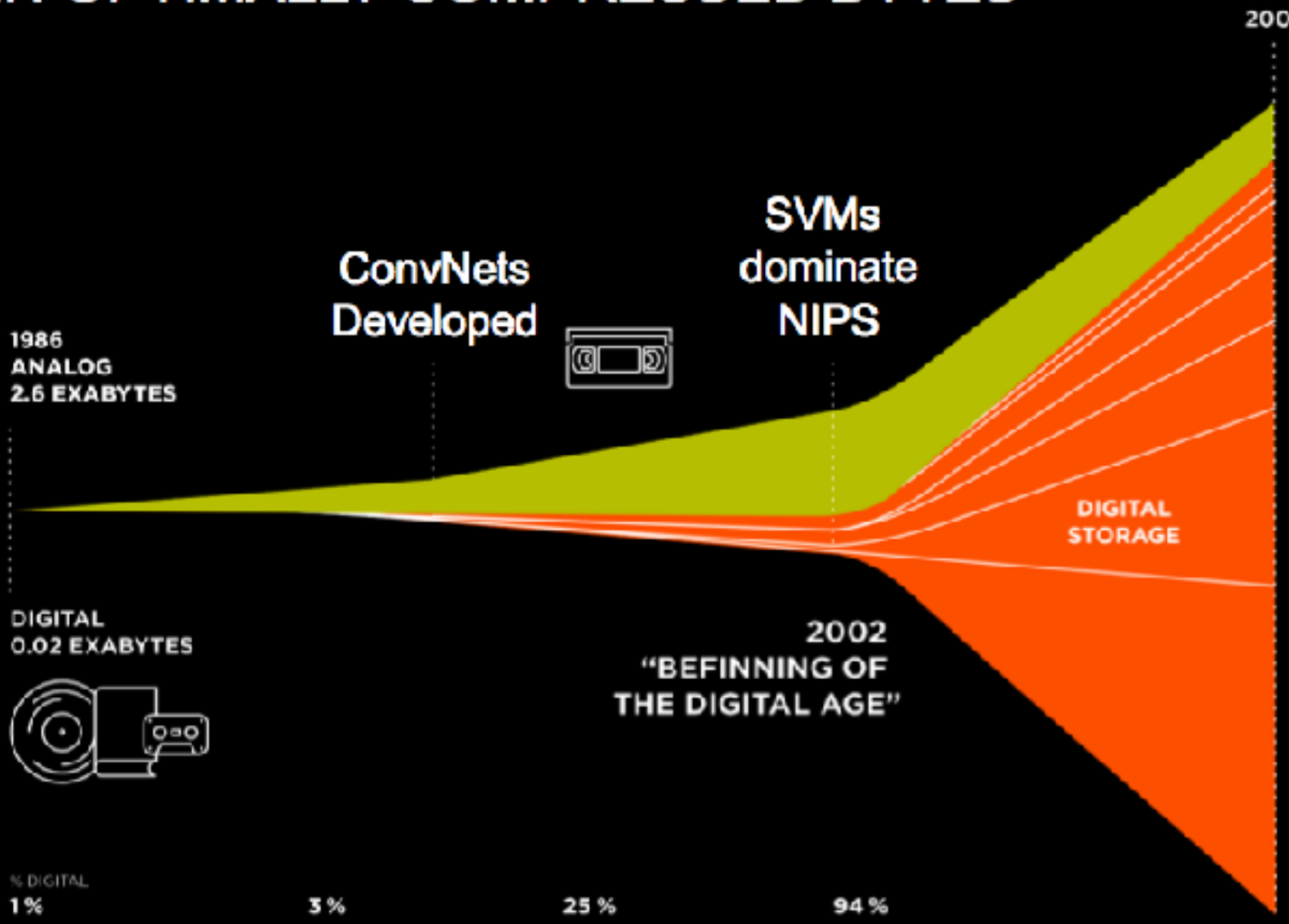
H. Y. Xiong et al., **"The human splicing code reveals new insights into the genetic determinants of disease"**, Science 347, 2015

M. Ramona et al., **"Capturing a Musician's Groove: Generation of Realistic Accompaniments from Single Song Recordings"**, In IJCAI 2015

And many more…

Why now?

GLOBAL INFORMATION STORAGE CAPACITY
IN OPTIMALLY COMPRESSED BYTES



Source: Hilbert, M., & López, P. (2011). The World's Technological Capacity to Store, Communicate, andCompute Information. Science, 332 (6025), 60-65. martinhilbert.net/worldinfocapacity.html

ANALOG
19 EXABYTES
- Paper, film, audiotape and vinyl: 6%
- Analog videotapes (VHS, etc): 94%

ANALOG

DIGITAL

- Portable media, flash drives: 2%
- Portable hard disks: 2.4%
- CDs & Minidisks: 6.8%
- Computer Servers and Mainframes: 8.9%
- Digital Tape: 11.8%
- DVD/Blu-Ray: 22.8%
- PC Hard Disks: 44.5%
  123 Billion Gigabytes
- Others: < 1% (incl. Chip Cards, Memory Cards, Floppy Disks, Mobile Phones, PDAs, Cameras/Camcorders, Video Games)

DIGITAL
280 EXABYTES

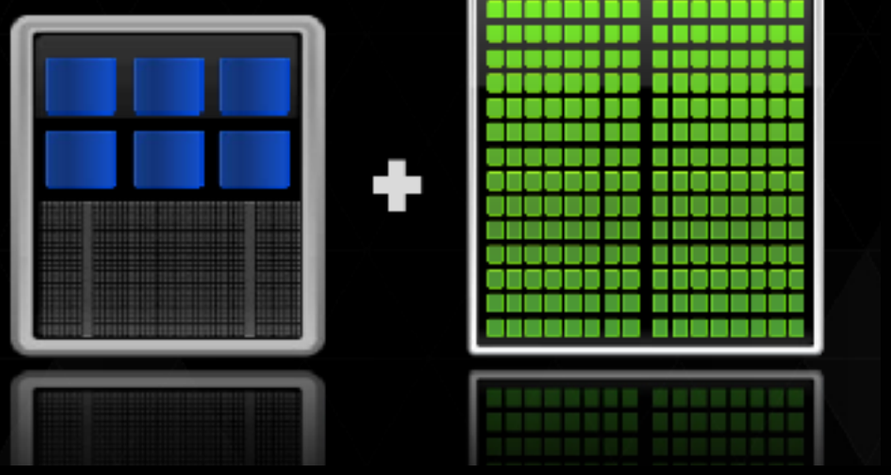
Slide credit: Neil Lawrence

Datasets vs. Algorithms

Year	Breakthroughs in AI	Datasets (First Available)	Algorithms (First Proposed)
1994	Human-level spontaneous speech recognition	Spoken Wall Street Journal articles and other texts (1991)	Hidden Markov Model (1984)
1997	IBM Deep Blue defeated Garry Kasparov	700,000 Grandmaster chess games, aka “The Extended Book” (1991)	Negascout planning algorithm (1983)
2005	Google’s Arabic-and Chinese-to-English translation	1.8 trillion tokens from Google Web and News pages (collected in 2005)	Statistical machine translation algorithm (1988)
2011	IBM Watson became the world Jeopardy! champion	8.6 million documents from Wikipedia, Wiktionary, and Project Gutenberg (updated in 2010)	Mixture-of-Experts (1991)
2014	Google’s GoogLeNet object classification at near-human performance	ImageNet corpus of 1.5 million labeled images and 1,000 object categories (2010)	Convolutional Neural Networks (1989)
2015	Google’s DeepMind achieved human parity in playing 29 Atari games by learning general control from video	Arcade Learning Environment dataset of over 50 Atari games (2013)	Q-learning (1992)
Average No. of Years to Breakthrough:		3 years	18 years

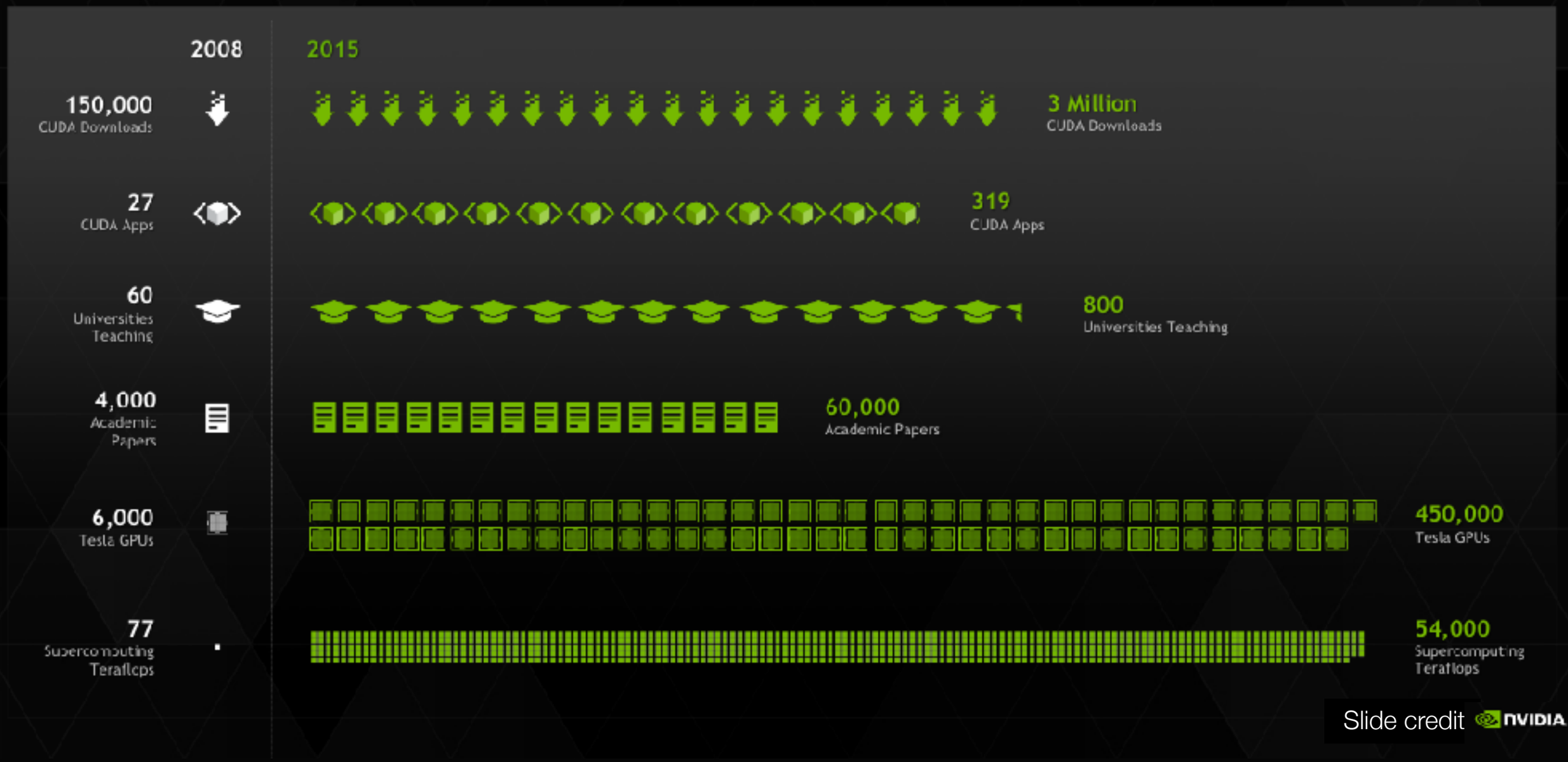
Table credit: Quant Quanto

Powerful Hardware



Slide credit NVIDIA

10X GROWTH IN GPU COMPUTING



Slide credit NVIDIA

Working ideas on how to train deep architectures

Dropout: A Simple Way to Prevent Neural Networks from Overfitting

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Geoffrey Hinton HINTON@CS.TORONTO.EDU
Alex Krizhevsky KRIZ@CS.TORONTO.EDU
Ilya Sutskever ILYA@CS.TORONTO.EDU
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Abstract

Deep neural nets with a large number of parameters are very powerful machine learning systems. However, overfitting is a serious problem in such networks. Large networks are also slow to use, making it difficult to deal with overfitting by combining the predictions of many different large neural nets at test time. Dropout is a technique for addressing this problem. The key idea is to randomly drop units (along with their connections) from the neural network during training. This prevents units from co-adapting too much. During training, dropout samples from an exponential number of different "thinned" networks. At test time,

- Better Learning Regularization (e.g. **Dropout**)

N. Srivastava, G. Hinton, A. Krizhevsky, I. Sutskever, R. Salakhutdinov, **"Dropout: A Simple Way to Prevent Neural Networks from Overfitting"**,
JMLR Vol. 15, No. 1,

Working ideas on how to train deep architectures

Batch Normalization: Accelerating Deep Network Training by Reducing Internal Covariate Shift

Sergey Ioffe
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Christian Szegedy
Google Inc., *szegedy@google.com*

Abstract

Training Deep Neural Networks is complicated by the fact that the distribution of each layer's inputs changes during training, as the parameters of the previous layers change. This slows down the training by requiring lower learning rates and careful parameter initialization, and makes it notoriously hard to train models with saturating nonlinearities. We refer to this phenomenon as *internal covariate shift*, and address the problem by normalizing layer inputs. Our method draws its strength from making normalization a part of the model architecture and performing the normalization *for each training mini-batch*. Batch Normalization allows us to use much higher learning rates and be less careful about initialization. It also acts as a regularizer, in some cases eliminating the need for Dropout. Applied to a state-of-the-art image classification model, Batch Normalization achieves the same accuracy with 14 times fewer training steps, and beats the original model by a significant margin. Using an ensemble of batch-normalized networks, we improve upon the best published result on ImageNet classification: reaching 4.9% top-5 validation error (and 4.8% test error), exceeding the accuracy of human raters.

Using mini-batches of examples, as opposed to one example at a time, is helpful in several ways. First, the gradient of the loss over a mini-batch is an estimate of the gradient over the training set, whose quality improves as the batch size increases. Second, computation over a batch can be much more efficient than m computations for individual examples, due to the parallelism afforded by the modern computing platforms.

While stochastic gradient is simple and effective, it requires careful tuning of the model hyper-parameters, specifically the learning rate used in optimization, as well as the initial values for the model parameters. The training is complicated by the fact that the inputs to each layer


Batch Normalization: Accelerating Deep Network Training by Reducing Internal Covariate Shift

Sergey Ioffe — Google Inc., sioffe@google.com
Christian Szegedy — Google Inc., szegedy@google.com

Abstract

1 Introduction

- Better Optimization Conditioning (e.g. **Batch Normalization**)

S. Ioffe, C. Szegedy, **"Batch Normalization: Accelerating Deep Network Training by Reducing Internal Covariate Shift"**, In ICML 2015

Working ideas on how to train deep architectures

Deep Residual Learning for Image Recognition

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{kahe, v-xiangz, v-shren, jiansun} @microsoft.com

Abstract

Deeper neural networks are more difficult to train. We present a residual learning framework to ease the training of networks that are substantially deeper than those used previously. We explicitly reformulate the layers as learning residual functions with reference to the layer inputs, instead of learning unreferenced functions. We provide comprehensive empirical evidence showing that these residual networks are easier to optimize, and can gain accuracy from considerably increased depth. On the ImageNet dataset we evaluate residual nets with a depth of up to 152 layers—8× deeper than VGG nets [41] but still having lower complexity. An ensemble of these residual nets achieves 3.57% error

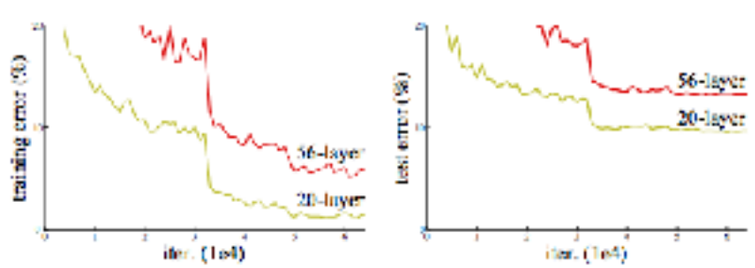
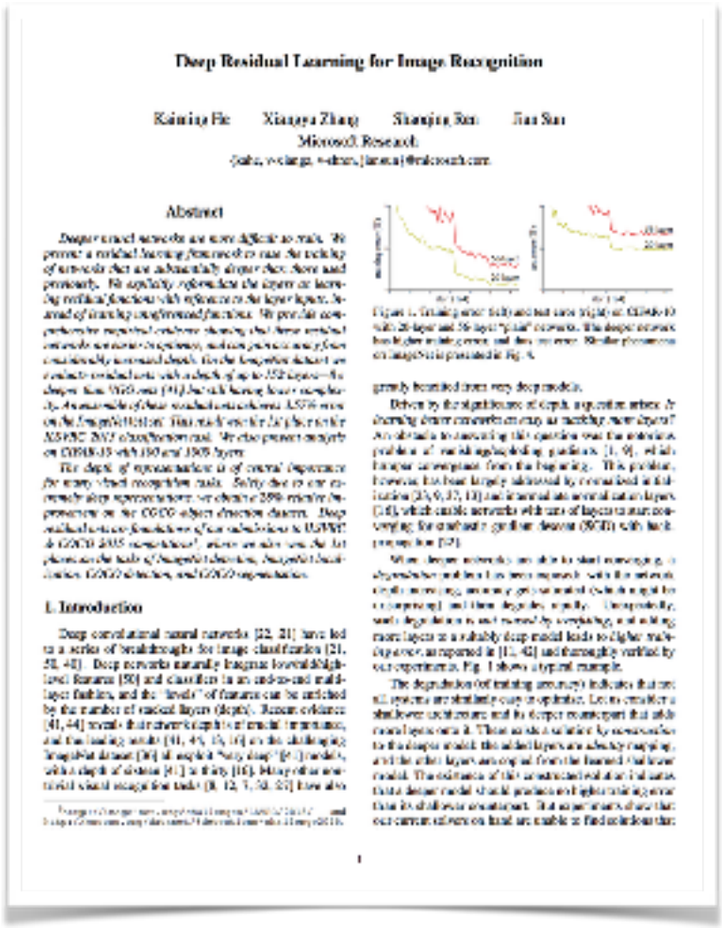


Figure 1. Training error (left) and test error (right) on CIFAR-10 with 20-layer and 56-layer "plain" networks. The deeper network has higher training error, and thus test error. Similar phenomena on ImageNet is presented in Fig. 4.

greatly benefited from very deep models.

