

Previously on CMP784

- Content-based attention
- Location-based attention
- Soft vs. hard attention
- Case study: Show, Attend and Tell
- Self-attention
- Case study: Transformer networks



Lecture overview

- Generative Modeling
- Basic Foundations
 - Sparse Coding
 - -Autoencoders
- Autoregressive Generative Models

Disclaimer: Much of the material and slides for this lecture were borrowed from

- -Pieter Abbeel, Peter Chen, Jonathan Ho, Aravind Srinivas' Berkeley CS294-158 class
- -Ruslan Salakhutdinov's talk titled "Unsupervised Learning: Learning Deep Generative Models"
- -Yoshua Bengio's IDT6266 class
- -Bill Freeman, Antonio Torralba and Phillip Isola's MIT 6.869 class
- -Nal Kalchbrenner's talks on "Generative Modelling as Sequence Learning" and "Generative Models of Language and Images"

Generative Modeling



• Goal: Learn some underlying hidden structure of the training samples to generate novel samples from same data distribution

Yann LeCun's Black Forest Cake

Pure Reinforcement Learning (cherry)

- The machine predicts a scalar reward given once in a while.
- A few bits for some samples

Supervised Learning (icing)

- The machine predicts a category or a few numbers for each input
- Predicting human-supplied data
- 10→10,000 bits per sample

Unsupervised/ Predictive Learning (cake génoise)

- <u>The machine predicts any part of its</u> input for any observed part.
- Predicts future frames in videos
- Millions of bits per sample



"If intelligence is a cake, the bulk of the cake is unsupervised learning, the icing on the cake is supervised learning, and the cherry on the cake is reinforcement learning (RL)."



Slide adapted from Yann Lecun 5

Learning a generative model

• We are given a training set of examples, e.g., images of dogs



- We want to learn a probability distribution p(x) over images x s.t.
 - Generation: If we sample $x_{new} \sim p(x)$, x_{new} should look like a dog (sampling)
 - Density estimation: p(x) should be high if x looks like a dog, and low otherwise (anomaly detection)
 - Unsupervised representation learning: We should be able to learn what these images have in common, e.g., ears, tail, etc. (features)

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[GAN, Goodfellow et al. 2014]



[DCGAN, Radford, Metz, Chintala 2015]





bicubic (21.59dB/0.6423)



SRResNet (23.53dB/0.7832)







original



[CycleGAN: Zhu, Park, Isola & Efros, 2017] ₁₃



[BigGAN, Brock, Donahue, Simonyan, 2018] ₁₄



[StyleGAN, Karras, Laine, Aila, 2018] 15

Generate Audio





[WaveNet, Oord et al., 2018] 16

Generate Video



DVD-GAN: Adversarial Video Generation on Complex Datasets, Clark, Donahue, Simonyan, 2019

Generate Text

PANDARUS:

Alas, I think he shall be come approached and the day When little srain would be attain'd into being never fed, And who is but a chain and subjects of his death, I should not sleep.

Second Senator: They are away this miseries, produced upon my soul, Breaking and strongly should be buried, when I perish The earth and thoughts of many states.

DUKE VINCENTIO: Well, your wit is in the care of side and that.

Generate Math

\begin{proof}

We may assume that $\lambda = 1$ is an abelian sheaf on $\lambda = C$.

\item Given a morphism $\Lambda = \mathbb{F} \setminus \mathbb{F} \setminus \mathbb{F}$ is an injective and let $\Lambda = \mathbb{F} \cap \mathbb{F}$ \$X\$.

Let $\operatorname{F}\$ be a fibered complex. Let $\operatorname{F}\$ be a category.

\begin{enumerate}

```
\item \hyperref[setain-construction-phantom]{Lemma}
\label{lemma-characterize-guasi-finite}
```

Let $\operatorname{F}\$ be an abelian quasi-coherent sheaf on $\operatorname{C}\$.

Let $\operatorname{F}\$ be a coherent $\operatorname{C}_X\$ -module. Then $\operatorname{C}_{F}\$ is an abelian catenary over $\operatorname{C}_{C}\$.

