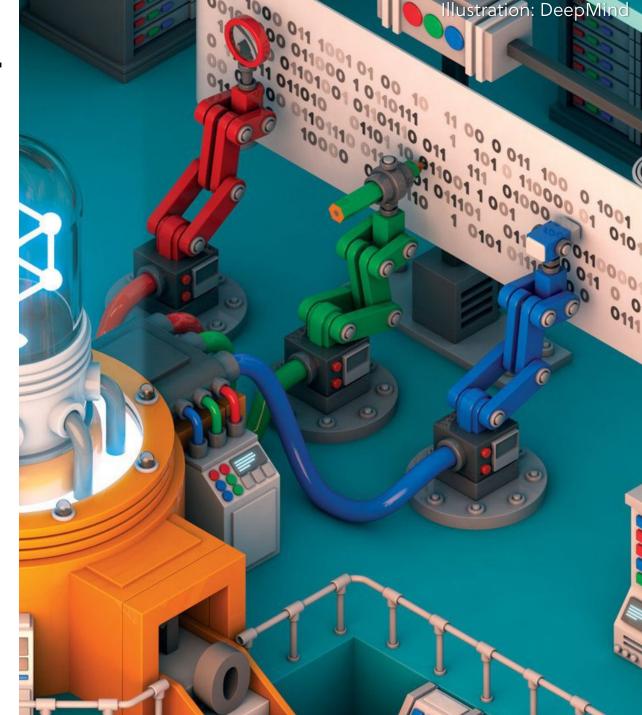


Previously on CMP784

- Content-based attention
- Location-based attention
- Soft vs. hard attention
- Show, Attend and Tell
- Self-attention and Transformer networks
- Vision Transformers
- Pretraining during transformers



Lecture overview

- Supervised vs. Unsupervised Learning
- Generative Modeling
- Basic Foundations
 - -Sparse Coding
 - -Autoencoders
- Autoregressive Generative Models

Disclaimer: Much of the material and slides for this lecture were borrowed from

- Pieter Abbeel, Peter Chen, Jonathan Ho, Aravind Srinivas' Berkeley CS294-158 class
- Ruslan Salakhutdinov's talk titled "Unsupervised Learning: Learning Deep Generative Models"
- Yoshua Bengio's IDT6266 class
- Bill Freeman, Antonio Torralba and Phillip Isola's MIT 6.869 class
- Nal Kalchbrenner's talks on "Generative Modelling as Sequence Learning" and "Generative Models of Language and Images"
- Justin Johnson's EECS 498/598 class

Supervised Learning

Data: (x, y) x is data, y is label

Goal: Learn a function to map x -> y

Examples: Classification, regression, object detection, semantic segmentation, image captioning, sentiment analysis, etc.

Classification



Cat

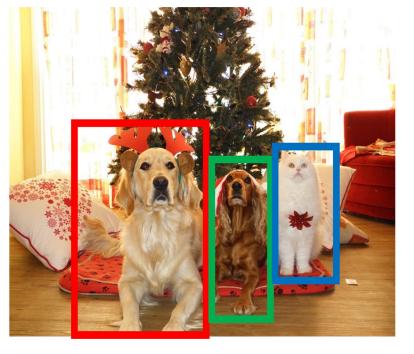
Supervised Learning

Data: (x, y) x is data, y is label

Goal: Learn a function to map x -> y

Examples: Classification, regression, object detection, semantic segmentation, image captioning, sentiment analysis, etc.

Object Detection



DOG, DOG, CAT

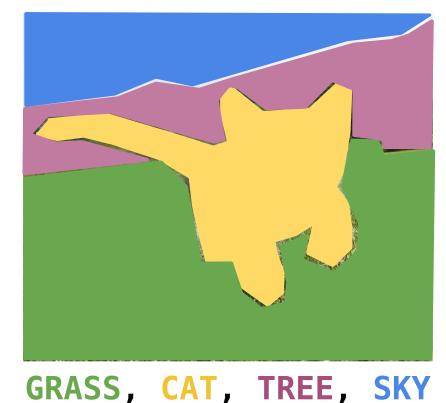
Supervised Learning

Data: (x, y) x is data, y is label

Goal: Learn a function to map x -> y

Examples: Classification, regression, object detection, semantic segmentation, image captioning, sentiment analysis, etc.

Semantic Segmentation



Supervised Learning

Data: (x, y) x is data, y is label

Goal: Learn a function to map x -> y

Examples: Classification, regression, object detection, semantic segmentation, image captioning, sentiment analysis, etc.

Image captioning



A cat sitting on a suitcase on the floor

Supervised Learning

Data: (x, y) x is data, y is label

Goal: Learn a function to map x -> y

Sentiment Analysis

"This Movie is amazing. It has a great plot and talented actors, and the supporting cast is really good as well."

Examples: Classification, regression, object detection, semantic segmentation, image captioning, sentiment analysis, etc.



Supervised Learning

Data: (x, y) x is data, y is label

Goal: Learn a function to map x -> y

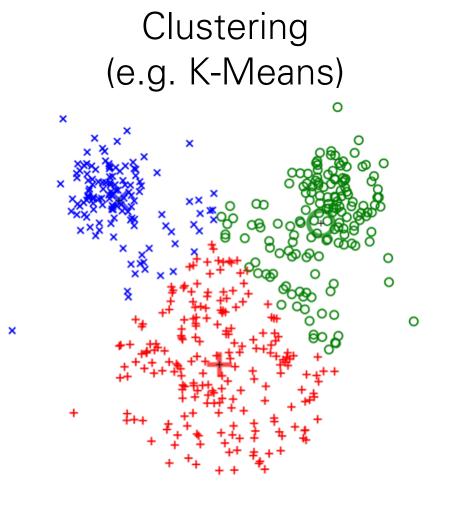
Unsupervised Learning

Data: x

Just data, no labels!