Driven by the significance of depth, a question arises: *Is*

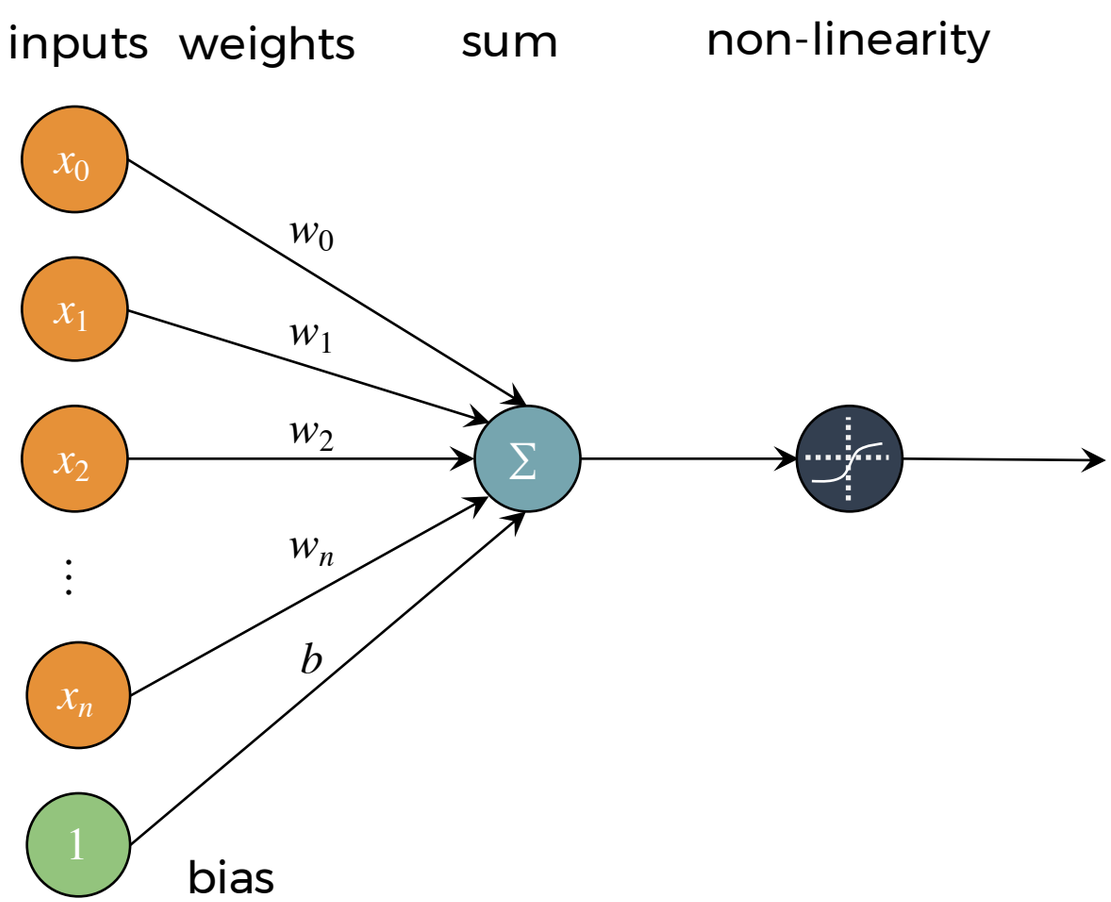


- Better neural achitectures (e.g. **Residual Nets**)

K. He, X. Zhang, S. Ren, J. Sun, **"Deep Residual Learning for Image Recognition"**, In CVPR 2016

Let’s make a review of neural networks

The Perceptron



Perceptron Forward Pass

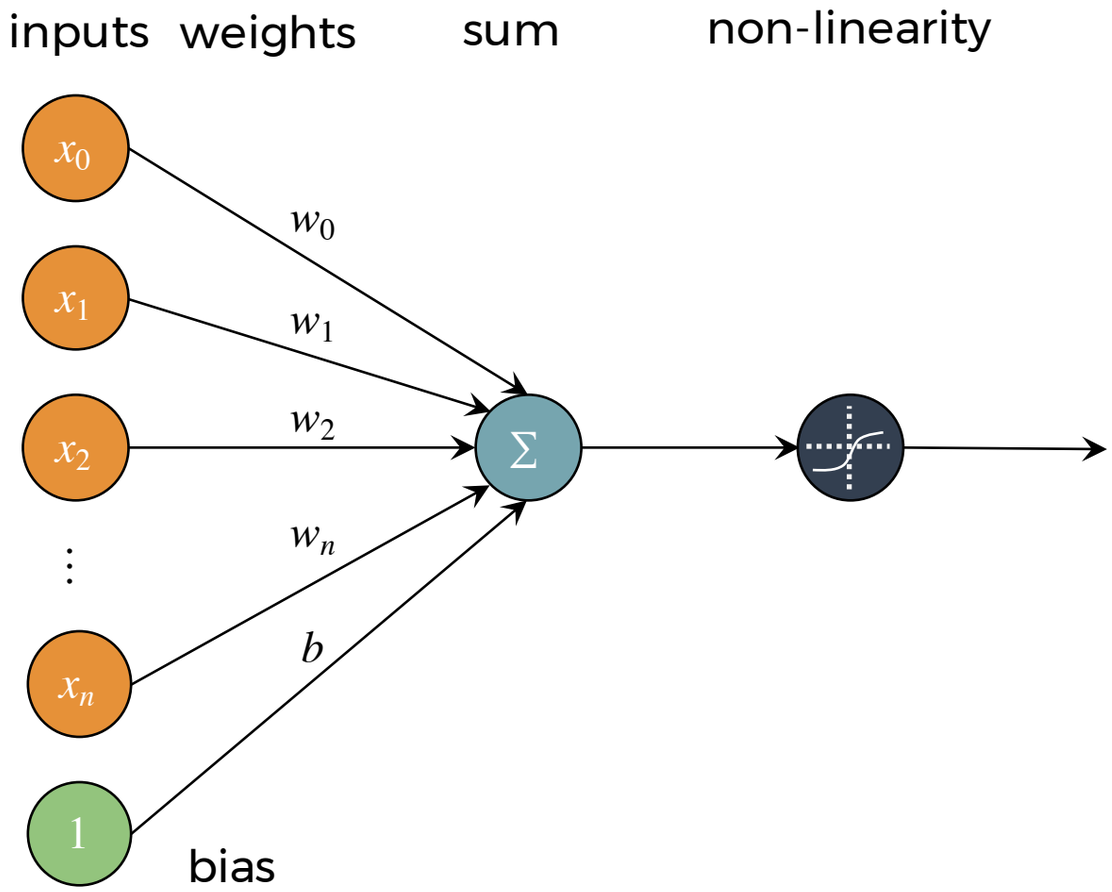
- Neuron pre-activation (or input activation)

$$a(\mathbf{x}) = b + \sum_i w_i x_i = b + \mathbf{w}^\top \mathbf{x}$$

- Neuron output activation:

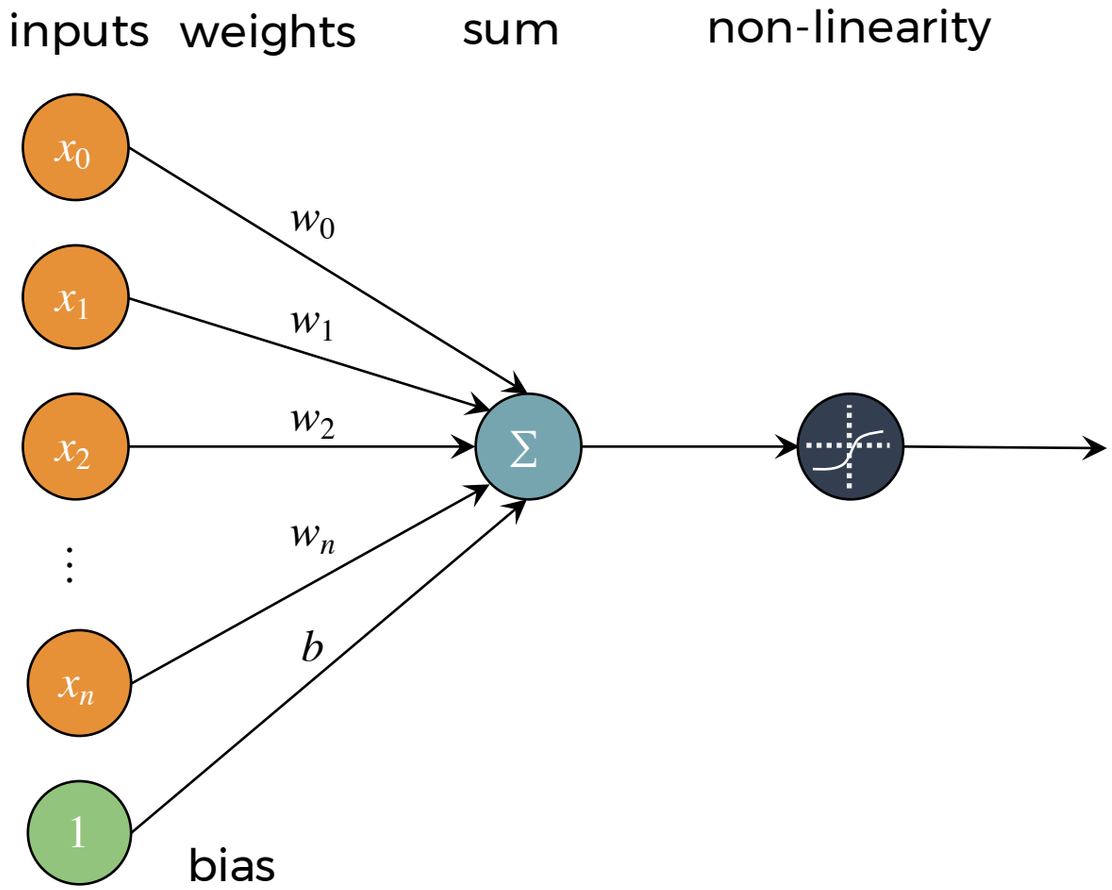
$$h(\mathbf{x}) = g(a(\mathbf{x})) = g(b + \sum_i w_i x_i)$$

where
w are the weights (parameters)
b is the bias term
g(·) is called the activation function



Output Activation of The Neuron

$$h(\mathbf{x}) = g(a(\mathbf{x})) = g(b + \sum_i w_i x_i)$$



Range is determined by $g(\cdot)$

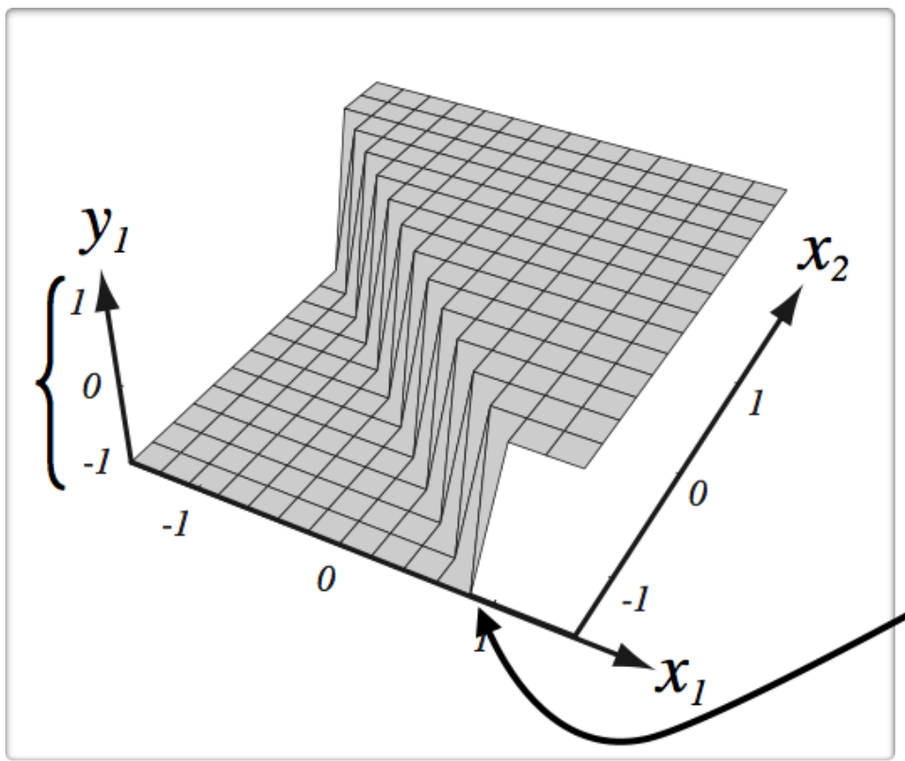


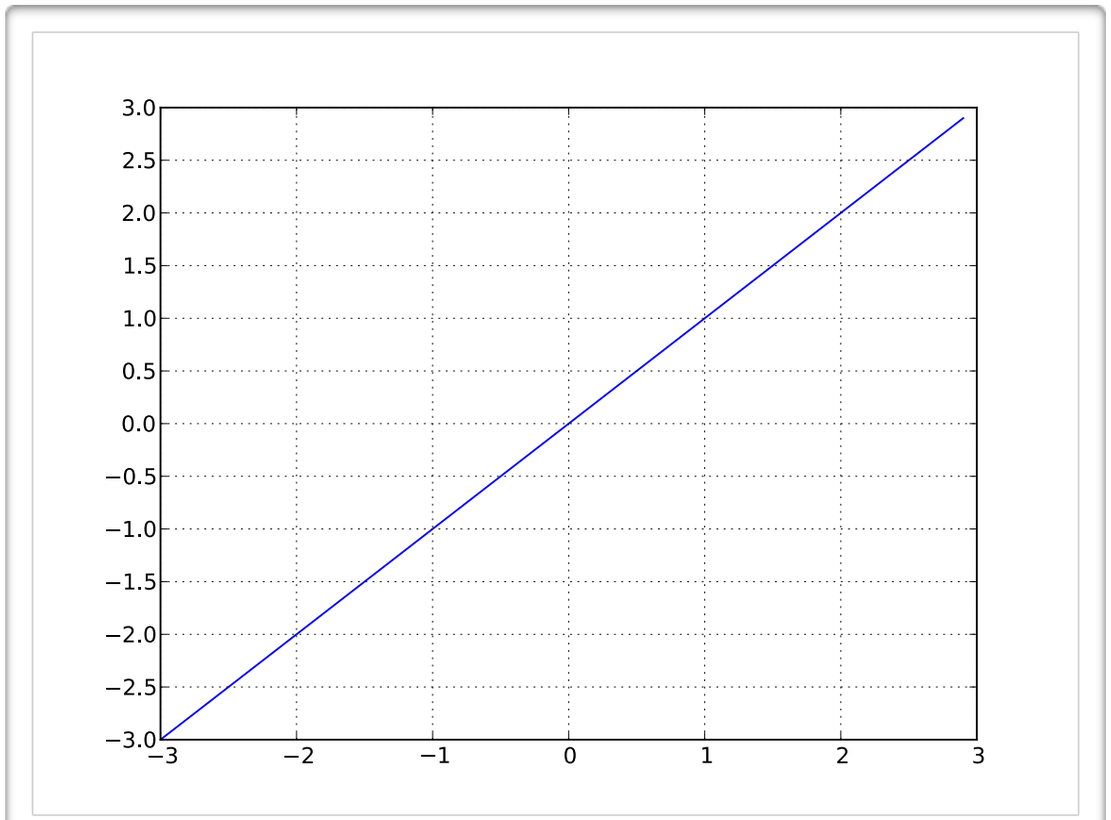
Image credit: Pascal Vincent

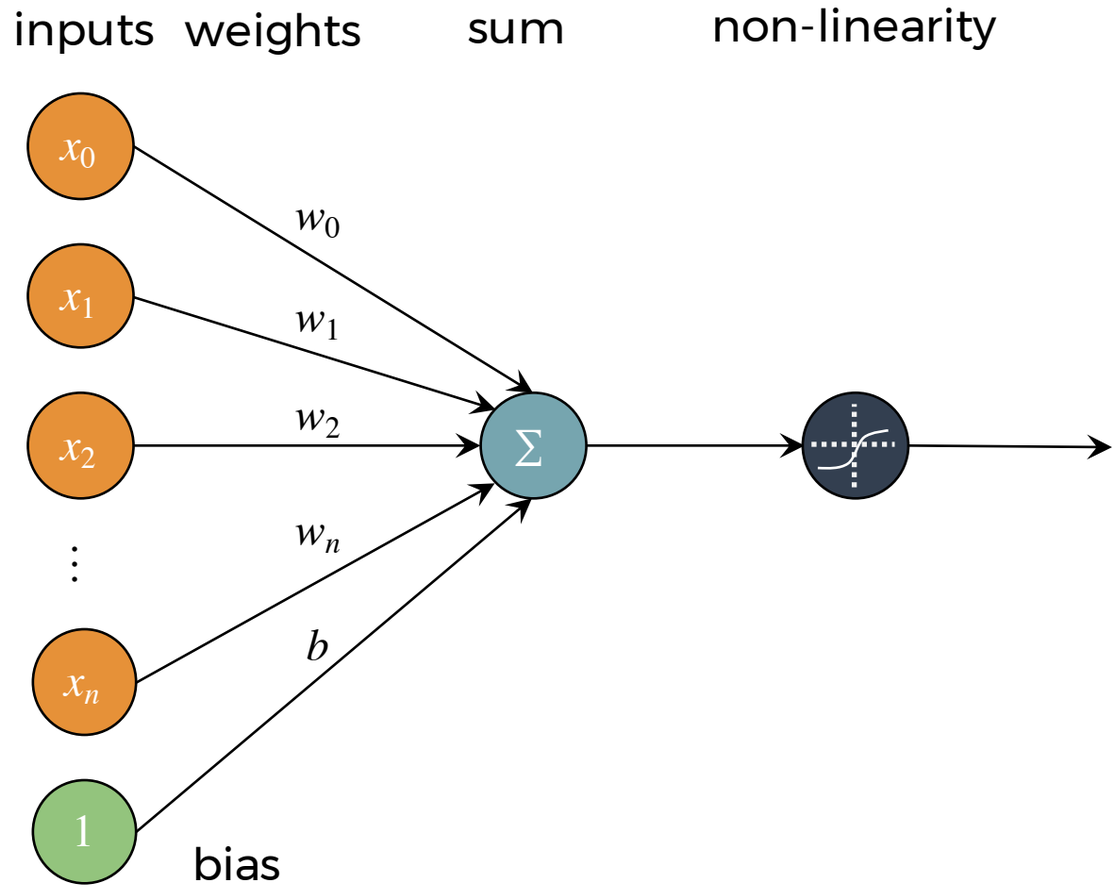
Bias only changes the position of the riff

Linear Activation Function

$$h(\mathbf{x}) = g(a(\mathbf{x})) = g(b + \sum_i w_i x_i)$$

$$g(a) = a$$



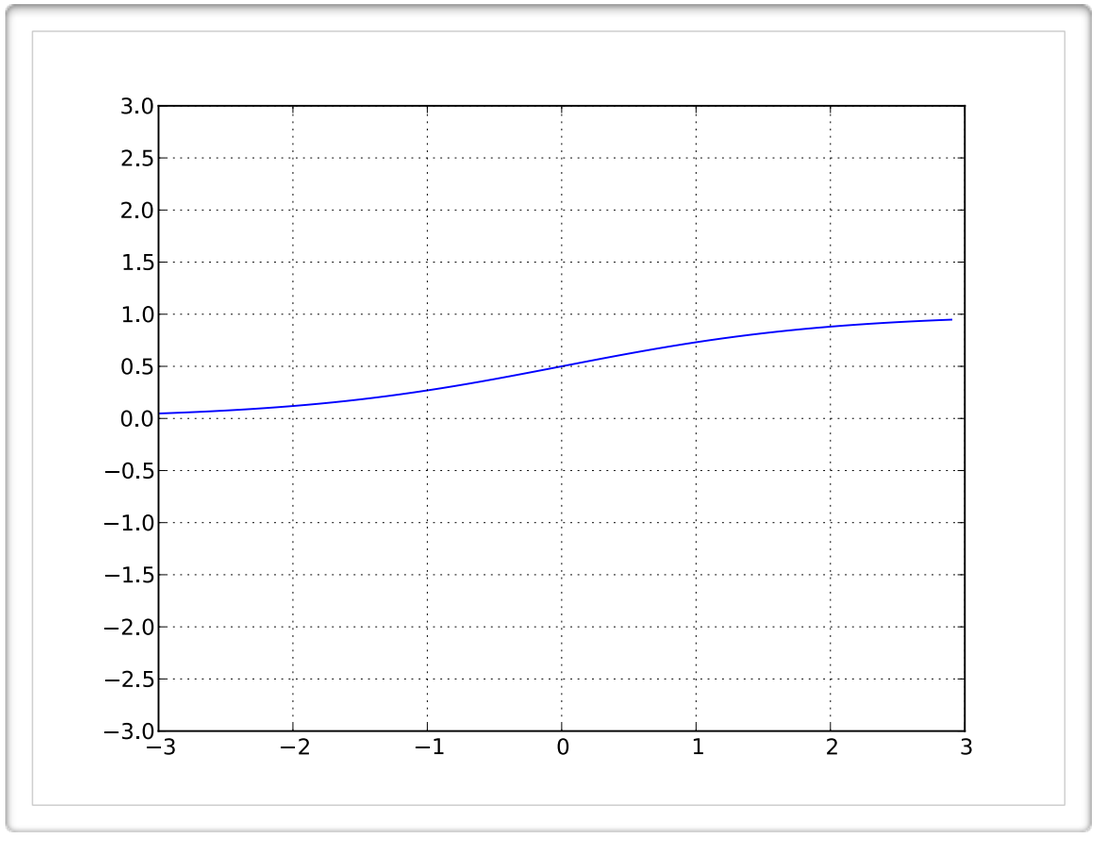


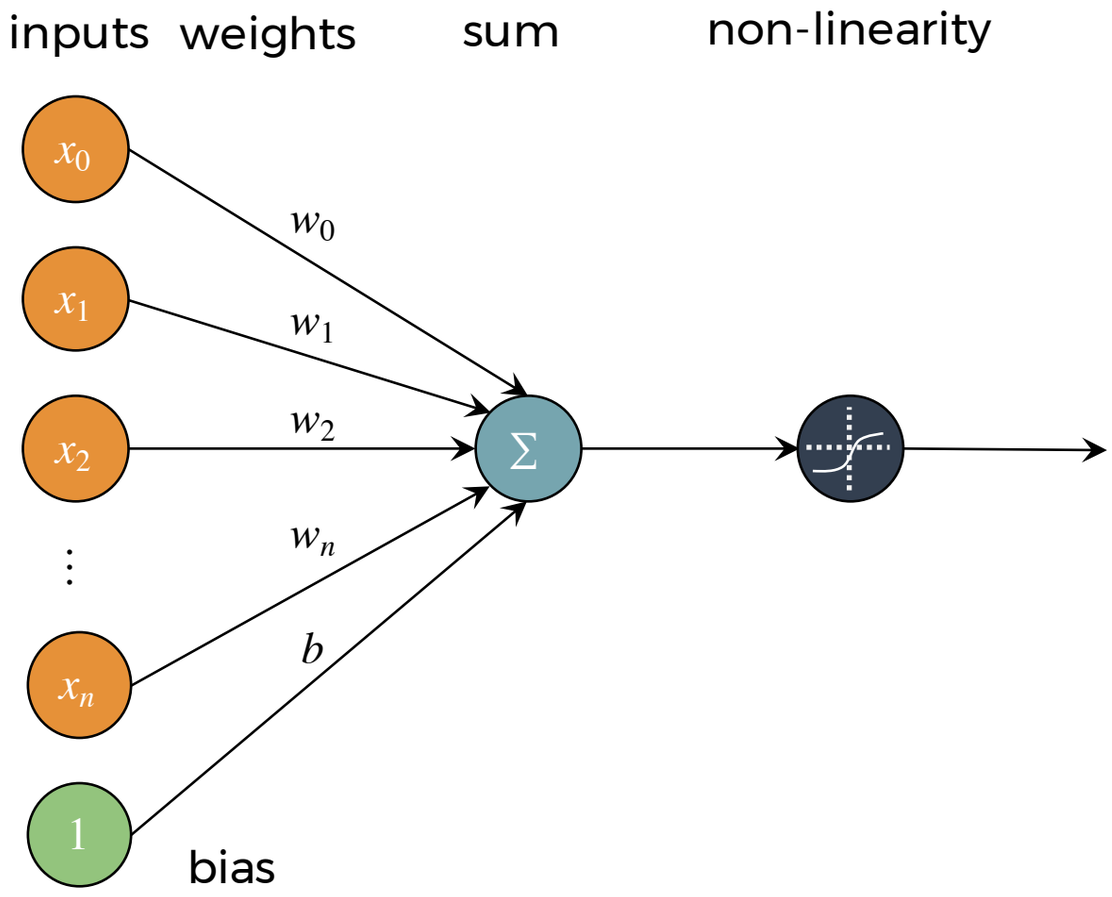
No nonlinear transformation
No input squashing