\item The following are equivalent

\begin{enumerate}

\item \$\mathcal{F}\$ is an \$\mathcal{O}_X\$-module. \end{lemma} For $\bigoplus_{n=1,\ldots,m}$ where $\mathcal{L}_{m_{\bullet}} = 0$, hence we can find a closed subset \mathcal{H} in \mathcal{H} and any sets \mathcal{F} on X, U is a closed immersion of S, then $U \to T$ is a separated algebraic space.

Proof. Proof of (1). It also start we get

 $S = \operatorname{Spec}(R) = U \times_X U \times_X U$

and the comparison in the fibre product covering we have to prove the lemma generated by $\coprod Z \times_U U \to V$. Consider the maps M along the set of points Sch_{fppf} and $U \to U$ is the fibre category of S in U in Section, ?? and the fact that any U affine, see Morphisms, Lemma ??. Hence we obtain a scheme S and any open subset $W \subset U$ in Sh(G) such that $Spec(R') \to S$ is smooth or an

 $U = \bigcup U_i \times_{S_i} U_i$

which has a nonzero morphism we may assume that f_i is of finite presentation over S. We claim that $\mathcal{O}_{X,x}$ is a scheme where $x, x', s'' \in S'$ such that $\mathcal{O}_{X,x'} \to \mathcal{O}'_{X',x'}$ is separated. By Algebra, Lemma ?? we can define a map of complexes $\operatorname{GL}_{S'}(x'/S'')$ and we win.

To prove study we see that $\mathcal{F}|_U$ is a covering of \mathcal{X}' , and \mathcal{T}_i is an object of $\mathcal{F}_{X/S}$ for i > 0 and \mathcal{F}_p exists and let \mathcal{F}_i be a presheaf of \mathcal{O}_X -modules on \mathcal{C} as a \mathcal{F} -module. In particular $\mathcal{F} = U/\mathcal{F}$ we have to show that

 $\widetilde{M}^{\bullet} = \mathcal{I}^{\bullet} \otimes_{\mathrm{Spec}(k)} \mathcal{O}_{S,s} - i_X^{-1} \mathcal{F})$

is a unique morphism of algebraic stacks. Note that

Arrows = $(Sch/S)_{fppf}^{opp}, (Sch/S)_{fppf}$

and

$$V = \Gamma(S, \mathcal{O}) \longmapsto (U, \operatorname{Spec}(A))$$

is an open subset of X. Thus U is affine. This is a continuous map of X is the inverse, the groupoid scheme S.

Proof. See discussion of sheaves of sets.

The result for prove any open covering follows from the less of Example ??. It may replace S by $X_{spaces,\acute{e}tale}$ which gives an open subspace of X and T equal to S_{Zar} , see Descent, Lemma ??. Namely, by Lemma ?? we see that R is geometrically regular over S.

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Generate Text

Prompt [human written]: A train carriage containing controlled nuclear materials was stolen in Cincinnati today. Its whereabouts are unknown.

GPT-2: The incident occurred on the downtown train line, which runs from Covington and Ashland stations. In an email to Ohio news outlets, the U.S. Department of Energy said it is working with the Federal Railroad Administration to find the thief.

'The theft of this nuclear material will have significant negative consequences on public and environmental health, our workforce and the economy of our nation,' said Tom Hicks, the U.S. Energy Secretary, in a statement. 'Our top priority is to secure the theft and ensure it doesn't happen again.'

The stolen material was taken from the University of Cincinnati's Research Triangle Park nuclear research site, according to a news release from Department officials.

The Nuclear Regulatory Commission did not immediately release any information. According to the release, the U.S. Department of Energy's Office of Nuclear Material Safety and Security is leading that team's investigation.

'The safety of people, the environment and the nation's nuclear stockpile is our highest priority,' Hicks said. 'We will get to the bottom of this and make no excuses.'

[OpenAl's GPT2 – Radford, Wu, Child, Luan, Amodei, Sutskever, 2019]

Generate Text

Prompt (human written): Recycling is good for the world, no, you could not be more wrong.

