

CMP 784 – Practical 1: Learning Distributed Word Representations

Due date: Wednesday, 01-11-2023, 11:59 PM.

Overview

The goal of this assignment is to get you familiarize with training neural networks, to learn distributed word representations¹.

Problem

In this assignment we will learn about word embeddings and make neural networks learn about words. We could try to match statistics about the words, or we could train a network that takes a sequence of words as input and learns to predict the word that comes next.

This assignment will ask you to implement a linear embedding and then the backpropagation computations for a neural language model and then run some experiments to analyze the learned representation. The amount of code you have to write is very short but each line will require you to think very carefully. You will need to derive the updates mathematically, and then implement them using matrix and vector operations in NumPy.

Starter code and data

Download and extract the archive from the course web page <https://web.cs.hacettepe.edu.tr/~erkut/cmp784.f23/practicals/practical1.zip>.

Look at the file `raw_sentences.txt`. It contains the sentences that we will be using for this assignment. These sentences are fairly simple ones and cover a vocabulary of only 250 words. We have already extracted the 4-grams from this dataset and divided them into training, validation, and test sets. To inspect this data, run the following within IPython:

```
import pickle
data = pickle.load(open('data.pk', 'rb'))
```

Now `data` is a Python dict which contains the vocabulary, as well as the inputs and targets for all three splits of the data. `data['vocab']` is a list of the 250 words in the dictionary; `data['vocab'][0]` is the word with index 0, and so on. `data['train_inputs']` is a $372,500 \times 3$ matrix where each row gives the indices of the 3 context words for one of the 372,500 training cases. `data['train_targets']` is a vector giving the index of the target word for each training case. The validation and test sets are handled analogously.

Now look at the file `language_model.ipynb`, which contains the starter code for the assignment. Even though you only have to modify a few specific locations in the code, you may want to read through this code before starting the assignment.

Part 1: Linear Embedding – GLoVE

In this section, we will be implementing a simplified version of GLoVE [Pennington et al., 2014]. Given a corpus with V distinct words, we define the co-occurrence matrix $X \in V \times V$ with entries X_{ij} representing the frequency of the i -th word and j -th word in the corpus appearing in the same context - in our case the adjacent words. GLoVE aims to find a d -dimensional embedding of the

¹Adapted from the practical developed by George E. Dahl for deep learning class

words that preserves properties of the co-occurrence matrix by representing the i -th word with a d -dimensional vector $\mathbf{w}_i \in \mathbb{R}^d$ and a scalar bias $b_i \in \mathbb{R}$. This objective can be written as²:

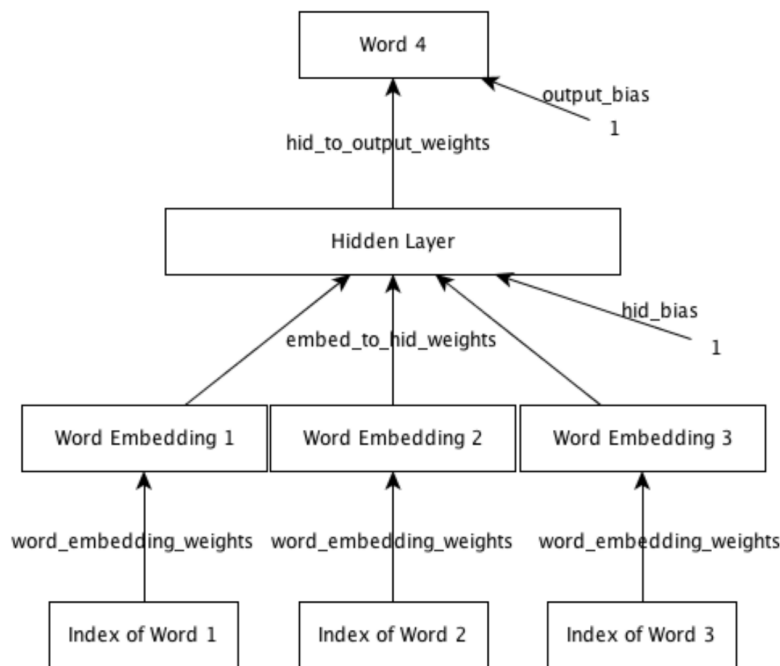
$$L(\{\mathbf{w}_i, b_i\}_{i=1}^V) = \sum_{i,j=1}^V (\mathbf{w}_i^\top \mathbf{w}_j + b_i + b_j - \log X_{ij})^2 \quad (1)$$