Sigmoid Activation Function

$$h(\mathbf{x}) = g(a(\mathbf{x})) = g(b + \sum_i w_i x_i)$$

$$g(a) = \text{sigm}(a) = \frac{1}{1+\exp(-a)}$$





Squashes the neuron's output between 0 and 1

Always positive

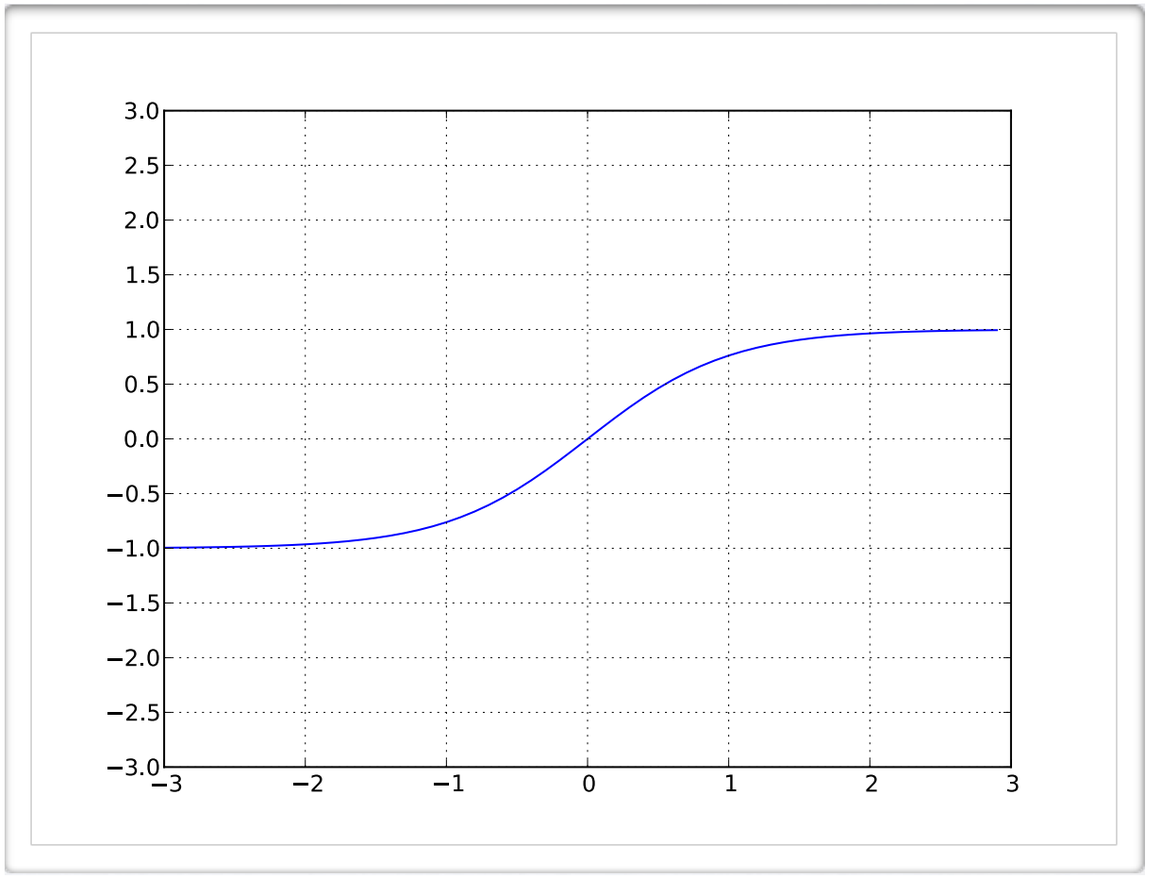
Bounded

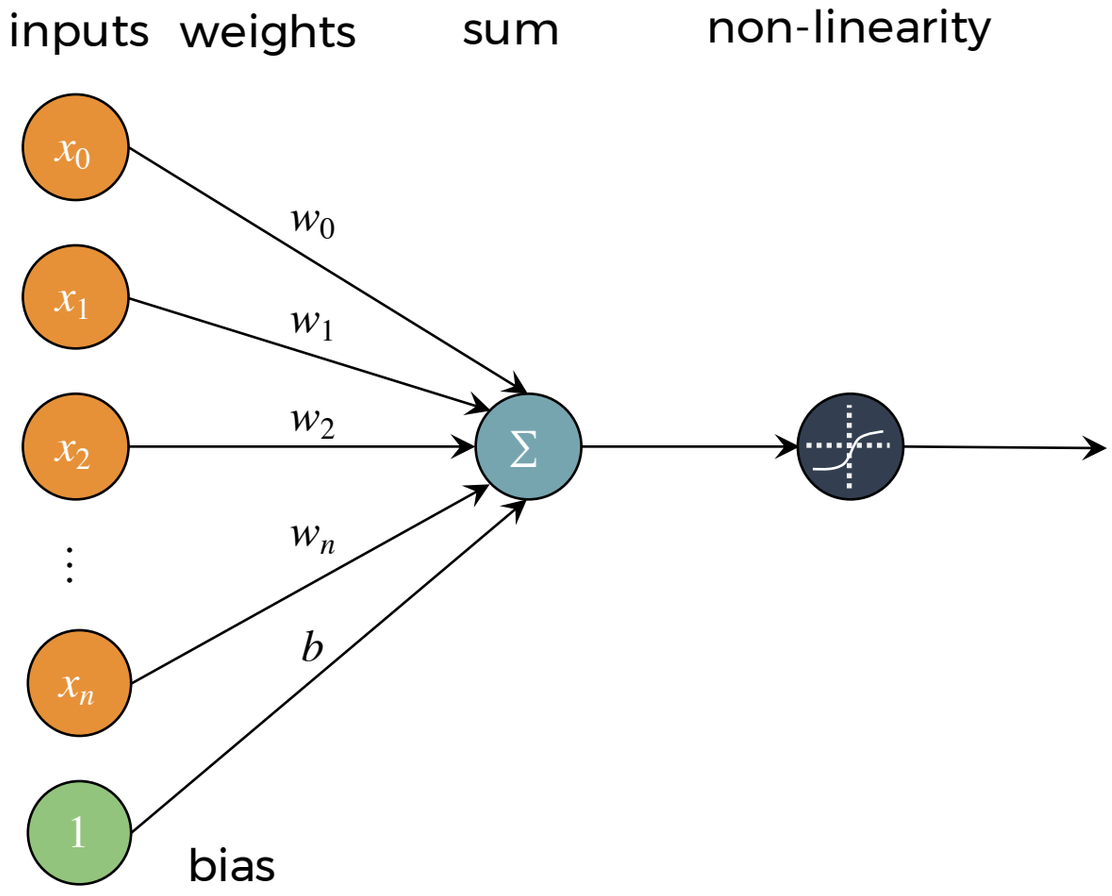
Strictly Increasing

Hyperbolic Tangent (tanh) Activation Function

$$h(\mathbf{x}) = g(a(\mathbf{x})) = g(b + \sum_i w_i x_i)$$

$$g(a) = \tanh(a) = \frac{\exp(a) - \exp(-a)}{\exp(a) + \exp(-a)} = \frac{\exp(2a) - 1}{\exp(2a) + 1}$$





Squashes the neuron's output between -1 and 1

Can be positive or negative

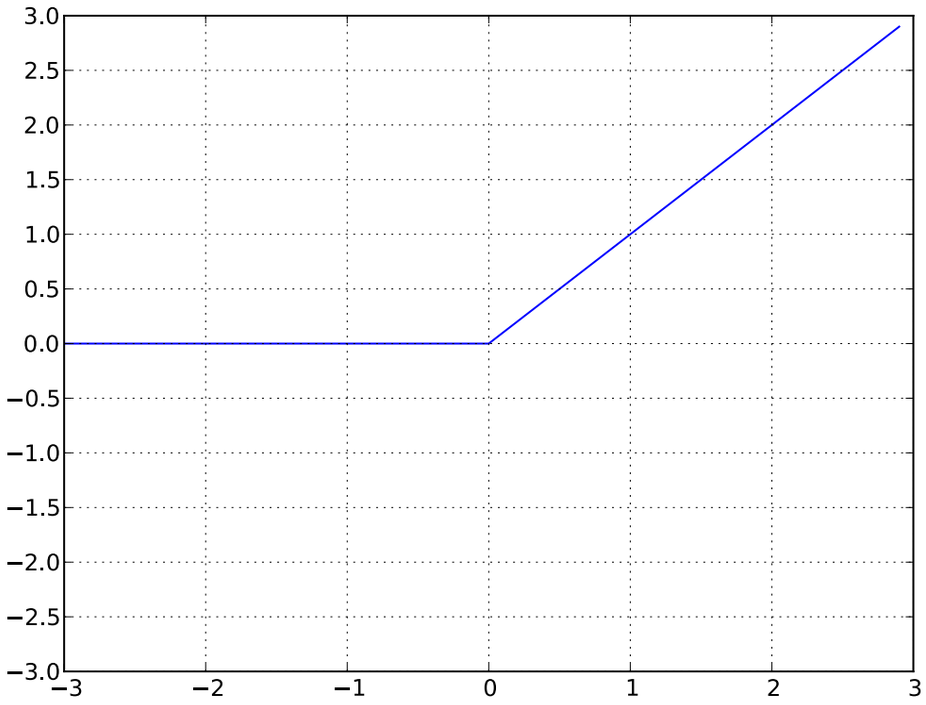
Bounded

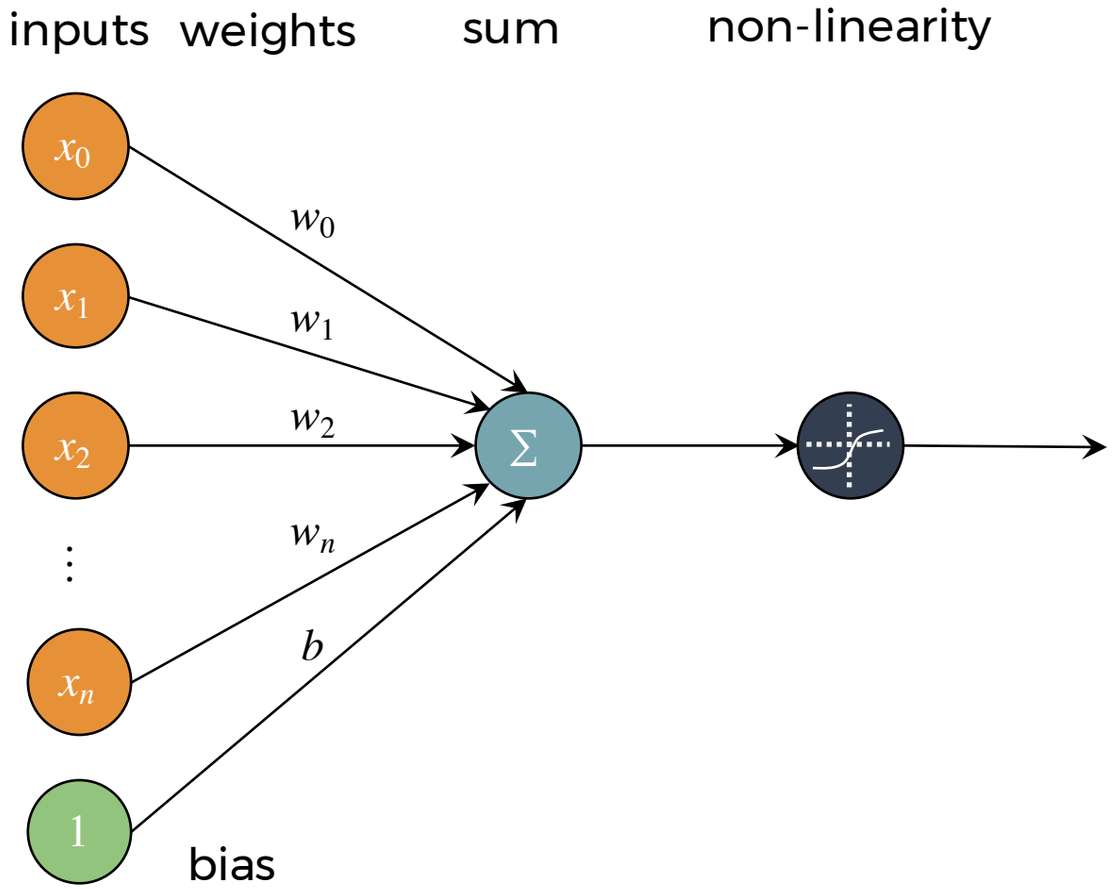
Strictly Increasing

Rectified Linear (ReLU) Activation Function

$$h(\mathbf{x}) = g(a(\mathbf{x})) = g(b + \sum_i w_i x_i)$$

$$g(a) = \text{reclin}(a) = \max(0, a)$$

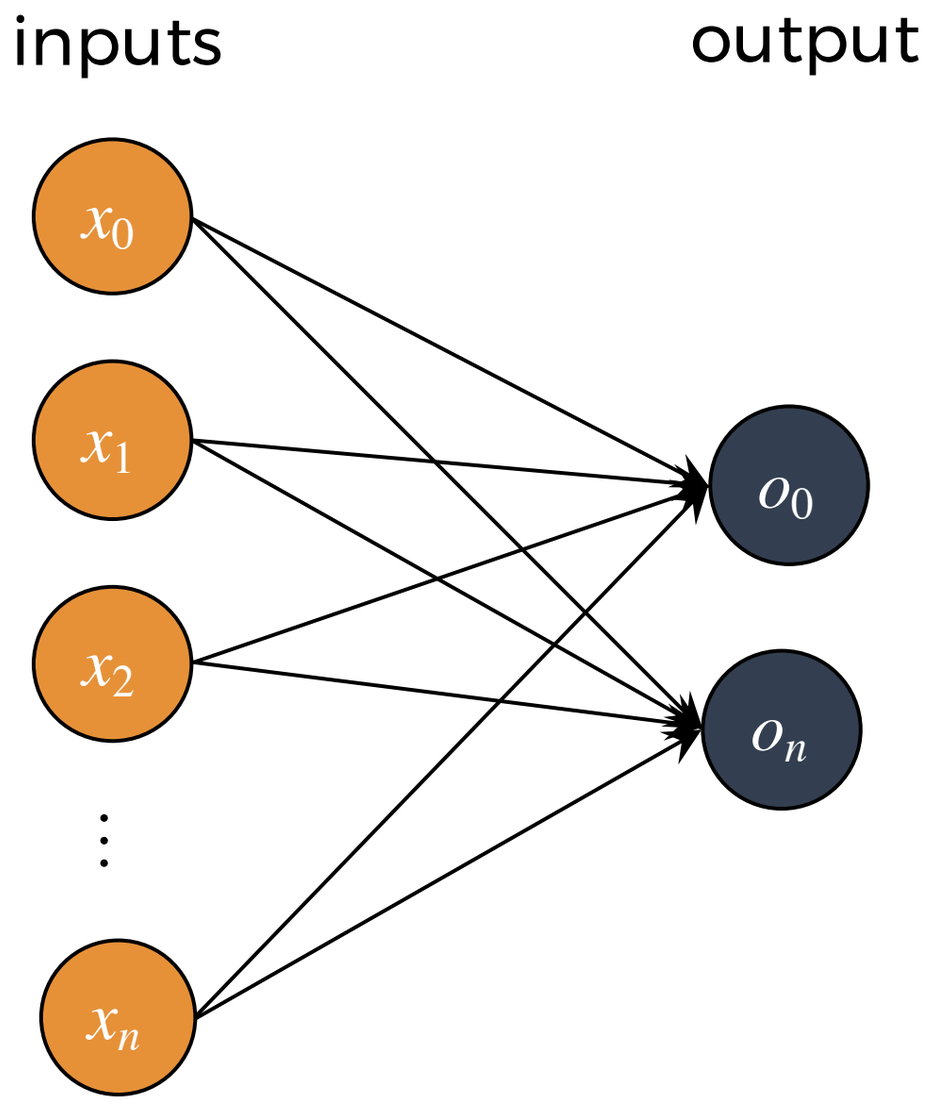




Bounded below by 0 (always non-negative)
Not upper bounded
Strictly increasing
Tends to produce units with sparse activities

Multi-Output Perceptron

- We need multiple outputs
  (1 output per class)i j
- We need to estimate conditional probability
  p(y = c|x)
- Discriminative Learning



- Softmax activation function at the output

$$\mathbf{o}(\mathbf{a}) = \text{softmax}(\mathbf{a}) = \left[\frac{\exp(a_1)}{\sum_c \exp(a_c)} \cdots \frac{\exp(a_C)}{\sum_c \exp(a_c)} \right]^\top$$

  - Strictly positive
  - sums to one
- Predict class with the highest estimated
  class conditional probability.

Single Hidden Layer Neural Network

- Hidden layer pre-activation:

$$\mathbf{a}(\mathbf{x}) = \mathbf{b}^{(1)} + \mathbf{W}^{(1)}\mathbf{x}$$

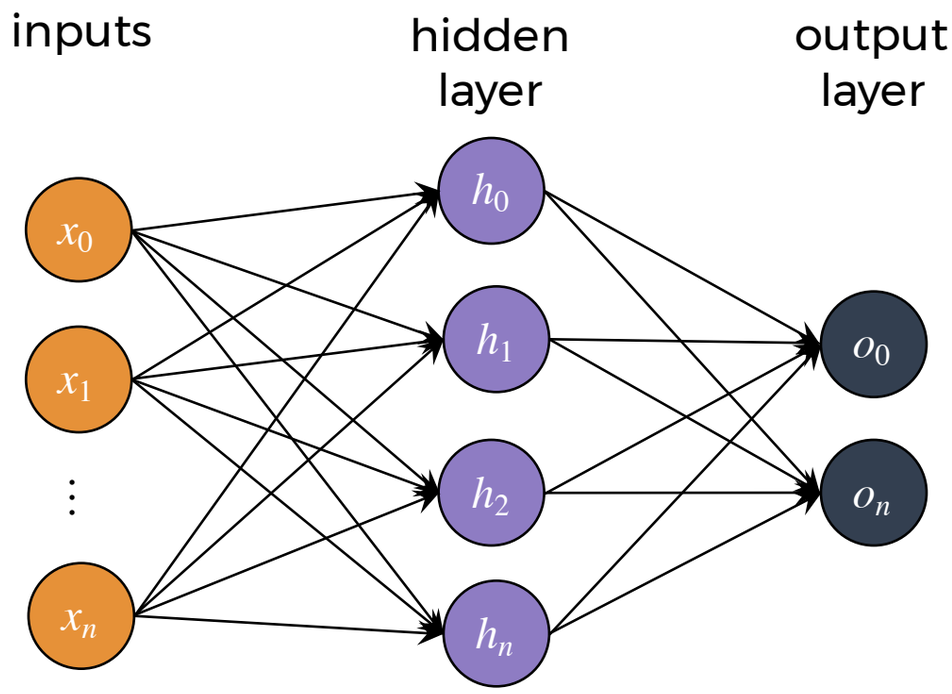
$$\left(a(\mathbf{x})_i = b_i^{(1)} + \sum_j W_{i,j}^{(1)} x_j\right)$$

- Hidden layer activation:

$$\mathbf{h}(\mathbf{x}) = \mathbf{g}(\mathbf{a}(\mathbf{x}))$$

- Output layer activation:

$$\mathbf{o}(\mathbf{x}) = \mathbf{o}\left(b^{(2)} + \mathbf{w}^{(2)}\mathbf{h}^{(1)}\mathbf{x}\right)$$



Multi-Layer Perceptron (MLP)

Consider a network with L hidden layers.