<u>GPT-2</u>: Recycling is NOT good for the world. It is bad for the environment, it is bad for our health, and it is bad for our economy. I'm not kidding. Recycling is not good for the environment. It is destructive to the earth and it is a major contributor to global warming. Recycling is not good for our health. It contributes to obesity and diseases like heart disease and cancer. Recycling is bad for our economy. It increases the cost of a product, and in turn, the price of everything that is made with that product. Recycling is not good for our nation. We pay a tremendous price for the privilege of having the world's most advanced and efficient recycling system. Recycling is a huge, colossal waste of time, energy, money, and resources.

[OpenAl's GPT2 – Radford, Wu, Child, Luan, Amodei, Sutskever, 2019]

Try it yourself

https://talktotransformer.com/

Compression - Lossless

Model	Bits per byte				
CIFAR-10					
PixelCNN (Oord et al., 2016)	3.03				
PixelCNN++ (Salimans et al., 2017)	2.92				
Image Transformer (Parmar et al., 2018)	2.90				
PixelSNAIL (Chen et al., 2017)	2.85				
Sparse Transformer 59M (strided)	2.80				
Enwik8					
Deeper Self-Attention (Al-Rfou et al., 2018)	1.06				
Transformer-XL 88M (Dai et al., 2018)	1.03				
Transformer-XL 277M (Dai et al., 2018)	0.99				
Sparse Transformer 95M (fixed)	0.99				
ImageNet 64x64					
PixelCNN (Oord et al., 2016)	3.57				
Parallel Multiscale (Reed et al., 2017)	3.7				
Glow (Kingma & Dhariwal, 2018)	3.81				
SPN 150M (Menick & Kalchbrenner, 2018)	3.52				
Sparse Transformer 152M (strided)	3.44				
Classical music, 5 seconds at 12 kHz					
Sparse Transformer 152M (strided)	1.97				

Generative models provide better bit-rates than distribution-unaware compression methods like JPEG, etc.

Compression - Lossy







JPEG

JPEG2000

WaveOne

[Rippel & Bourdev, 2017]

Downstream Task - Sentiment Detection

This is one of Crichton's best books. The characters of Karen Ross, Peter Elliot, Munro, and Amy are beautifully developed and their interactions are exciting, complex, and fast-paced throughout this impressive novel. And about 99.8 percent of that got lost in the film. Seriously, the screenplay AND the directing were horrendous and clearly done by people who could not fathom what was good about the novel. I can't fault the actors because frankly, they never had a chance to make this turkey live up to Crichton's original work. I know good novels, especially those with a science fiction edge, are hard to bring to the screen in a way that lives up to the original. But this may be the absolute worst disparity in quality between novel and screen adaptation ever. The book is really, really good. The movie is just dreadful.

Downstream Tasks - NLP (BERT Revolution)

	Ran	kName	Model	URL	Score E	BoolQ CB	COPA I	MultiRC	ReCoRD	RTE	WiC \	WSC	AX-b	AX-g
	1	ERNIE Team - Baidu	ERNIE 3.0		90.6	91.0 98.6/99.2	97.48	8.6/63.2	94.7/94.2	92.6	77.4	97.3	68.6	92.7/94.7
+	2	Zirui Wang	T5 + UDG, Single Model (Google Brain)		90.4	91.4 95.8/97.6	98.08	8.3/63.0	94.2/93.5	93.0 7	77.9	96.6	69.1	92.7/91.9
+	3	DeBERTa Team - Microsoft	DeBERTa / TuringNLRv4		90.3	90.4 95.7/97.6	98.48	8.2/63.7	94.5/94.1	93.2	77.5	95.9	66.7	93.3/93.8
	4	SuperGLUE Human Baseline	s SuperGLUE Human Baselines		89.8	89.0 95.8/98.9	100.08	1.8/51.9	91.7/91.3	93.6 8	80.0 1	00.0	76.6	99.3/99.7
+	5	T5 Team - Google	Т5		89.3	91.293.9/96.8	94.88	8.1/63.3	94.1/93.4	92.5	76.9	93.8	65.6	92.7/91.9
+	6	Huawei Noah's Ark Lab	NEZHA-Plus		86.7	87.894.4/96.0	93.68	4.6/55.1	90.1/89.6	89.1	74.6	93.2	58.0	87.1/74.4
+	7	Alibaba PAI&ICBU	PAI Albert		86.1	88.1 92.4/96.4	91.88	4.6/54.7	89.0/88.3	88.8	74.1	93.2	75.6	98.3/99.2
+	8	Infosys : DAWN : AI Research	n RoBERTa-iCETS		86.0	88.593.2/95.2	91.28	6.4/58.2	89.9/89.3	89.9	72.9	89.0	61.8	88.8/81.5
+	9	Tencent Jarvis Lab	RoBERTa (ensemble)		85.9	88.292.5/95.6	90.88	4.4/53.4	91.5/91.0	87.9 7	74.1	91.8	57.6	89.3/75.6
	10	Zhuiyi Technology	RoBERTa-mtl-adv		85.7	87.1 92.4/95.6	91.28	5.1/54.3	91.7/91.3	88.1 7	72.1	91.8	58.5	91.0/78.1