When the bias terms are omitted, then GLoVe corresponds to finding a rank- d symmetric factorization of the co-occurrence matrix.

1. Given the vocabulary size V and embedding dimensionality d , how many trainable parameters does the GLoVe model have?
2. Write the gradient of the loss function with respect to one parameter vector \mathbf{w}_i .
3. Implement the gradient update of GLoVe in `language_model.ipynb`.
4. Train the model with varying dimensionality d . Which d leads to optimal validation performance? Why does / doesn't larger d always lead to better validation error?

Part 2: Network architecture

In this assignment, we will train a neural language model like the one we covered in lecture and as in [Bengio et al., 2003]. It receives as input 3 consecutive words, and its aim is to predict a distribution over the next word (the target word). We train the model using the cross-entropy criterion, which is equivalent to maximizing the probability it assigns to the targets in the training set. Hopefully it will also learn to make sensible predictions for sequences it hasn't seen before. The model architecture is as follows:



The network consists of an input layer, embedding layer, hidden layer and output layer. The input consists of a sequence of 3 consecutive words, given as integer valued indices. (*i.e.*, the 250 words

²We have simplified the objective by omitting the weighting function and the additional weight vector $\tilde{\mathbf{w}}$, due to the symmetry of our co-occurrence matrix. For the complete algorithm please see [Pennington et al., 2004].

in our dictionary are arbitrarily assigned integer values from 0 to 249.) The embedding layer maps each word to its corresponding vector representation. This layer has $3 \times D$ units, where D is the embedding dimension, and it essentially functions as a lookup table. We share the same lookup table between all 3 positions, i.e. we don't learn a separate word embedding for each context position. The embedding layer is connected to the hidden layer, which uses a logistic nonlinearity. The hidden layer in turn is connected to the output layer. The output layer is a softmax over the 250 words.

As a warm-up, please answer the following question.

1. As above, assume we have 250 words in the dictionary and use the previous 3 words as inputs. Suppose we use a 16-dimensional word embedding and a hidden layer with 128 units. The trainable parameters of the model consist of 3 weight matrices and 2 sets of biases. What is the total number of trainable parameters in the model? Which part of the model has the largest number of trainable parameters?

Part 3: Training the Neural Network

In this part of the assignment, you implement a method which computes the gradient using backpropagation. To start you out, the `Model` class contains several important methods used in training:

- `compute_activations` computes the activations of all units on a given input batch
- `compute_loss` computes the total cross-entropy loss on a mini-batch
- `evaluate` computes the average cross-entropy loss for a given set of inputs and targets

You will need to complete the implementation of two additional methods which are needed for training:

- `compute_loss_derivative` computes the derivative of the loss function with respect to the output layer inputs. In other words, if C is the cost function, and the softmax computation is

$$y_i = \frac{e^{z_i}}{\sum_j e^{z_j}} \tag{2}$$

this function should compute a $B \times N_V$ matrix where the entries correspond to the partial derivatives $\partial C / \partial z_i$

- `back_propagate` is the function which computes the gradient of the loss with respect to model parameters using backpropagation. It uses the derivatives computed by `compute_loss_derivative`. Some parts are already filled in for you, but you need to compute the matrices of derivatives for `embed_to_hid_weights`, `hid_bias`, `hid_to_output_weights`, and `output_bias`. These matrices have the same sizes as the parameter matrices (see previous section).