- layer pre-activation for k>0

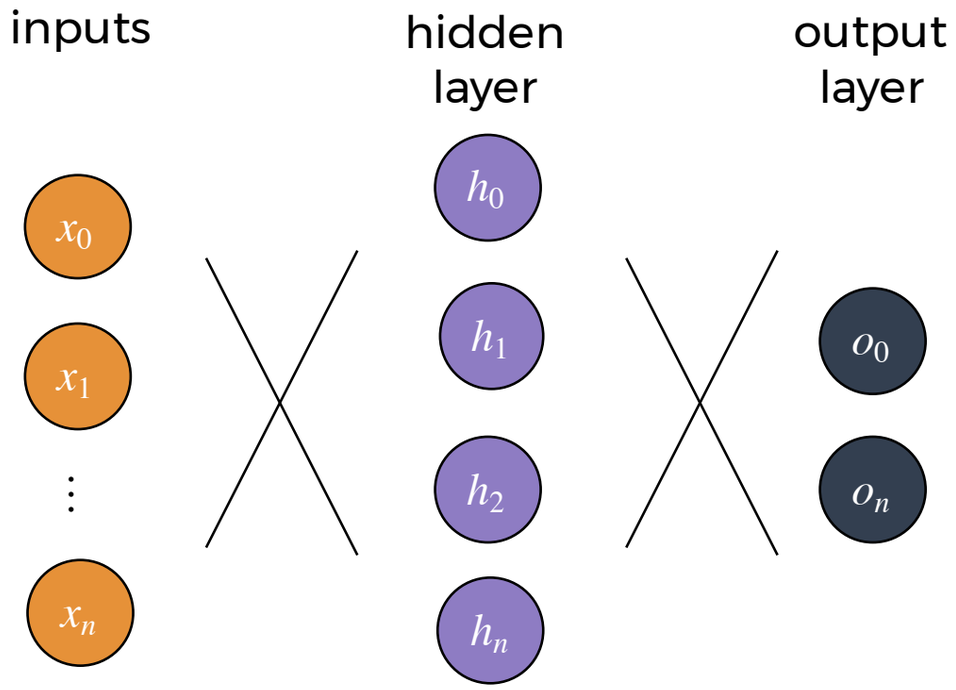
$$\mathbf{a}^{(k)}(\mathbf{x}) = \mathbf{b}^{(k)} + \mathbf{W}^{(k)}\mathbf{h}^{(k-1)}(\mathbf{x})$$

- hidden layer activation from 1 to L:

$$\mathbf{h}^{(k)}(\mathbf{x}) = \mathbf{g}(\mathbf{a}^{(k)}(\mathbf{x}))$$

- output layer activation (k=L+1)

$$\mathbf{h}^{(L+1)}(\mathbf{x}) = \mathbf{o}(\mathbf{a}^{(L+1)}(\mathbf{x})) = \mathbf{f}(\mathbf{x})$$



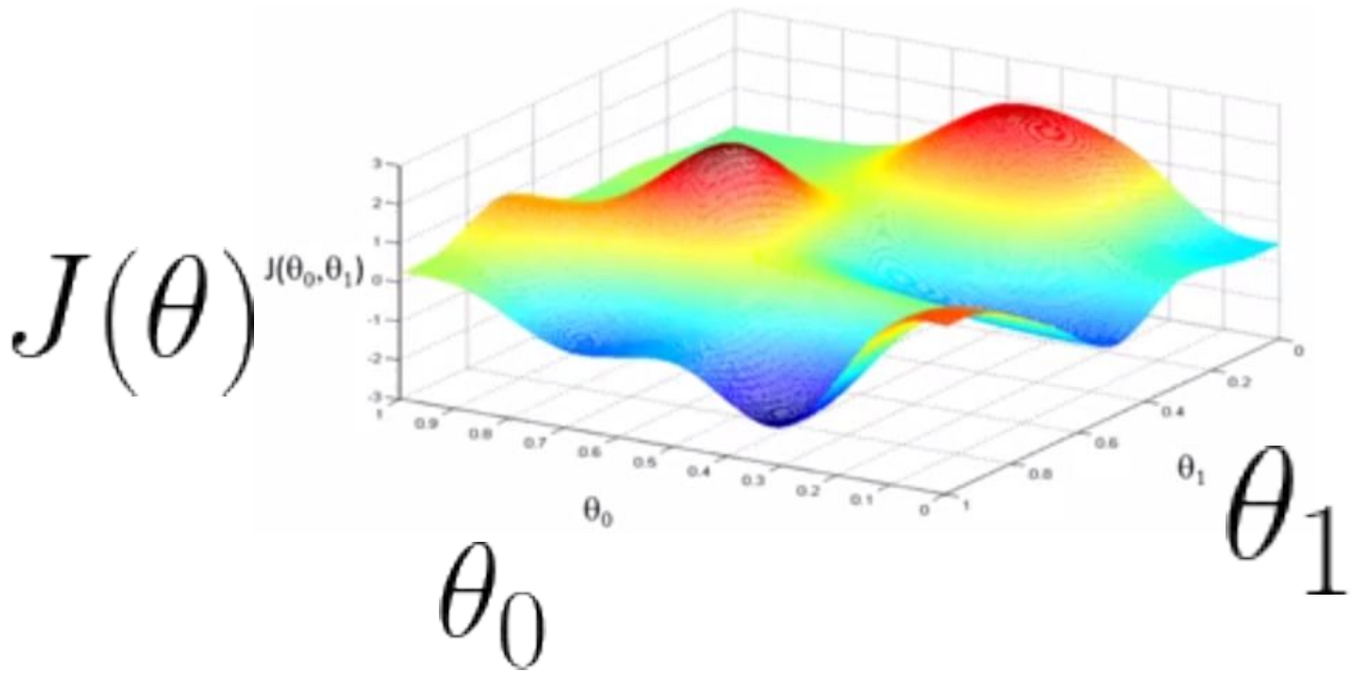
Training

$$J(\theta) = \arg\min_{\boldsymbol{\theta}} \frac{1}{T} \sum_t \underbrace{l(f(\mathbf{x}^{(t)}; \boldsymbol{\theta}), y^{(t)})}_{\text{Loss function}} + \underbrace{\lambda \Omega(\boldsymbol{\theta})}_{\text{Regularizer}}$$

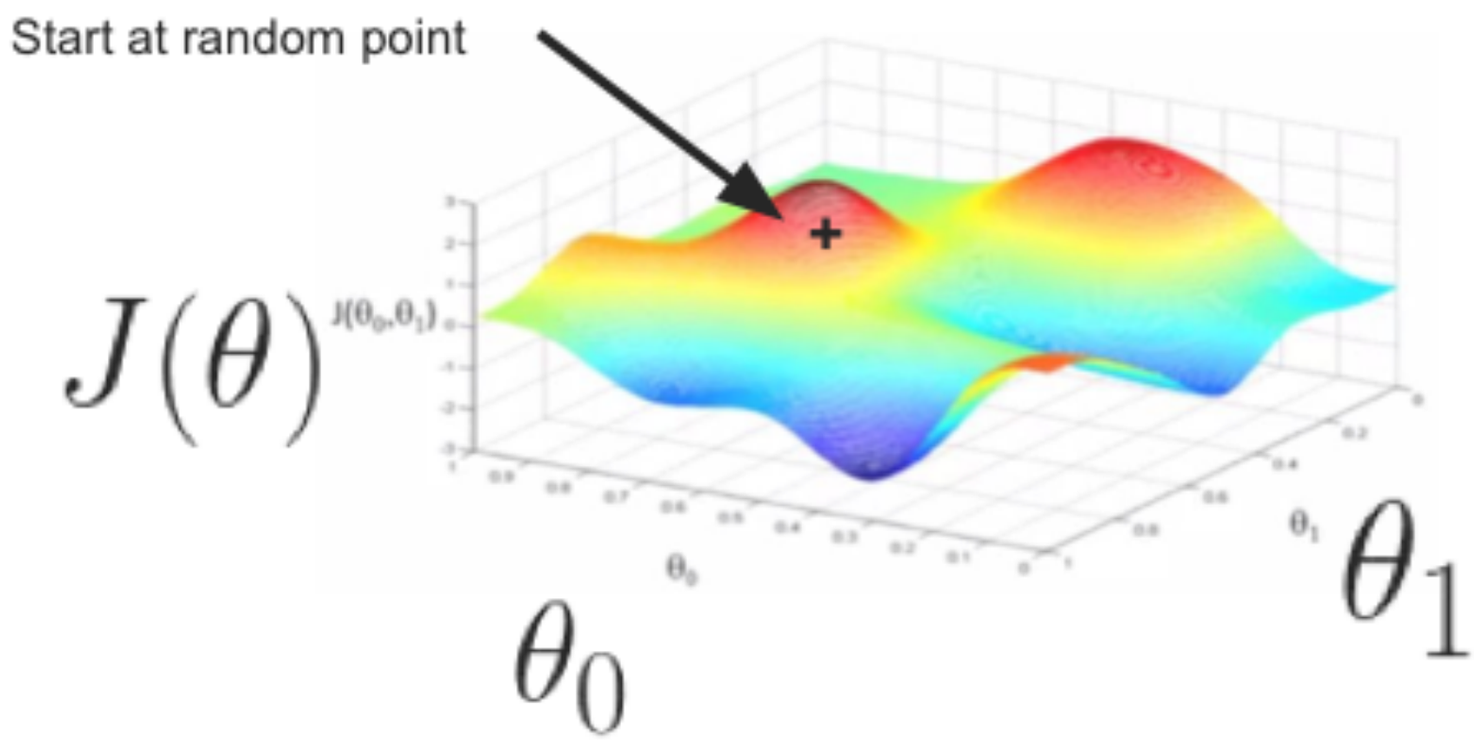
$$\theta = W_1, W_2 ... W_n$$

- Learning is cast as optimization.
- For classification problems, we would like to minimize classification error
- Loss function can sometimes be viewed as a surrogate for what we want to optimize (e.g. upper bound)

Loss is a **function** of the model's parameters

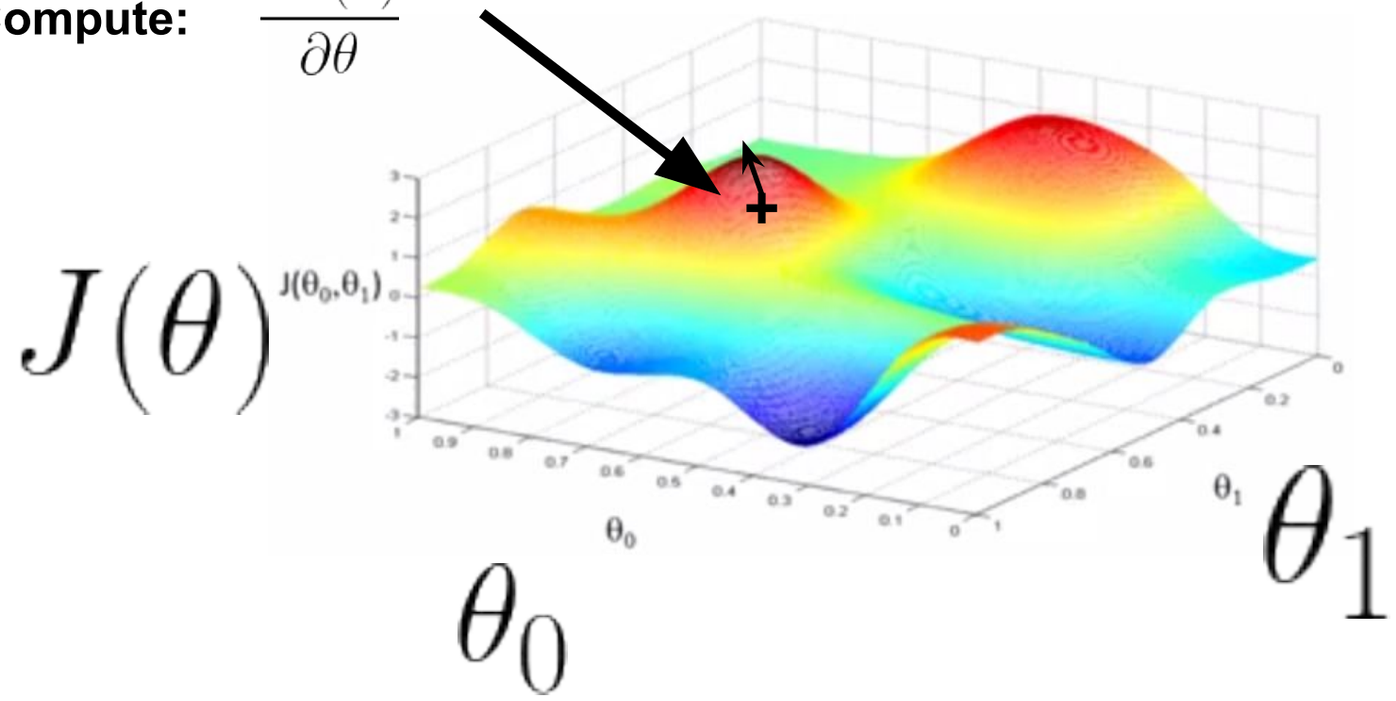


How to minimize loss?



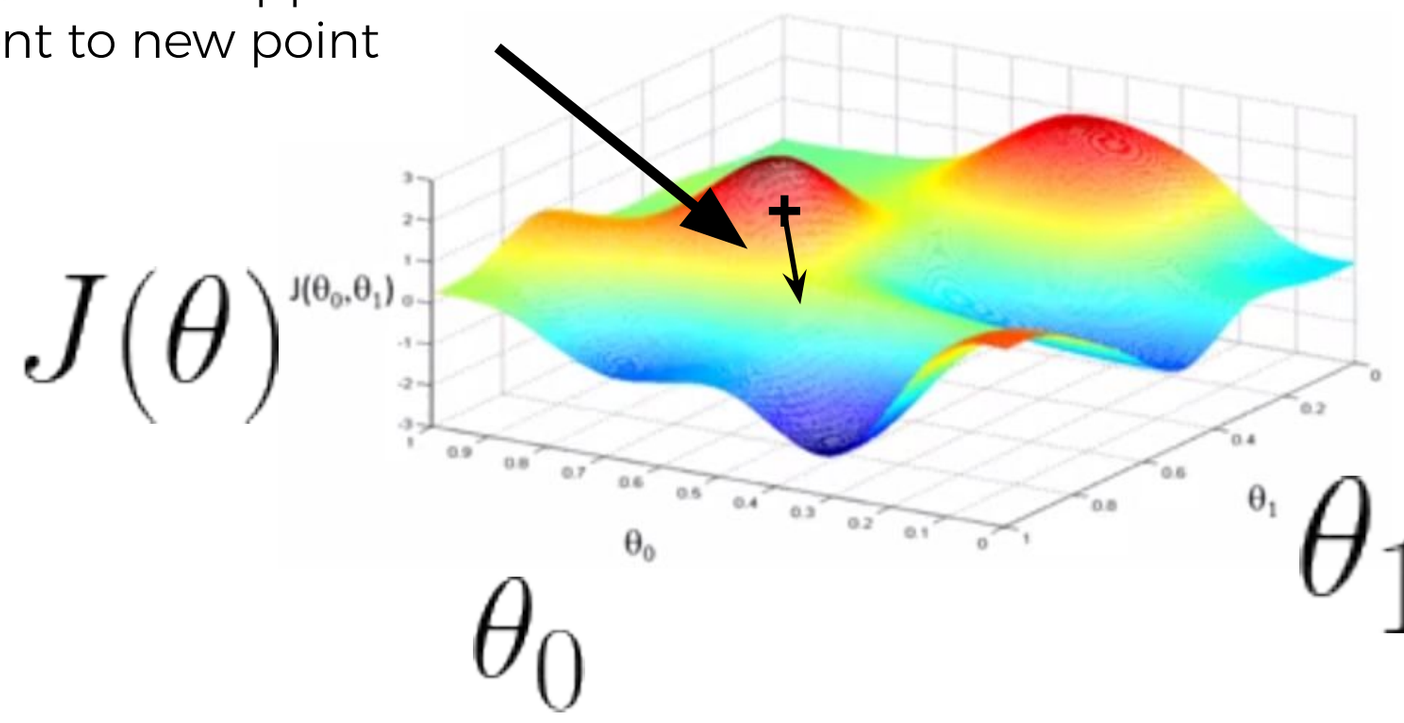
How to minimize loss?

Compute: $\frac{\partial J(\theta)}{\partial \theta}$



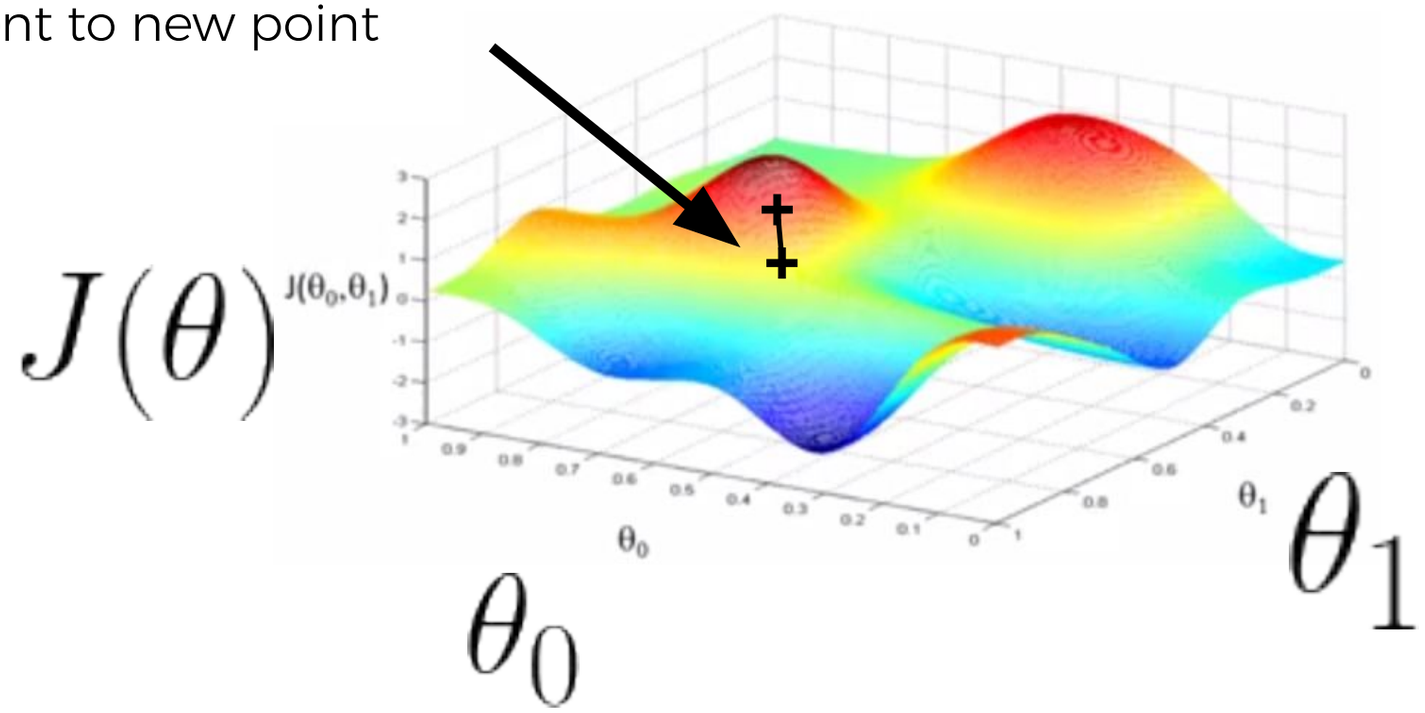
How to minimize loss?