[https://super.gluebenchmark.com/leaderboard] 26

Downstream Tasks - Vision (Contrastive)

Method	Architecture	mAP	
<i>Transfer from labeled data:</i> Supervised baseline	ResNet-152	74.7	
Transfer from unlabeled data: Exemplar [17] by [13] Motion Segmentation [47] by [13] Colorization [64] by [13] Relative Position [14] by [13] Multi-task [13] Instance Discrimination [60] Deep Cluster [7] Deeper Cluster [8] Local Aggregation [66] Momentum Contrast [25]	ResNet-101 ResNet-101 ResNet-101 ResNet-101 ResNet-50 VGG-16 VGG-16 ResNet-50 ResNet-50 ResNet-50	60.9 61.1 65.5 66.8 70.5 65.4 65.9 67.8 69.1 74.9 76.6	"If, by the first day of autumn (Sept 23) of 2015, a method will exist that can match beat the performance of R-CNN on Pasca VOC detection, without the use of any ex human annotations (e.g. ImageNet) as pre training, Mr. Malik promises to buy Mr. Et one (1) gelato (2 scoops: one chocolate, o vanilla)."
			[Henaff, Srinivas, et al.

Why Unsupervised Learning?

- Given high-dimensional data $X = (x_1, \ldots, x_n)$ we want to find a low-dimensional model characterizing the population.
- Recent progress mostly in supervised DL
- Real challenges for unsupervised DL
- Potential benefits:
 - Exploit tons of unlabeled data
 - -Answer new questions about the variables observed
 - Regularizer transfer learning domain adaptation
 - Easier optimization (divide and conquer)
 - -Joint (structured) outputs

Why Latent Factors & Unsupervised Representation Learning? Because of Causality.

• If Ys of interest are among the causal factors of X, then

$$P(Y|X) = \frac{P(X|Y)P(Y)}{P(X)}$$

is tied to P(X) and P(X|Y), and P(X) is defined in terms of P(X|Y), i.e.

- The best possible model of X (unsupervised learning) MUST involve Y as a latent factor, implicitly or explicitly.
- Representation learning SEEKS the latent variables H that explain the variations of X, making it likely to also uncover Y.

On causal and anticausal learning, Janzing et al. ICML 2012

If Y is a Cause of X, Semi-Supervised Learning Works

- Just observing the x-density reveals the causes y (cluster ID)
- After learning p(x) as a mixture, a single labeled example per class suffices to learn p(y|x)



Invariance & Disentangling Underlying Factors

- Invariant features
- Which invariances?
- Alternative: learning to disentangle factors, i.e. keep all the explanatory factors in the representation
- Good disentangling \rightarrow avoid the curse of dimensionality
- Emerges from representation learning



p(x), $x \in \mathbb{R}^{n}$ (or $x \in \Omega^{n}$) Curse of Dimensionality

• Challenge: How to model p(x), $x \in \mathbb{R}^N$ (or $x \in \Omega^N$) for grave N?

• An existing hypothesis is that, although the ambient dimensionality is high, the intrinsic dimensionality of x is low.