Goal: Learn some underlying hidden structure of the data

Examples: Classification, regression, object detection, semantic segmentation, image captioning, sentiment analysis, etc.



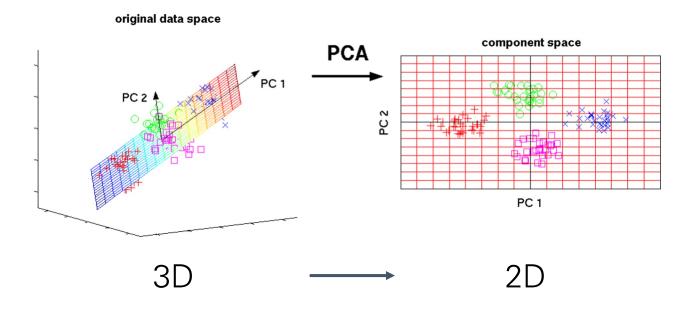
Unsupervised Learning

Data: x

Just data, no labels!

Goal: Learn some underlying hidden structure of the data

Dimensionality Reduction (e.g. Principal Components Analysis)



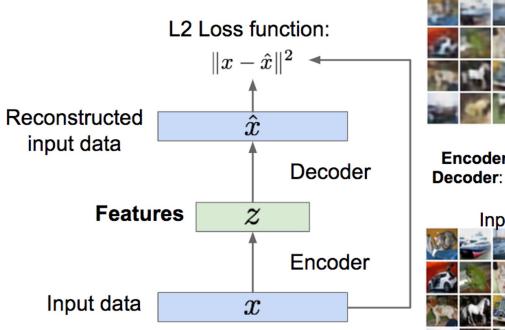
Unsupervised Learning

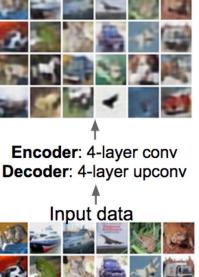
Data: x

Just data, no labels!

Goal: Learn some underlying hidden structure of the data

Feature Learning (e.g. autoencoders)





Reconstructed data

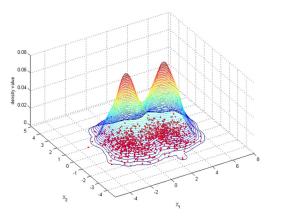
Unsupervised Learning

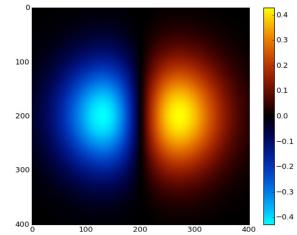
Data: x

Just data, no labels!

Goal: Learn some underlying hidden structure of the data

Density Estimation





Unsupervised Learning

Data: x

Just data, no labels!

Goal: Learn some underlying hidden structure of the data

Supervised Learning

Data: (x, y) x is data, y is label

Goal: Learn a function to map x -> y

Unsupervised Learning

Data: x

Just data, no labels!

Goal: Learn some underlying hidden structure of the data

Examples: Classification, regression, object detection, semantic segmentation, image captioning, sentiment analysis, etc.

Discriminative Model: Learn a probability distribution p(y|x)

Generative Model: Learn a probability distribution p(x) Data: x



Conditional Generative Model: Learn p(x|y) Label: y Cat

Discriminative Model: Learn a probability distribution p(y|x)

Generative Model: Learn a probability distribution p(x) Data: x



Conditional Generative Model: Learn p(x|y)

Label: y Cat Probability Recap:

Density Function p(x) assigns a positive number to each possible x; higher numbers mean x is more likely

Density functions are **normalized**:

 $\int_X p(x)dx = 1$

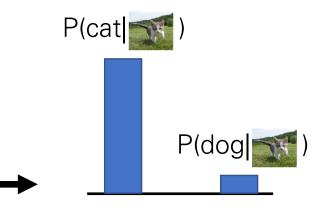
Different values of x **compete** for density

Discriminative Model: Learn a probability distribution p(y|x)

Generative Model: Learn a probability distribution p(x)

Conditional Generative Model: Learn p(x|y) Data: x





Density functions are **normalized**:

 $\int p(x)dx = 1$

Different values of x **compete** for density

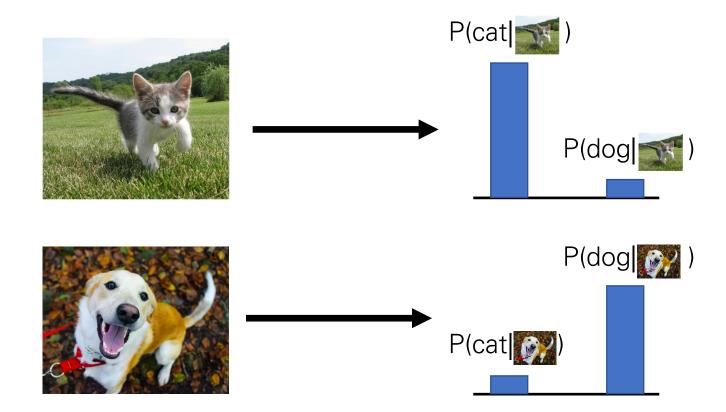
Density Function

p(x) assigns a positive number to each possible x; higher numbers mean x is more likely

