

# CMP717

# Image Processing

## Image Deblurring

Erkut Erdem  
Hacettepe University  
Computer Vision Lab (HUCVL)

# Image Deblurring\*

- Introduction
- Blind deconvolution
- Non-blind deconvolution

# Image Deblurring

- Introduction
- Blind deconvolution
- Non-blind deconvolution



## blur [blɜ:(r)]

- Long exposure
- Moving objects
- Camera motion
  - panning shot



## blur [blɜ:(r)]

- Often degrades image/video quality severely
- Unavoidable under dim light circumstances

# Various Kinds of Blurs



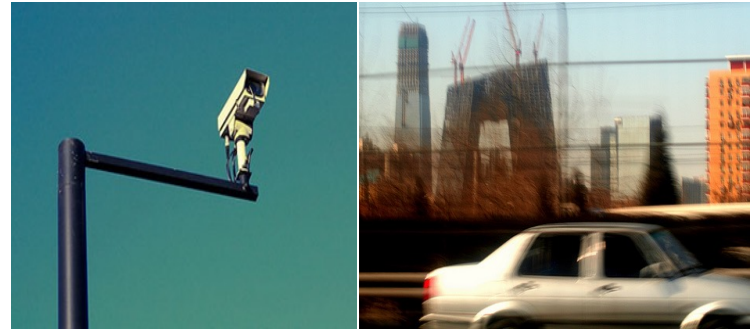
Camera shake (Camera motion blur)



Object movement (Object motion blur)



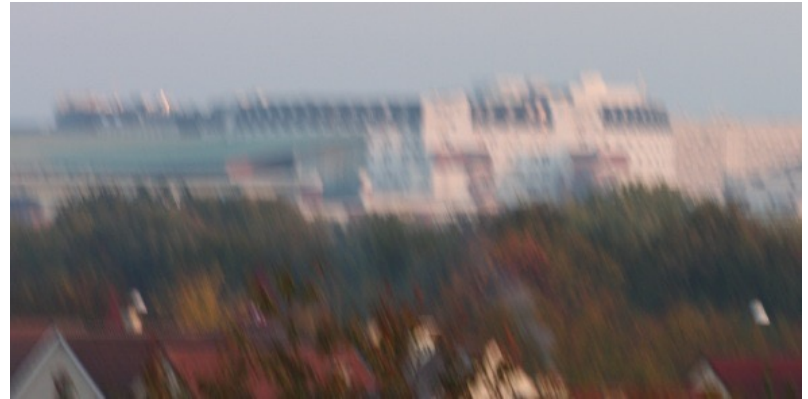
Out of focus (Defocus blur)



Combinations (vibration & motion, ...)

# Camera Motion Blur

- Caused by camera shakes during exposure time
  - Motion can be represented as a camera trajectory



# Object Motion Blur

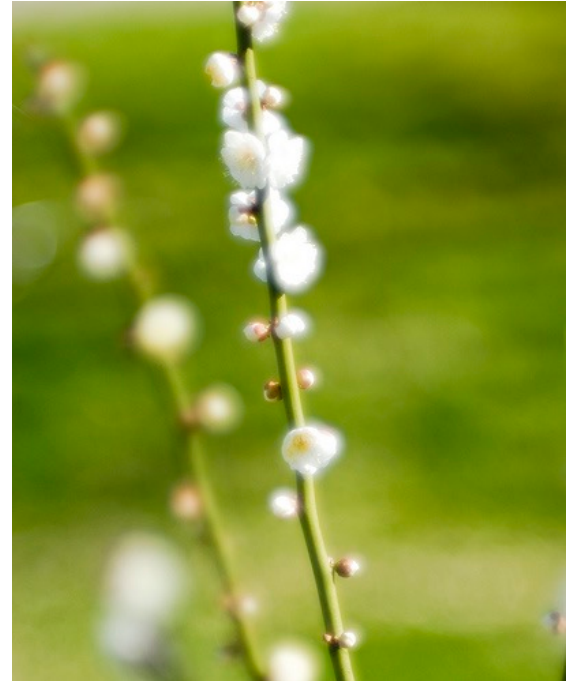
- Caused by object motions during exposure time





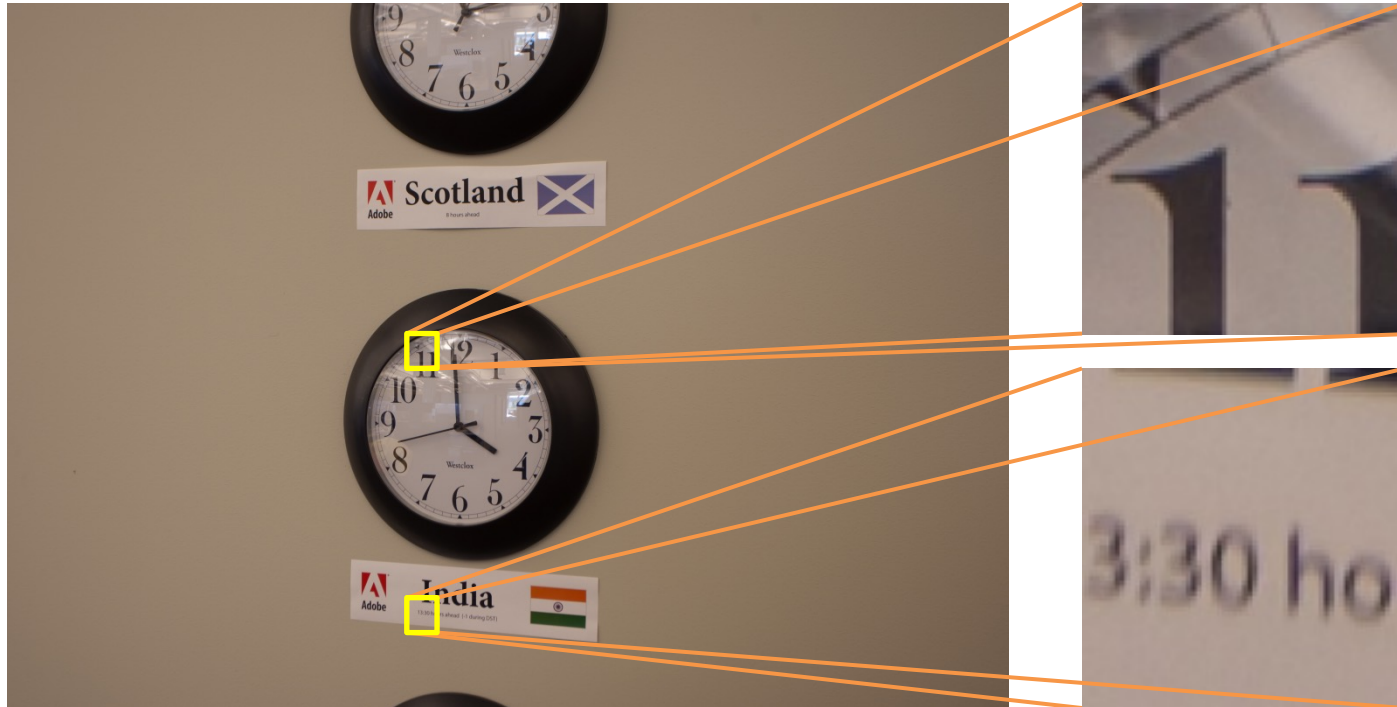
# Defocus Blur

- Caused by the limited depth of field of a camera



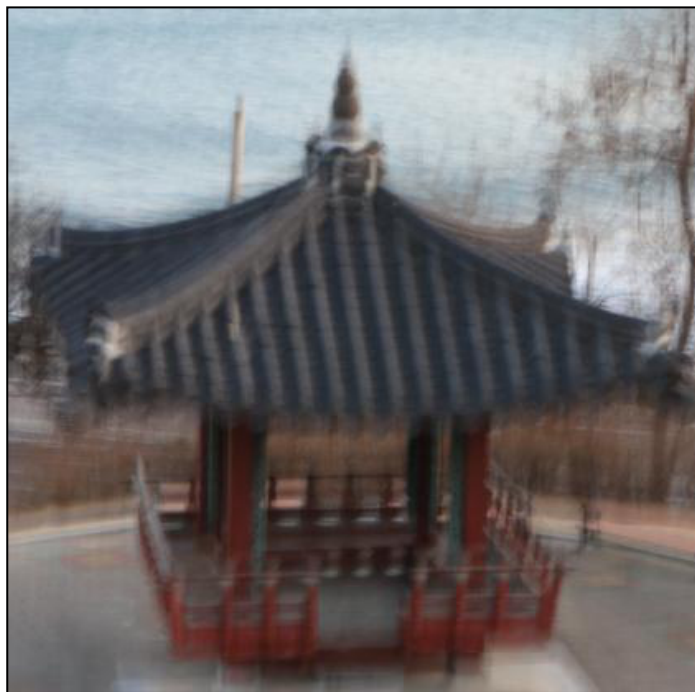
# Optical Lens Blur

- Caused by lens aberration



# Deblurring?

- Remove blur and restore a latent sharp image



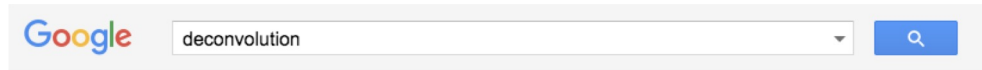
from a given blurred image



find its latent sharp image

# Deblurring: Old Problem!

- Trott, T., “The Effect of Motion of Resolution”, *Photogrammetric Engineering*, Vol. 26, pp. 819-827, 1960.
- Slepian, D., “Restoration of Photographs Blurred by Image Motion”, *Bell System Tech.*, Vol. 46, No. 10, pp. 2353-2362, 1967.



About 474,000 results

**Articles**

Case law

My library

Any time

Since 2017

Since 2016

Since 2013

Custom range...

Sort by relevance

Sort by date

include patents

include citations

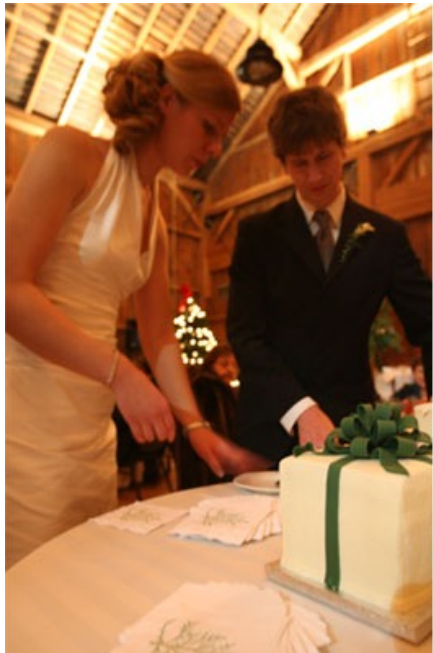
**An information-maximization approach to blind separation and blind deconvolution**  
AJ Bell, TJ Sejnowski - Neural computation, 1995 - MIT Press  
We derive a new self-organizing learning algorithm that maximizes the information transferred in a network of nonlinear units. The algorithm does not assume any knowledge of the input distributions, and is defined here for the zero-noise limit. Under these conditions, Cited by 8401 Related articles All 36 versions Web of Science: 4298 Cite Save More

**Deconvolution of impulse response in event-related bold fmri 1**  
GH Glover - Neuroimage, 1999 - Elsevier  
The temporal characteristics of the BOLD response in sensorimotor and auditory cortices were measured in subjects performing finger tapping while listening to metronome pacing tones. A repeated trial paradigm was used with stimulus durations of 167 ms to 16 s and Cited by 1082 Related articles All 15 versions Web of Science: 707 Cite Save

**Fourier self-deconvolution: a method for resolving intrinsically overlapped bands**  
JK Kauppinen, DJ Moffatt, HH Mantsch... - Applied ..., 1981 - journals.sagepub.com  
The general theory of Fourier self-deconvolution, ie, spectral deconvolution using Fourier transforms and the intrinsic lineshape, is developed. The method provides a way of computationally resolving overlapped lines that can not be instrumentally resolved due to Cited by 1202 Related articles All 7 versions Web of Science: 1110 Cite Save More

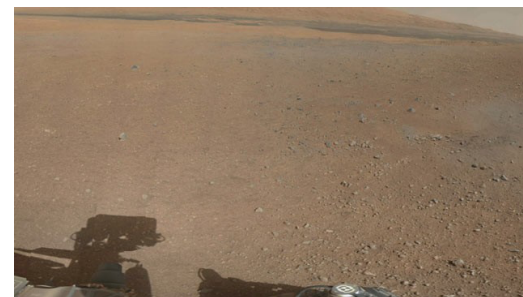
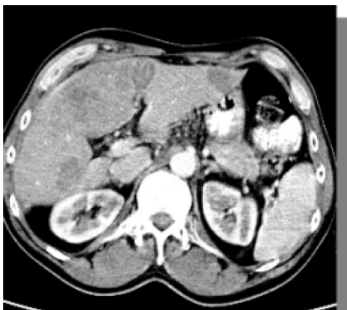
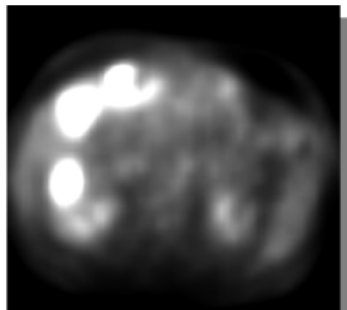
# Why is it important?

- Image/video in our daily lives
  - Sometimes a retake is difficult!



# Why is it **important**?

- Strong demand for high quality deblurring



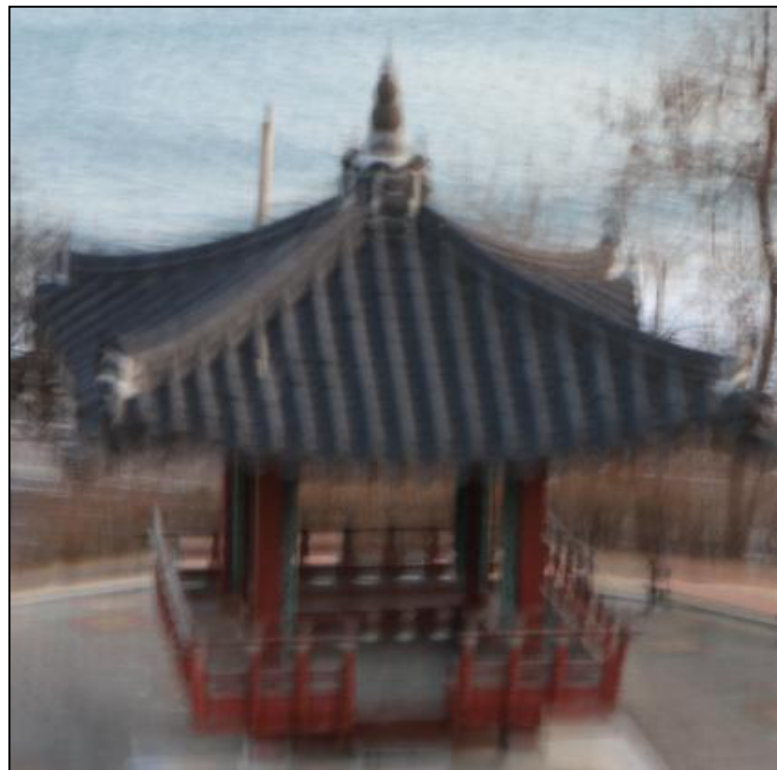
CCTV, car black box

Medical imaging

Aerial/satellite  
photography

Robot vision

# Deblurring

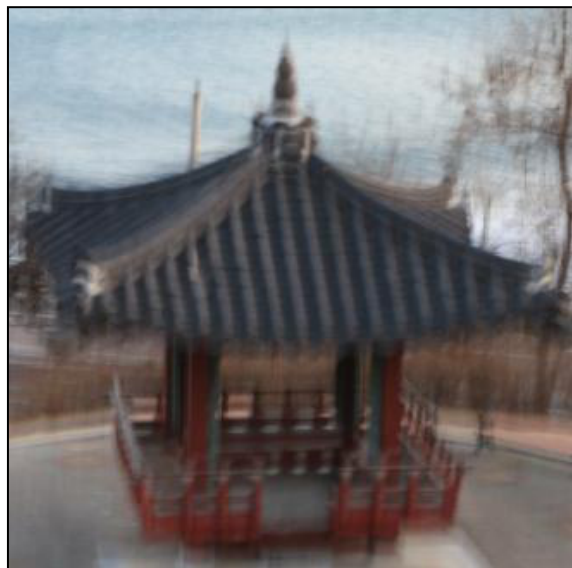


from a given blurred image

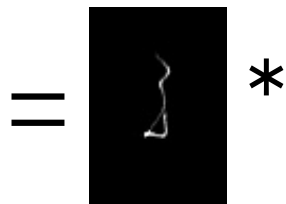


find its latent sharp image

# Commonly Used Blur Model



Blurred image



Blur kernel  
or Point Spread  
Function (PSF)



Latent sharp image

Convolution  
operator

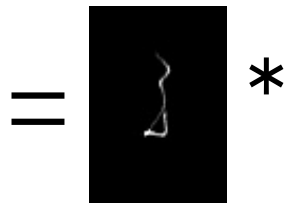


# Blind Deconvolution



Blurred image

?



Blur kernel  
or Point Spread  
Function (PSF)

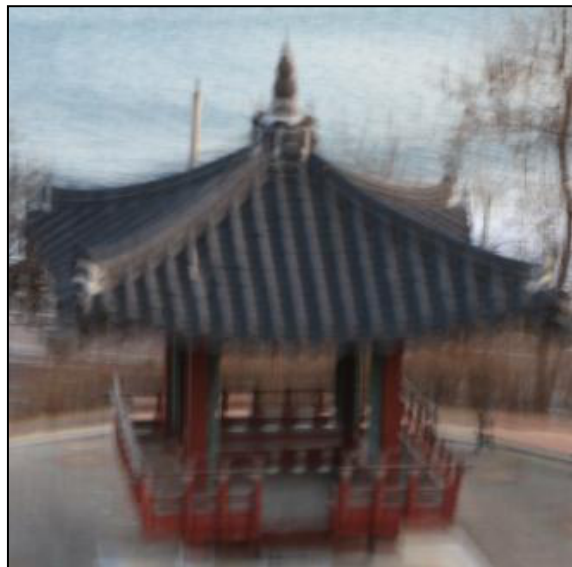
Convolution  
operator



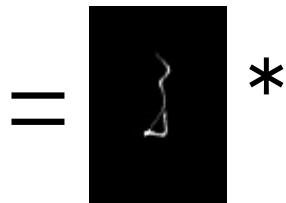
Latent sharp image

?

# Non-blind Deconvolution



Blurred image



Blur kernel  
or Point Spread  
Function (PSF)



Latent sharp image

Convolution  
operator

# Uniform vs. Non-uniform Blur



## Uniform blur

- Every pixel is blurred in the same way
- Convolution based blur model

# Uniform vs. Non-uniform Blur



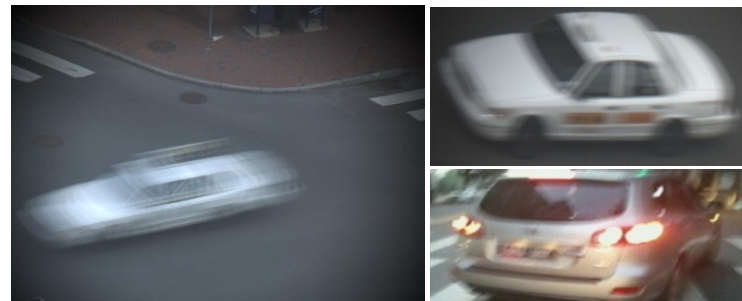
## Non-uniform blur

- Spatially-varying blur
- Pixels are blurred differently
- More faithful to real camera shakes

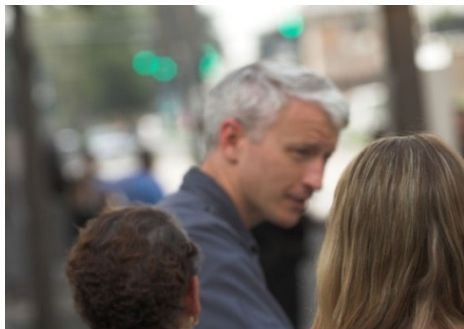
# Most Blurs Are Non-Uniform



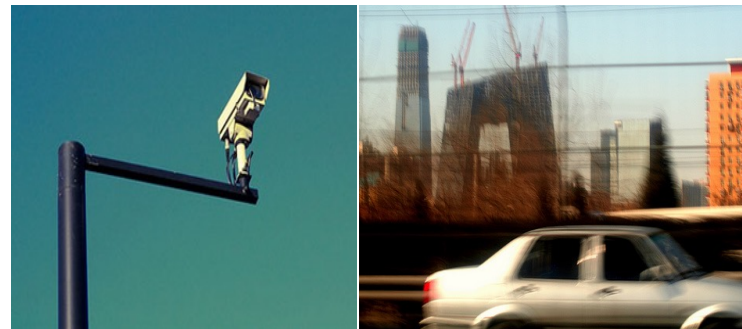
Camera shake (Camera motion blur)



Object movement (Object motion blur)



Out of focus (Defocus blur)



Combinations (vibration & motion, ...)