Unsupervised Learning

- Basic Building Blocks:
 - Sparse Coding
 - Autoencoders
- Autoregressive Generative Models
- Generative Adversarial Networks
- Variational Autoencoders
- Normalizing Flow Models

Sparse Coding

- Sparse coding (Olshausen & Field, 1996). Originally developed to explain early visual processing in the brain (edge detection).
- **Objective:** Given a set of input data vectors $\{x_1, x_2, ..., x_N\}$, learn a dictionary of bases, such that:



• Each data vector is represented as a sparse linear combination of bases.

Sparse Coding

Natural Images Learned bases: "Edges" New example = 0.8 * +0.5 *+0.3 * $= 0.8 * \phi_{36} + 0.3 * \phi_{42} + 0.5 *$ ϕ_{65} X [0.0, 0.0, ... **0.8**, ..., **0.3**, ..., **0.5**, ...] = coefficients (feature representation)

Slide Credit: Honglak Lee
Sparse Coding: Training

- Input image patches: $\mathbf{x}_{\mathbf{X}_1}, \mathbf{x}_2, \dots, \mathbf{X}_N \in \mathbb{R}^D$ Learn dictionary of bases: $\phi_1, \phi_2, \dots, \phi_K \in \mathbb{R}^D$



- Alternating Optimization:
 - 1. Fix dictionary of bases and $\hat{q}_{\phi_1}^{(1)}, \hat{\phi}_2, \dots, \hat{\phi}_K$ is **a** (a standard Lasso problem).
 - Fix activations **a**, optimize the dictionary of bases (convex QP problem). 2.

Sparse Coding: Testing Time

- Input: a new image patch x* , and K learned bases $oldsymbol{\phi}_1, oldsymbol{\phi}_2, ..., oldsymbol{\phi}_K, ..., oldsymbol{\phi}_K$
- Output: sparse representation **a** of an image patch x*.

$$\min_{\mathbf{a}} \left\| \mathbf{x}^* - \sum_{k=1}^K a_k \boldsymbol{\phi}_k \right\|_2^2 + \lambda \sum_{k=1}^K \left| a_k \right|_{:=1}^K \left| a_k \right|$$



Sparse Coding: Testing Time

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Image Classification

• Evaluated on Caltech101 object category dataset.

Slide Credit: Honglak Lee

Modeling Image Patches

- Natural image patches:
 - small **image regions** extracted from an image of nature (forest, grass, ...)

Image taken from: Emergence of complex cell properties by learning to generalize in natural scenes. Karklin and Lewicki, 2009 🛛 🖉

Relationship to V1

- When trained on natural image patches
 - the dictionary columns ('atoms'') look
 like edge detectors
 - each atom is tuned to a particular
 position, orientation and spatial
 frequency
 - V1 neurons in the mammalian brain have a similar behavior

Relationship to V1

- Suggests that the brain might be learning a sparse code of visual stimulus
 - Since then, many other models have been shown to learn similar features
 - they usually all incorporate a notion of sparsity

Interpreting Sparse Coding

Interpreting Sparse Coding

- Sparse, over-complete representation **a**.
- **Encoding** $\mathbf{a} = f(\mathbf{x})$ is implicit and nonlinear function of \mathbf{x} .
- **Reconstruction** (or decoding) $\mathbf{x'} = g(\mathbf{a})$ is linear and explicit.

- Details of what goes insider the encoder and decoder matter!
- Need constraints to avoid learning an identity.

- Need additional constraints to avoid learning an identity.
- Relates to Restricted Boltzmann Machines (later).

• Feed-forward neural network trained to reproduce its input at the output layer

$Loss Function_{\widehat{\mathbf{x}} \to \widehat{\mathbf{y}} \to \widehat{\mathbf{y} \to \widehat{\mathbf{y}} \to \widehat{\mathbf{y}} \to$

 $\widehat{x}_{k} \xrightarrow{}^{2} x_{k} (\widehat{f}(\underline{f}(\underline{f}(\underline{f}(\underline{f}))))) \xrightarrow{} \sum x_{k} d (\widehat{g}(\underline{f}(\underline{f}))) \xrightarrow{}^{2} x_{k} d (\widehat{g}(\underline{f})) \xrightarrow{}^{2} x_{k}$

- Cross-entropy error function (reconstruction $\underbrace{\operatorname{sss}}_{\mathbf{X}} = \underbrace{\operatorname{sss}}_{\mathcal{S}} (\widehat{\mathbf{x}}_{\mathbf{X}}) = \sum_{k} (\widehat{x}_{k} - x)$