Discriminative Model: Learn a probability distribution p(y|x)

Generative Model: Learn a probability distribution p(x)

Conditional Generative Model: Learn p(x|y)

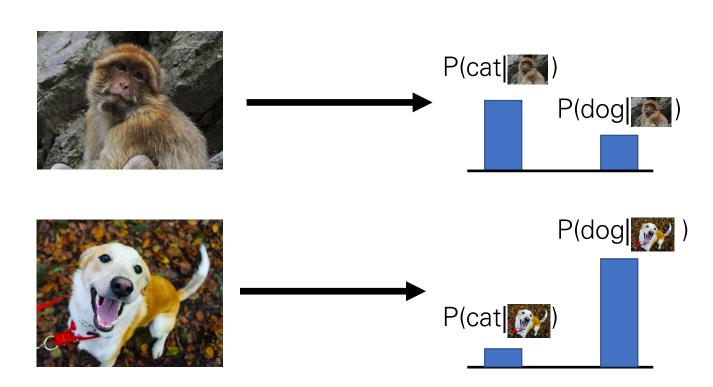


Discriminative model: the possible labels for each input "compete" for probability mass. But no competition between **images**

Discriminative Model: Learn a probability distribution p(y|x)

Generative Model: Learn a probability distribution p(x)

Conditional Generative Model: Learn p(x|y)

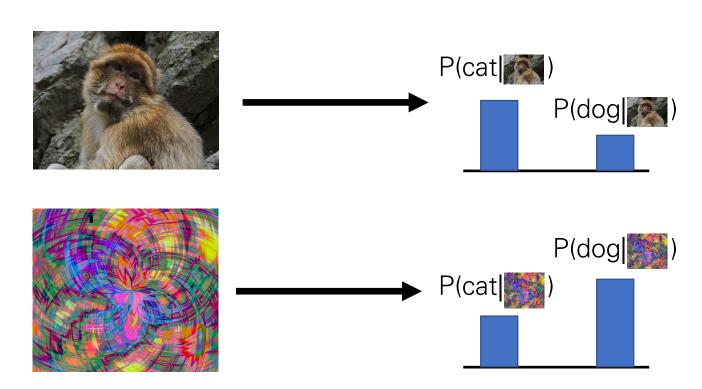


Discriminative model: No way for the model to handle unreasonable inputs; it must give label distributions for all images

Discriminative Model: Learn a probability distribution p(y|x)

Generative Model: Learn a probability distribution p(x)

Conditional Generative Model: Learn p(x|y)

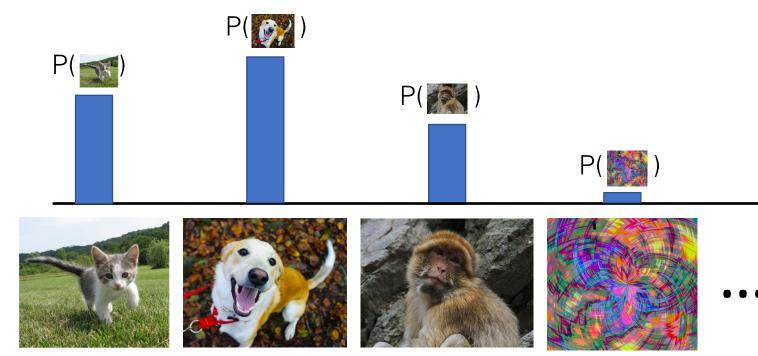


Discriminative model: No way for the model to handle unreasonable inputs; it must give label distributions for all images

Discriminative Model: Learn a probability distribution p(y|x)

Generative Model: Learn a probability distribution p(x)

Conditional Generative Model: Learn p(x|y)

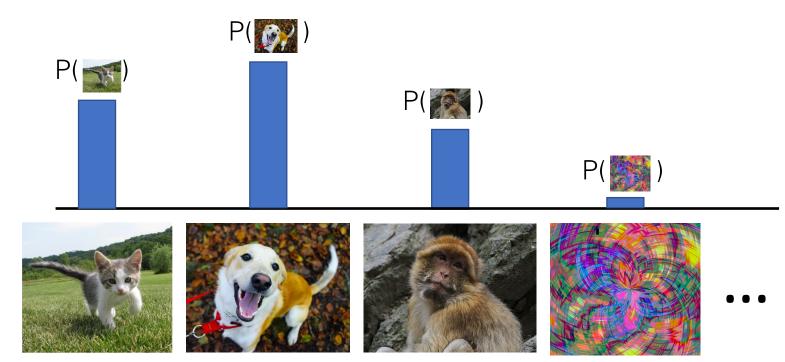


Generative model: All possible images compete with each other for probability mass

Discriminative Model: Learn a probability distribution p(y|x)

Generative Model: Learn a probability distribution p(x)

Conditional Generative Model: Learn p(x|y)



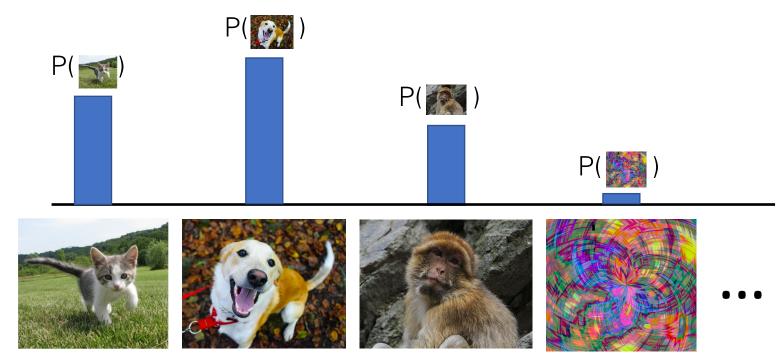
Generative model: All possible images compete with each other for probability mass

Requires deep image understanding! Is a dog more likely to sit or stand? How about 3-legged dog vs 3-armed monkey?