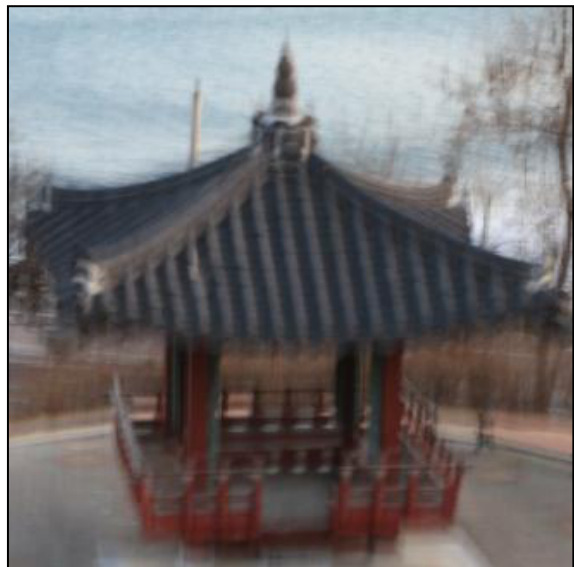
# Image Deblurring

- Introduction
- Blind deconvolution
- Non-blind deconvolution

# Blind Deconvolution

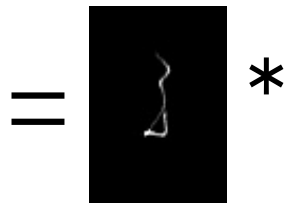
- Introduction
- Recent popular approaches
- Non-uniform blur

# Blind Deconvolution (Uniform Blur)



Blurred image

?



Blur kernel  
or Point Spread  
Function (PSF)

Convolution  
operator

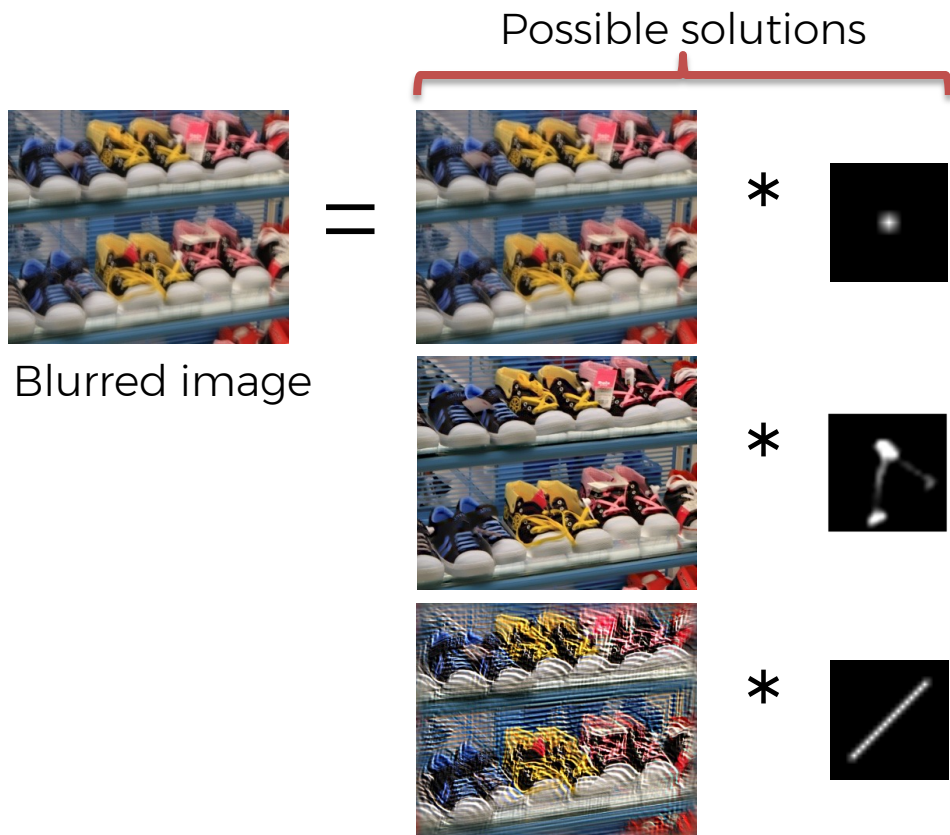


Latent sharp image

?



# Key challenge: Ill-posedness!



- Infinite number of solutions satisfy the blur model

- Analogous to

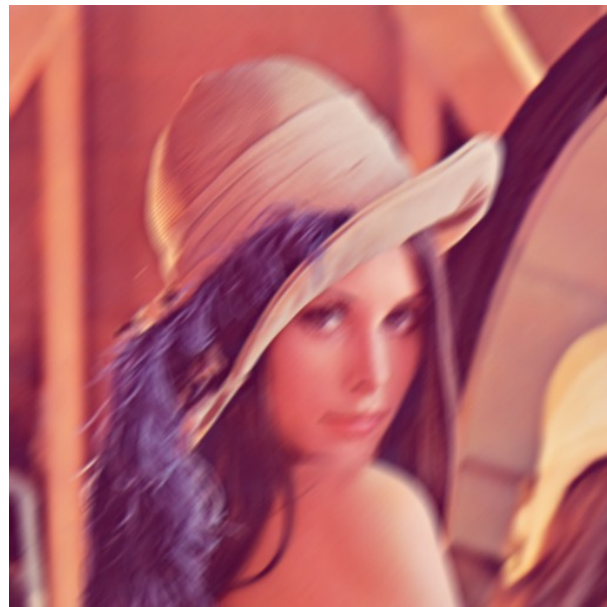
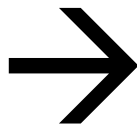
$$100 = \begin{cases} 2 \times 50 \\ 4 \times 25 \\ 3 \times 33.333 \dots \end{cases}$$

# In The Past...

- Parametric blur kernels
  - [Yitzhakey et al. 1998], [Rav-Acha and Peleg 2005], ...
  - Directional blur kernels defined by (length, angle)



\*



# In The Past...

- But real camera shakes are much more complex

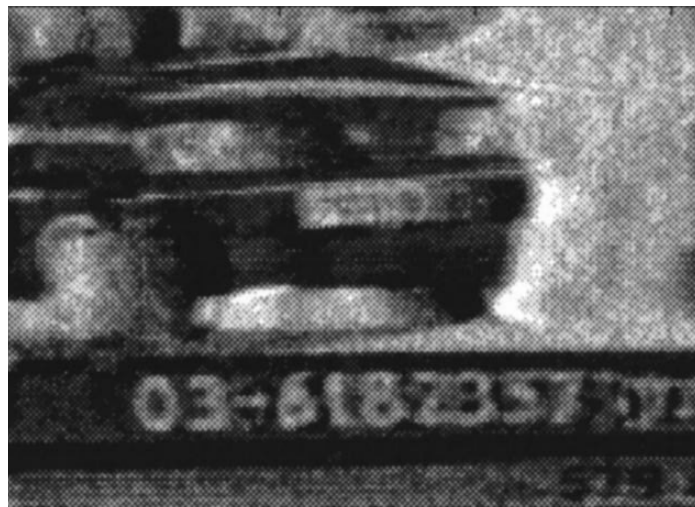


# In The Past...

- Parametric blur kernels
  - Very restrictive assumption
  - Often failed, poor quality



Blurred image

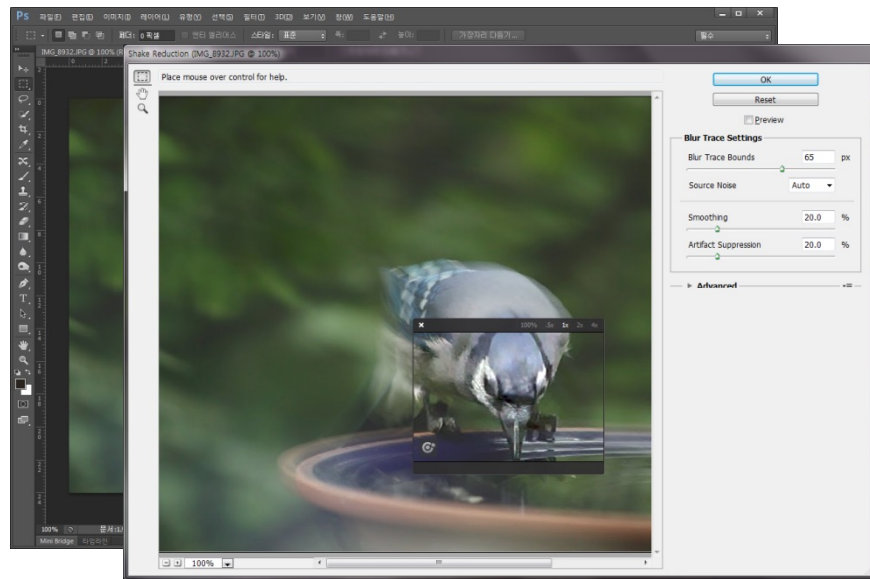


Latent sharp image

\* Images from [Yitzhaky et al. 1998]

# Nowadays...

- Some successful approaches have been introduced...
  - [Fergus et al. SIGGRAPH 2006], [Shan et al. SIGGRAPH 2008], [Cho and Lee, SIGGRAPH Asia 2009], ...
  - More realistic blur kernels
  - Better quality
  - More robust
- Commercial software
  - Photoshop CC Shake reduction



# Blind Deconvolution

- Introduction
- Recent popular approaches
- Non-uniform blur

# Recent Popular Approaches

- Maximum Posterior (MAP) based
- Variational Bayesian based
- Edge Prediction based

Which one is better?

# Recent Popular Approaches

- Maximum Posterior (MAP) based
  - Variational Bayesian based
  - Edge Prediction based
- [Shan et al. SIGGRAPH 2008], [Krishnan et al. CVPR 2011], [Xu et al. CVPR 2013], ...
  - Seek the most probable solution, which maximizes a posterior distribution
  - Easy to understand
  - Convergence problem

Which one is better?



# Recent Popular Approaches

- Maximum Posterior (MAP) based
  - Variational Bayesian based
  - Edge Prediction based
- [Fergus et al. SIGGRAPH 2006], [Levin et al. CVPR 2009], [Levin et al. CVPR 2011], ...
  - Not seek for one most probable solution, but consider all possible solutions
  - Theoretically more robust
  - Slow

Which one is better?

# Recent Popular Approaches

- Maximum Posterior (MAP) based
  - Variational Bayesian based
  - Edge Prediction based
- [Cho & Lee. SIGGRAPH Asia 2009], [Xu et al. ECCV 2010], [Hirsch et al. ICCV 2011], ...
  - Explicitly try to recover sharp edges using heuristic image filters
  - Fast
  - Proven to be effective in practice, but hard to analyze because of heuristic steps

Which one is better?

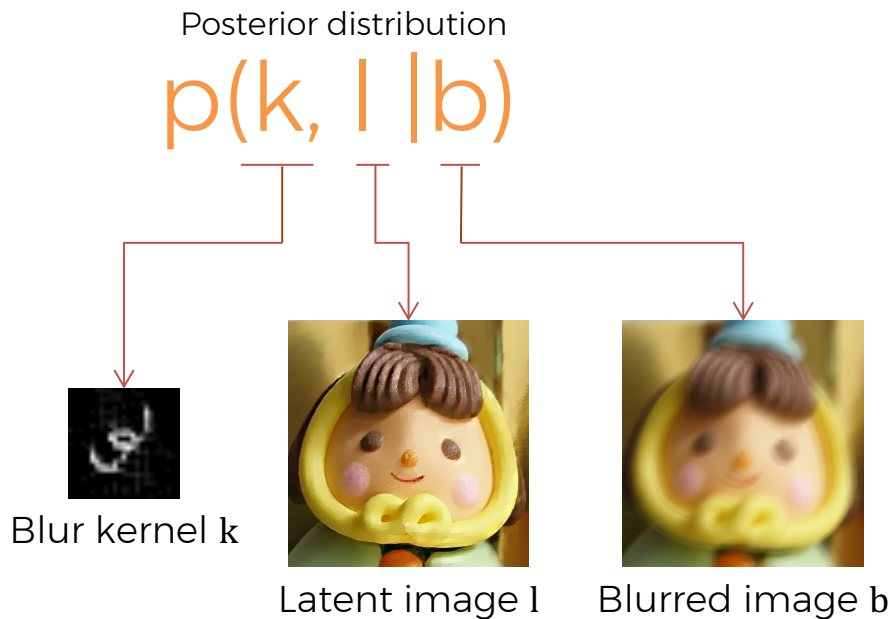
# Recent Popular Approaches

- Maximum Posterior (MAP) based
  - Variational Bayesian based
  - Edge Prediction based
- [Shan et al. SIGGRAPH 2008], [Krishnan et al. CVPR 2011], [Xu et al. CVPR 2013], ...
  - Seek the most probable solution, which maximizes a posterior distribution
  - Easy to understand
  - Convergence problem

Which one is better?

# MAP based Approaches

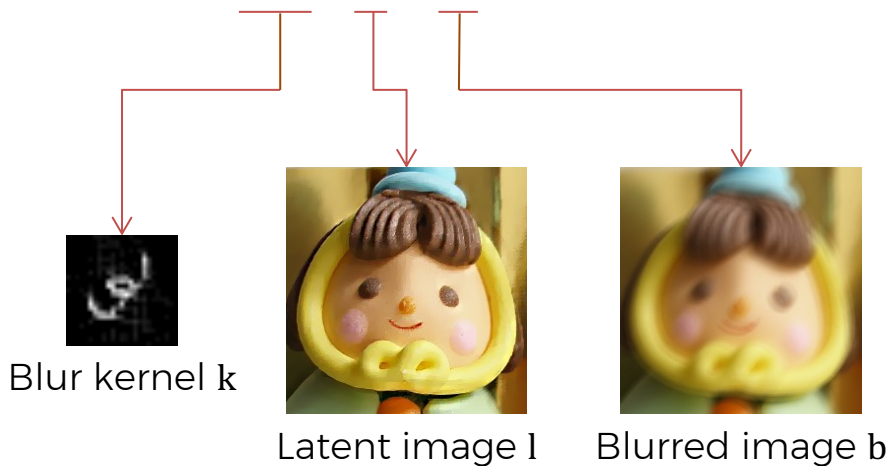
Maximize a joint posterior probability with respect to  $k$  and  $l$



# MAP based Approaches

Bayes rule:

$$\text{Posterior distribution } p(k, l | b) \propto \text{Likelihood } p(b | l, k) \text{ Prior on } l \text{ Prior on } k$$



# MAP based Approaches

Negative log-posterior:

$$\begin{aligned} -\log p(k, l|b) &\Rightarrow -\log p(b|k, l) - \log p(l) - \log p(k) \\ &\Rightarrow \underbrace{\|k * l - b\|^2}_{\text{Data fitting term}} + \underbrace{\rho_l(l)}_{\text{Regularization on latent image } l} + \underbrace{\rho_k(k)}_{\text{Regularization on blur kernel } k} \end{aligned}$$

Data fitting term

Regularization on  
latent image  $l$

Regularization on  
blur kernel  $k$

# MAP based Approaches

Negative log-posterior:

$$\begin{aligned} -\log p(k, l|b) &\Rightarrow -\log p(b|k, l) - \log p(l) - \log p(k) \\ &\Rightarrow \underbrace{\|k * l - b\|^2}_{\text{Data fitting term}} + \underbrace{\rho_l(l)}_{\text{Regularization on latent image } l} + \underbrace{\rho_k(k)}_{\text{Regularization on blur kernel } k} \end{aligned}$$

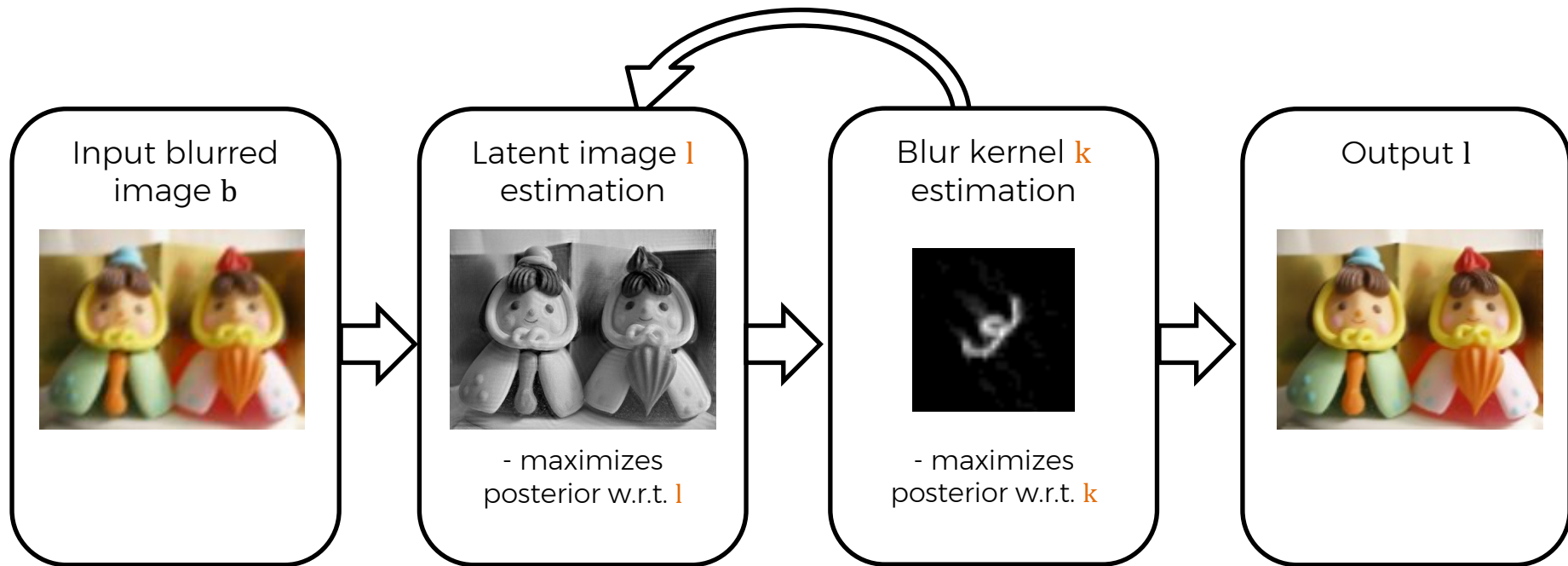
Data fitting term

Regularization on  
latent image  $l$

Regularization on  
blur kernel  $k$

Alternatingly minimize the energy function w.r.t.  $k$  and  $l$

# MAP based Approaches





# MAP based Approaches

- Chan and Wong, TIP 1998
  - Total variation based priors for estimating a parametric blur kernel
- Shan et al. SIGGRAPH 2008
  - First MAP based method to estimate a nonparametric blur kernel
- Krishnan et al. CVPR 2011
  - Normalized sparsity measure, a novel prior on latent images
- Xu et al. CVPR 2013
  - L0 norm based prior on latent images

# Shan et al. SIGGRAPH 2008

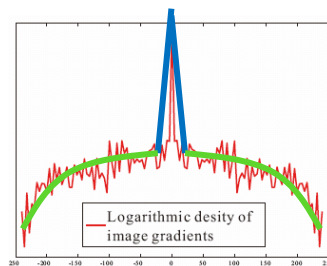
- Carefully designed likelihood & priors

$$p(k, l|b) \propto p(b|l, k)p(l)p(k)$$

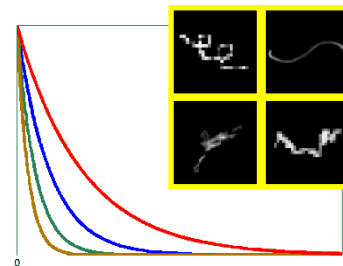
Likelihood based on intensities & derivatives