 $== \operatorname{sign}(\operatorname{c}(\operatorname{c-WWh}(\operatorname{b}(\operatorname{x})))$

Loss function for real-valued inputs

 $(\mathbf{x}) = \frac{1}{2} \sum_{k} (\hat{x}_{k} - x_{k})^{2} |_{k}^{2} l(\mathbf{x}) = \sum_{k} (x_{k}) \log(\widehat{g}(\mathbf{x})_{k}) + (1(1 - x_{k})_{k})$

 $T_{(\widehat{\mathbf{x}},\widehat{\mathbf{y}})} = \mathcal{T}_{(\widehat{\mathbf{x}},\widehat{\mathbf{y}})} = \mathcal{T}_{(\widehat{\mathbf{x}},\widehat{\mathbf{x}})} = \mathcal{T}_{(\widehat{\mathbf{x},\widehat{\mathbf{x}})} = \mathcal{T}_{(\widehat{\mathbf{x},\widehat{\mathbf{x},\widehat{\mathbf{x}})} = \mathcal{T}_{(\widehat{\mathbf{x},\widehat{\mathbf{x},\widehat{\mathbf{x}})}$

$$\mathbf{a}(\mathbf{x}(\mathbf{x}^{(t)})) \iff \mathbf{b} + \mathbf{W}(\mathbf{x}^{(t)})$$

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- If the hidden and output layers are linear, it will learn hidden units that are a linear function of the data and minimize the squared error.
- The K hidden units will span the same space as the first k principal components. The weight vectors may not be orthogonal.

• With nonlinear hidden units, we have a nonlinear generalization of PCA.

- Idea: Representation should be robust to introduction \mathbf{x} heis \mathbf{x}_{T}
 - random assignment of subset of interaction h with probability h $n(\mathbf{x}, \mathbf{x})$
- Gaussian addition and strategy and the most the strategy and the strateg
- Reconstruction $\hat{\mathbf{x}}$ computed from $\hat{\mathbf{x}}$ $\hat{\mathbf$
- Loss function compares $\hat{\mathbf{x}}$ for struction $\hat{\mathbf{x}}$ is the struction $\hat{\mathbf{x}}$ is the set of set of struction $\hat{\mathbf{x}}$ is the set of set

Denoising Autoencoder

 $\widehat{\mathbf{x}} = \operatorname{sigm}(\mathbf{c} + \mathbf{W}^* \mathbf{h}(\widetilde{\mathbf{x}}))^*$ $\widetilde{\mathbf{X}}$ \mathbf{X}

Learned Filters

Non-corrupted

25% corrupted input

Learned Filters

Non-corrupted

50% corrupted input

(a) a) oN dester sty eye in jupps to

(b) b2 525 Dedustruiction

Predictive Sparse Decomposition

$$\min_{D,W,\mathbf{z}} ||D\mathbf{z} - \mathbf{x}||_2^2 + \lambda |\mathbf{z}|_1 + ||\sigma(W\mathbf{x}) - \mathbf{z}||_2^2$$

(Kavukcuoglu, Ranzato, Fergus, LeCun, 2009) 57

Predictive Sparse Decomposition

• Remove decoders and use feed-forward part.

- Remove decoders and use feed-forward part.
- Standard, or convolutional neural network architecture.
- Parameters can be fine-tuned using backpropagation.

Deep Autoencoder

Deep Autoencoders

 25x25 – 2000 – 1000 – 500 – 30 autoencoder to extract 30-D realvalued codes for Oliver face patches.

- **Top:** Random samples from the test dataset.
- Middle: Reconstructions by the 30-dimensional deep autoencoder.
- Bottom: Reconstructions by the 30-dimensional PCA.

Information Retrieval

- The Reuters Corpus Volume II contains 804,414 newswire stories (randomly split into **402,207 training** and **402,207 test**).
- "Bag-of-words" representation: each article is represented as a vector containing the counts of the most frequently used 2000 words in the training set.

Semantic Hashing

- Learn to map documents into semantic 20-D binary codes.
- Retrieve similar documents stored at the nearby addresses with no search at all.