Discriminative Model: Learn a probability distribution p(y|x)

Generative Model: Learn a probability distribution p(x)

Conditional Generative Model: Learn p(x|y)



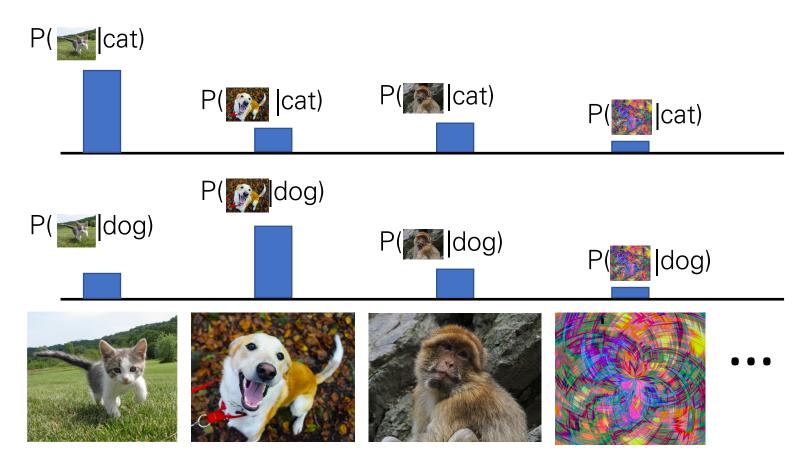
Generative model: All possible images compete with each other for probability mass

Model can "reject" unreasonable inputs by assigning them small values

Discriminative Model: Learn a probability distribution p(y|x)

Generative Model: Learn a probability distribution p(x)

Conditional Generative Model: Learn p(x|y)



Conditional Generative Model: Each possible label induces a competition among all images

Discriminative Model: Learn a probability distribution p(y|x)

Generative Model: Learn a probability distribution p(x)

Conditional Generative Model: Learn p(x|y) Recall Bayes' Rule:

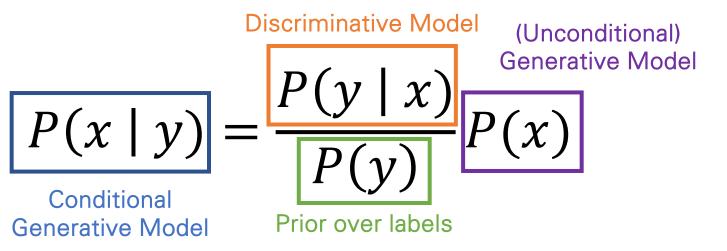
$$P(x \mid y) = \frac{P(y \mid x)}{P(y)} P(x)$$

Discriminative Model: Learn a probability distribution p(y|x)

Generative Model: Learn a probability distribution p(x)

Conditional Generative Model: Learn p(x|y)

Recall Bayes' Rule:



We can build a conditional generative model from other components!

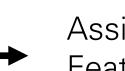
What can we do with a discriminative model?

Discriminative Model:

Learn a probability distribution p(y|x)

Generative Model: Learn a probability distribution p(x)

Conditional Generative Model: Learn p(x|y)



Assign labels to data Feature learning (with labels)

What can we do with a discriminative model?

Discriminative Model:

Learn a probability distribution p(y|x)

Generative Model: Learn a probability distribution p(x)

Conditional Generative Model: Learn p(x|y)



Assign labels to data Feature learning (with labels)

Detect outliers Feature learning (without labels) Sample to **generate** new data

What can we do with a discriminative model?

Discriminative Model:

Learn a probability distribution p(y|x)

Generative Model: Learn a probability distribution p(x)

Conditional Generative Model: Learn p(x|y)



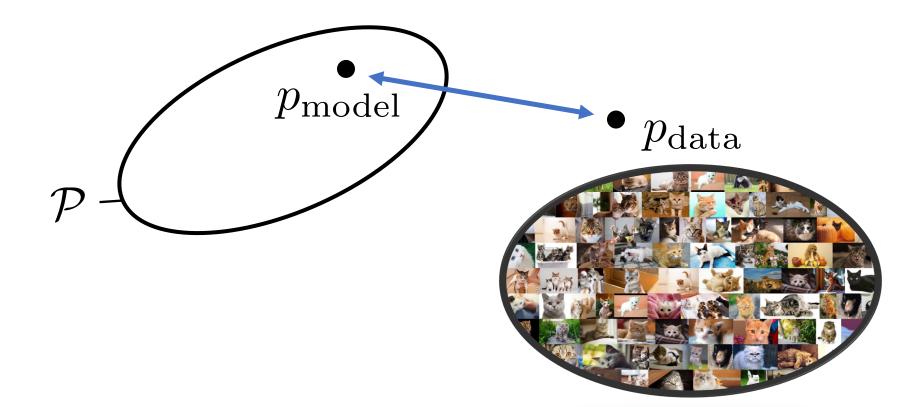
Assign labels to data Feature learning (with labels)