Natural image statistics based prior on  $l$

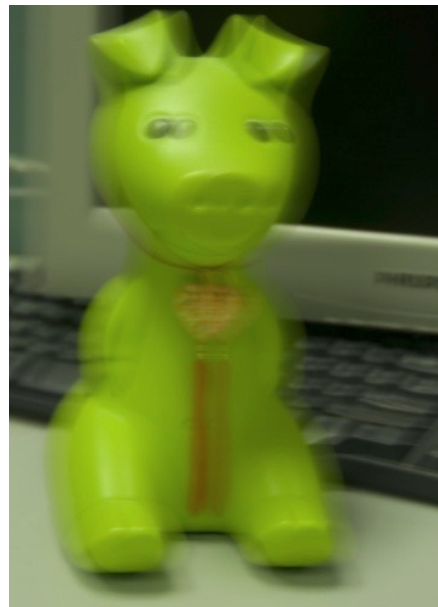


Kernel statistics based prior on  $k$



# Shan et al. SIGGRAPH 2008

- A few minutes for a small image
- High-quality results



# Shan et al. SIGGRAPH 2008

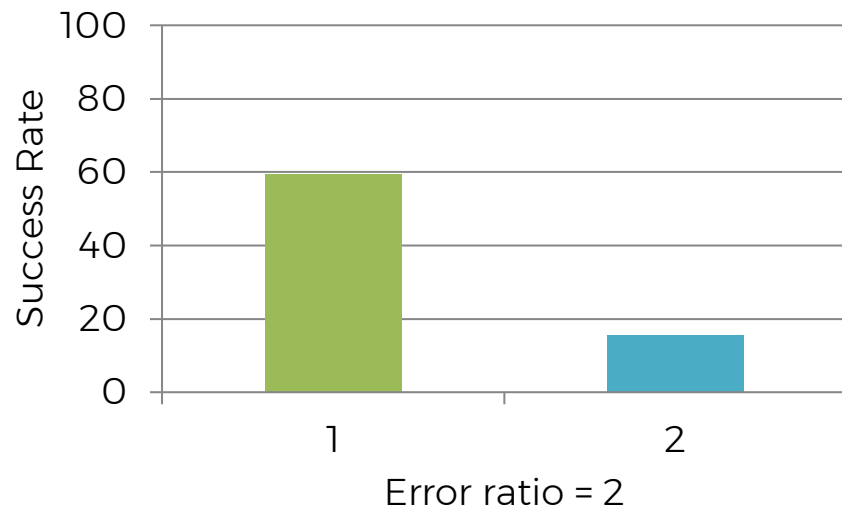
- Convergence problem
  - Often converge to the no-blur solution [Levin et al. CVPR 2009]
  - Natural image priors prefer blurry images



Shan et al. SIGGRAPH 2008



Fergus et al. SIGGRAPH  
2006  
(variational Bayesian based)



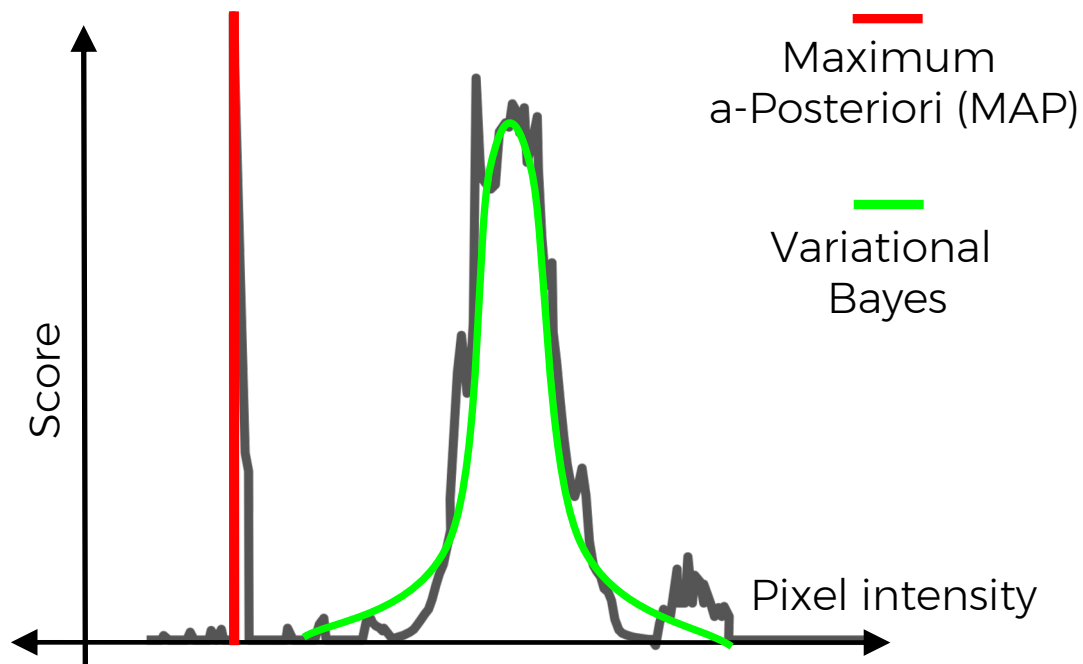
# Recent Popular Approaches

- Maximum Posterior (MAP) based
  - Variational Bayesian based
  - Edge Prediction based
- [Fergus et al. SIGGRAPH 2006], [Levin et al. CVPR 2009], [Levin et al. CVPR 2011], ...
  - Not seek for one most probable solution, but consider all possible solutions
  - Theoretically more robust
  - Slow

Which one is better?

# Variational Bayesian

MAP v.s. Variational Bayes



- MAP
  - Find the most probable solution
  - May converge to a wrong solution
- Variational Bayesian
  - Approximate the underlying distribution and find the mean
  - More stable
  - Slower

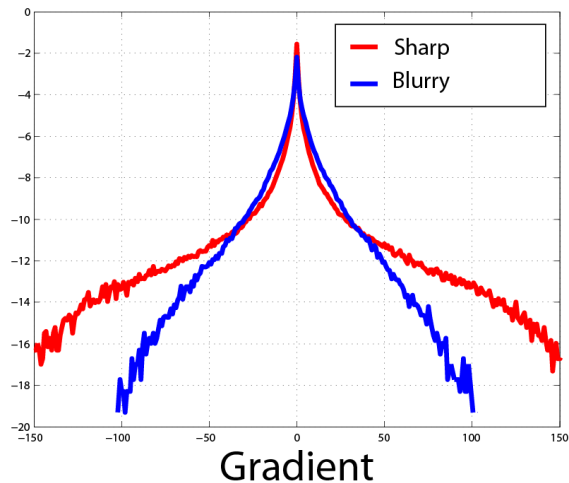
# Variational Bayesian

- Fergus et al. SIGGRAPH 2006
  - First approach to handle non-parametric blur kernels
- Levin et al. CVPR 2009
  - Show that variational Bayesian approaches can perform more robustly than MAP based approaches
- Levin et al. CVPR 2010
  - EM based efficient approximation to variational Bayesian approach

# Fergus et al. SIGGRAPH 2006

- Posterior distribution

$$p(k, l|b) \propto p(b|k, l)p(l)p(k)$$





# Fergus et al. SIGGRAPH 2006

- Find an approximate distribution by minimizing Kullback-Leibler (KL) divergence

$$\arg \min_{q(k), q(l), q(\sigma^{-2})} KL(\underbrace{q(k)q(l)q(\sigma^{-2})}_{\downarrow} || p(k, l|b))$$

approximate distributions for blur kernel  $k$ ,  
latent image  $l$ , and noise variance  $\sigma^2$

- cf MAP based approach:

$$\arg \min_{k, l} p(k, l|b)$$

# Fergus et al. SIGGRAPH 2006

- First method to estimate a nonparametric blur kernel
- Complex optimization
- Slow: more than an hour for a small image



# Recent Popular Approaches

- Maximum Posterior (MAP) based
  - Variational Bayesian based
  - Edge Prediction based
- [Cho & Lee. SIGGRAPH Asia 2009], [Xu et al. ECCV 2010], [Hirsch et al. ICCV 2011], ...
  - Explicitly try to recover sharp edges using heuristic image filters
  - Fast
  - Proven to be effective in practice, but hard to analyze because of heuristic steps

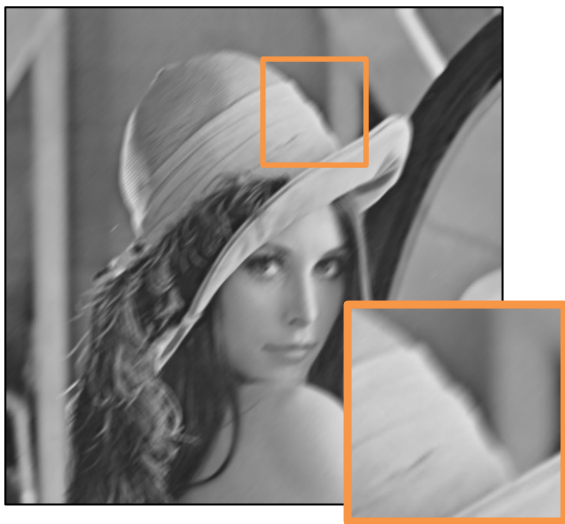
Which one is better?

# Edge Prediction based Approaches

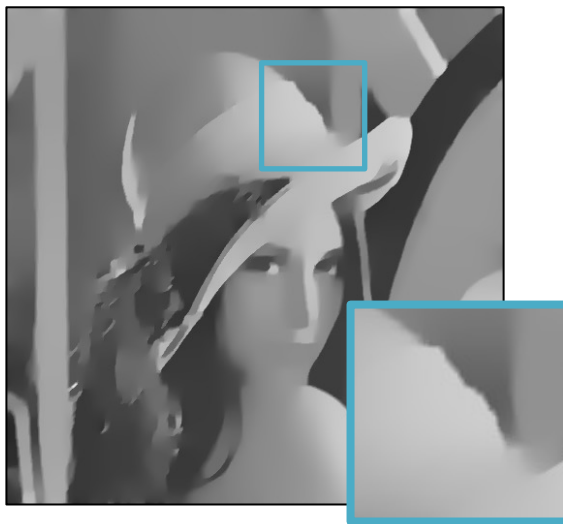
- Joshi et al. CVPR 2008
  - Proposed sharp edge prediction to estimate blur kernels
  - No iterative estimation
  - Limited to small scale blur kernels
- Cho & Lee, SIGGRAPH Asia 2009
  - Proposed sharp edge prediction to estimate large blur kernels
  - Iterative framework
  - State-of-the-art results & very fast
- Cho et al. CVPR 2010
  - Applied Radon transform to estimate a blur kernel from blurry edge profiles
  - Small scale blur kernels
- Xu et al. ECCV 2010
  - Proposed a prediction scheme based on structure scales as well as gradient magnitudes
- Hirsch et al. ICCV 2011
  - Applied a prediction scheme to estimate spatially-varying camera shakes

# Cho & Lee, SIGGRAPH Asia 2009

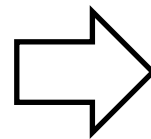
- Key idea: blur can be estimated from a few edges  
➔ No need to restore every detail for kernel estimation



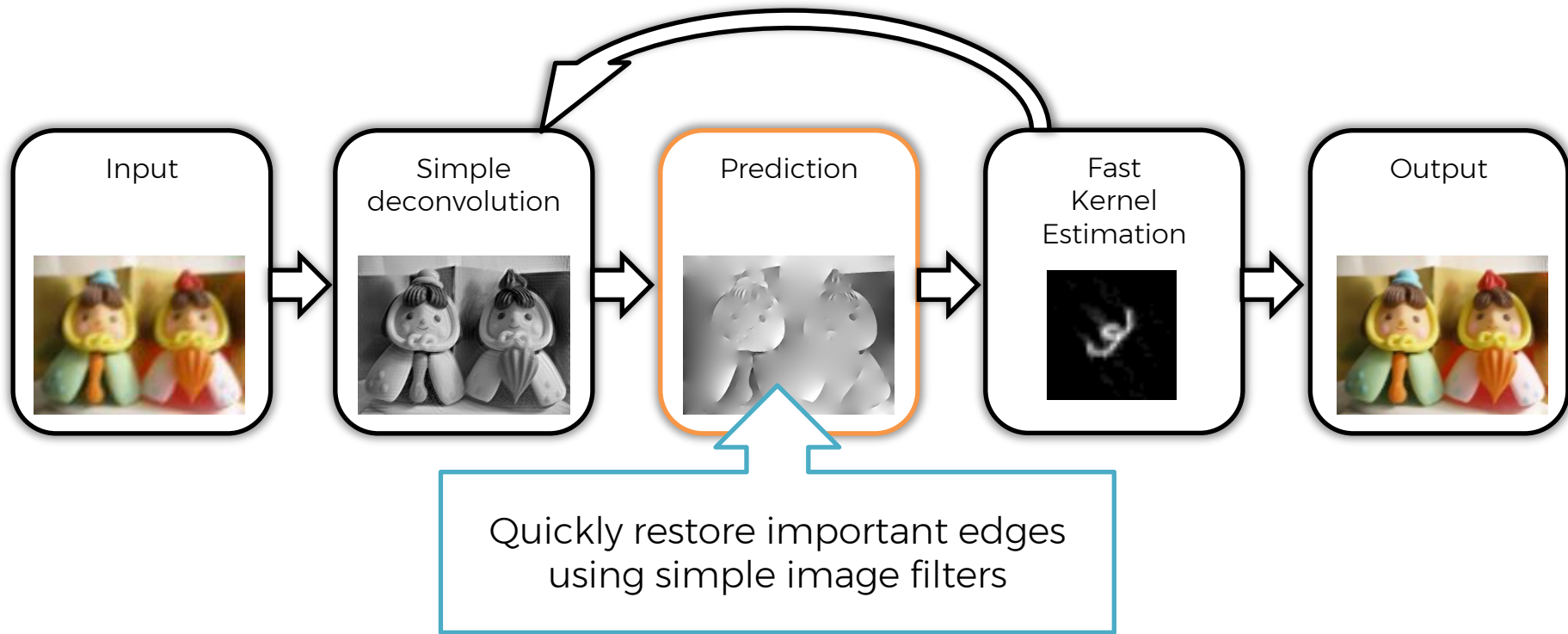
Blurred image



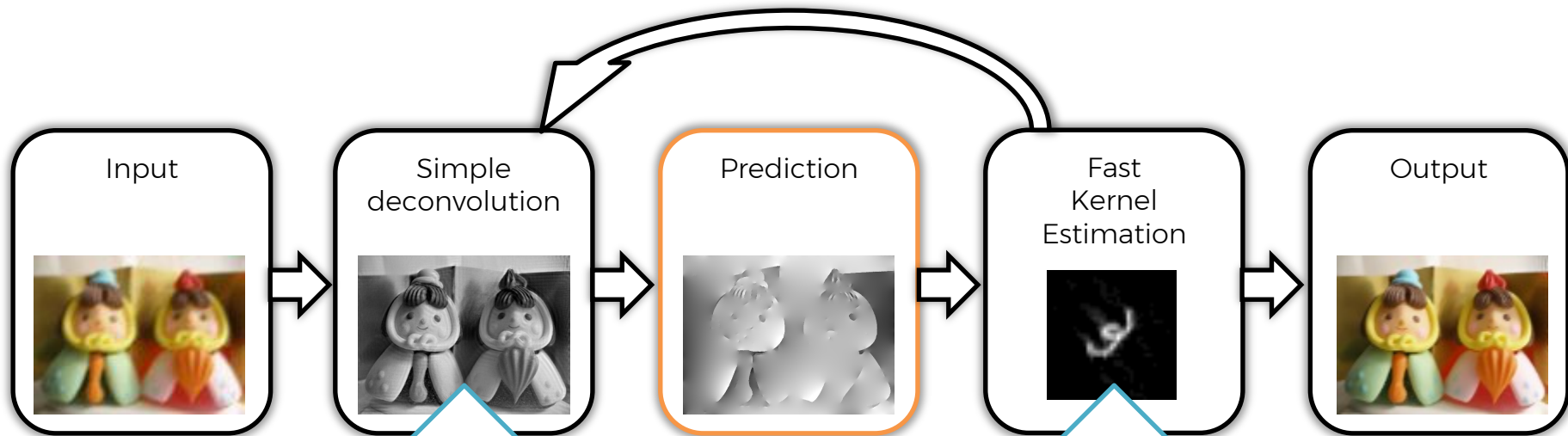
Latent image with only a few edges and no texture