Move in direction opposite of gradient to new point



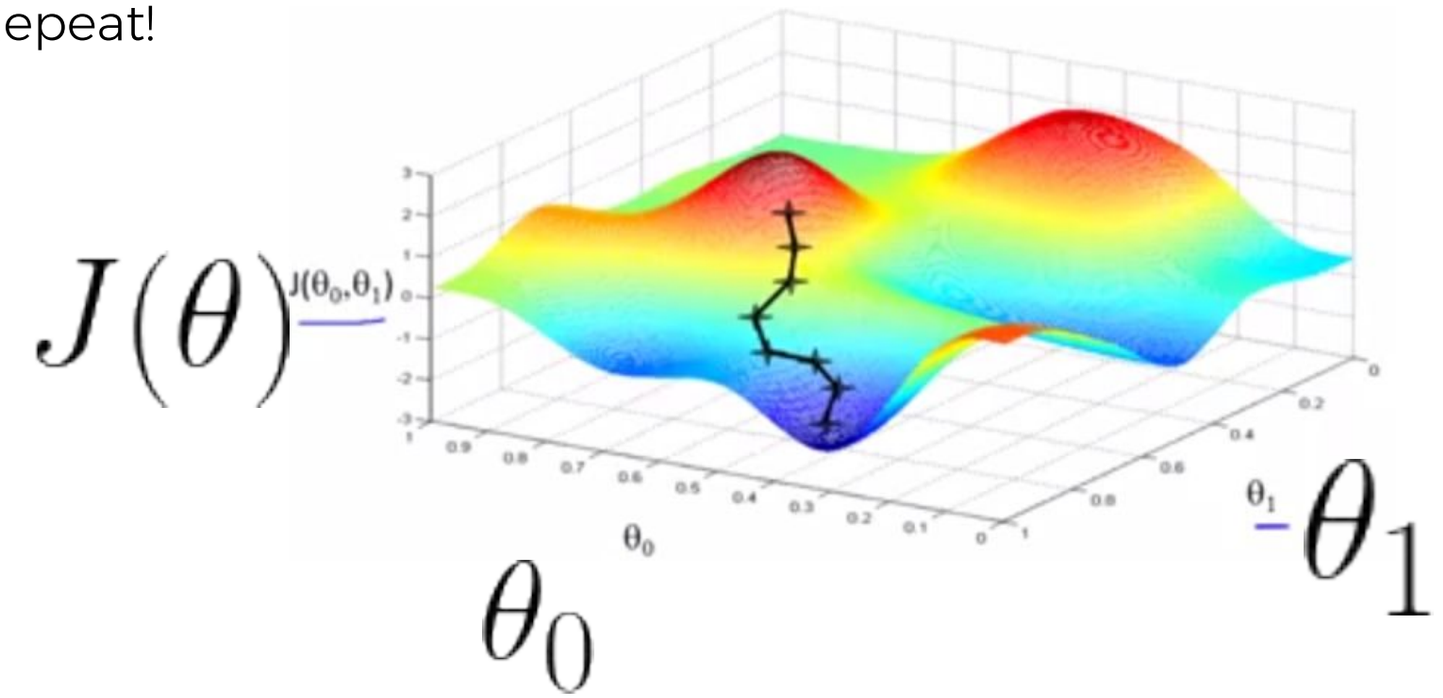
How to minimize loss?

Move in direction opposite of gradient to new point



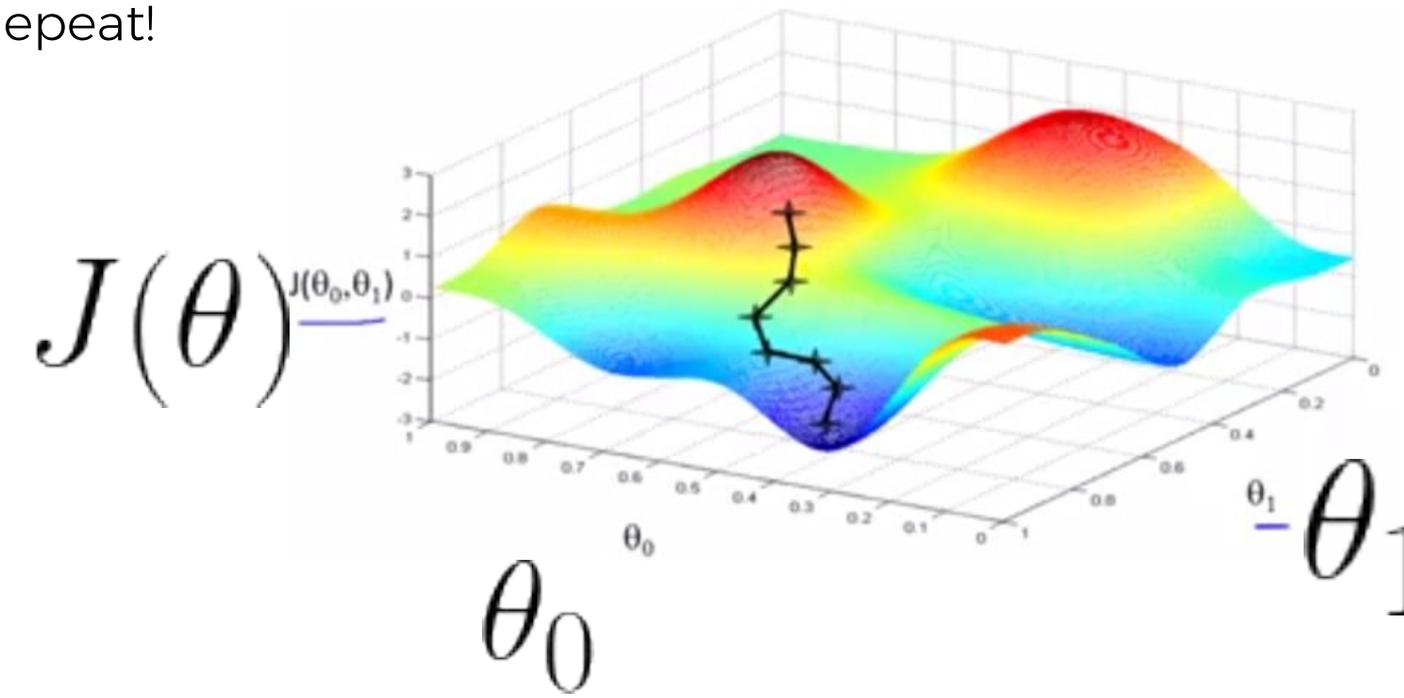
How to minimize loss?

Repeat!



This is called
Stochastic Gradient Descent (SGD)

Repeat!



Stochastic Gradient Descent (SGD)

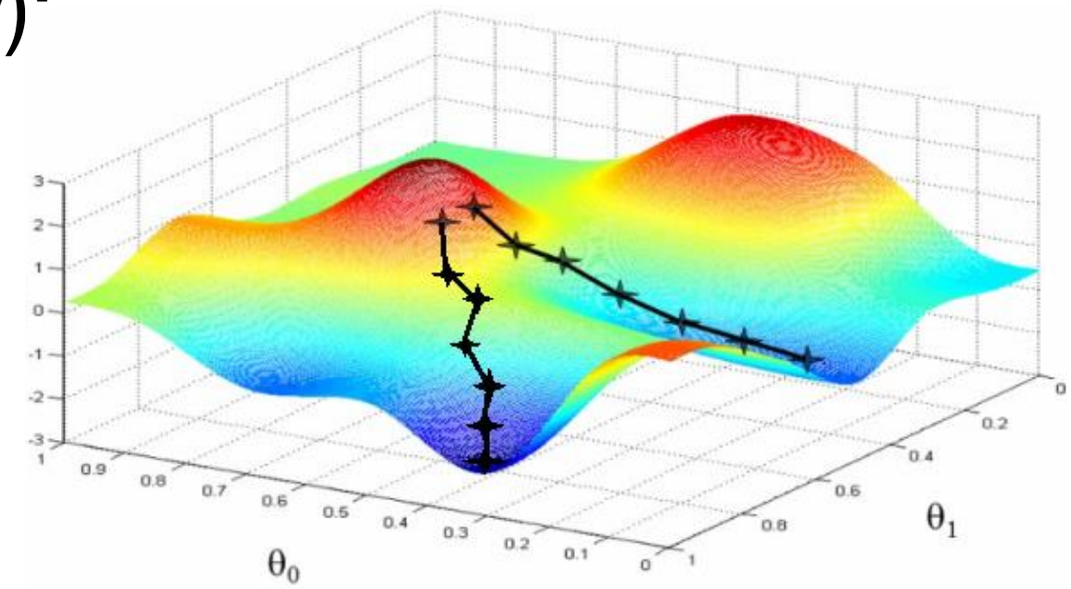
- Initialize θ randomly
- For N Epochs
- For each training example (x, y):

- Compute Loss Gradient:

$$\frac{\partial J(\theta)}{\partial \theta}$$

- Update θ with update rule:

$$\theta := \theta - \eta \frac{\partial J(\theta)}{\partial \theta}$$



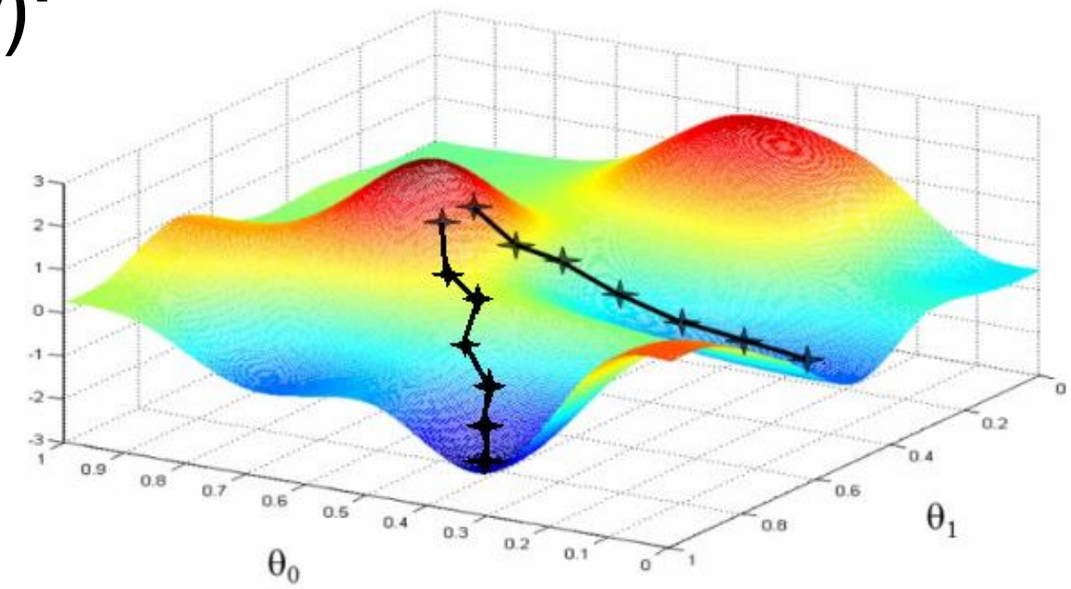
Why is it **Stochastic** Gradient Descent?

- Initialize θ randomly
- For N Epochs
- For each training example (x, y):

- Compute Loss Gradient:

$$\frac{\partial J(\theta)}{\partial \theta}$$

Only an estimate of true gradient!



- Update θ with update rule:

$$\theta := \theta - \eta \frac{\partial J(\theta)}{\partial \theta}$$

Advantages:

- More accurate estimation of gradient
  - Smoother convergence
  - Allows for larger learning rates
- Minibatches lead to fast training!
  - Can parallelize computation + achieve significant speed increases on GPU's

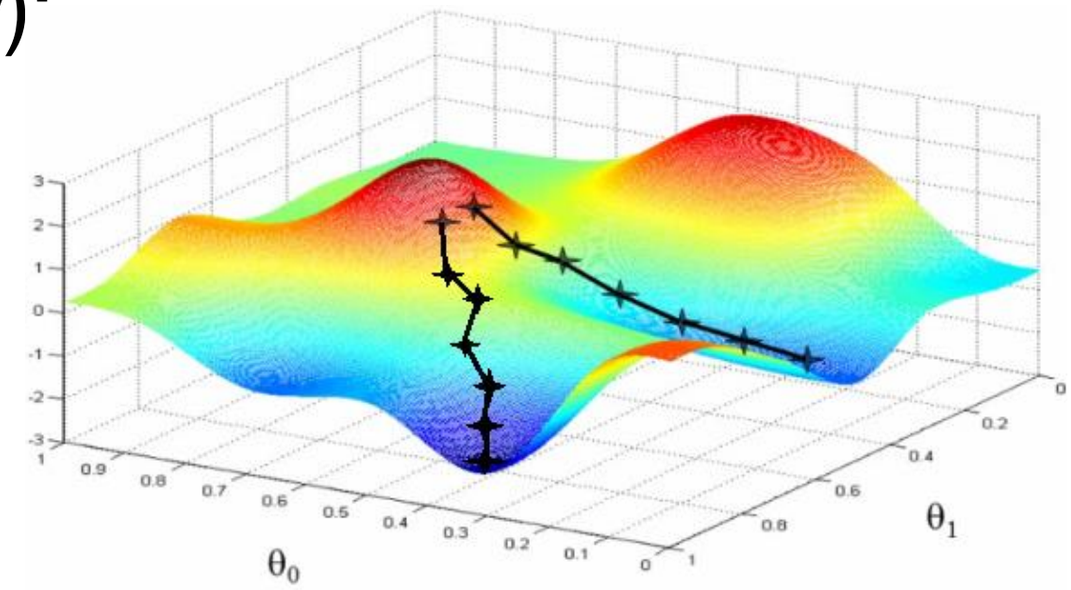
Why is it **Stochastic** Gradient Descent?

- Initialize θ randomly
- For N Epochs
- For each training example (x, y):

- Compute Loss Gradient:

$$\frac{\partial J(\theta)}{\partial \theta} = \frac{1}{B}\sum_{i}^{B}\frac{\partial J_i(\theta)}{\partial \theta}$$

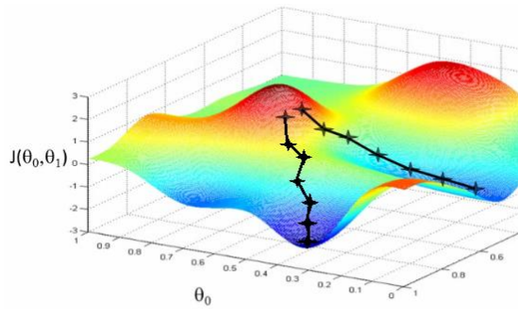
More accurate estimate!



- Update θ with update rule:

$$\theta := \theta - \eta\frac{\partial J(\theta)}{\partial \theta}$$

Stochastic Gradient Descent (SGD)



- Algorithm that performs updates after each example
  - initialize $\boldsymbol{\theta} \equiv \{\mathbf{W}^{(1)}, \mathbf{b}^{(1)}, \ldots, \mathbf{W}^{(L+1)}, \mathbf{b}^{(L+1)}\}$
  - for N iterations
    - for each training example $(\mathbf{x}^{(t)}, y^{(t)})$ or batch

$$\Delta = -\nabla_{\boldsymbol{\theta}} l(f(\mathbf{x}^{(t)}; \boldsymbol{\theta}), y^{(t)}) - \lambda \nabla_{\boldsymbol{\theta}} \Omega(\boldsymbol{\theta})$$

$$\boldsymbol{\theta} \leftarrow \boldsymbol{\theta} + \alpha \, \Delta$$

Training epoch
=
Iteration over **all** examples

- To apply this algorithm to neural network training, we need:
  - the loss function $l(\mathbf{f}(\mathbf{x}^{(t)}; \boldsymbol{\theta}), y^{(t)})$
  - a procedure to compute the parameter gradients: $\nabla_{\boldsymbol{\theta}} l(\mathbf{f}(\mathbf{x}^{(t)}; \boldsymbol{\theta}), y^{(t)})$
  - the regularizer $\Omega(\boldsymbol{\theta})$ (and the gradient $\nabla_{\boldsymbol{\theta}} \Omega(\boldsymbol{\theta})$)

What is a neural network again?

- A family of parametric, non-linear and hierarchical representation learning functions

- $a_L(x; \theta_{1,\ldots,L}) = h_L(h_{L-1}(\ldots h_1(x, \theta_1), \theta_{L-1}), \theta_L)$
- x: input, θl: parameters for layer l, al = hl(x, θl): (non-)linear function

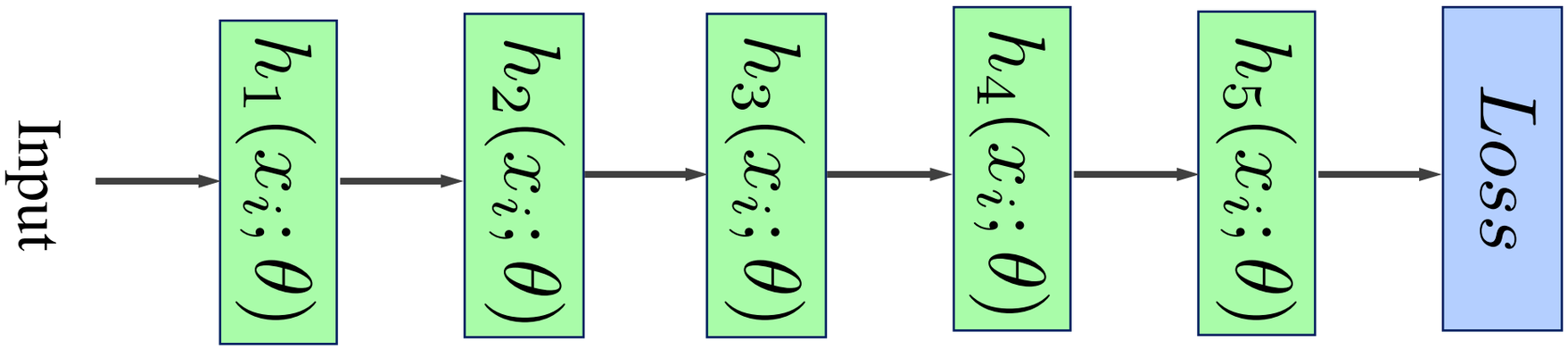
- Given training corpus {X, Y} find optimal parameters

$$\theta^* \leftarrow \arg\min_{\theta} \sum_{(x,y)\in(X,Y)} \ell(y, a_L(x; \theta_{1,\ldots,L}))$$

Neural network models

- A neural network model is a series of hierarchically connected functions
- The hierarchy can be very, very complex

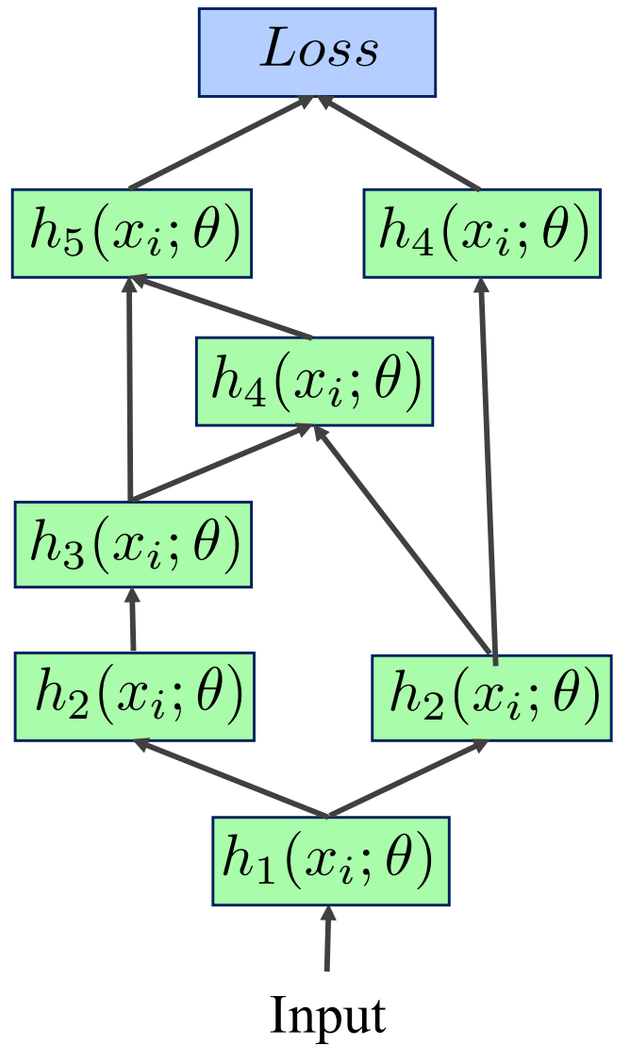
Forward connections (Feedforward architecture)



Neural network models

- A neural network model is a series of hierarchically connected functions
- The hierarchy can be very, very complex

Interweaved connections (Directed Acyclic Graph architecture – DAGNN)



Again, what is a neural network again?