Detect outliers Feature learning (without labels) Sample to **generate** new data

Assign la Generate

Assign labels, while rejecting outliers! Generate new data conditioned on input labels

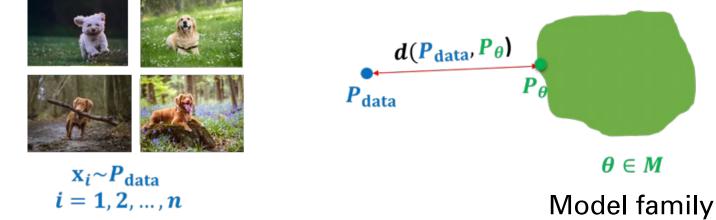
Generative Modeling



• Goal: Learn some underlying hidden structure of the training samples to generate novel samples from same data distribution

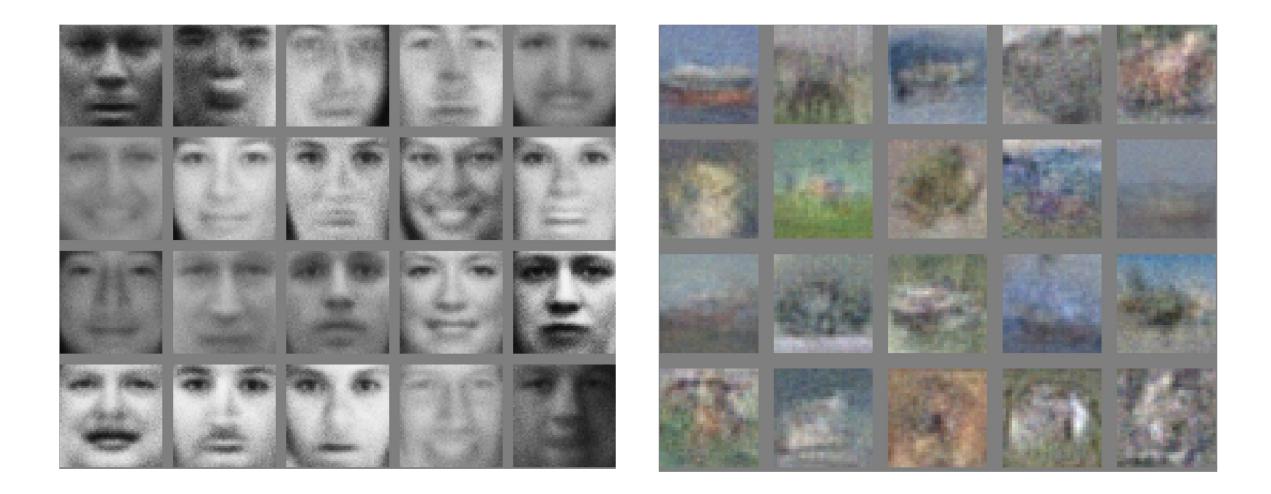
Learning a generative model

• We are given a training set of examples, e.g., images of dogs



- We want to learn a probability distribution p(x) over images x s.t.
 - Generation: If we sample $x_{new} \sim p(x)$, x_{new} should look like a dog (sampling)
 - Density estimation: p(x) should be high if x looks like a dog, and low otherwise (anomaly detection)
 - **Unsupervised representation learning**: We should be able to learn what these images have in common, e.g., ears, tail, etc. (features)

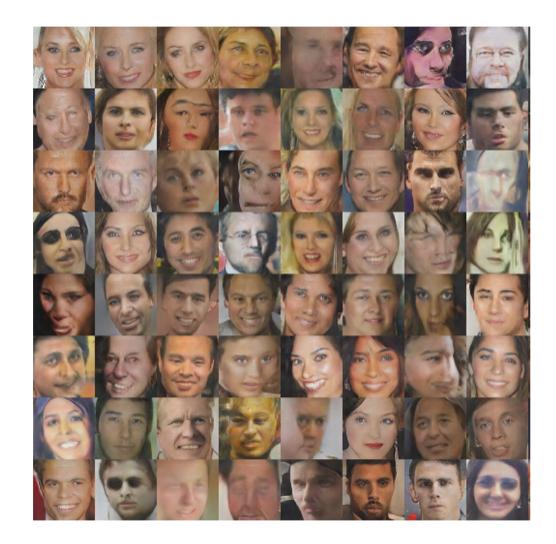
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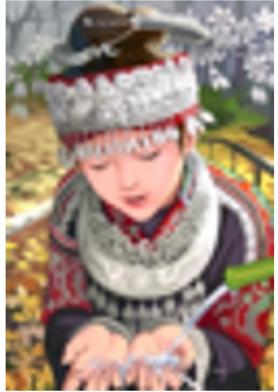


[DCGAN, Radford, Metz, Chintala 2015]





bicubic (21.59dB/0.6423)



SRResNet (23.53dB/0.7832)



SRGAN (21.15dB/0.6868)