# Cho & Lee, SIGGRAPH Asia 2009

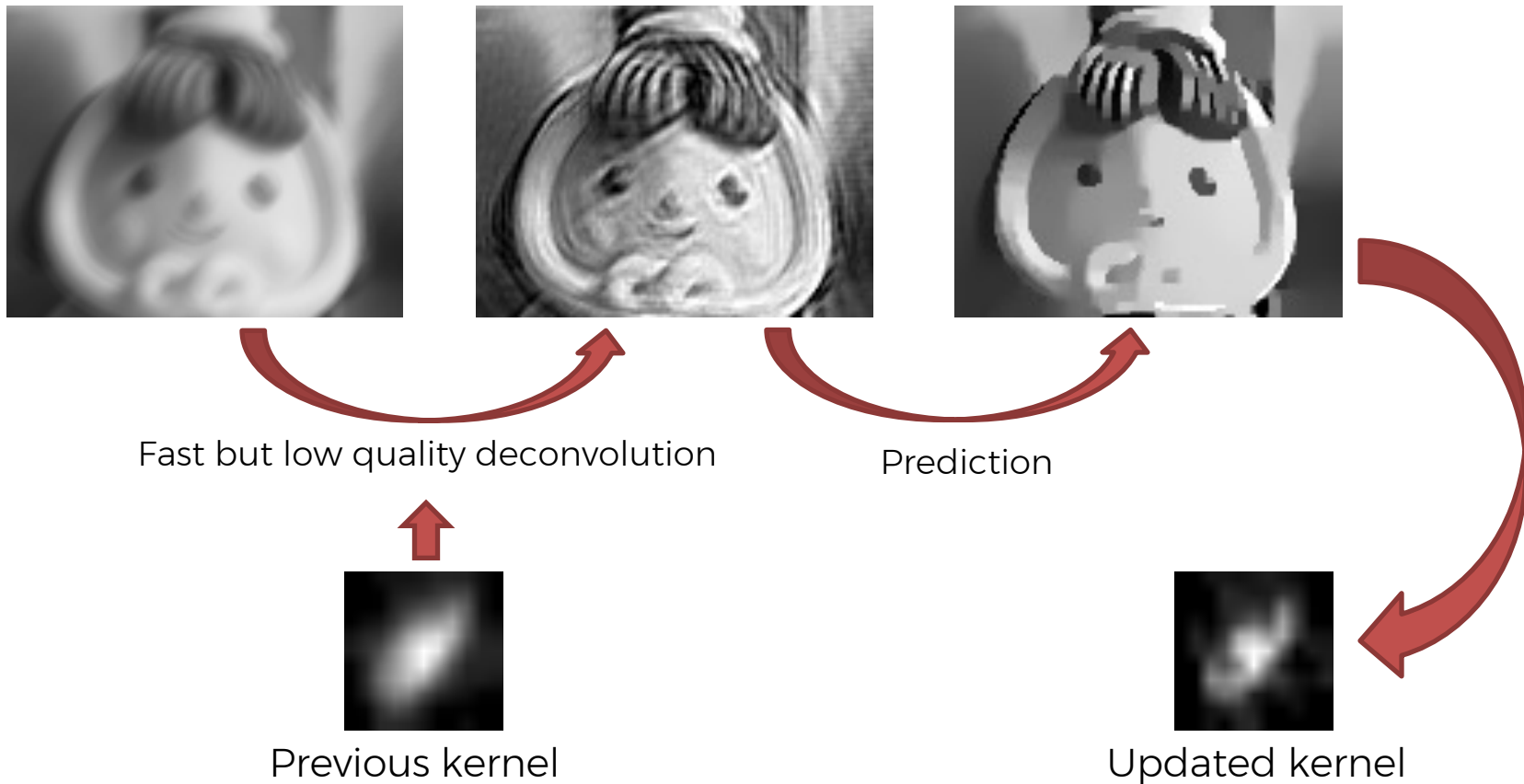


# Cho & Lee, SIGGRAPH Asia 2009



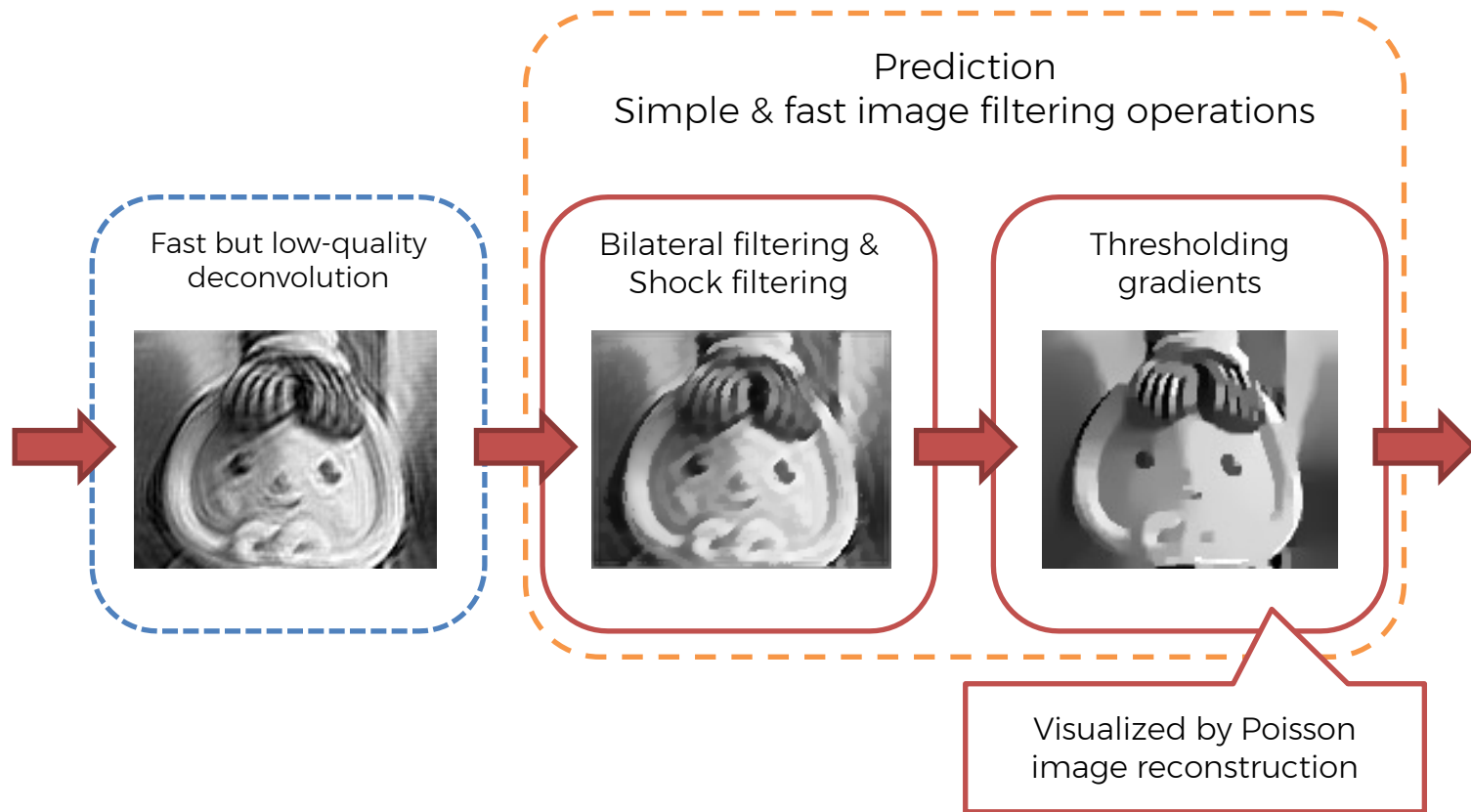
Do not need complex priors for the latent image and the blur kernel  
→ Significantly reduce the computation time

# Cho & Lee, SIGGRAPH Asia 2009





# Cho & Lee, SIGGRAPH Asia 2009



# Cho & Lee, SIGGRAPH Asia 2009



Blurry input



Deblurring result

- State of the art results
- A few seconds
- 1Mpix image
- in C++



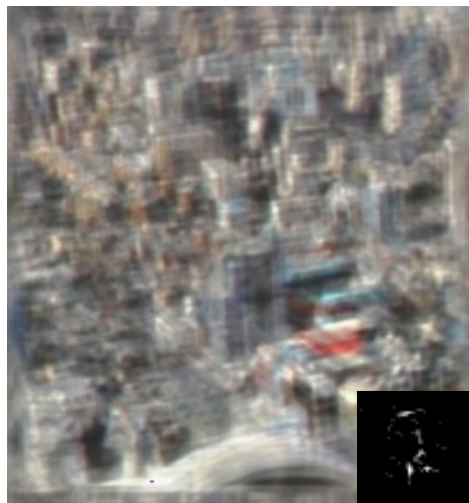
Blur kernel

# Xu & Jia, ECCV 2010

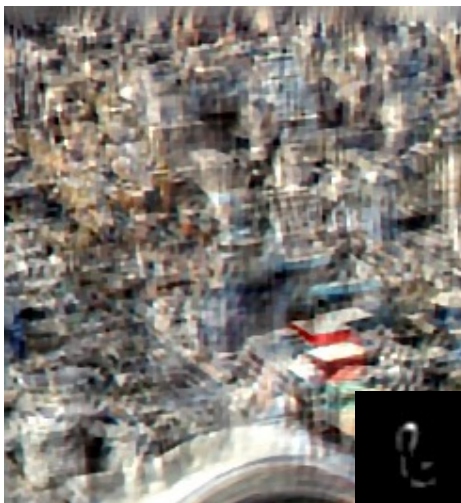
- Extended edge prediction to handle blur larger than image structures



Blurred image



Fergus et al.  
SIGGRAPH 2006



Shan et al.  
SIGGRAPH 2008

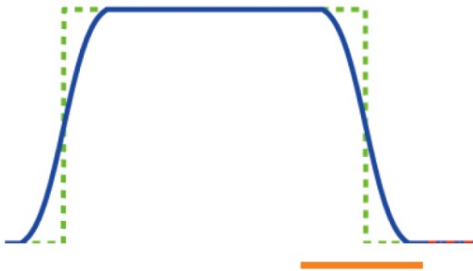
For this complex scene, most methods fail to estimate a correct blur kernel. Why?

# Xu & Jia, ECCV 2010



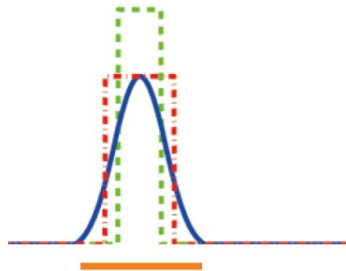
Blur < structures

- Each blurry pixel is caused by one edge
- Easy to figure out the original sharp structure

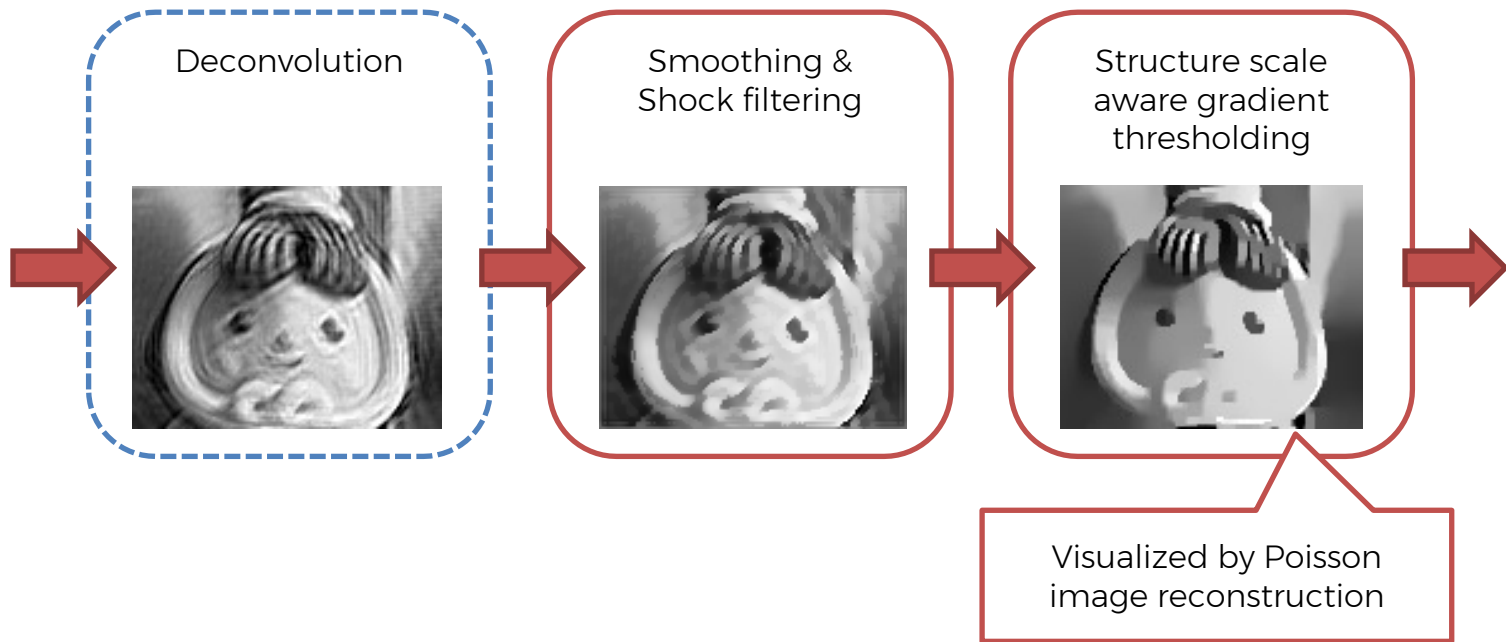


Blur > structures

- Hard to tell which blur is caused by which edge
- Most method fails



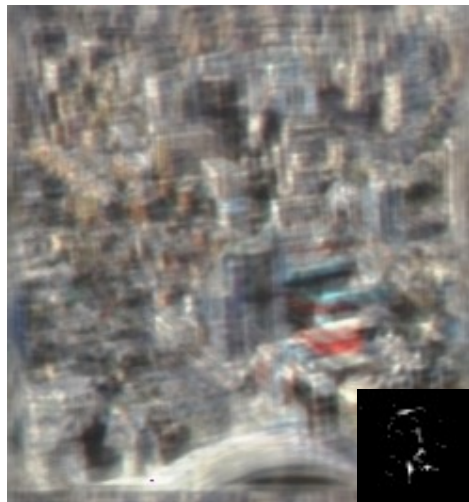
# Xu & Jia, ECCV 2010



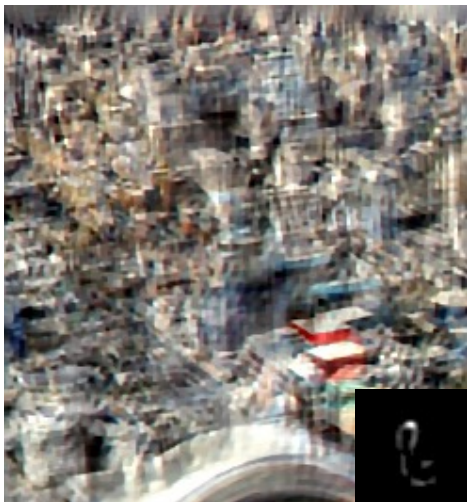
# Xu & Jia, ECCV 2010



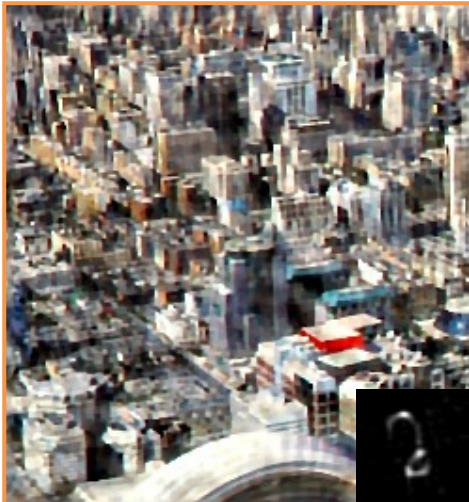
Blurred image



Fergus et al.  
SIGGRAPH 2006



Shan et al.  
SIGGRAPH 2008



Xu & Jia, ECCV 2010

# Recent Popular Approaches

- Maximum Posterior (MAP) based
- Variational Bayesian based
- Edge Prediction based

Which one is better?

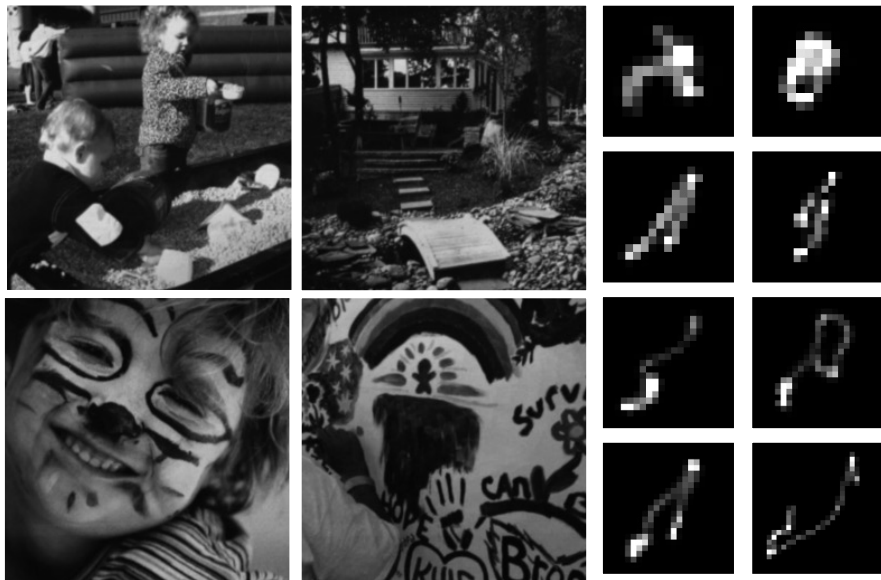
# Benchmarks

- Many different methods...
- Which one is the best?
  - Quality
  - Speed
- Different works report different benchmark results
  - Depending on test data
  - Levin et al. CVPR 2009, 2010
  - Köhler et al. ECCV 2012



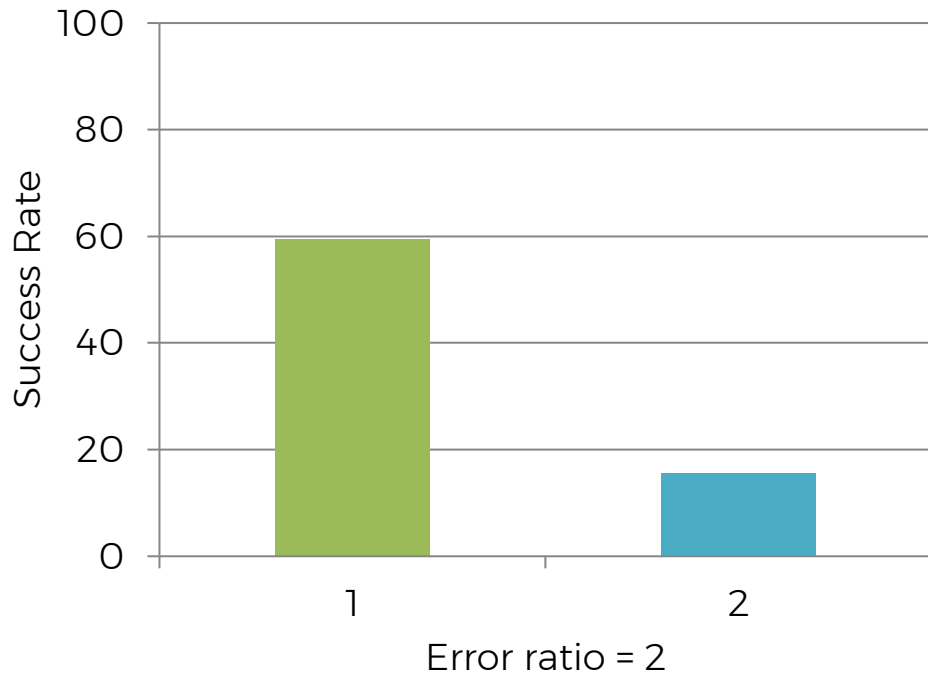
# Benchmarks

- Levin et al. CVPR 2009
  - Provide a dataset
    - 32 test images
    - 4 clear images (255x255)
    - 8 blur kernels (10x10 ~ 25x25)
    - One of the most widely used datasets
  - Evaluate blind deconvolution methods using the dataset



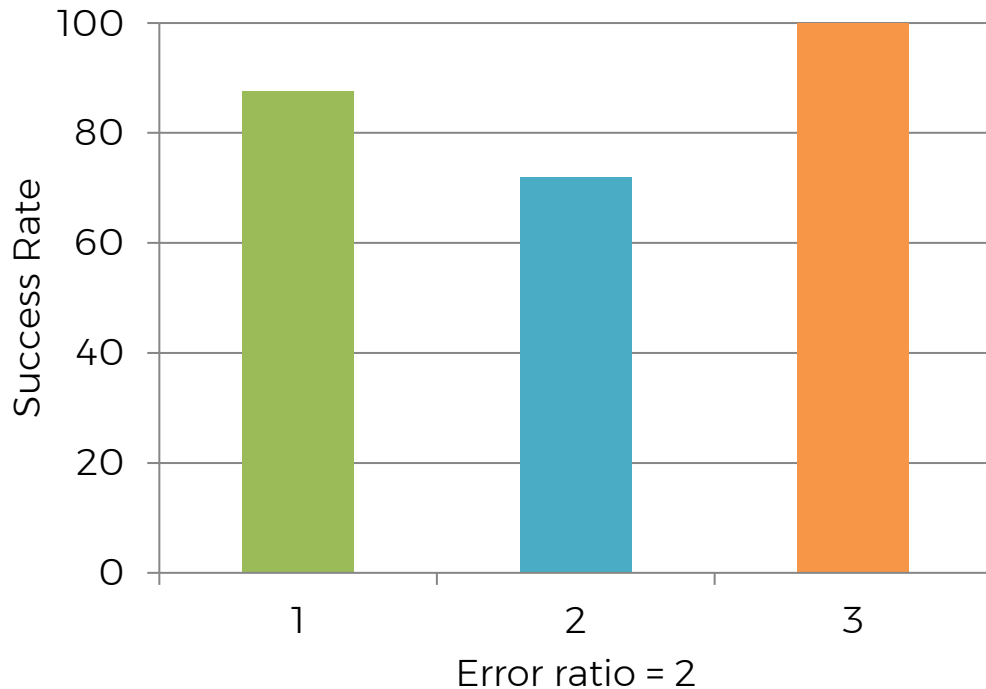
# Benchmarks

- Levin et al. CVPR 2009
  - Counted the number of successful results



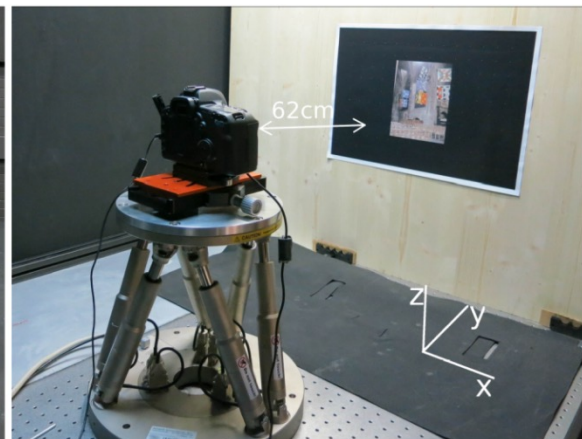
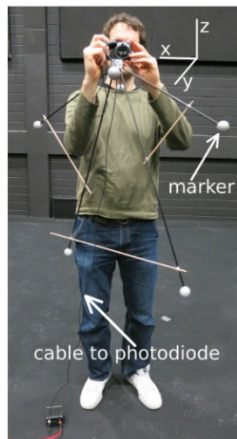
# Benchmarks

- Cho & Lee, SIGGRAPH Asia 2009
  - Comparison based on Levin et al.'s dataset
  - Slightly different parameter settings



# Benchmarks

- Köhler et al. ECCV 2012
  - Record and analyze real camera motions
    - Recorded 6D camera shakes in the 3D space using markers
    - Played back camera shakes using a robot arm
  - Provide a benchmark dataset based on real camera shakes
  - Provide benchmark results for recent state-of-the-art methods