Searching Large Image Database using Binary Codes

• Map images into binary codes for fast retrieval.

- Small Codes, Torralba, Fergus, Weiss, CVPR 2008
- Spectral Hashing, Y. Weiss, A. Torralba, R. Fergus, NIPS 2008
- Kulis and Darrell, NIPS 2009, Gong and Lazebnik, CVPR 2011
- Norouzi and Fleet, ICML 2011

Autoregressive Generative Models

Texture synthesis by non-parametric sampling

Models P(p|N(p))

[Efros & Leung 1999] 72
Texture synthesis with a deep net



[PixelRNN, PixelCNN, van der Oord et al. 2016] 73



[PixeIRNN, PixeICNN, van der Oord et al. 2016] 74

Idea: We can represent colors as discrete classes



 $\mathcal{L}(\mathbf{y}, f_{\theta}(\mathbf{x})) = H(\mathbf{y}, \texttt{softmax}(f_{\theta}(\mathbf{x})))$

And we can interpret the learner as modeling P(next pixel | previous pixels):

Softmax regression (a.k.a. multinomial logistic regression)

$$\hat{\mathbf{y}} \equiv [P_{\theta}(Y = 1 | X = \mathbf{x}), \dots, P_{\theta}(Y = K | X = \mathbf{x})] \longleftarrow$$
 predicted probability of each class given input \mathbf{x}

$$H(\mathbf{y}, \hat{\mathbf{y}}) = -\sum_{k=1}^{K} y_k \log \hat{y}_k \quad \longleftarrow \quad \text{picks out the -log likelihood} \\ \text{of the ground truth class } \mathbf{y} \\ \text{under the model prediction } \hat{\mathbf{y}}$$

$$f^* = \operatorname*{arg\,min}_{f \in \mathcal{F}} \sum_{i=1}^{N} H(\mathbf{y}_i, \hat{\mathbf{y}}_i) \longleftarrow \max$$
 likelihood learner!

Network output





P(next pixel | previous pixels) $P(p_i|p_1,\cdots,p_{i-1})$ probability

































$$p_1 \sim P(p_1)$$

 $p_2 \sim P(p_2|p_1)$
 $p_3 \sim P(p_3|p_1, p_2)$
 $p_4 \sim P(p_4|p_1, p_2, p_3)$

$$p_3$$
 p_4 p_2 p_1

 $\{p_1, p_2, p_3, p_4\} \sim P(p_4|p_1, p_2, p_3) P(p_3|p_1, p_2) P(p_2|p_1) P(p_1)$

$$p_i \sim P(p_i|p_1,\ldots,p_{i-1})$$

$$\mathbf{p} \sim \prod_{i=1}^{N} P(p_i | p_1, \dots, p_{i-1})$$

Autoregressive probability model

$$\mathbf{p} \sim \prod_{i=1}^{N} P(p_i | p_1, \dots, p_{i-1})$$

$$P(\mathbf{p}) = \prod_{i=1}^N P(p_i | p_1, \dots, p_{i-1}) \quad \bigstar \quad \mathsf{General product rule}$$

The sampling procedure we defined above takes exact samples from the learned probability distribution (pmf).

Multiplying all conditionals evaluates the probability of a full joint configuration of pixels.

$$p(\mathbf{x}) = \prod_{i} p(x_i | \mathbf{x}_{<})$$

for 1D sequences such as text or sound

 $p(\mathbf{x}) = \prod p(x_{i,j} | \mathbf{x}_{<})$ i i

Autoregressive model for 2D tensors such as images

 $p(\mathbf{x}) = \prod p(x_{i,j,k} | \mathbf{x}_{<})$ k j i

And for 3D tensors such as videos

 $p(\mathbf{x}) = \begin{bmatrix} p(x_{i,j,k} | \mathbf{x}_{<}) \end{bmatrix}$ k j i

PixelRNN/PixelCNN (Images)

Video Pixel Nets (Videos) ByteNet (Language/seq2seq) WaveNet (Audio) [van den Oord, Kalchbrenner, Kavukcuoglu, 2016]

[van den Oord, Kalchbrenner, Vinyals, et al, 2016]