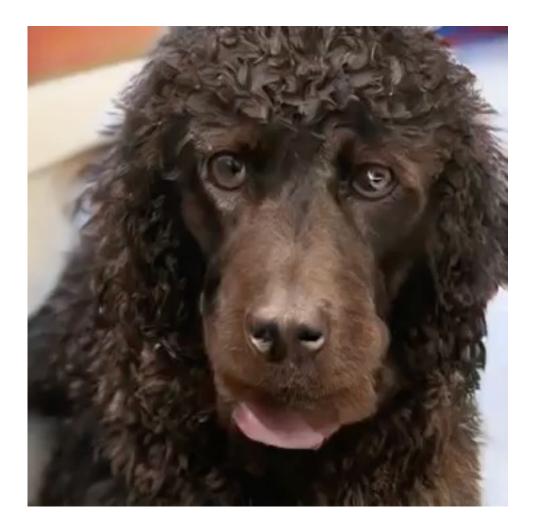
original



37



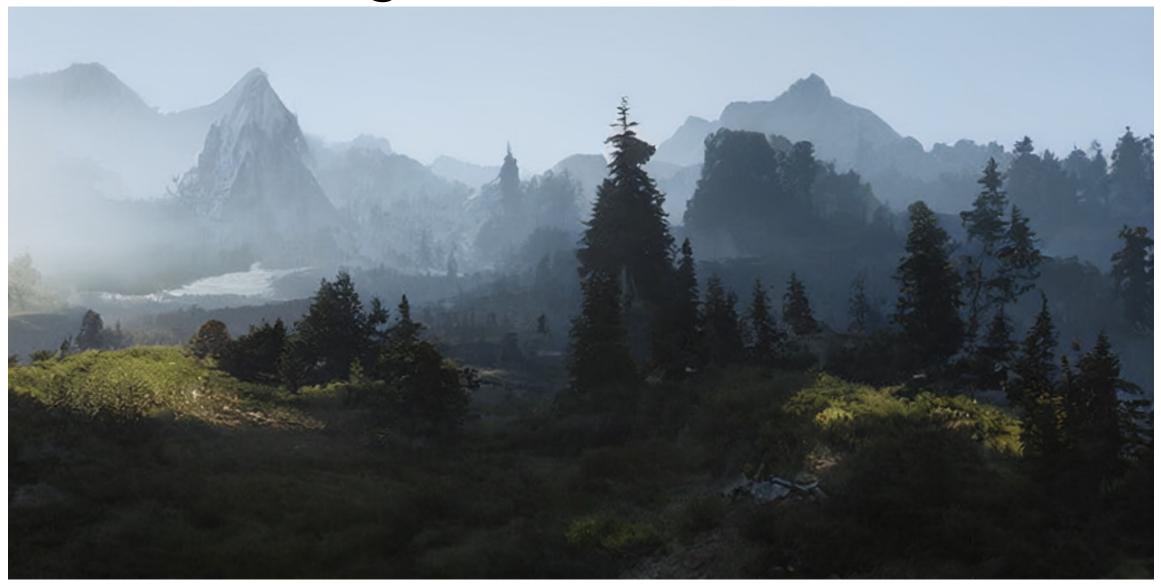
[CycleGAN: Zhu, Park, Isola & Efros, 2017] 38



[BigGAN, Brock, Donahue, Simonyan, 2018] ₃₉



[StyleGAN, Karras, Laine, Aila, 2018] 40



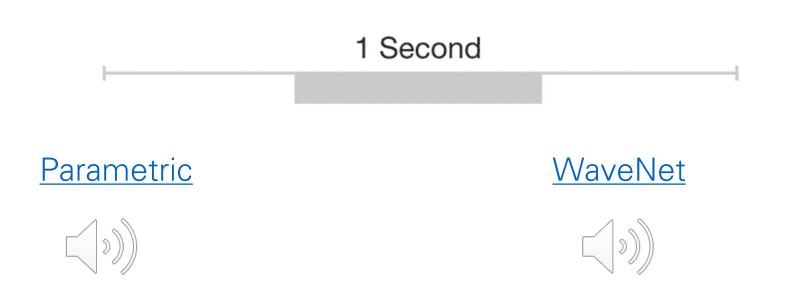
[Latent Diffusion, Rombach, Blattmann, Lorenz, Esser, Ommer, 2022] 41