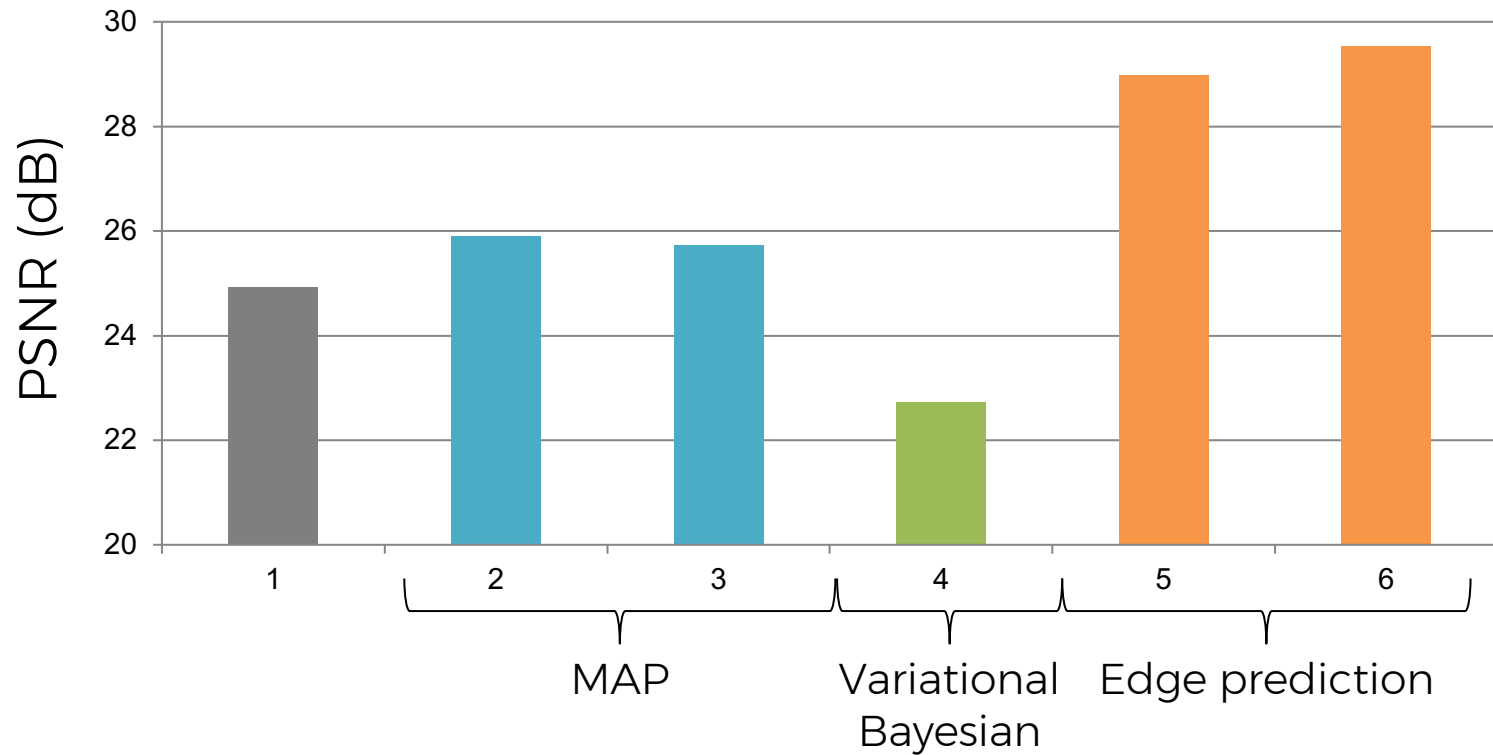
# Benchmarks

- Köhler et al. ECCV 2012
  - Dataset
    - 48 test images
    - 4 sharp images
    - 12 non-uniform camera shakes



# Benchmarks

- Köhler et al. ECCV 2012



# Benchmarks

- Benchmark results depend on
  - Implementation details & tricks
  - Benchmark datasets
  - Parameters used in benchmarks
- But, in general, more recent one shows better quality
- Speed?
  - Edge prediction > MAP >> Variational Bayesian

# Blind Deconvolution

- Introduction
- Recent popular approaches
- Non-uniform blur



# Convolution based Blur Model

- Uniform and spatially invariant blur



# Real Camera Shakes: Spatially Variant!



# Uniform Blur Model Assumes



x & y translational  
camera shakes



Planar scene

# Real Camera Shakes

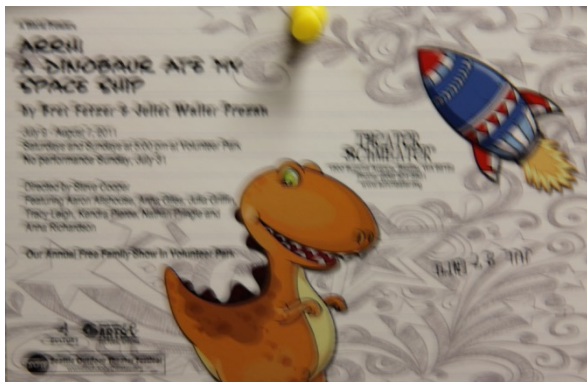


6D real camera motion

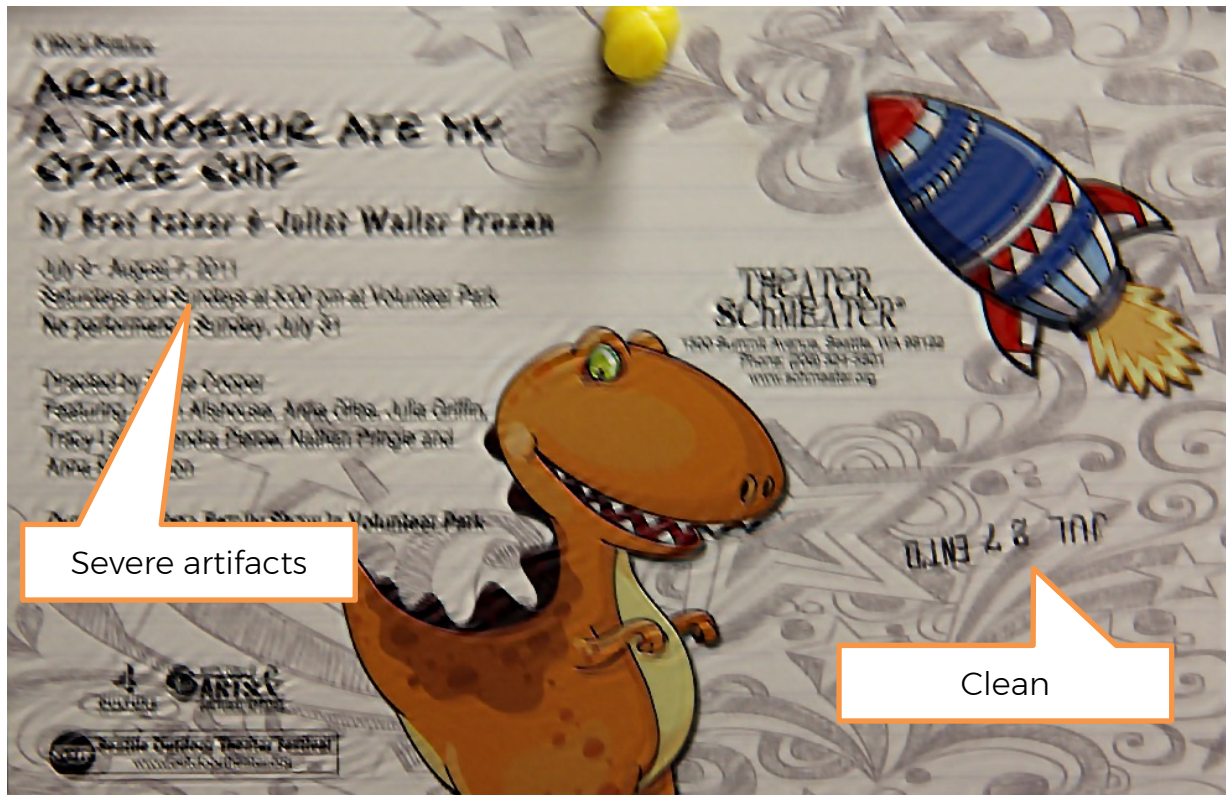


Different depths

# Real Blurred Image



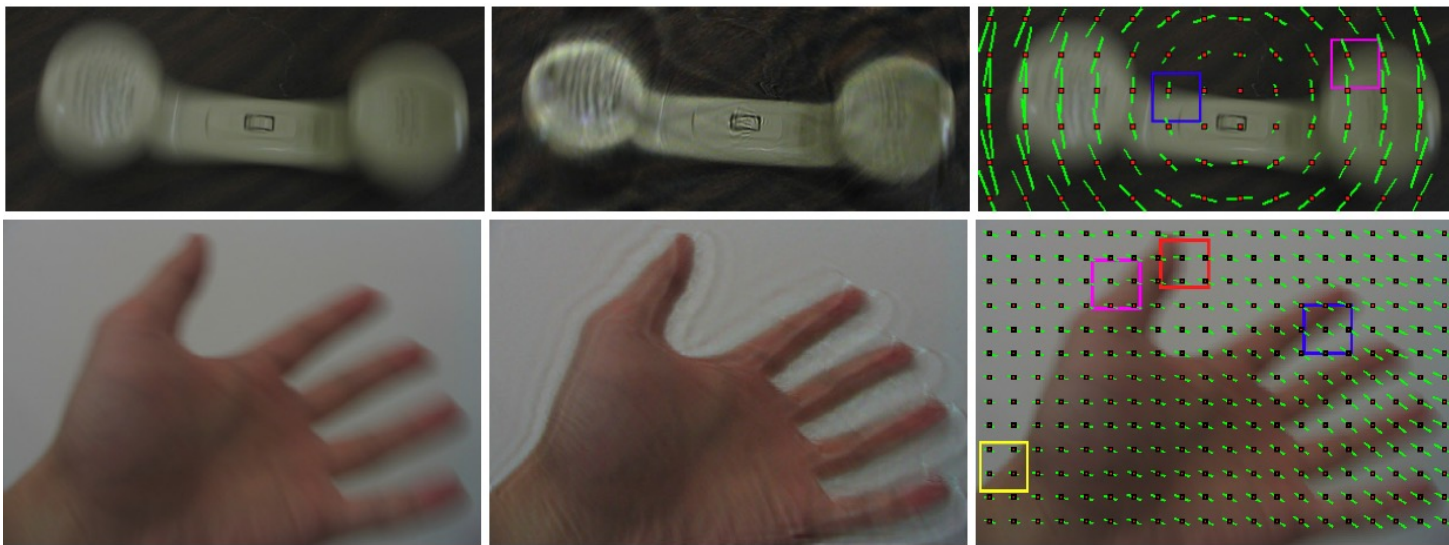
Non-uniformly blurred image



Uniform deblurring result

# Pixel-wise Blur Model

- Dai and Wu, CVPR 2008
  - Estimate blur kernels for every pixel from a single image
  - Severely ill-posed
  - Parametric blur kernels



# Pixel-wise Blur Model

- Tai et al. CVPR 2008
  - Hybrid camera to capture hi-res image & low-res video
  - Estimate per-pixel blur kernels using low-res video

Hi-res.  
image



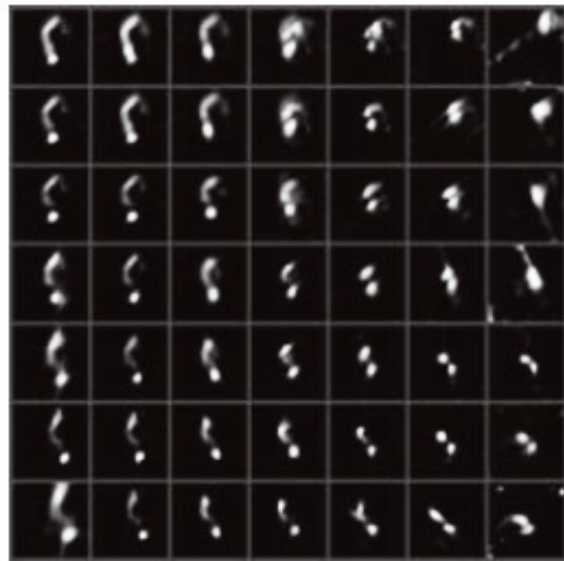
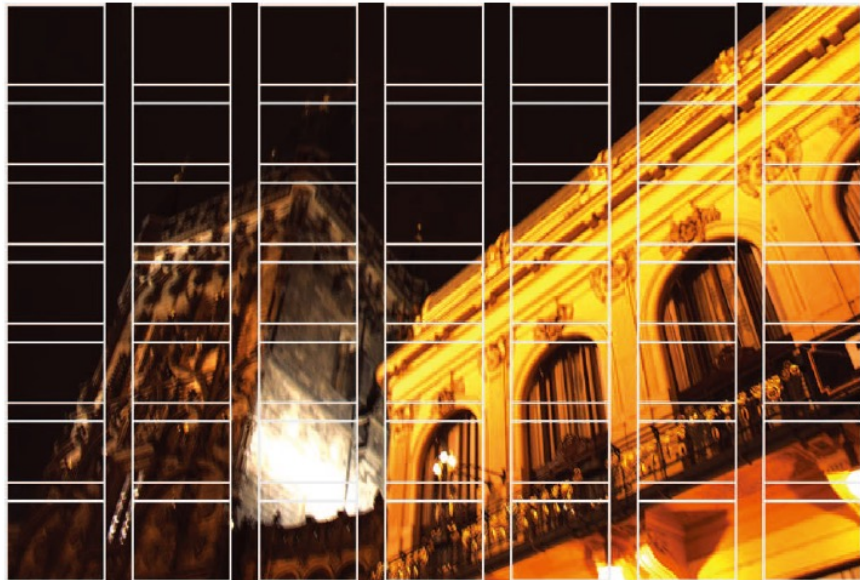
Low-res.  
video



time

# Patch-wise Blur Model

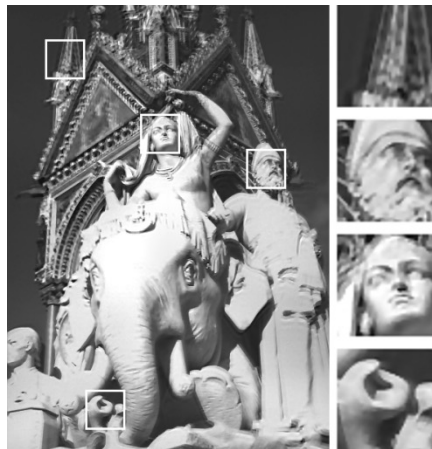
- Sorel and Sroubek, ICIP 2009
  - Estimate per-patch blur kernels from a blurred image and an underexposed noisy image





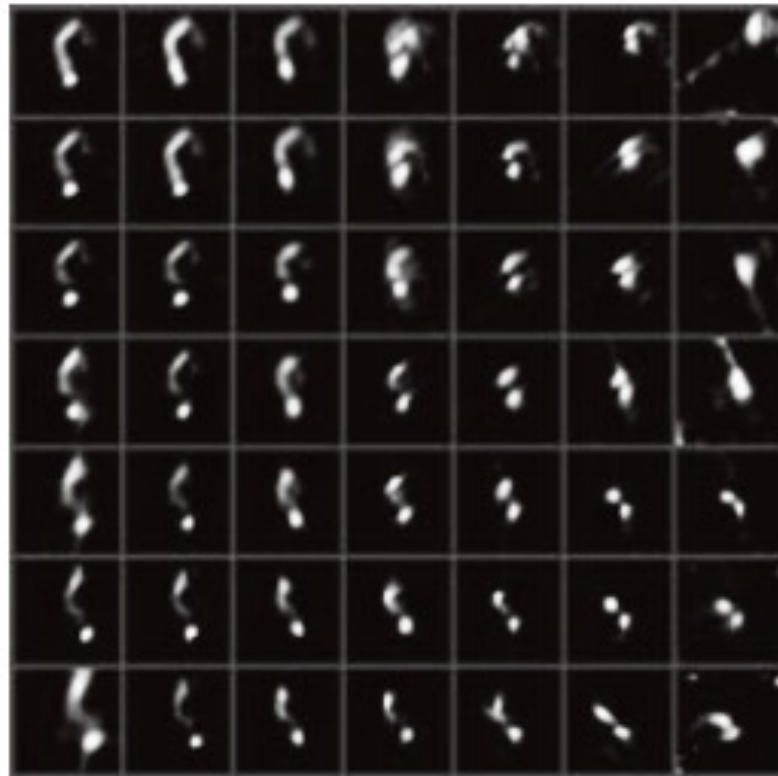
# Patch-wise Blur Model

- Hirsch et al. CVPR 2010
  - Efficient filter flow (EFF) framework
  - More accurate approximation than the naïve patch-wise blur model
- Harmeling et al. NIPS 2010
  - Estimate per-patch blur kernels based on EFF from a single image

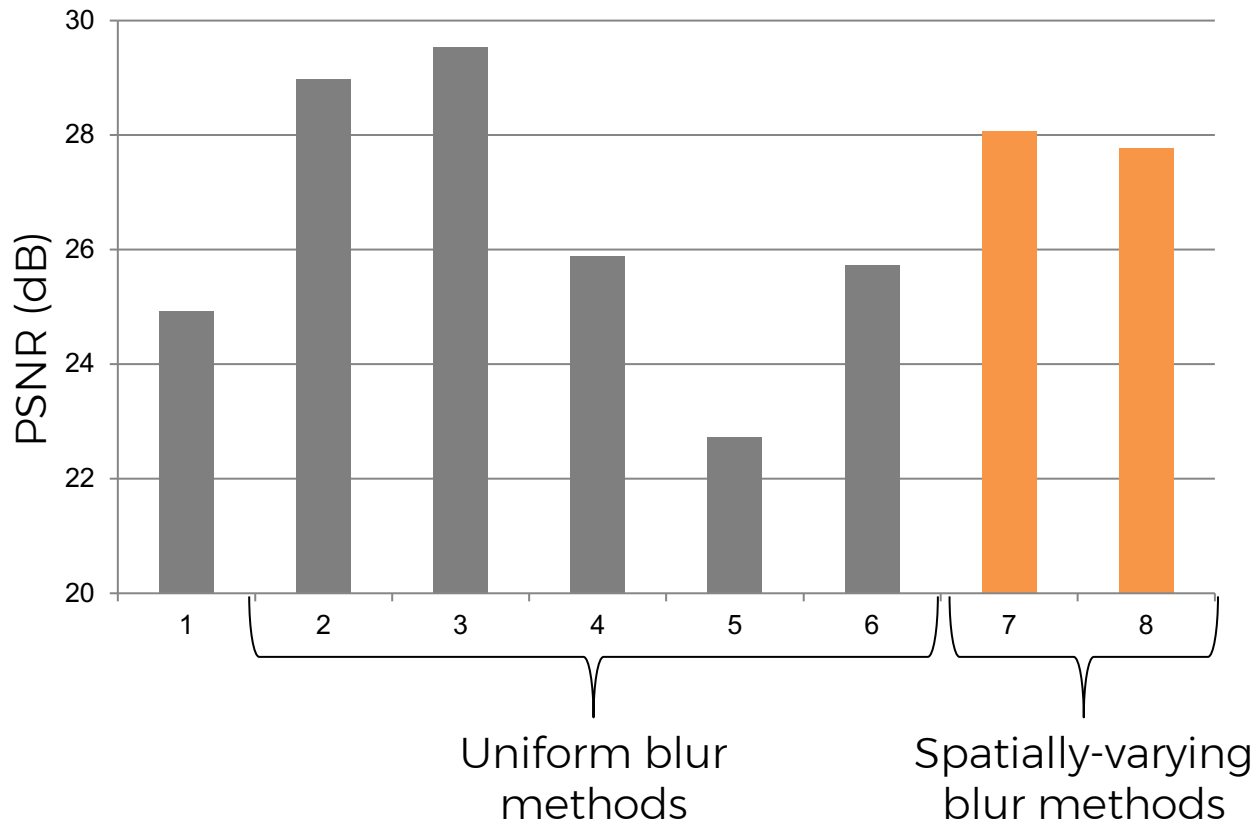


# Patch-wise Blur Model

- Approximation
  - More patches  $\rightarrow$  more accurate
- Computationally efficient
  - Patch-wise uniform blur
  - FFTs can be used
- Physically implausible blurs
  - Adjacent blur kernels cannot be very different from each other



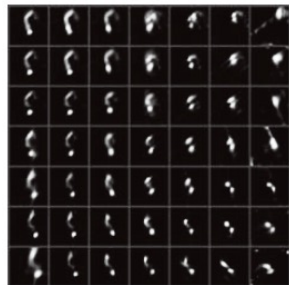
# Benchmark [Köhler et al. ECCV 2012]



Due to high dimensionality, spatially-varying blur methods are less stable.