- $a_L(x; \theta_{1,\ldots,L}) = h_L(h_{L-1}(\ldots h_1(x, \theta_1), \theta_{L-1}), \theta_L)$
- x: input, θl: parameters for layer l, al = hl(x, θl): (non-)linear function
- Given training corpus {X, Y} find optimal parameters

$$\theta^* \leftarrow \arg\min_{\theta} \sum_{(x,y)\in(X,Y)} \ell(y, a_L(x; \theta_{1,\ldots,L}))$$

- To use gradient descent optimization $\left(\theta^{t+1} = \theta^t - \eta_t \frac{\partial \mathcal{L}}{\partial \theta^t}\right)$
- we need the gradients $\frac{\partial \mathcal{L}}{\partial \theta_l}, l = 1, \ldots, L$
- How to compute the gradients for such a complicated function enclosing other functions, like aL (...)?

Chain rule

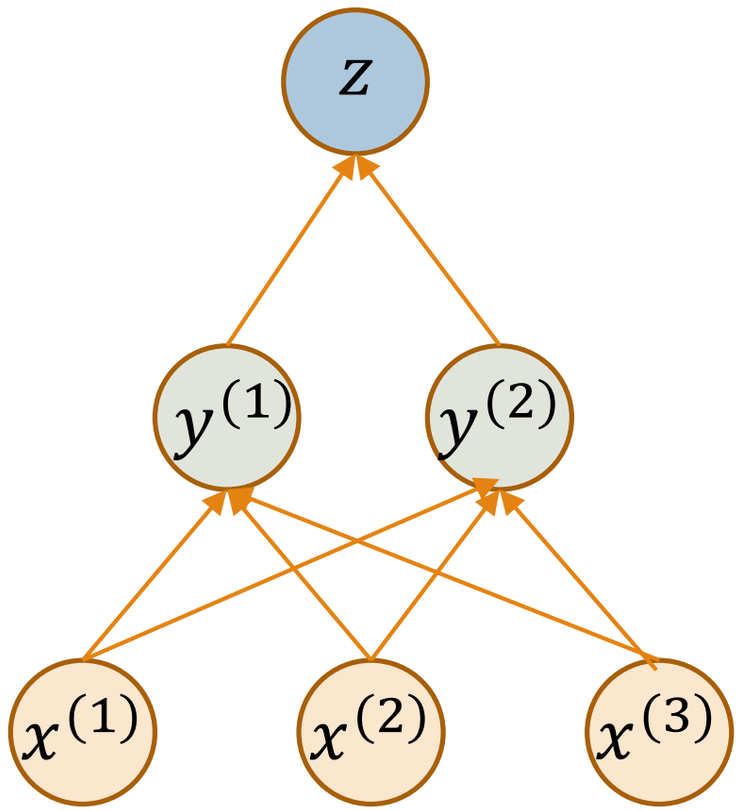
- Assume a nested function, $z = f(y)$ and $y = g(x)$
- Chain Rule for scalars x, y, z

$$\frac{dz}{dx} = \frac{dz}{dy}\frac{dy}{dx}$$

- When

$$\frac{dz}{dx^i} = \sum_j \frac{dz}{dy^j}\frac{dy^j}{dx^i}$$

gradients from all possible paths



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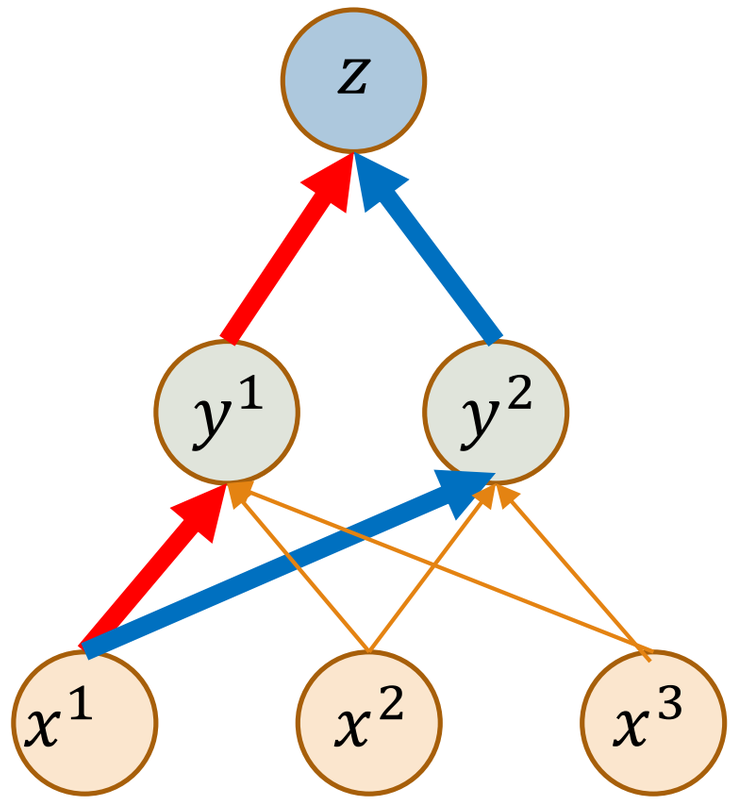

$$\frac{dz}{dx^1} = \frac{dz}{dy^1}\frac{dy^1}{dx^1} + \frac{dz}{dy^2}\frac{dy^2}{dx^1}$$

Chain rule

- Assume a nested function, $z = f(y)$ and $y = g(x)$
- Chain Rule for scalars x, y, z

$$\frac{dz}{dx} = \frac{dz}{dy}\frac{dy}{dx}$$

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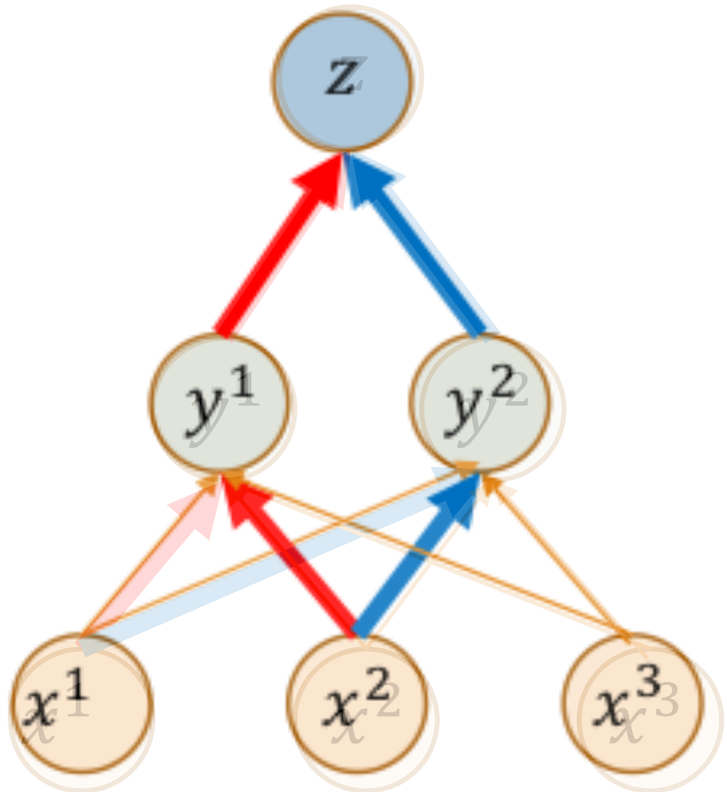
gradients from all possible paths



$$\frac{dz}{dx^2} = \frac{dz}{dy^1}\frac{dy^1}{dx^2} + \frac{dz}{dy^2}\frac{dy^2}{dx^2}$$

Chain rule

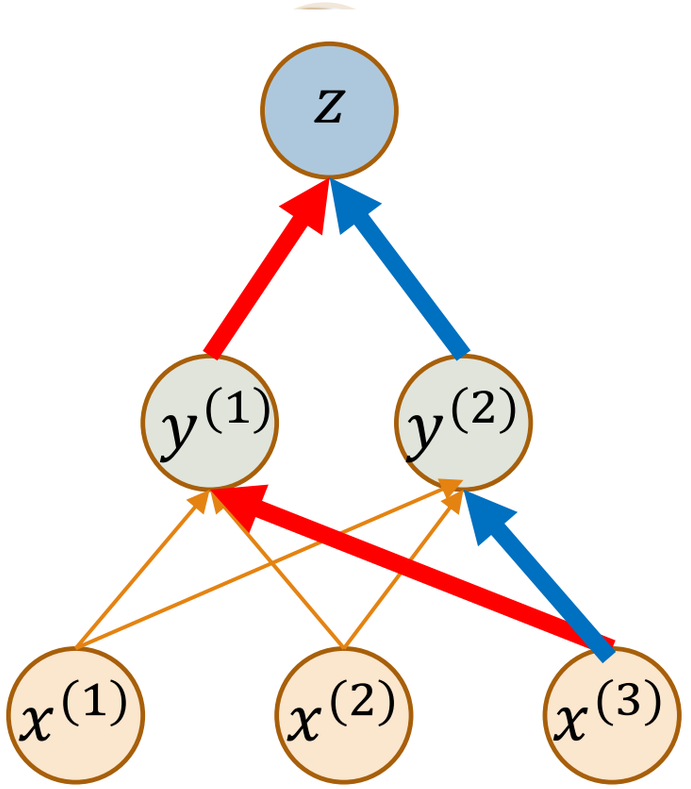
- Assume a nested function, $z = f(y)$ and $y = g(x)$
- Chain Rule for scalars x, y, z

$$\frac{dz}{dx} = \frac{dz}{dy}\frac{dy}{dx}$$

- When

$$\frac{dz}{dx^i} = \sum_j \frac{dz}{dy^j}\frac{dy^j}{dx^i}$$

gradients from all possible paths



$$\frac{dz}{dx^3} = \frac{dz}{dy^1}\frac{dy^1}{dx^3} + \frac{dz}{dy^2}\frac{dy^2}{dx^3}$$

Backpropagation ⟺ Chain rule!!!

- The loss function $\mathcal{L}(y, a_L)$ depends on aL, which depends on aL-1 , …, which depends on a2:

$$a_L(x; \theta_{1,\ldots,L}) = h_L(h_{L-1}(\ldots h_1(x, \theta_1), \theta_{L-1}), \theta_L)$$

- Gradients of parameters of layer l → Chain rule

$$\frac{\partial \mathcal{L}}{\partial \theta_l} = \frac{\partial \mathcal{L}}{\partial a_l} \cdot \frac{\partial a_L}{\partial a_{L-1}} \cdot \frac{\partial a_{L-1}}{\partial a_{L-2}} \cdot \ldots \cdot$$

- When shortened, we need to two quantities

$$\frac{\partial \mathcal{L}}{\partial \theta_l} = \left(\frac{\partial a_l}{\partial \theta_l}\right)^T \cdot \frac{\partial \mathcal{L}}{\partial a_l}$$

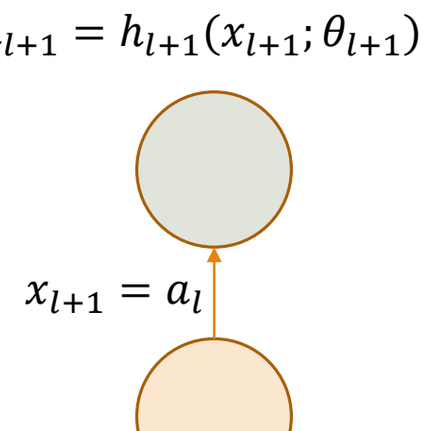
Gradient of a module w.r.t. its parameters

Gradient of loss w.r.t. the module output

Backpropagation ⟺ Chain rule!!!

- For $\frac{\partial \mathcal{L}}{\partial a_l}$ in $\frac{\partial \mathcal{L}}{\partial \theta_l} = \left(\frac{\partial a_l}{\partial \theta_l}\right)^T \cdot \frac{\partial \mathcal{L}}{\partial a_l}$ we apply chain rule again

$$\frac{\partial \mathcal{L}}{\partial a_l} = \left(\frac{\partial a_{l+1}}{\partial a_l}\right)^T \cdot \frac{\partial \mathcal{L}}{\partial a_{l+1}}$$



- We can rewrite $\frac{\partial a_{l+1}}{\partial a_l}$ as gradient of module w.r.t. to input
- Remember, the output of a module is the input for the next one:

$$\frac{\partial \mathcal{L}}{\partial a_l} = \left(\frac{\partial a_{l+1}}{\partial x_{l+1}}\right)^T \cdot \frac{\partial \mathcal{L}}{\partial a_{l+1}}$$

Recursive rule

So what is deep learning?

Three key ideas

- (Hierarchical) Compositionality
- End-to-End Learning
- Distributed Representations

slide by Dhruv Batra

Three key ideas

- **(Hierarchical) Compositionality**
  - Cascade of non-linear transformations
  - Multiple layers of representations
- End-to-End Learning
  - Learning (goal-driven) representations
  - Learning to feature extract
- Distributed Representations
  - No single neuron “encodes” everything
  - Groups of neurons work together

slide by Dhruv Batra

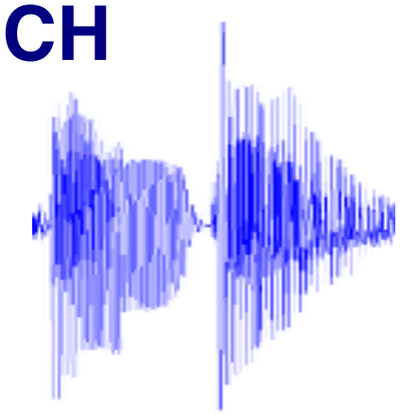
Traditional Machine Learning

VISION

hand-crafted features SIFT/HOG → your favorite classifier → "car"

fixed | learned

SPEECH



hand-crafted features MFCC → your favorite classifier → \ˈd ē p\

fixed | learned

NLP

This burrito place is yummy and fun!

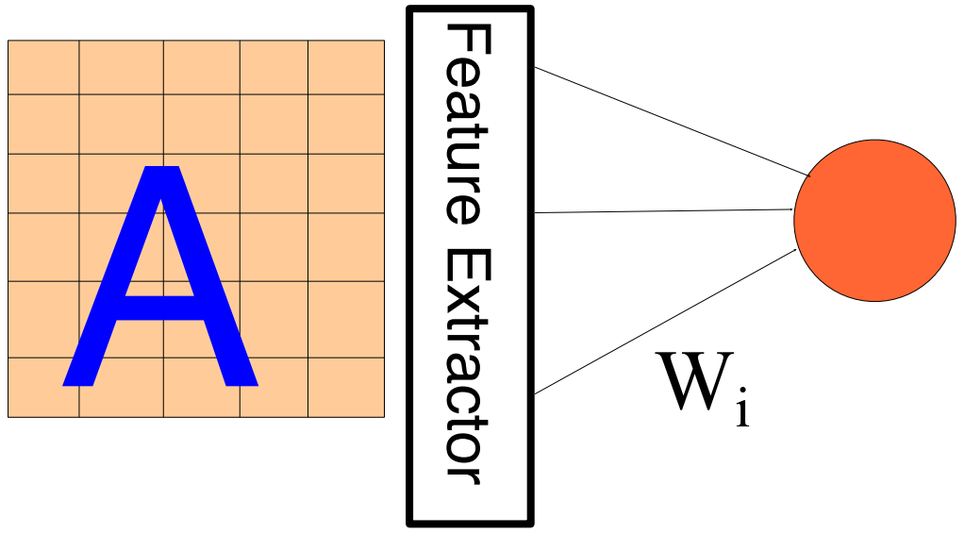
hand-crafted features Bag-of-words → your favorite classifier → "+"

fixed | learned

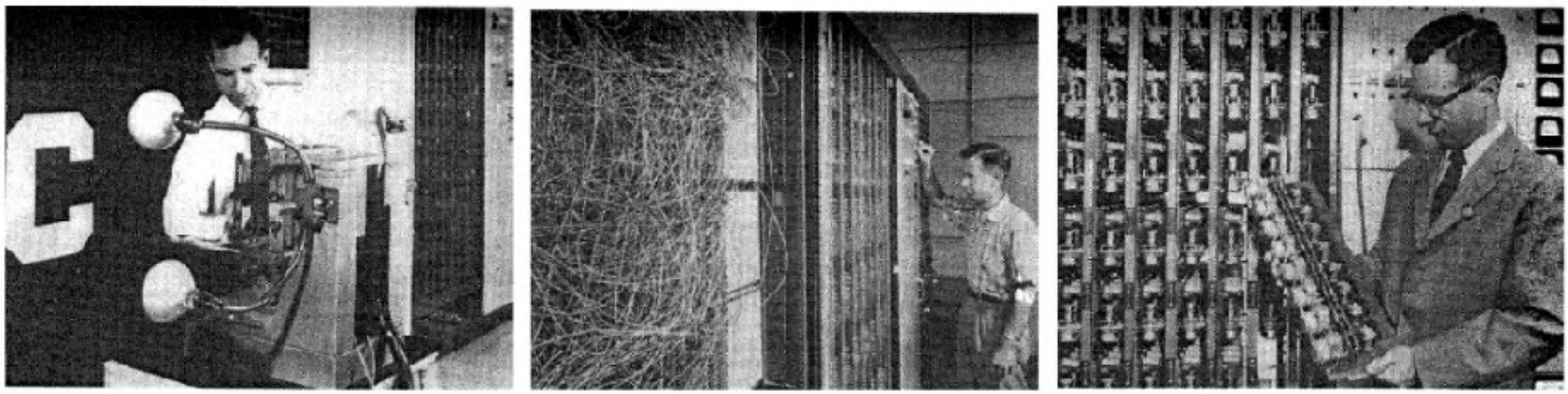
slide by Marc'Aurelio Ranzato, Yann LeCun

It’s an old paradigm

- The first learning machine: the Perceptron
  - Built at Cornell in 1960
- The Perceptron was a linear classifier on top of a simple feature extractor
- The vast majority of practical applications of ML today use glorified linear classifiers or glorified template matching.
- Designing a feature extractor requires considerable efforts by experts.



$$y = sign\left(\sum_{i=1}^{N} W_i F_i(X) + b\right)$$



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Hierarchical Compositionality

VISION

pixels → edge → texton → motif → part → object

SPEECH

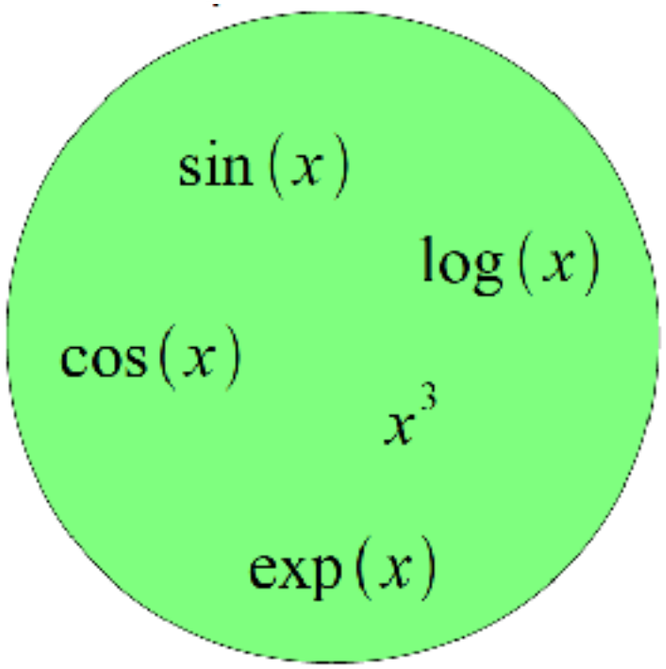
sample → spectral band → formant → motif → phone → word