[Latent Diffusion, Rombach, Blattmann, Lorenz, Esser, Ommer, 2022] 42

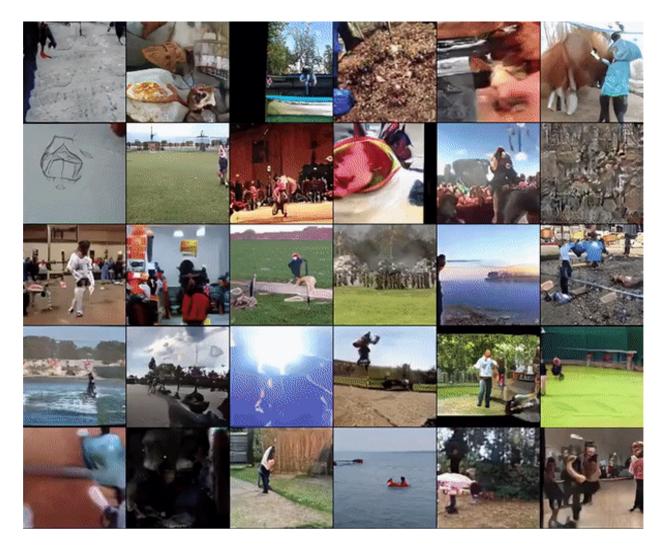
Generate Audio





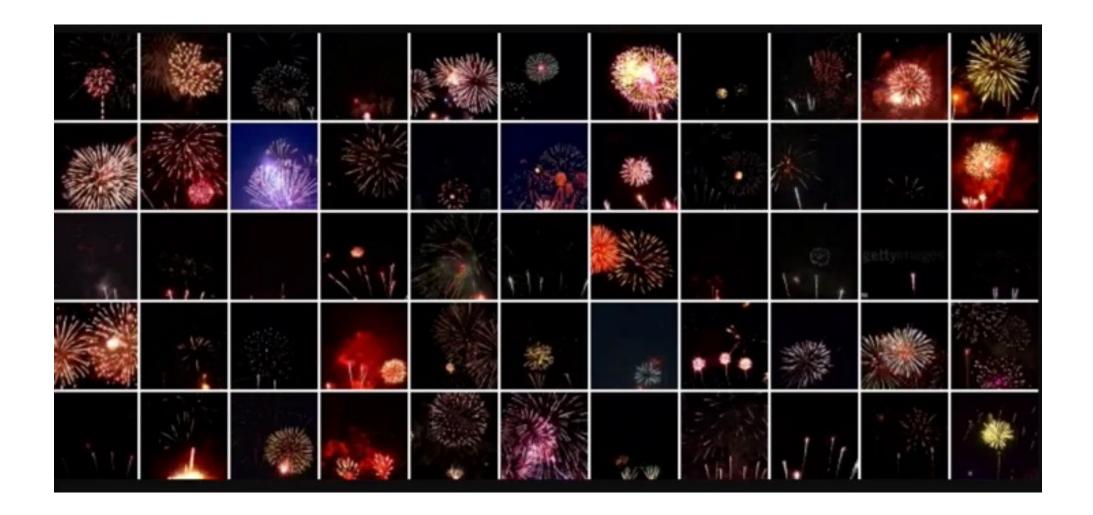
[WaveNet, Oord et al., 2018] 43

Generate Video



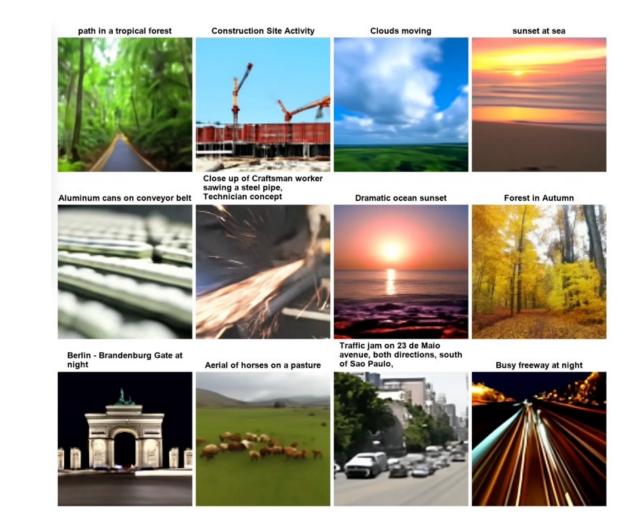
DVD-GAN: Adversarial Video Generation on Complex Datasets, Clark, Donahue, Simonyan, 2019

Generate Video



[Video Diffusion Models, Ho, Salimans, Gritsenko, Chan, Norouzi, Fleet, 2022] 45

Generate Video



[Video Diffusion Models, Ho, Salimans, Gritsenko, Chan, Norouzi, Fleet, 2022] 46

Generate Text

PANDARUS:

Alas, I think he shall be come approached and the day When little srain would be attain'd into being never fed, And who is but a chain and subjects of his death, I should not sleep.

Second Senator:

They are away this miseries, produced upon my soul, Breaking and strongly should be buried, when I perish The earth and thoughts of many states.

DUKE VINCENTIO: Well, your wit is in the care of side and that.

Generate Math

\begin{proof}

We may assume that $\lambda = 1$ is an abelian sheaf on $\lambda = C$.

Let $\operatorname{F}\$ be a fibered complex. Let $\operatorname{F}\$ be a category.

\begin{enumerate}

```
\item \hyperref[setain-construction-phantom]{Lemma}
\label{lemma-characterize-quasi-finite}
```

Let $\operatorname{F}\$ be an abelian quasi-coherent sheaf on $\operatorname{C}\$.

Let $\operatorname{F}\$ be a coherent $\operatorname{C}_X\$ -module. Then $\operatorname{C}_Y\$ is an abelian catenary over C_S . \item The following are equivalent

\begin{enumerate}

\item $\lambda_{F}\$ is an $\lambda_{O}_X\-module. \end{lemma}$

For $\bigoplus_{n=1,\ldots,m}$ where $\mathcal{L}_{m_{\bullet}} = 0$, hence we can find a closed subset \mathcal{H} in \mathcal{H} and any sets \mathcal{F} on X, U is a closed immersion of S, then $U \to T$ is a separated algebraic space.

Proof. Proof of (1). It also start we get

 $S = \operatorname{Spec}(R) = U \times_X U \times_X U$

and the comparison in the fibre product covering we have to prove the lemma generated by $\coprod Z \times_U U \to V$. Consider the maps M along the set of points Sch_{fppf} and $U \to U$ is the fibre category of S in U in Section, ?? and the fact that any U affine, see Morphisms, Lemma ??. Hence we obtain a scheme S and any open subset $W \subset U$ in Sh(G) such that $Spec(R') \to S$ is smooth or an

 $U = \bigcup U_i \times_{S_i} U_i$

which has a nonzero morphism we may assume that f_i is of finite presentation over S. We claim that $\mathcal{O}_{X,x}$ is a scheme where $x, x', s'' \in S'$ such that $\mathcal{O}_{X,x'} \to \mathcal{O}'_{X',x'}$ is separated. By Algebra, Lemma ?? we can define a map of complexes $\operatorname{GL}_{S'}(x'/S'')$ and we win.