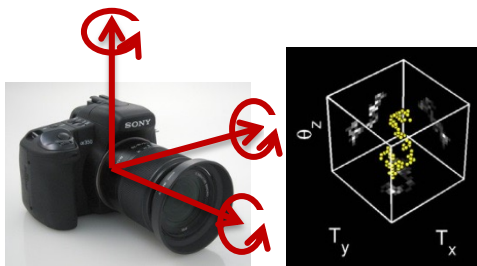
# Summary

- Different blur models



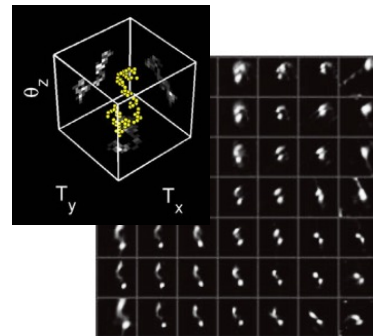
Patch based

Efficient but no global constraint



Projective Motion Path

Globally consistent but inefficient



Hybrid

Efficient & globally consistent

- More realistic than uniform blur model
- Still approximations
  - Real camera motions: 6 DoF + more (zoom-in, depth, etc...)
- High dimensionality
  - Less stable & slower than uniform blur model

# Remaining Challenges



- All methods still fail quite often
- Noise
- Outliers
- Non-uniform blur
- Limited amount of edges
- Speed...
- Etc...

Failure example of Photoshop Shake Reduction

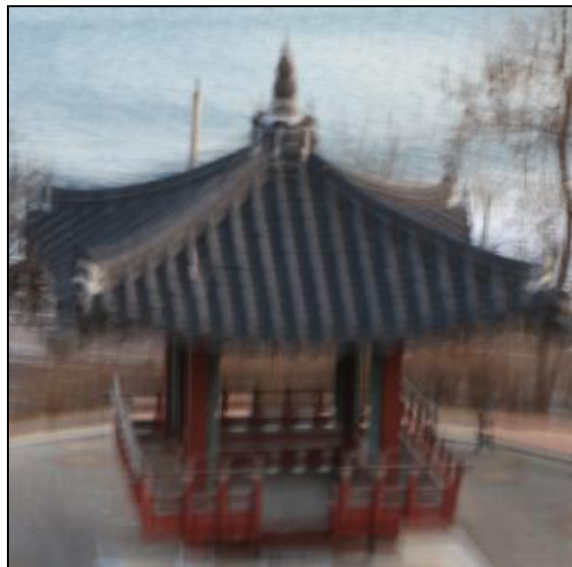
# Image Deblurring

- Introduction
- Blind deconvolution
- Non-blind deconvolution

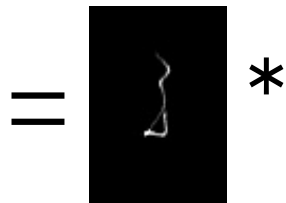
# Non-blind Deconvolution

- Introduction
- Natural image statistics
- High-order natural image statistics
- Ringing artifacts
- Outliers

# Non-blind Deconvolution (Uniform Blur)



Blurred image



Blur kernel

Convolution operator

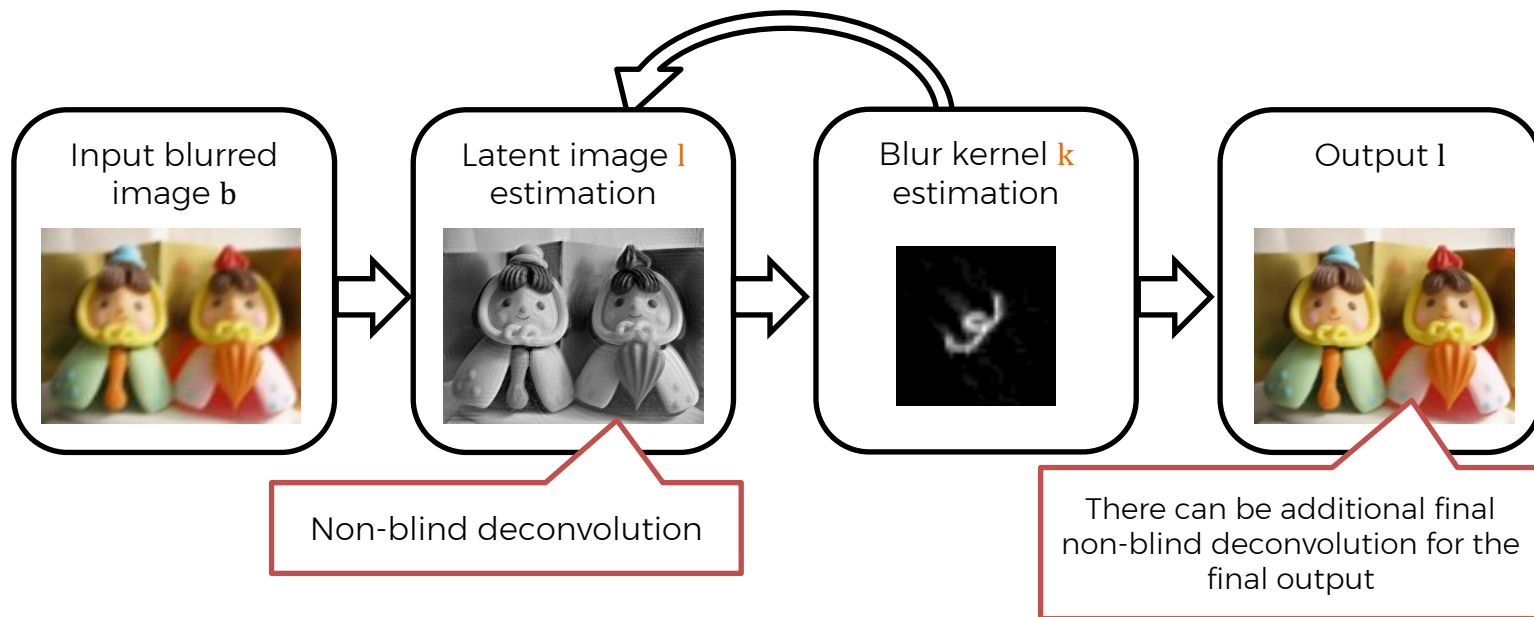


Latent sharp image



# Non-blind Deconvolution

- Key component in many deblurring systems
  - For example, in MAP based blind deconvolution:



# Non-blind Deconvolution



- Wiener filter
- Richardson-Lucy deconvolution
- Rudin et al. Physica 1992
- Bar et al. IJCV 2006
- Levin et al. SIGGRAPH 2007
- Shan et al. SIGGRAPH 2008
- Yuan et al. SIGGRAPH 2008
- Harmeling et al. ICIP 2010
- Etc...

# Ill-Posed Problem

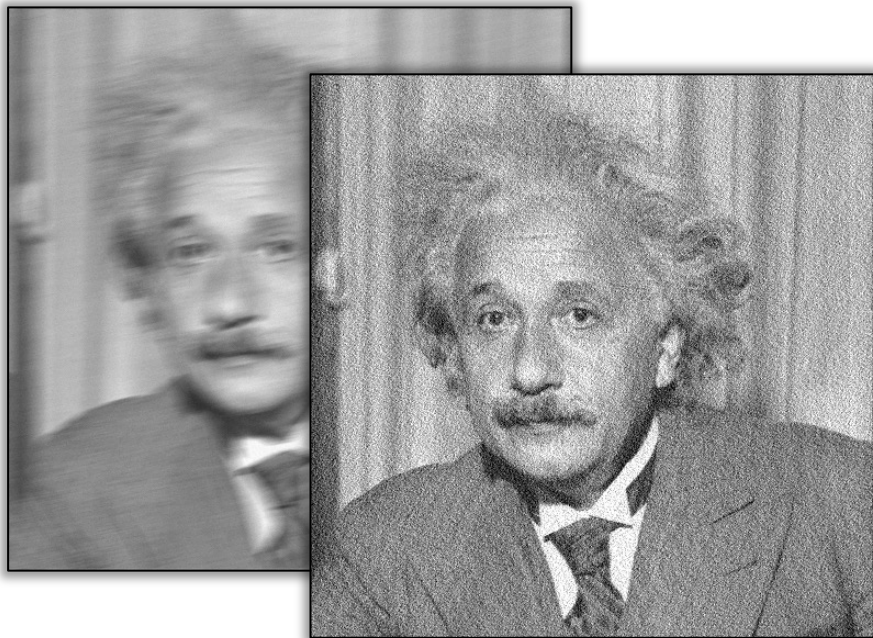
- Even if we know the true blur kernel, we cannot restore the latent image perfectly, because



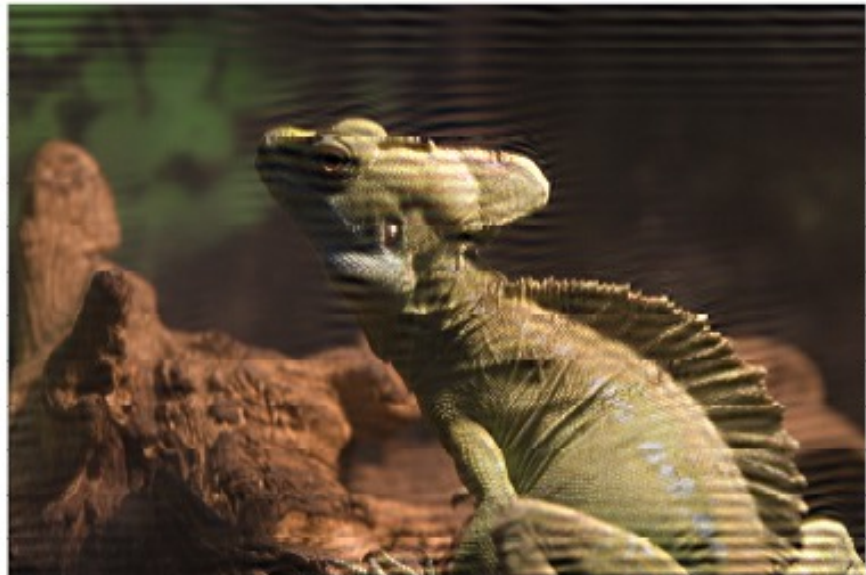
- Loss of high-freq info & noise  $\approx$  denoising & super-resolution

# Ill-Posed Problem

- Deconvolution amplifies noise as well as sharpens edges

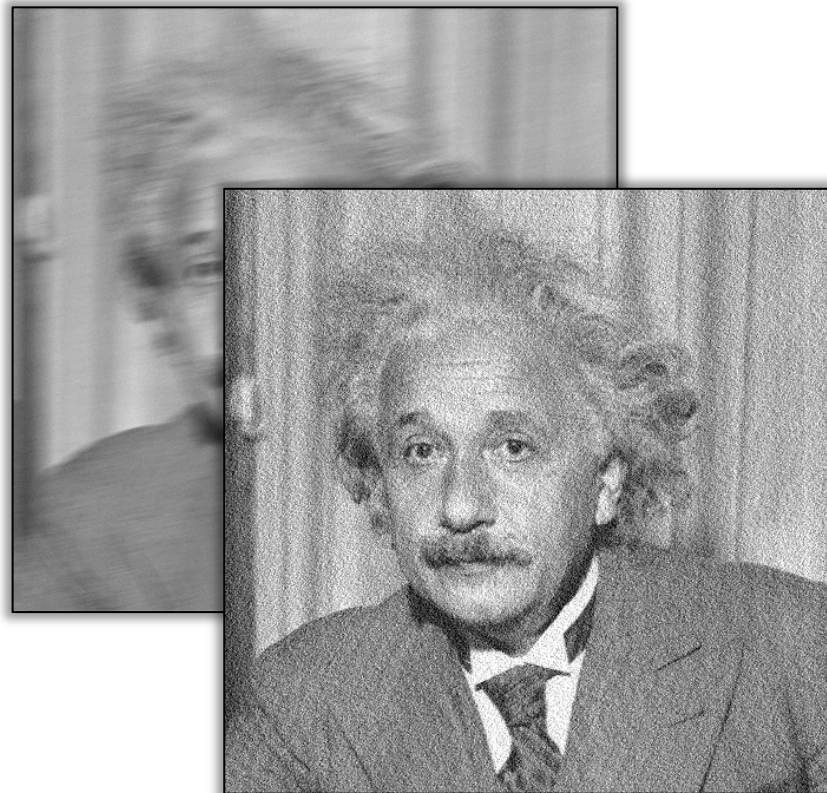


- Ringing artifacts
  - Inaccurate blur kernels, outliers cause ringing artifacts



# Classical Methods

- Popular methods
  - Wiener filtering
  - Richardson-Lucy deconvolution
  - Constrained least squares
- Matlab Image Processing Toolbox
  - `deconvwnr`, `deconvlucy`,  
`deconvreg`
- Simple assumption on noise and latent images
  - Simple & fast
  - Prone to noise & artifacts

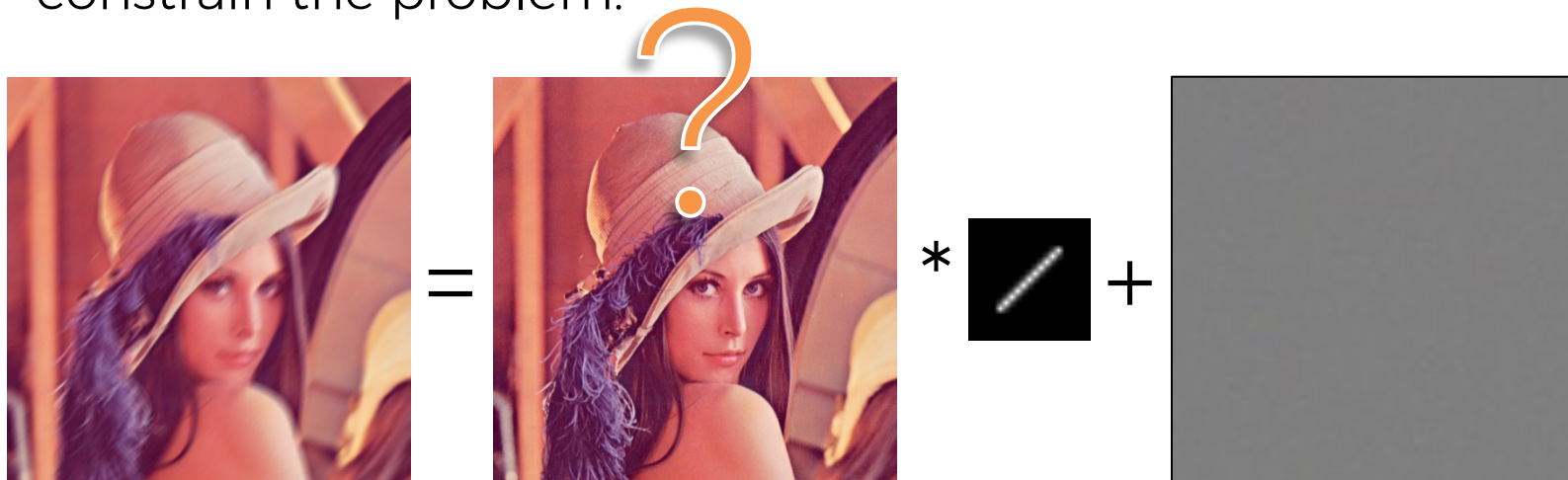


# Non-blind Deconvolution

- Introduction
- Natural image statistics
- High-order natural image statistics
- Ringing artifacts
- Outliers

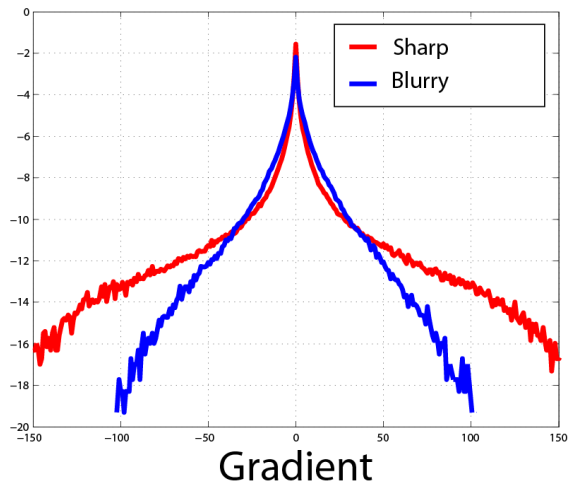
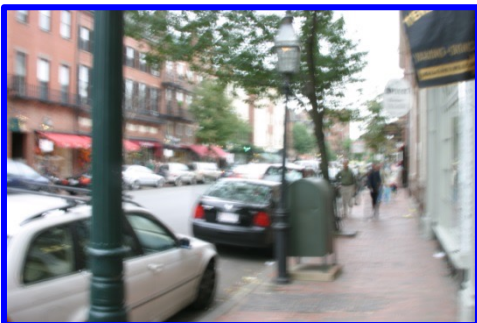
# Natural Image Statistics

- Non-blind deconvolution: ill-posed problem
- We need to assume something on the latent image to constrain the problem.



# Natural Image Statistics

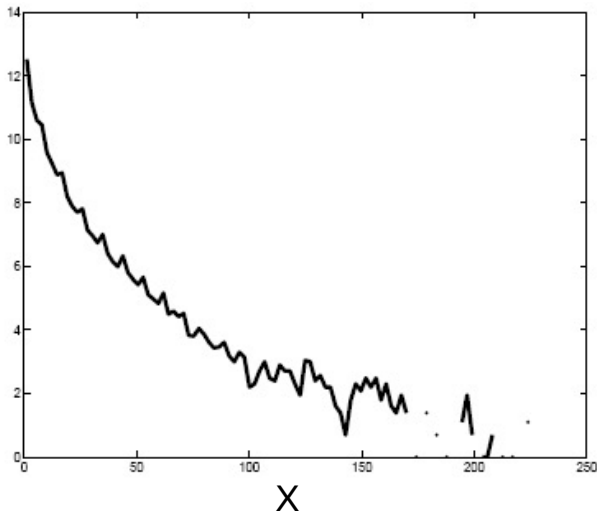
- Natural images have a heavy-tailed distribution on gradient magnitudes
  - Mostly zero & a few edges
  - Levin et al. SIGGRAPH 2007, Shan et al. SIGGRAPH 2008, Krishnan & Fergus, NIPS 2009



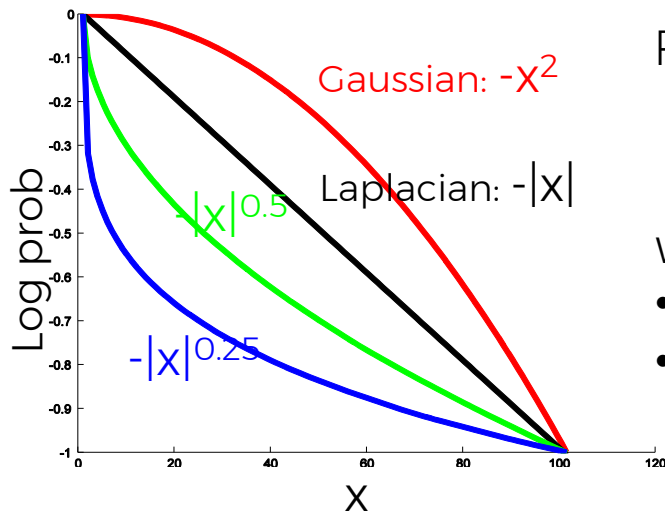


# Natural Image Statistics

- Levin et al. SIGGRAPH 2007
  - Propose a parametric model for natural image priors based on image gradients



Derivative histogram from a natural image



Parametric models

Proposed prior

$$\log p(x) = - \sum_i |\nabla x_i|^\alpha$$

where:

- $x$ : image
- $\alpha$ : model parameter,  $\alpha < 1$

# Natural Image Statistics

- Levin et al. SIGGRAPH 2007

$$l = \arg \min_l \left\{ \underbrace{\|k * l - b\|^2}_{\text{Data term}} + \underbrace{\lambda \sum_i |\nabla l_i|^\alpha}_{\text{Prior}} \right\} \quad (\alpha < 1)$$

Diagram illustrating the optimization process for finding the natural image  $l$  that best fits the data term and the prior term.

The top row shows the optimization process:

- The data term is  $\|k * l - b\|^2$ , where  $k$  is a kernel,  $l$  is the image, and  $b$  is the target image.
- The prior term is  $\lambda \sum_i |\nabla l_i|^\alpha$ , which penalizes high-frequency noise.
- The result is a low-frequency image  $l$  (shown in a green box) that matches the target image  $b$  (shown in a gray box) and has a low prior value (indicated by a blue checkmark).
- The label "Low" is placed below the result image.

The bottom row shows a comparison:

- The data term is the same as in the top row.
- The prior term is high (indicated by an orange X), because the image  $l$  (shown in a green box) is noisy and has high-frequency components.
- The label "High" is placed below the result image.