NLP

character → word → NP/VP/.. → clause → sentence → story

Building A Complicated Function

Given a library of simple functions

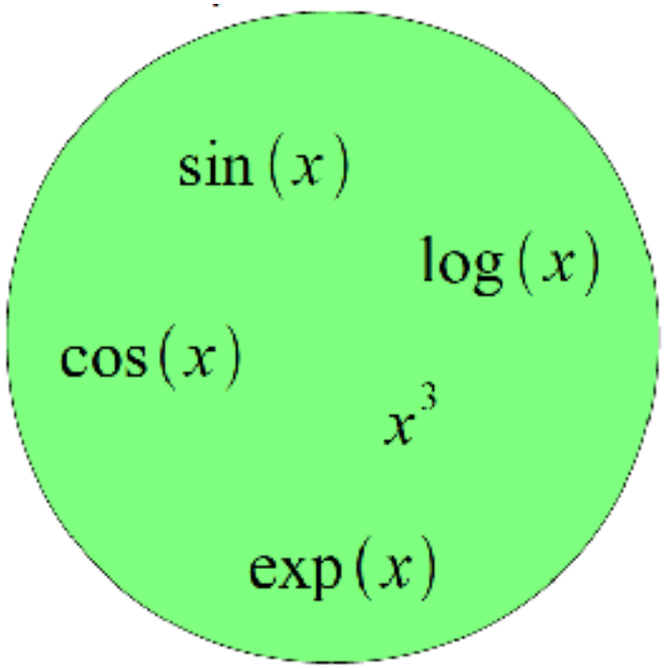


Compose into a

complicate function

Building A Complicated Function

Given a library of simple functions

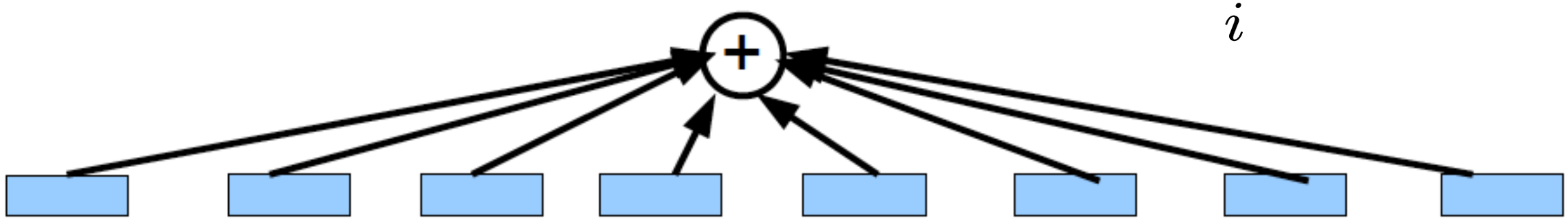


Compose into a complicate function

Idea 1: Linear Combinations

- Boosting
- Kernels
- …

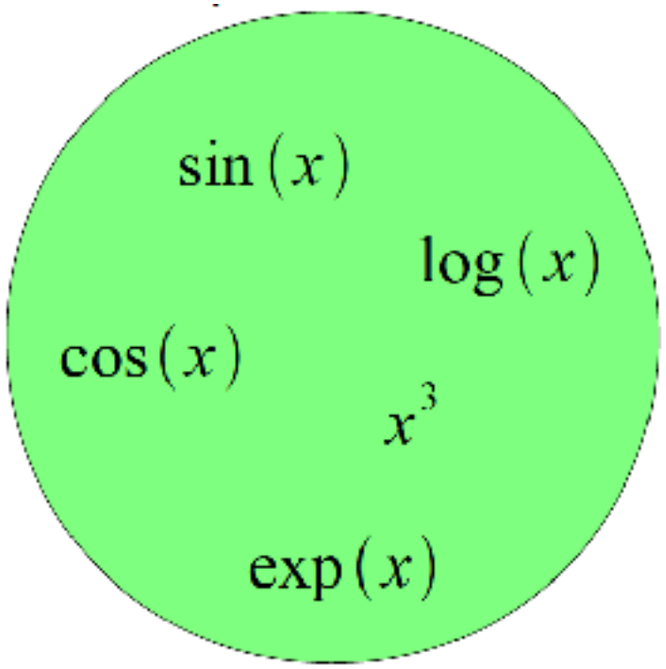
$$f(x) = \sum_i \alpha_i g_i(x)$$



slide by Marc'Aurelio Ranzato, Yann LeCun

Building A Complicated Function

Given a library of simple functions



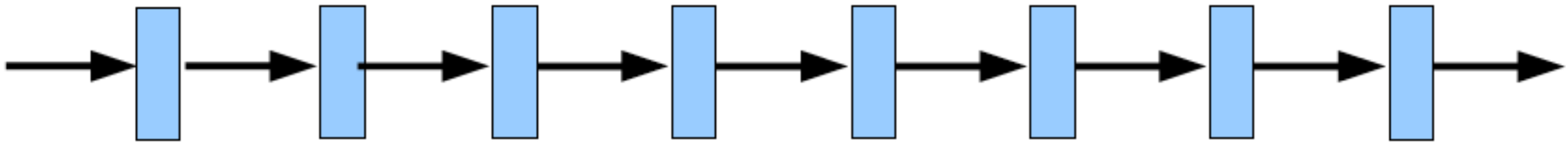
Compose into a

complicate function

Idea 2: Compositions

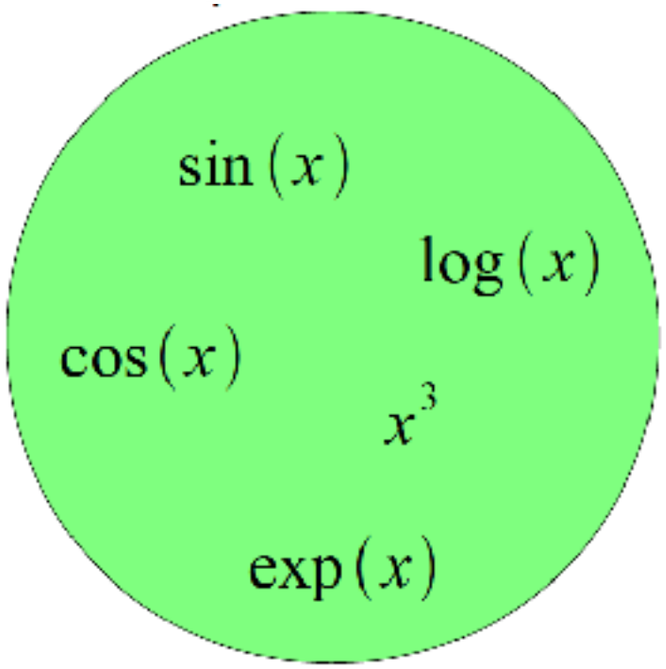
- Deep Learning
- Grammar models
- Scattering transforms…

$$f(x) = g_1(g_2(\dots(g_n(x)\dots))$$



Building A Complicated Function

Given a library of simple functions



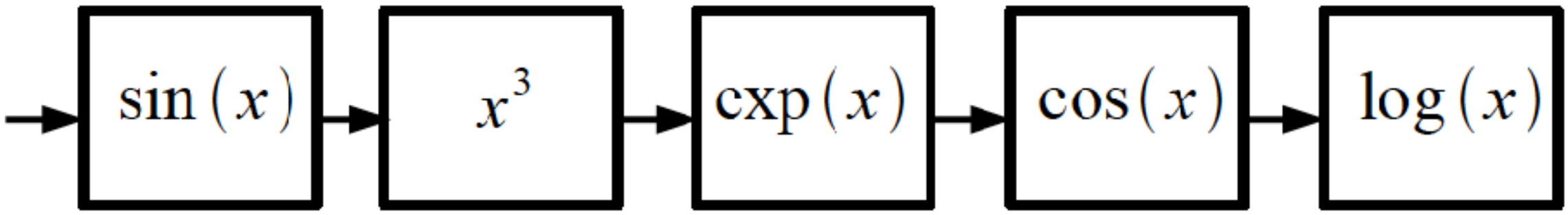
Compose into a

complicate function

Idea 2: Compositions

- Deep Learning
- Grammar models
- Scattering transforms…

$$f(x) = \log(\cos(\exp(\sin^3(x))))$$



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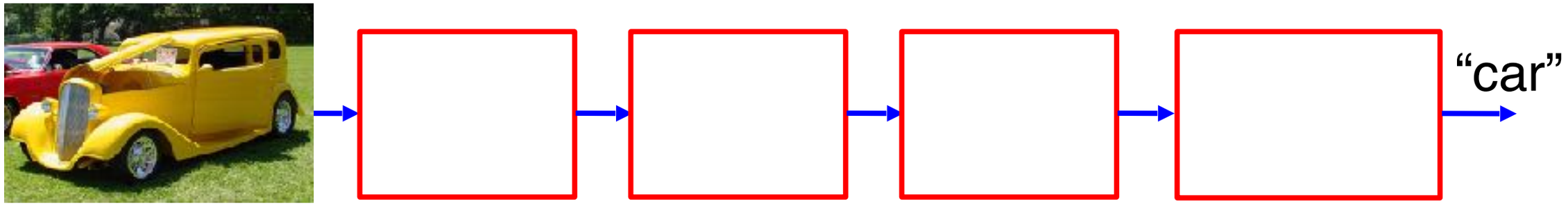
Deep Learning = Hierarchical Compositionality



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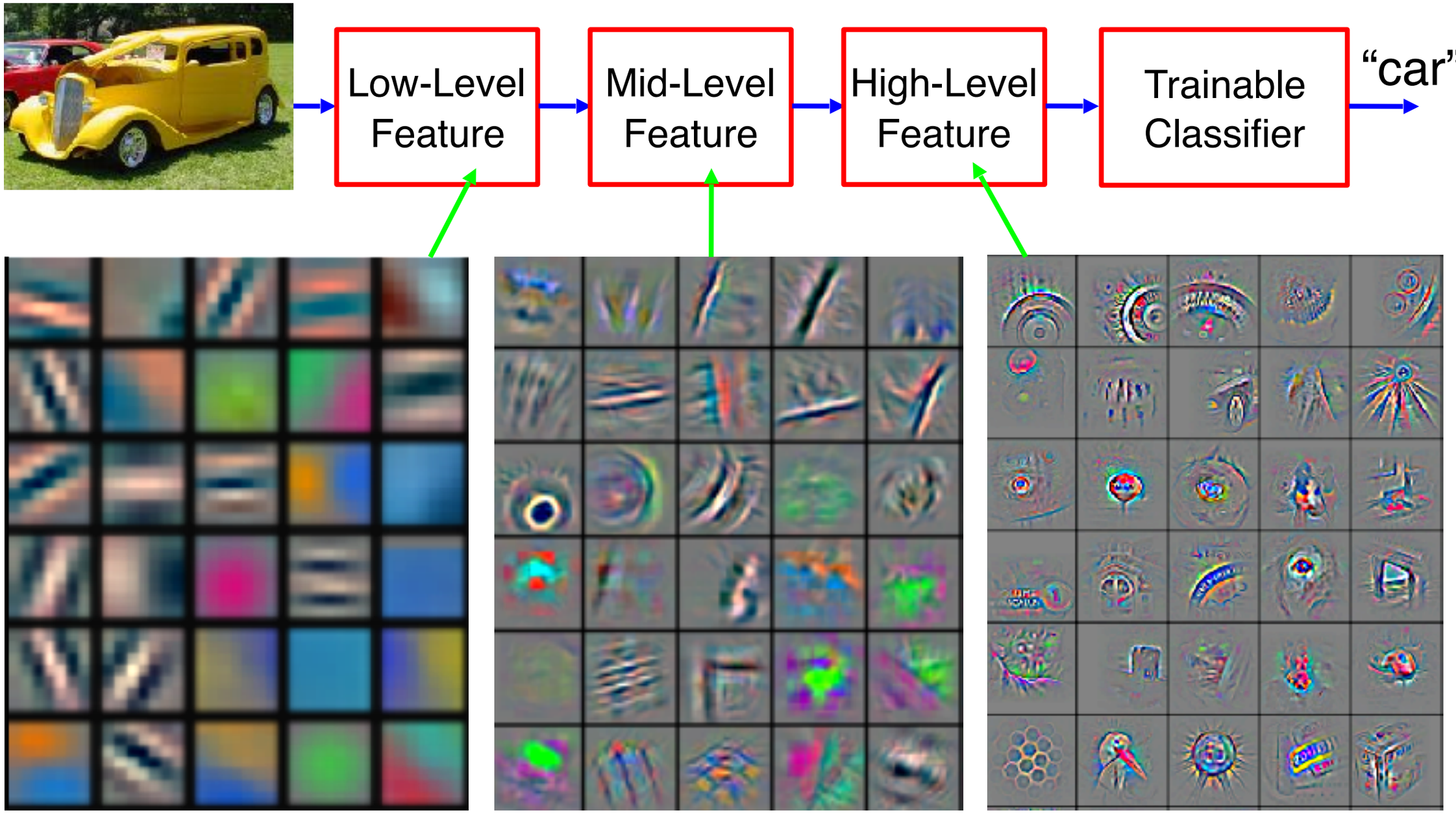
Deep Learning = Hierarchical Compositionality



Feature visualization of convolutional net trained on ImageNet from [Zeiler & Fergus 2013]

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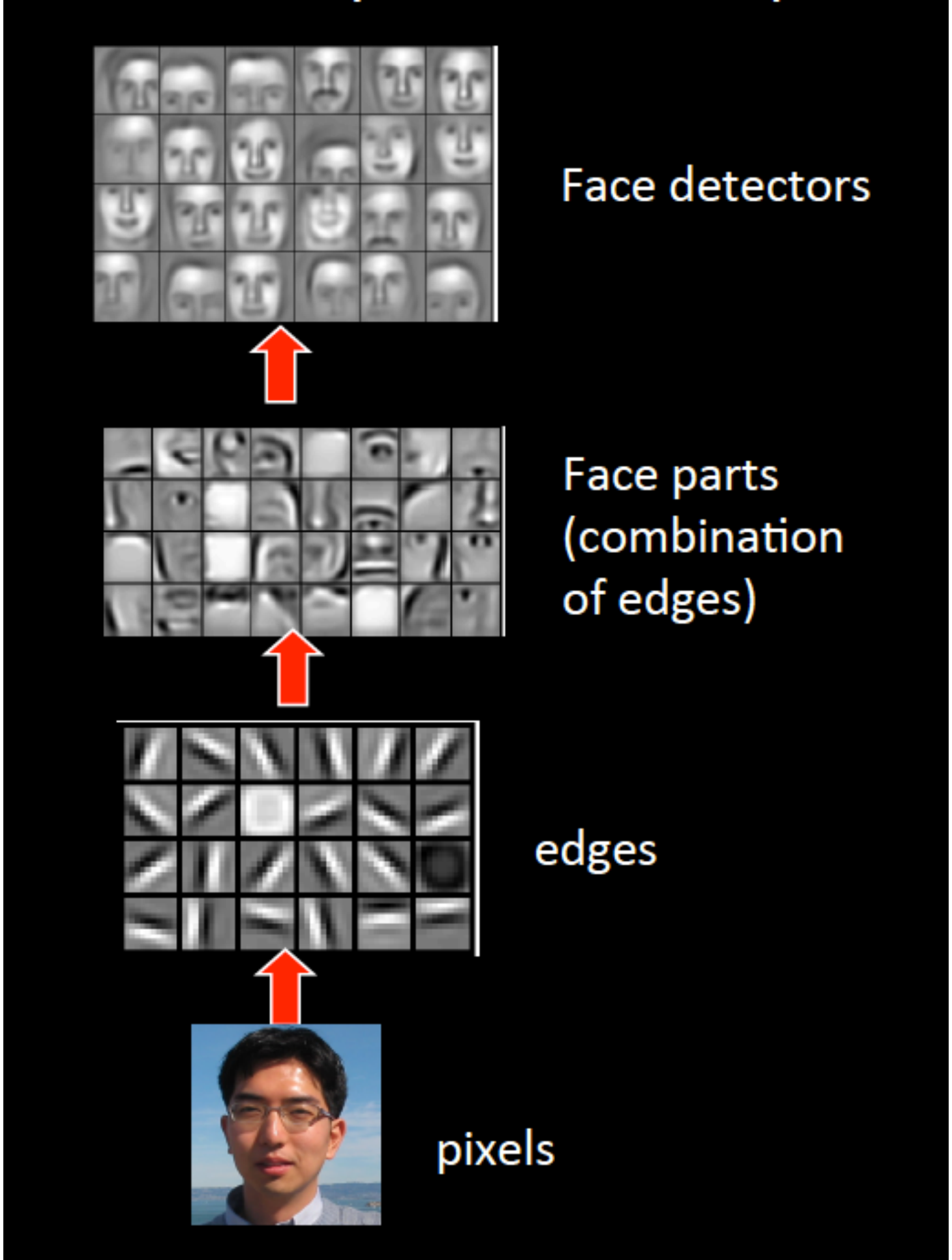


Sparse DBNs
[Lee et al. ICML '09]
Figure courtesy: Quoc Le

slide by Dhruv Batra

Three key ideas

- (Hierarchical) Compositionality
  - Cascade of non-linear transformations
  - Multiple layers of representations

- **End-to-End Learning**
  - Learning (goal-driven) representations
  - Learning to feature extract

- Distributed Representations
  - No single neuron “encodes” everything
  - Groups of neurons work together

slide by Dhruv Batra

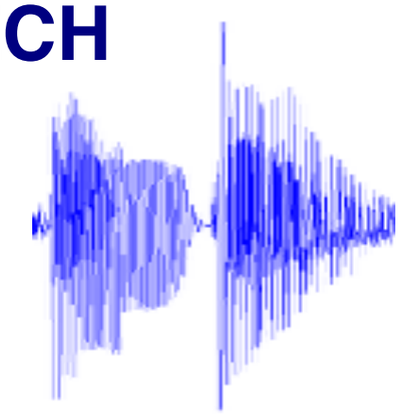
Traditional Machine Learning

VISION

hand-crafted features SIFT/HOG → your favorite classifier → "car"

fixed | learned

SPEECH



hand-crafted features MFCC → your favorite classifier → \ˈd ē p\

fixed | learned

NLP

This burrito place is yummy and fun!

hand-crafted features Bag-of-words → your favorite classifier → "+"

fixed | learned

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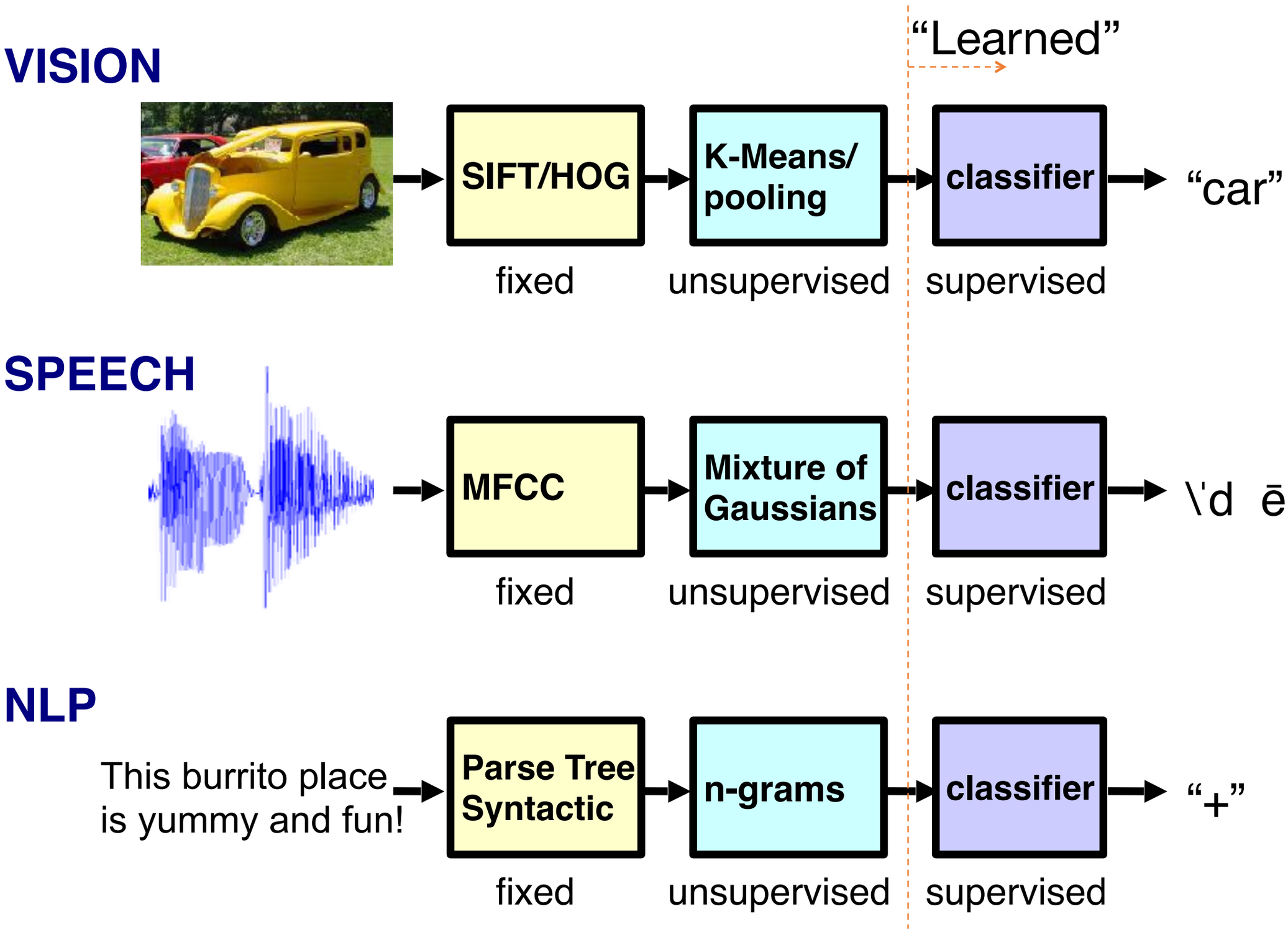
Traditional Machine Learning (more accurately)