In order to implement backpropagation efficiently, you need to express the computations in terms of matrix operations, rather than `for` loops. You should first work through the derivatives on pencil and paper. First, apply the chain rule to compute the derivatives with respect to individual units, weights, and biases. Next, take the formulas you've derived, and express them in matrix form. You should be able to express all of the required computations using only matrix multiplication, matrix transpose, and elementwise operations – no `for` loops! If you want inspiration, read through the code for `Model.compute_activations` and try to understand how the matrix operations correspond to the computations performed by all the units in the network.

To make your life easier, we have provided the routine `check_gradients`, which checks your gradients using finite differences. You should make sure this check passes before continuing with the assignment.

Once you've implemented the gradient computation, you'll need to train the model. The function `train` in `language_model.ipynb` implements the main training procedure. It takes two arguments:

- `embedding_dim`: The number of dimensions in the distributed representation
- `num_hid`: The number of hidden units

For example, execute the following:

```
model = train(16, 128)
```

As the model trains, the script prints out some numbers that tell you how well the training is going. It shows:

- The cross entropy on the last 100 mini-batches of the training set. This is shown after every 100 mini-batches.
- The cross entropy on the entire validation set every 1000 mini-batches of training.

At the end of training, this function shows the cross entropies on the training, validation and test sets. It will return a `Model` instance. To convince us that you have correctly implemented the gradient computations, please include the following with your assignment submission:

- You will submit `language_model.ipynb` through e-mail. You do not need to modify any of the code except the parts we asked you to implement.
- In your writeup, include the output of the function `print_gradients`. This prints out part of the gradients for a partially trained network which we have provided, and we will check them against the correct outputs. *Important*: make sure to give the output of `print_gradients`, not `check_gradients`.

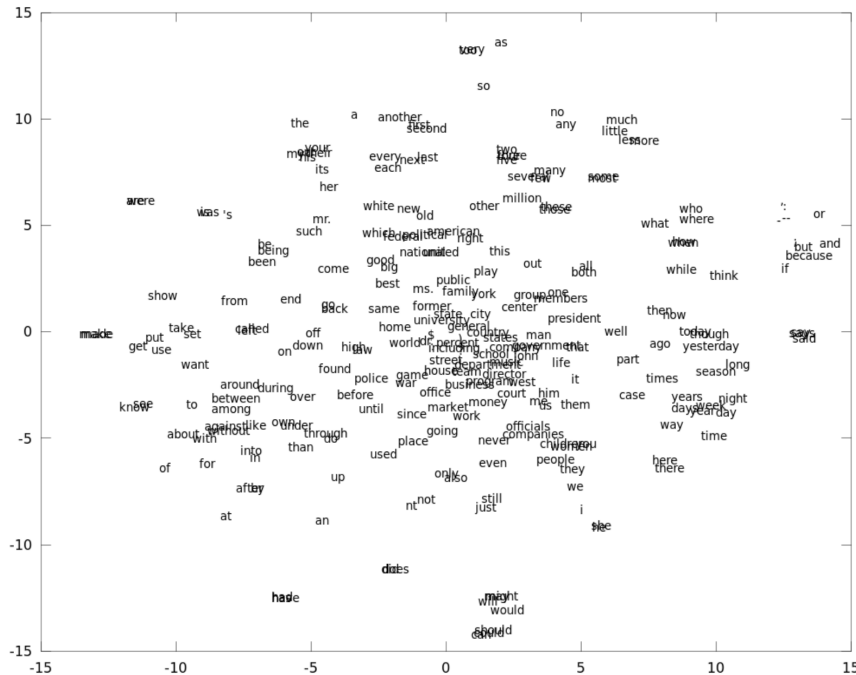
Part 4: Analysis

In this part, you will analyze the representation learned by the network. You should first train a model with a 16-dimensional embedding and 128 hidden units, as discussed in the previous section; you'll use this trained model for the remainder of this section. **Important**: if you've made any fixes to your gradient code, you must reload the `language_model` module and then re-run the training procedure. Python does not reload modules automatically, and you don't want to accidentally analyze an old version of your model.