Orange arrows indicate that the two data terms are equal, but the prior term is lower for the smooth result than for the noisy result.

Equal convolution error

# Natural Image Statistics

- Levin et al. SIGGRAPH 2007



Input



Richardson-Lucy



Gaussian prior

$$\sum_i |\nabla l_i|^2$$

“spread” gradients



Sparse prior

$$\sum_i |\nabla l_i|^{0.8}$$

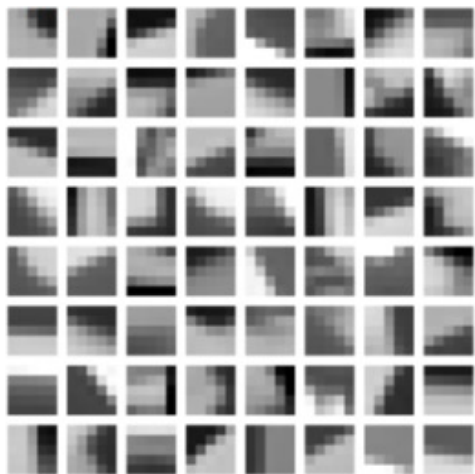
“localizes”  
gradients

# Non-blind Deconvolution

- Introduction
- Natural image statistics
- High-order natural image statistics
- Ringing artifacts
- Outliers

# High-order Natural Image Priors

- Patches, large neighborhoods, ...
- Effective for various kinds of image restoration problems
  - Denoising, inpainting, super-resolution, deblurring, ...

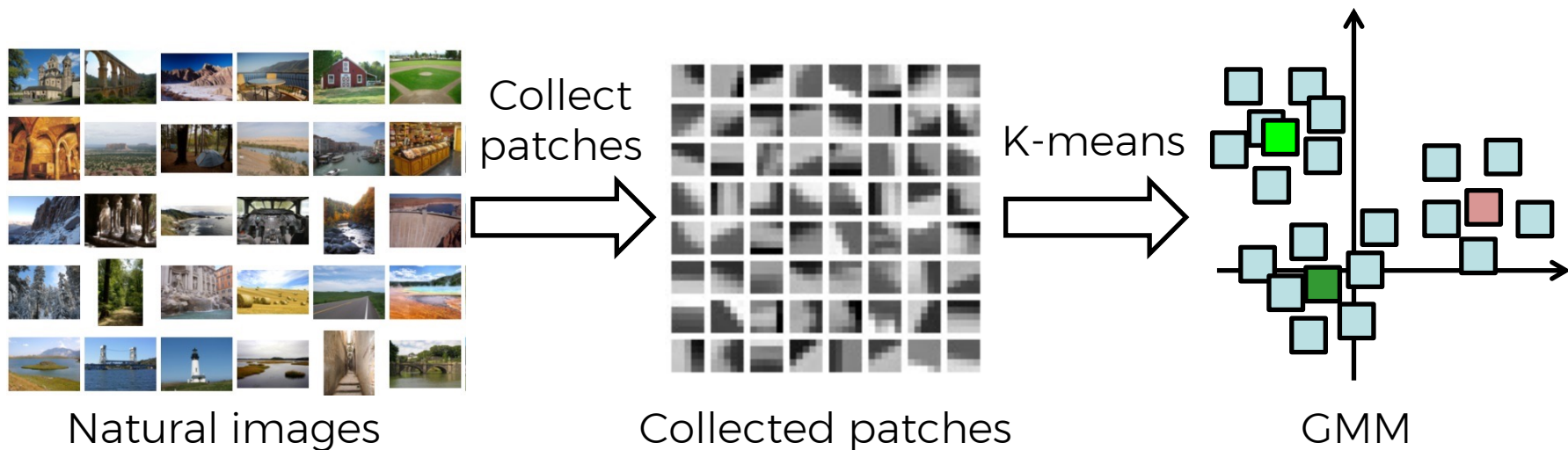


# High-order Natural Image Priors

- Schmidt et al. CVPR 2011
  - Fields of Experts
- Zoran & Weiss, ICCV 2011
  - Trained Gaussian mixture model for natural image patches
- Schuler et al. CVPR 2013
  - Trained Multi-layer perceptron to remove artifacts and to restore sharp patches
- Schmidt et al. CVPR 2013
  - Trained regression tree fields for 5x5 neighborhoods

# High-order Natural Image Priors

- Zoran & Weiss, ICCV 2011
  - Gaussian Mixture Model (GMM) learned from natural images



# High-order Natural Image Priors

- Zoran & Weiss, ICCV 2011
  - Given a patch, we can compute its likelihood based on the GMM.
  - Deconvolution can be done by solving:

$$\arg \min_l \left\{ \|k * l - b\|^2 - \lambda \sum_i \underbrace{\log p(l_i)} \right\}$$

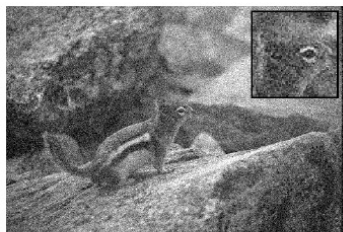
Log-likelihood of a patch  $l_i$  at  $i$ -th pixel  
based on GMM



# High-order Natural Image Priors

- Zoran & Weiss, ICCV 2011

Denoising



(a) Noisy Image - PSNR: 20.17



(b) KSVD - PSNR: 28.72



(c) LLSC - PSNR: 29.30



(d) EPLL GMM - PSNR: 29.39

Deblurring



Blurred image



Krishnan & Fergus  
PSNR: 26.38



Zoran & Weiss  
PSNR: 27.70

# Non-blind Deconvolution

- Introduction
- Natural image statistics
- High-order natural image statistics
- Ringing artifacts
- Outliers

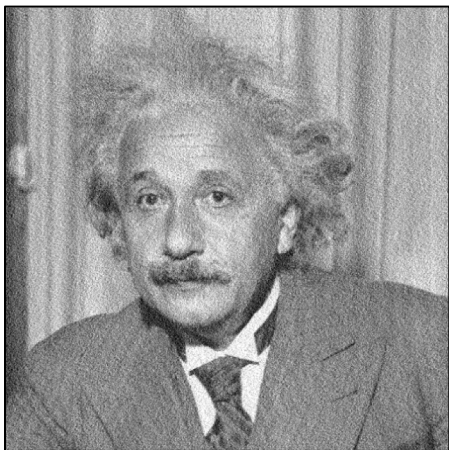
# Ringing Artifacts

- Wave-like artifacts around strong edges
- Caused by
  - Inaccurate blur kernels
  - Nonlinear response curve
  - Etc...

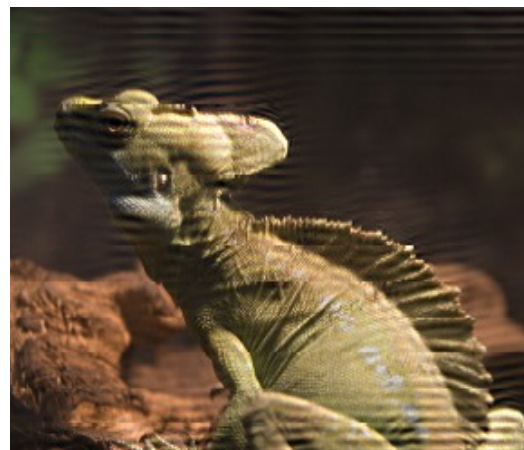


# Ringling Artifacts

- Noise
  - High-freq
  - Independent and identical distribution
  - Priors on image gradients work well

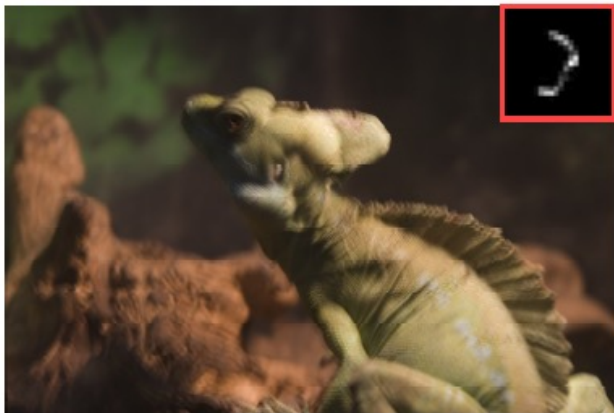


- Ringing
  - Mid-freq
  - Spatial correlation
  - Priors on image gradients are not very effective

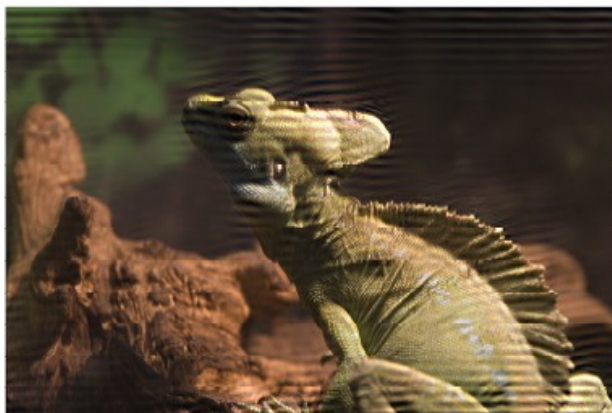


# Ringing Artifacts

- Yuan et al. SIGGRAPH 2007
  - Residual deconvolution & de-ringing
- Yuan et al. SIGGRAPH 2008
  - Multi-scale deconvolution framework based on residual deconvolution



Blurred image



Richardson-Lucy



Yuan et al. SIGGRAPH 2008

# Residual Deconvolution [Yuan et al. SIGGRAPH 2007, 2008]



Blurred image



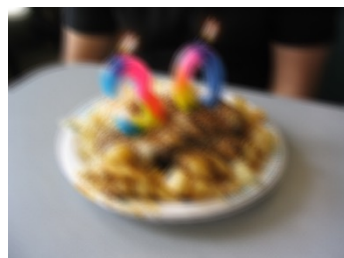
Guide image



Residual deconvolution  
result with less ringing  
artifacts

- Relatively accurate edges, but less details
- Obtained from a deconvolution result from a smaller scale

# Residual Deconvolution [Yuan et al. SIGGRAPH 2007, 2008]



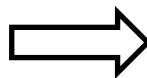
Blurred image



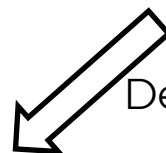
- \*



Guide image



Residual blur



Deconvolution

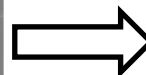


Guide image

+



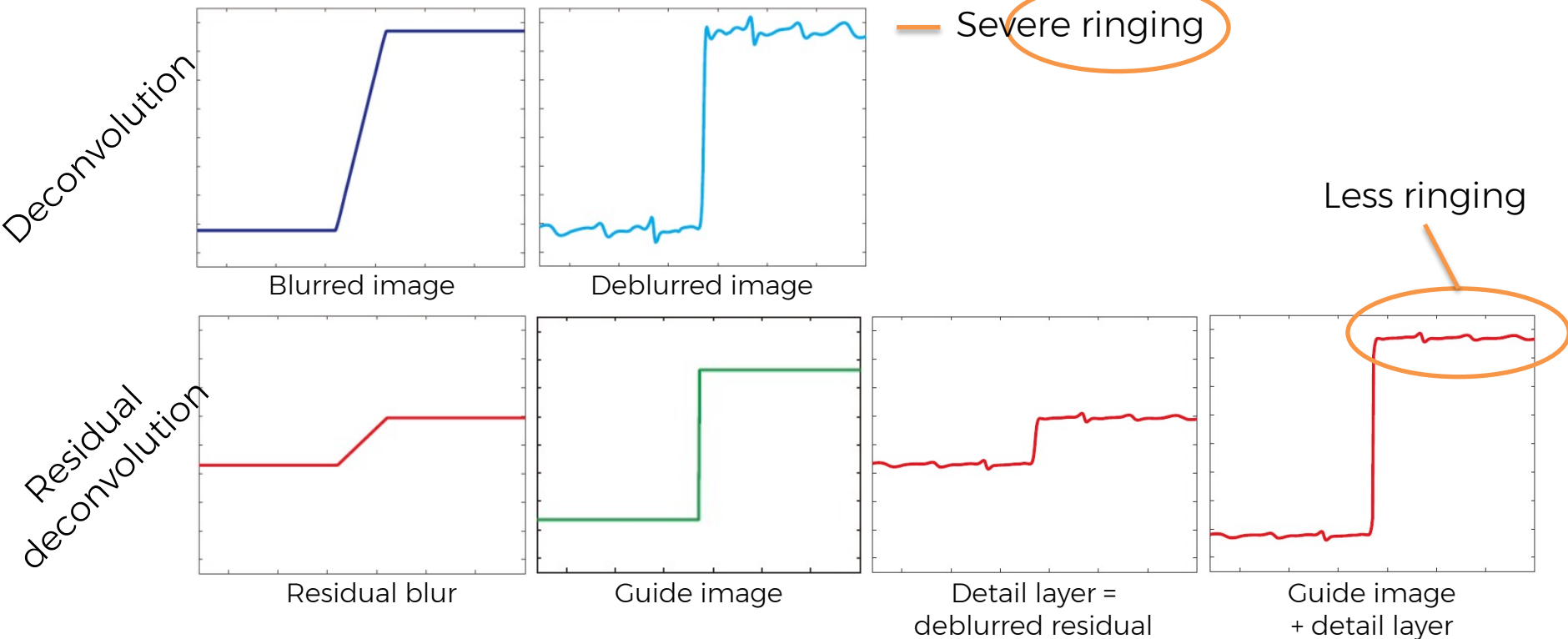
Detail layer



Result

# Residual Deconvolution [Yuan et al. SIGGRAPH 2007, 2008]

- Residual deconvolution

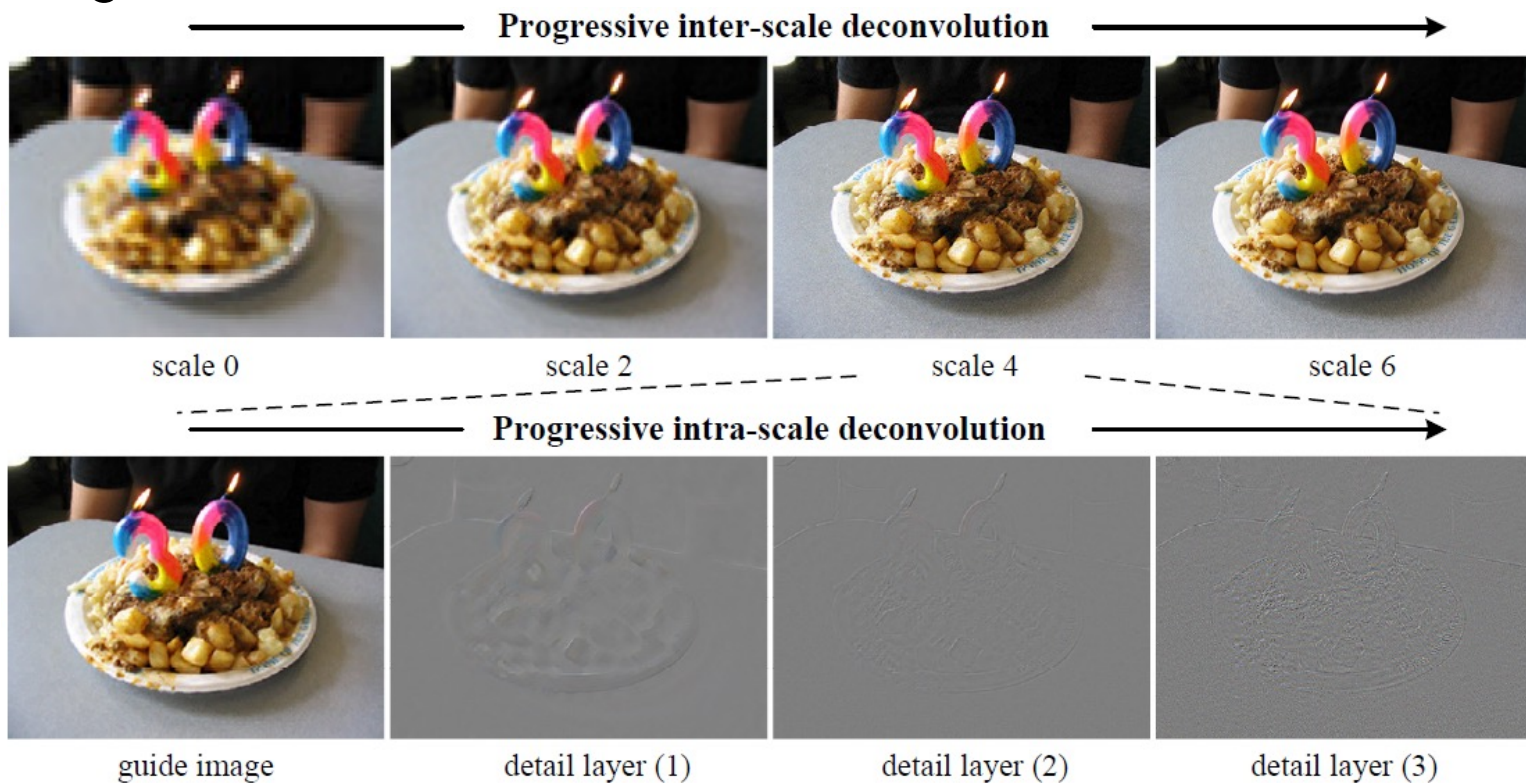




# Progressive Inter-scale & Intra-scale Deconvolution

[Yuan et al. SIGGRAPH 2008]

- Progressive inter-scale & intra-scale deconvolution





Blurred image



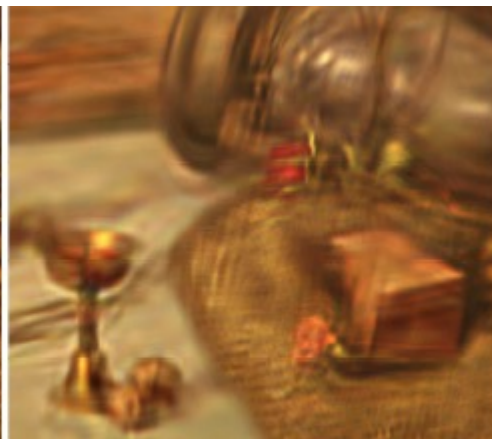
Richardson-Lucy



TV regularization



Levin et al. SIGGRAPH 2007



Wavelet regularization



Yuan et al. SIGGRAPH 2008

# Non-blind Deconvolution

- Introduction
- Natural image statistics
- High-order natural image statistics
- Ringing artifacts
- Outliers

# Outliers

- A main source of severe ringing artifacts



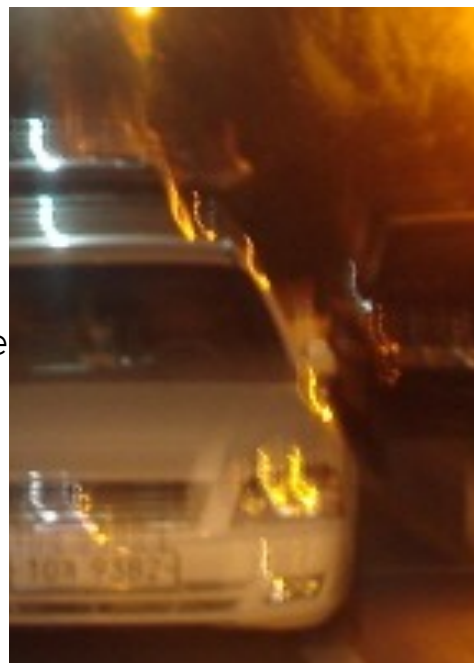
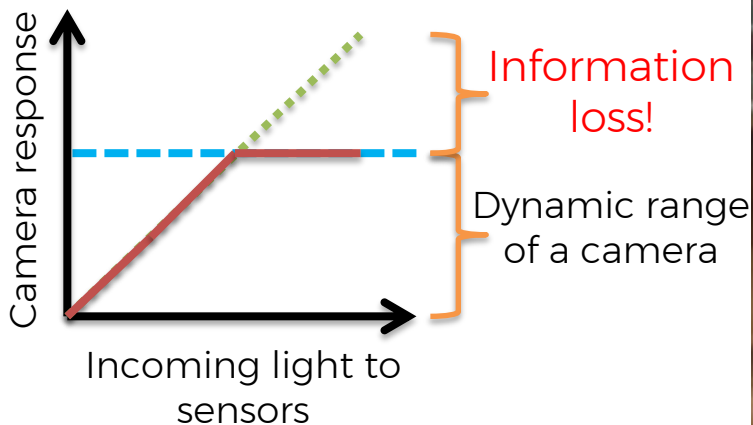
Blurred image with outliers



Deblurring result  
[Levin et al. SIGGRAPH 2007]

# Outliers

- Saturated pixels caused by limited dynamic range of sensors



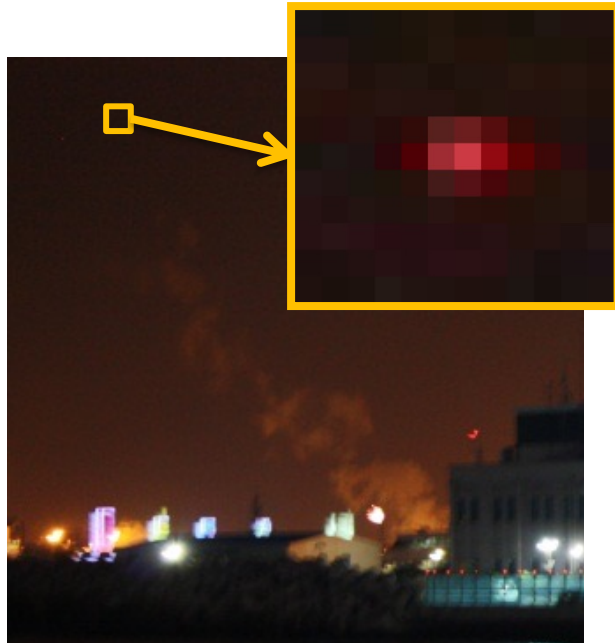
Blurred image



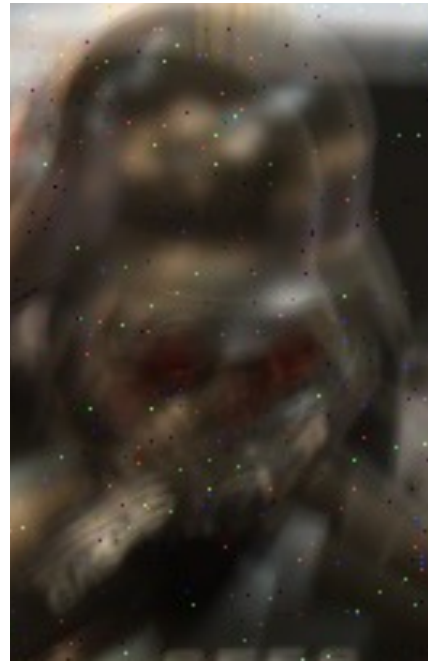
[Levin et al. 2007]

# Outliers

- Hot pixels, dead pixels, compression artifacts, etc...