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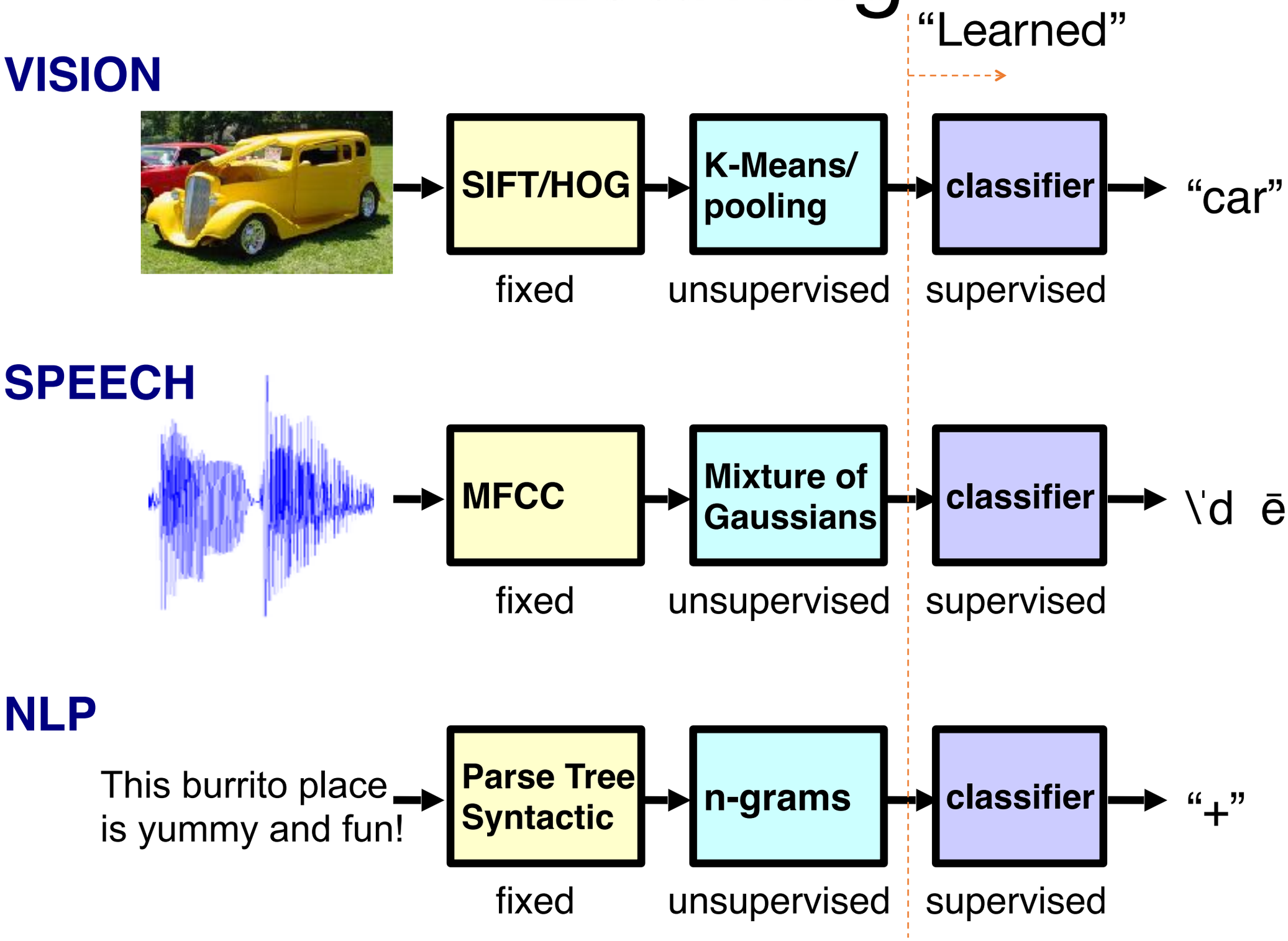
Deep Learning = End-to-End Learning



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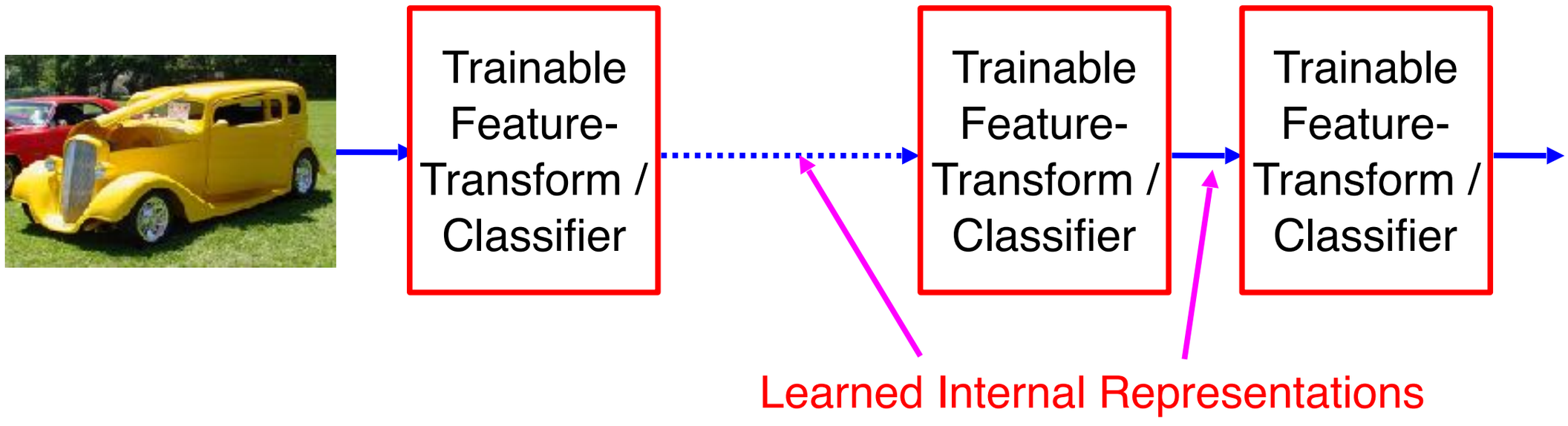
Deep Learning = End-to-End Learning

- A hierarchy of trainable feature transforms
  - Each module transforms its input representation into a higher-level one.
  - High-level features are more global and more invariant
  - Low-level features are shared among categories



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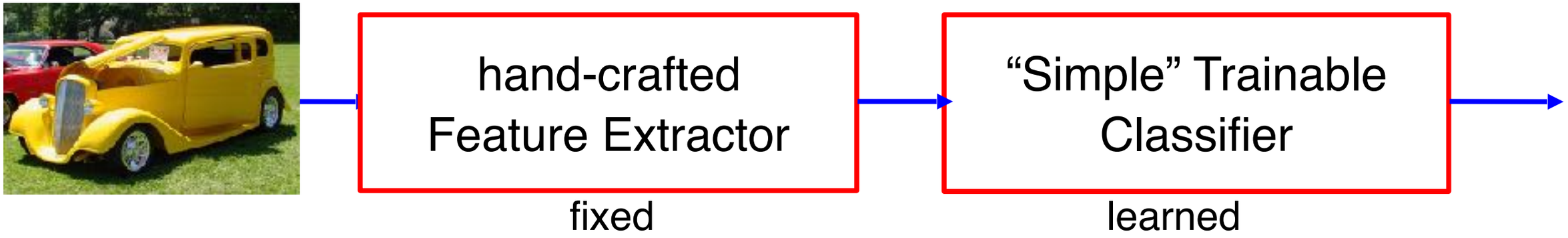
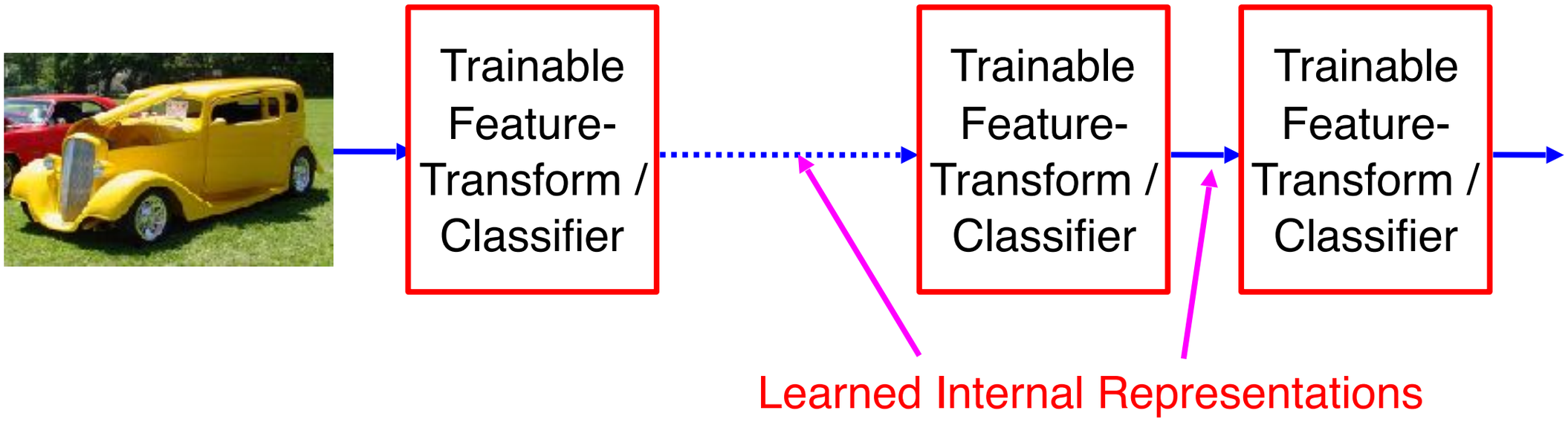
“Shallow” vs Deep Learning

- “Shallow” models



- Deep models



slide by Marc’Aurelio Ranzato, Yann LeCun

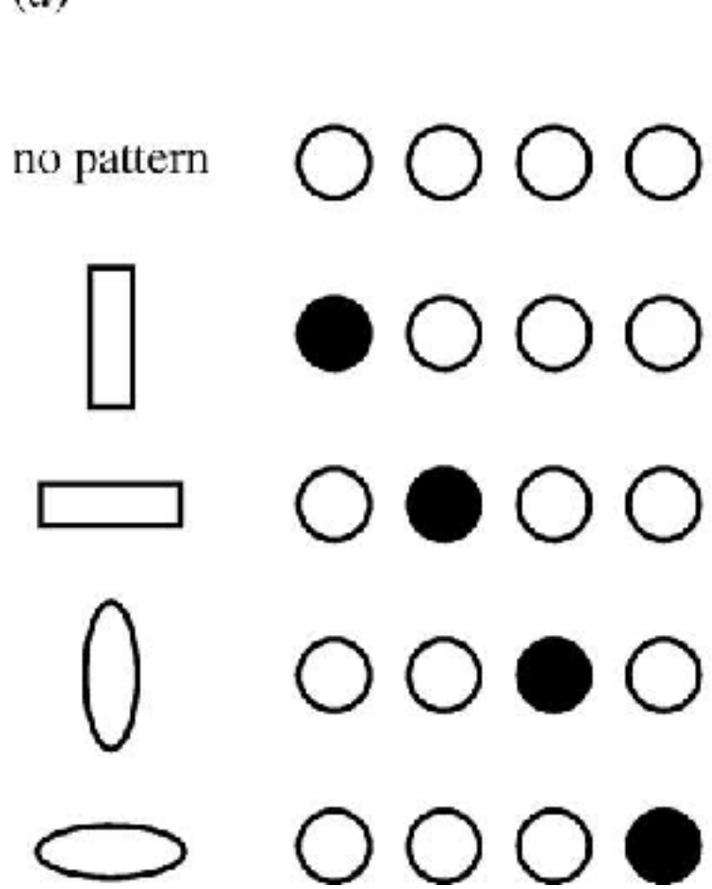
Three key ideas

- (Hierarchical) Compositionality
  - Cascade of non-linear transformations
  - Multiple layers of representations
- End-to-End Learning
  - Learning (goal-driven) representations
  - Learning to feature extract
- **Distributed Representations**
  - No single neuron “encodes” everything
  - Groups of neurons work together

slide by Dhruv Batra

Localist representations

- The simplest way to represent things with neural networks is to **dedicate one neuron to each thing**.
  - Easy to understand.
  - Easy to code by hand
    - Often used to represent inputs to a net
  - Easy to learn
    - This is what mixture models do.
    - Each cluster corresponds to one neuron
  - Easy to associate with other representations or responses.



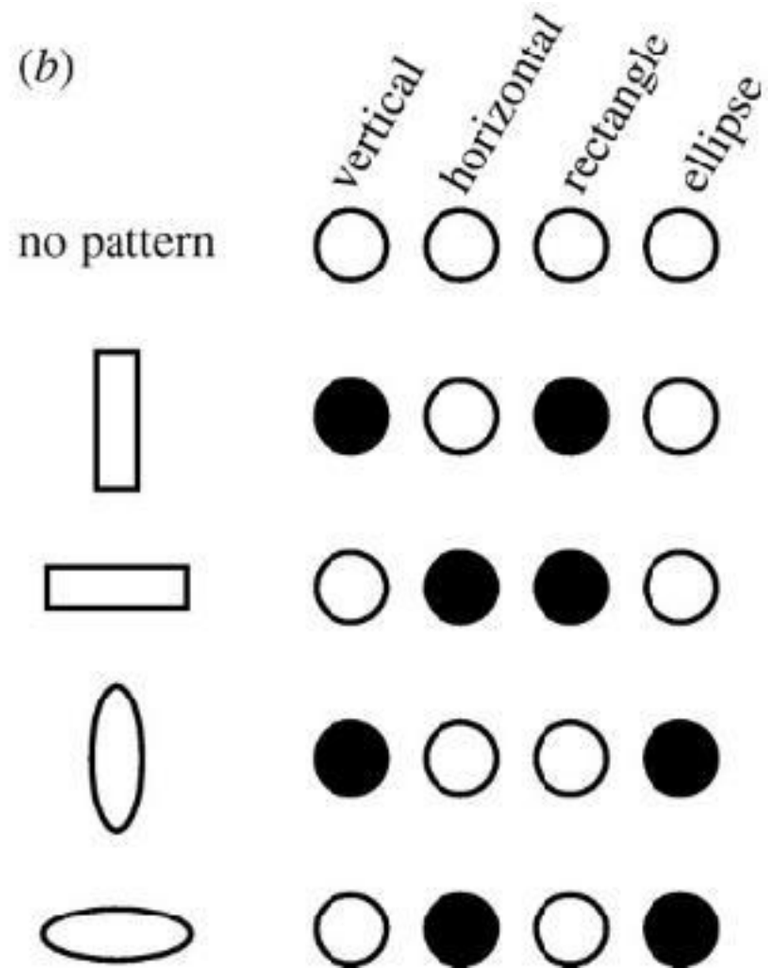
- But localist models are very inefficient whenever the data has componential structure.

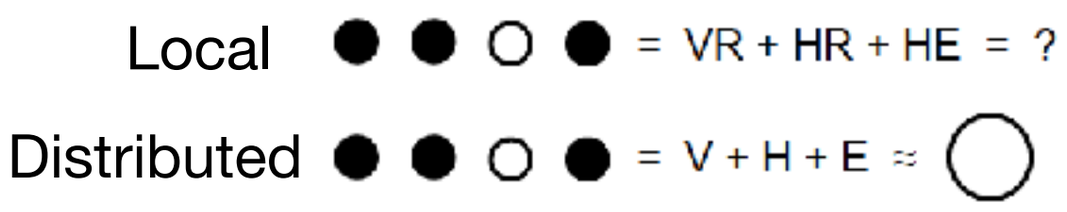
Image credit: Moontae Lee

slide by Geoff Hinton

Distributed Representations

- Each neuron must represent something, so this must be a local representation.
- **Distributed representation** means a many-to-many relationship between two types of representation (such as concepts and neurons).
  - Each concept is represented by many neurons
  - Each neuron participates in the representation of many concepts





slide by Geoff Hinton

Image credit: Moontae Lee

Power of distributed representations!

Scene Classification

bedroom

mountain

- Possible internal representations:
  - Objects
  - Scene attributes
  - Object parts
  - Textures

B. Zhou, A. Khosla, A. Lapedriza, A. Oliva, and A. Torralba **“Object Detectors Emerge in Deep Scene CNNs”**, ICLR 2015

slide by Bolei Zhou

Deep Convolutional Neural Networks

Convolutions

- Images typically have invariant patterns
  - E.g., directional gradients are translational invariant:

- Apply convolution to local sliding windows

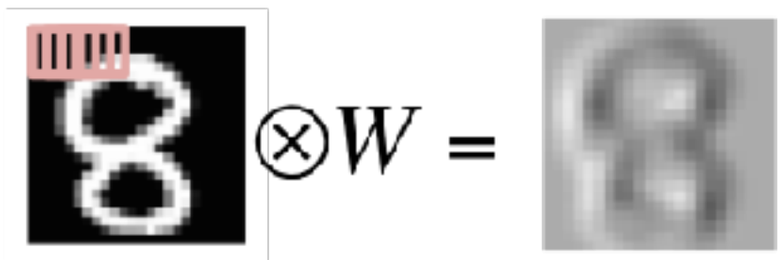
slide by Yisong Yue

Convolution Filters

- Applies to an image patch x
  - Converts local window into single value
  - Slide across image

$$x \otimes W = \sum_{ij} W_{ij} x_{ij}$$

Local Image Patch



Left-to-Right
Edge Detector

-1	0	+1
-1	0	+1
-1	0	+1

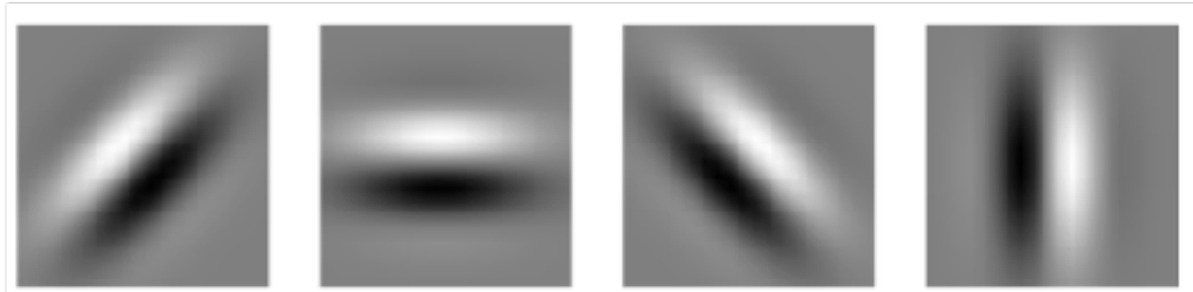
W

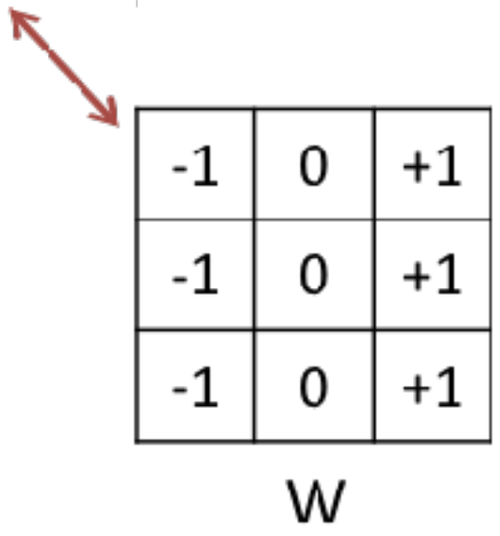
slide by Yisong Yue

Gabor Filters

- Most common low-level convolutions for computer vision

Example W:





-1	0	+1
-1	0	+1
-1	0	+1

W

http://en.wikipedia.org/wiki/Gabor_filter

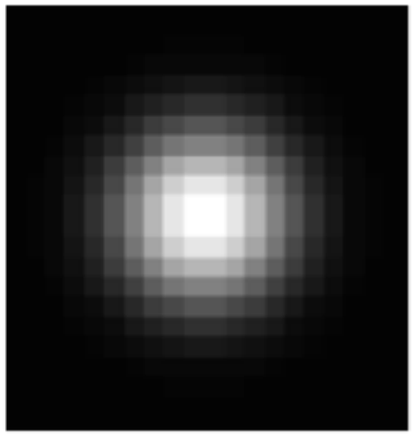
slide by Yisong Yue

Gaussian Blur Filters

- Weights decay according to Gaussian Distribution
  - Variance term controls radius

Example W:

Apply per RGB Channel



- Black = 0
- White = Positive

http://en.wikipedia.org/wiki/Gaussian_blur

slide by Yisong Yue