[Kalchbrenner, van den Oord, Simonyan, et al, 2016]

[Kalchbrenner, Espeholt, Simonyan, et al, 2016]

[van den Oord, Dieleman, Zen, et al, 2016]

$$p(\mathbf{x}) = \prod_{k \neq j} \prod_{i} p(x_{i,j,k} | \mathbf{x}_{<})$$

Prior work:

Autoregressive image models: [Larochelle, Murray, 2011] [Theis, Bethge, 2015] [Uria, et al 2016]

Dilated convolutions: [Chen et al, 2015] [Yu, Koltun, 2016] [Holschneider, et al, 1989]

RNN and language/translation modelling: [Hochreiter, Schmidhuber, 1997] [Mikolov et al, 2010] [Kalchbrenner, Blunsom 2013] [Sutskever et al, 2014] [Stollenga et al, 2015] [Kaiser and Bengio, 2016]







X	1				x_n
			x_i		
					x_{n^2}





By chain rule and using pixels as variables,

 $P(X) = P(x_1) P(x_2|x_1) P(x_3|x_1,x_2)$



x_1				$\overline{x_n}$
		x_i		
				x_{n^2}

1		
n	r.	Y .
P	01	$\Lambda < 2.1$

x_1				x_n	
		x_i			
				$\hat{\boldsymbol{\alpha}}$	

Masked Convolutions









Masked Convolutions







 x_n

 x_1



Pixel CNN









 x_n



 x_n

 x_n



Improving PixelCNN I

There is a problem with this form of masked convolution.





Stacking layers of masked convolution creates a blindspot



Samples from PixelCNN

Conditional Image Generation with PixelC van den Oord, Kalchbrenner, Vinyals, Espeholt, Graves, K

- **Topics:** CIFAR-10
- Samples from a class-conditioned PixelCNN



Coral Reef

Samples from PixelCNN

Topics: CIFAR-10

• Samples from a class-conditioned PixelCNN



Sorrel horse



Sandbar



Convolutional Long Short-Term Memory





Stollenga et al, 2015 Oord, Kalchbrenner, Kavukcuoglu, 2016

Multiple layers of convolutional LSTM





 x_1



Samples from PixelRNN

occlusion

completions

original



Samples from PixelRNN



[PixeIRNN, van der Oord et al. 2016]

Image completions (conditional samples) from PixelRNN

occluded

completions



[PixelRNN, van der Oord et al. 2016]

original

Modeling Audio



1 Second
Architecture for 1D sequences (Bytenet / Wavenet)

Deep RNN



Bytenet decoder



))))

- Stack of dilated, masked 1-D convolutions in the decoder
- The architecture is parallelizable
- along the time dimension (during training or scoring)
- Easy access to many states from the past























Multiple Stacks

- Improved receptive field with dilated convolutions
- Gated Residual block with skip connections





Sampling

Output 🔴 🔴 🔴 🔴 🔴 🔴 🔴 🔴 🔴 🔴 🔴 🔴 🔴

Input	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
Hidden Layer	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
Hidden Layer	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
Hidden Layer	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	







Output 🔴 🔴 🔴 🔴 🔴 🔴 🔴 🔴 🔴 🔴 🔴 🔴 🔴

Hidden Layer	0	0	0	0	0	0	0	0	0	0	0	0	0	0	\bigcirc
Hidden Layer	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
Hidden Layer	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
Input	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0 0

Video Pixel Net





Masked convolution

Video Pixel Net



Resolution Preserving CNN Encoders

VPN Samples for Moving MNIST

B 9 5 9°

No frame dependencies

VPN

Videos on nal.ai/vpn

VPN Samples for Robotic Pushing



No frame dependencies



VPN

Videos on nal.ai/vpn

VPN Samples for Robotic Pushing



Sparse Transformers















Sparse Transformer (fixed)

- Strided attention is roughly equivalent to each position attending to its row and its column
- Fixed attention attends to a fixed column and the elements after the latest column element (especially used for text).

Sparse

Transformer

(strided)

[Child, Gray, Radford, Sutskever, 2019] 129

Next Lecture: Generative Adversarial Networks and Flow Models