Hot pixel




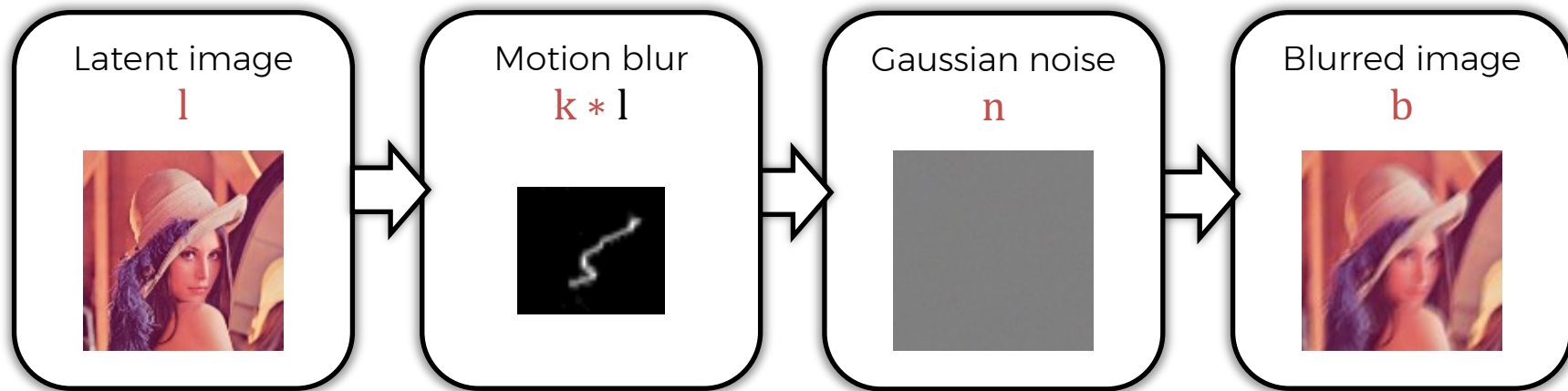
Blurred image with outliers [Levin et al. 2007]

# Outlier Handling

- Most common blur model:

$$b = k * l + n$$

Equivalent to  small amount of Gaussian noise



# Outlier Handling

- An energy function derived from this model:

$$E(l) = \underbrace{\|k * l - b\|^2}_{L^2\text{-norm based data term:}} + \underbrace{\rho(l)}_{\text{Regularization term on a latent image } l}$$

$L^2$ -norm based data term:  
known to be vulnerable to  
outliers

Regularization term on  
a latent image  $l$

- More robust norms to outliers
  - $L^1$ -norm, other robust statistics...

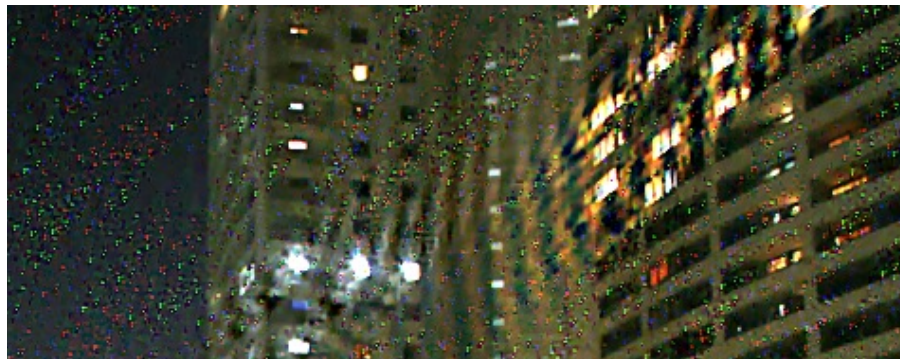
$$E(l) = \|k * l - b\|_1 + \rho(l)$$

- Bar et al. IJCV 2006, Xu et al. ECCV 2010, ...

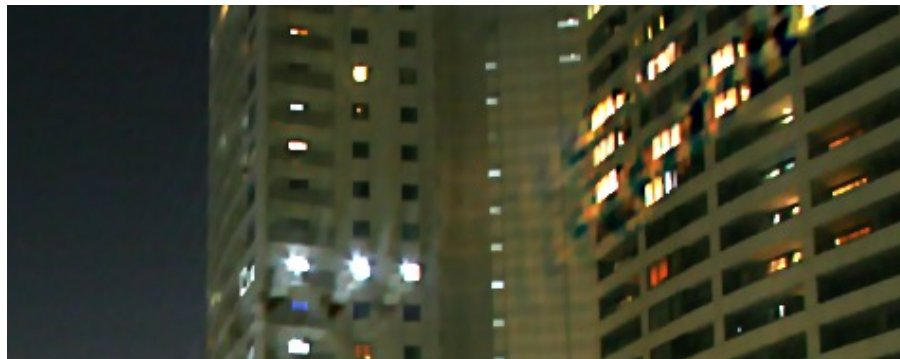


# Outlier Handling

- $L^1$ -norm based data term
  - Simple & efficient
  - Effective on salt & pepper noise
  - Not effective on saturated pixels



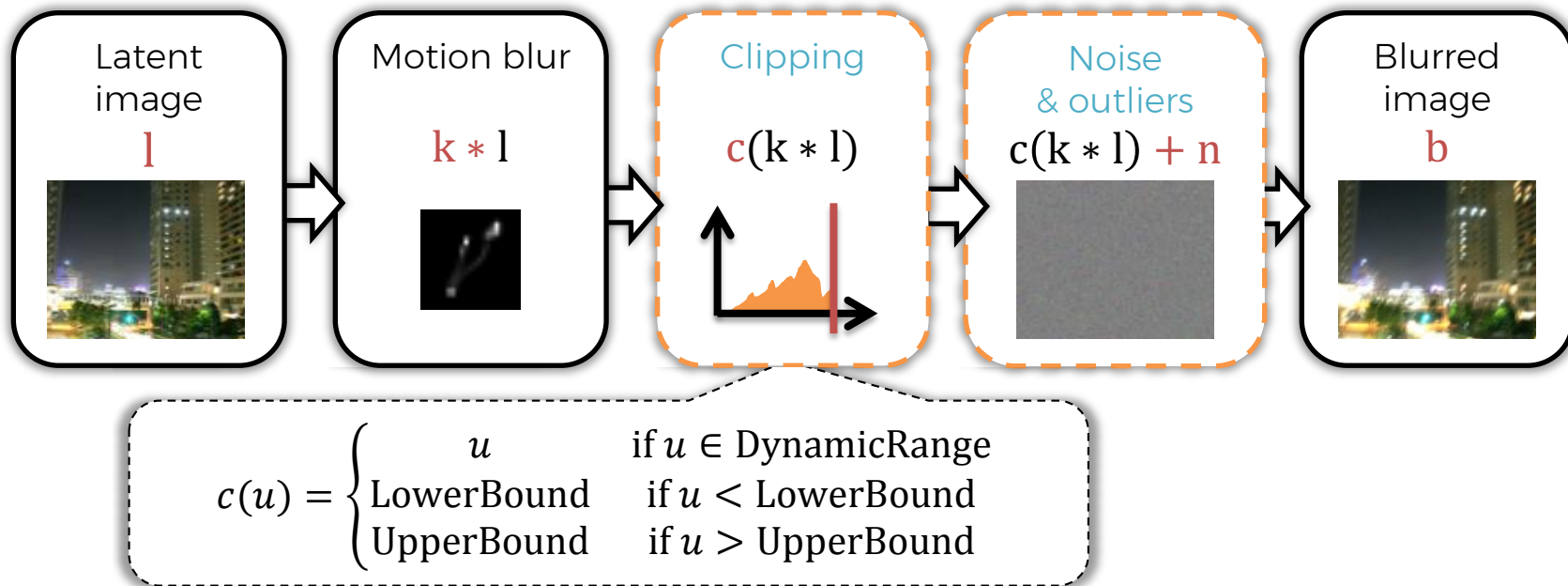
$L^2$ -norm based data term



$L^1$ -norm based data term

# Cho et al. ICCV 2011

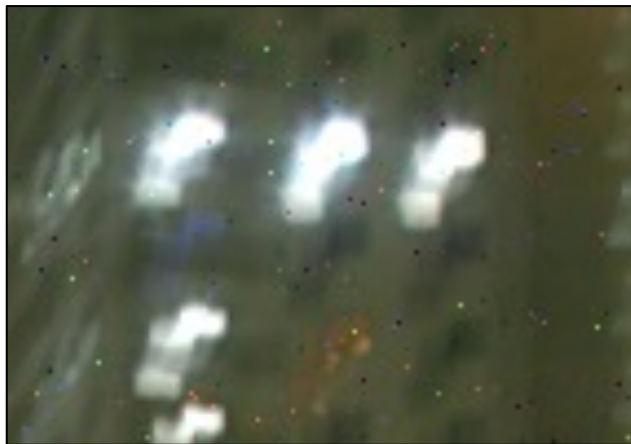
- More accurate blur model reflecting outliers



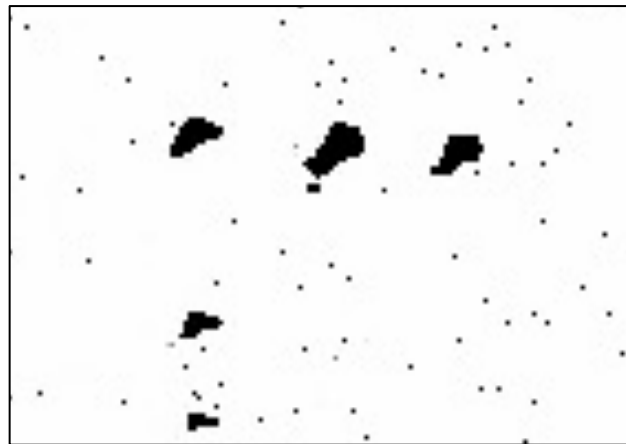
# Cho et al. ICCV 2011

- Classification mask

$$m(x) = \begin{cases} 1 & \text{if } b(x) \text{ is an inlier} \\ 0 & \text{if } b(x) \text{ is an outlier} \end{cases}$$



Blurred image **b**



Classification mask **m**

# Cho et al. ICCV 2011

- MAP estimation



Classification  
mask  $m$

Given  $b$  &  $k$ , find the most probable  $l$

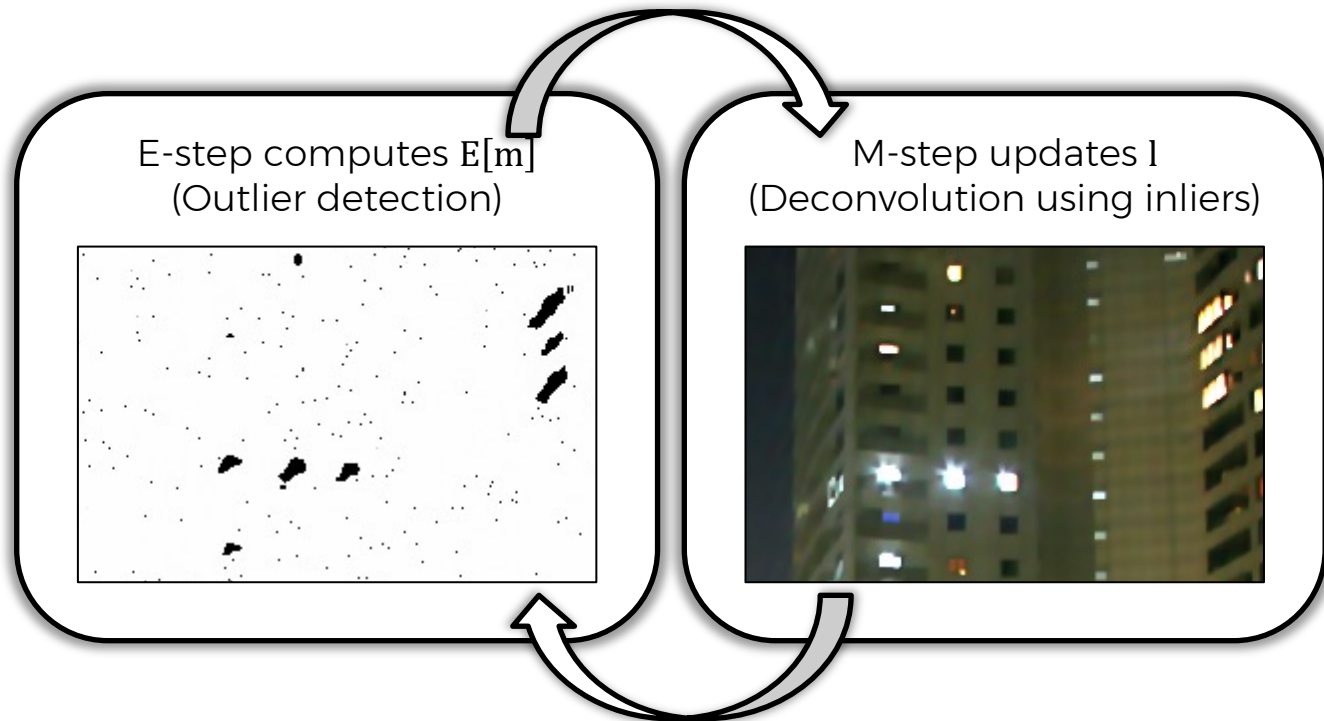


$$l_{MAP} = \arg \max_l p(l|b, k)$$

$$= \arg \max_l \sum_{m \in M} p(b|m, k, l) p(m|k, l) p(l)$$

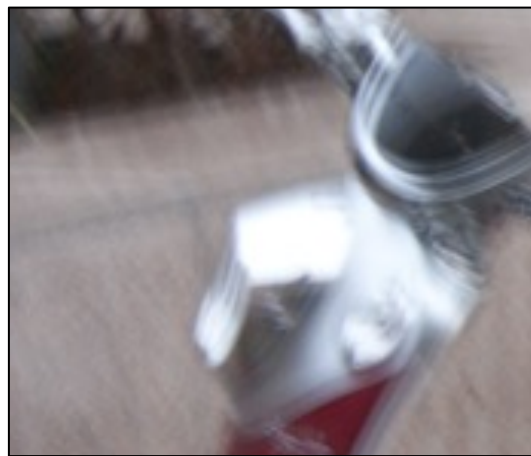
# Cho et al. ICCV 2011

- EM based optimization

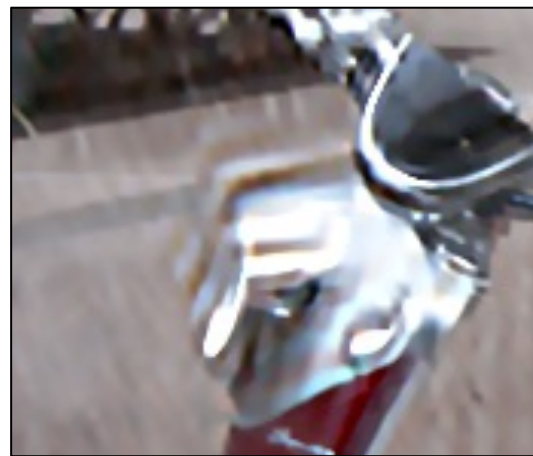




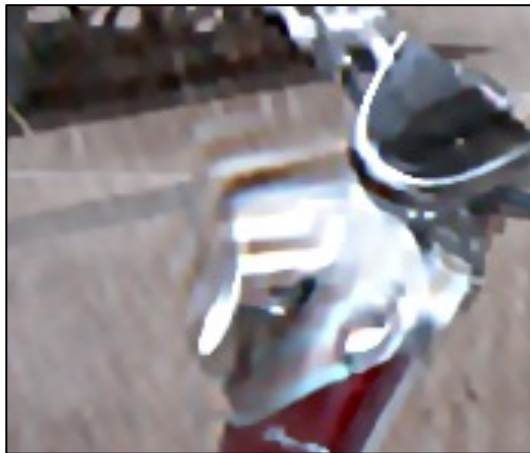
Blurred image



Blurred image



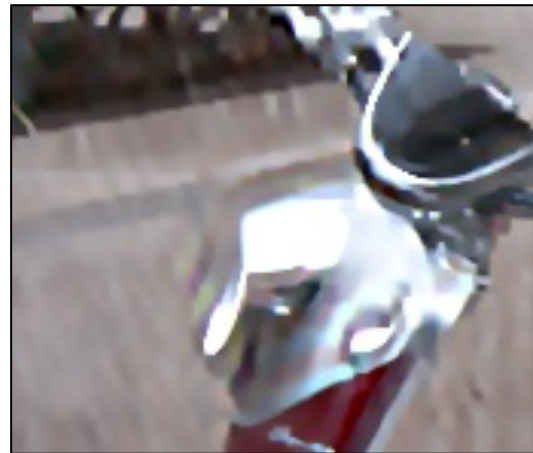
[Levin et al. 2007]



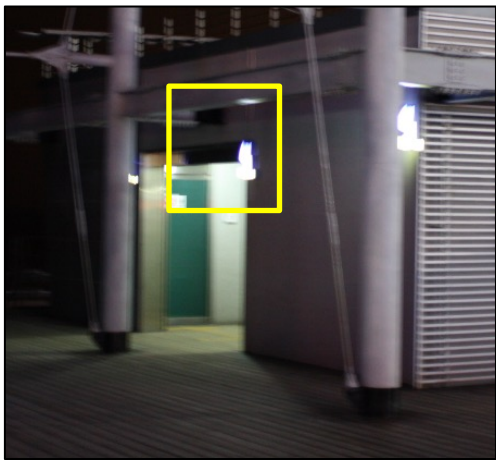
L1-norm based deconv.



[Harmeling et al. 2010]



[Cho et al. ICCV 2011]



Blurred image



Blurred image



[Levin et al. 2007]



L1-norm based deconv.



[Harmeling et al. 2010]



[Cho et al. ICCV 2011]

# Summary & Remaining Challenges

- Ill-posed problem - Noise & blur
- Noise
  - High-freq & unstructured
  - Natural image priors
- Ringing
  - Mid-freq & structured
  - More difficult to handle
- Outliers
  - Cause severe ringing artifacts
  - More accurate blur model
- Speed
  - More complex model → Slower
- Many source codes are available on the authors' website