These methods of the `Model` class can be used for analyzing the model after the training is done.

- `display_nearest_words` lists the words whose embedding vectors are nearest to the given word
- `word_distance` computes the distance between the embeddings of two words
- `predict_next_word` shows the possible next words the model considers most likely, along with their probabilities

- `tsne_plot` creates a 2-dimensional embedding of the distributed representation space using an algorithm called t-SNE [van der Maaten and Hinton, 2008]. You don't need to know what this is for the assignment, but we may cover it later in the course. Nearby points in this 2-D space are meant to correspond to nearby points in the 16-D space. From the learned model, you can create pictures that are given above:



Using these methods, please answer the following questions.

1. Pick three words from the vocabulary that go well together (for example, 'government of united', 'city of new', 'life in the', 'he is the' etc.). Use the model to predict the next word. Does the model give sensible predictions? Try to find an example where it makes a plausible prediction even though the 4-gram wasn't present in the dataset (`raw_sentences.txt`). To help you out, the function `find_occurrences` lists the words that appear after a given 3-gram in the training set.
2. Plot the 2-dimensional visualization using the method `tsne_plot_representation`. Look at the plot and find a few clusters of related words. What do the words in each cluster have in common? Plot the 2-dimensional visualization using the method `tsne_plot_GLoVE_representation` for a 256 dimensional embedding. How do the t-SNE embeddings for both models compare? Plot the 2-dimensional visualization using the method `plot_2d_GLoVE_representation`. How does this compare to the t-SNE embeddings? (You don't need to include the plots with your submission.)
3. Are the words 'new' and 'york' close together in the learned representation? Why or why not?
4. Which pair of words is closer together in the learned representation: ('government', 'political'), or ('government', 'university')? Why do you think this is?

Grading

The assignment will be graded out of 4: 0 (*no submission*), 1 (*an attempt at a solution*), 2 (*a partially correct solution*), 3 (*a mostly correct solution*), 4 (*a correct solution*), 5 (*a particularly creative or insightful solution*).

What to Hand In

You are required to submit all your code along with a report in pdf format. The codes you will submit should be well commented and in the form of a Jupyter notebook. Your report should include the answers to the given questions and your observations about your experimental analysis. Finally, prepare a ZIP file named `name-surname(s)-practical1.zip` containing

- Your code file `language_model.ipynb`
- A pdf file titled `practical1-report.pdf` containing the following:
 - Answers to the questions from Part 1
 - Answer to the question from Part 2
 - The output of `print_gradients()`
 - Answers to all four questions from Part 4

The ZIP file will be submitted via email to `enkaranfiles@gmail.com`.

Late policy

You may use up to five *extension* days (in total) over the course of the semester for the programming assignments. Late submission will not be allowed.

Academic Integrity

All work on assignments must be done individually unless stated otherwise. You are encouraged to discuss with your other classmates about the given assignments, but these discussions should be carried out in an abstract way. That is, discussions related to a particular solution to a specific problem (either in actual code or in the pseudocode) will not be tolerated. In short, turning in someone else's work, in whole or in part, as your own will be considered as a violation of academic integrity. Please note that the former condition also holds for the material found on the web as everything on the web has been written by someone else.

References

Jeffrey Pennington, Richard Socher, and Christopher D. Manning. GloVe: Global Vectors for Word Representatio. *Empirical Methods in Natural Language Processing (EMNLP)*, 2014.

Yoshua Bengio, Réjean Ducharme, Pascal Vincent, and Christian Jauvin. A Neural Probabilistic Language Model. *Journal of Machine Learning Research*, Vol 3, 1137-1155, February 2003.

Laurens van der Maaten and Geoffrey Hinton. Visualizing Data using t-SNE. *Journal of Machine Learning Research*, Vol 9, 2579-2605, November 2008.