To prove study we see that $\mathcal{F}|_U$ is a covering of \mathcal{X}' , and \mathcal{T}_i is an object of $\mathcal{F}_{X/S}$ for i > 0 and \mathcal{F}_p exists and let \mathcal{F}_i be a presheaf of \mathcal{O}_X -modules on \mathcal{C} as a \mathcal{F} -module. In particular $\mathcal{F} = U/\mathcal{F}$ we have to show that

 $\widetilde{M}^{\bullet} = \mathcal{I}^{\bullet} \otimes_{\mathrm{Spec}(k)} \mathcal{O}_{S,s} - i_X^{-1} \mathcal{F})$

is a unique morphism of algebraic stacks. Note that

Arrows = $(Sch/S)_{fppf}^{opp}, (Sch/S)_{fppf}$

and

$$V = \Gamma(S, \mathcal{O}) \longmapsto (U, \operatorname{Spec}(A))$$

is an open subset of X. Thus U is affine. This is a continuous map of X is the inverse, the groupoid scheme S.

Proof. See discussion of sheaves of sets.

The result for prove any open covering follows from the less of Example ??. It may replace S by $X_{spaces,\acute{e}tale}$ which gives an open subspace of X and T equal to S_{Zar} , see Descent, Lemma ??. Namely, by Lemma ?? we see that R is geometrically regular over S.

Generate Text

Prompt [human written]: A train carriage containing controlled nuclear materials was stolen in Cincinnati today. Its whereabouts are unknown.

GPT-2: The incident occurred on the downtown train line, which runs from Covington and Ashland stations. In an email to Ohio news outlets, the U.S. Department of Energy said it is working with the Federal Railroad Administration to find the thief.

'The theft of this nuclear material will have significant negative consequences on public and environmental health, our workforce and the economy of our nation,' said Tom Hicks, the U.S. Energy Secretary, in a statement. 'Our top priority is to secure the theft and ensure it doesn't happen again.'

The stolen material was taken from the University of Cincinnati's Research Triangle Park nuclear research site, according to a news release from Department officials.

The Nuclear Regulatory Commission did not immediately release any information. According to the release, the U.S. Department of Energy's Office of Nuclear Material Safety and Security is leading that team's investigation.

'The safety of people, the environment and the nation's nuclear stockpile is our highest priority,' Hicks said. 'We will get to the bottom of this and make no excuses.'

[OpenAl's GPT2 – Radford, Wu, Child, Luan, Amodei, Sutskever, 2019]

Generate Text

Prompt (human written): Recycling is good for the world, no, you could not be more wrong.

<u>GPT-2:</u> Recycling is NOT good for the world. It is bad for the environment, it is bad for our health, and it is bad for our economy. I'm not kidding. Recycling is not good for the environment. It is destructive to the earth and it is a major contributor to global warming. Recycling is not good for our health. It contributes to obesity and diseases like heart disease and cancer. Recycling is bad for our economy. It increases the cost of a product, and in turn, the price of everything that is made with that product. Recycling is not good for our nation. We pay a tremendous price for the privilege of having the world's most advanced and efficient recycling system. Recycling is a huge, colossal waste of time, energy, money, and resources.

[OpenAl's GPT2 – Radford, Wu, Child, Luan, Amodei, Sutskever, 2019]

Try it yourself

InferKit DEMO	9400 / 10000 weekly free characters Sign In
Generate Options Learn more in the docs.	Legolas and Gimli advanced on the orcs, raising their weapons with a harrowing war cry.
Length to generate 👔 400	Karamail, however, backed off and called upon the armies of Mordor.
Start at beginning @ Advanced Settings »	His voice rumbled forth, resonating with power, and the earth trembled.
	Korr crept up, looking for a chance to strike the orcs. All around him, hundreds of orcs were killing thousands of men.
	His black eyes seemed to pierce the darkness.
	He was panting with the effort of carrying such a heavy burden.
	But he continued forward, with the steady hiss of an undervalued seraph $ imes$ in his ear.
	He needed just a little more power.
	He concentrated his might on the earth, and almost without thinking, his sword shot out of the ground
	Generate Text × 🕞
https	s://talktotransformer.com/

Try it yourself

OpenAI's API Now Available with No Waitlist Wider availability made possible by safety progress

November 18, 2021 2 minute read OpenAI is committed to the safe deployment of AI. Since the launch of our API, we've made deploying applications faster and more streamlined while adding new safety features. Our progress with safeguards makes it possible to remove the waitlist for GPT-3. Starting today, developers in <u>supported</u> <u>countries</u> can <u>sign up</u> and start experimenting with our API right away.

Improvements to our API over the past year include the <u>Instruct Series</u> models that adhere better to human instructions, specialized endpoints for more truthful <u>question-answering</u>, and a free <u>content filter</u> to help developers mitigate abuse. Our work also allows us to review applications before they <u>go live</u>, monitor for misuse, support developers as their product scales, and better <u>understand the effects</u> of this technology.

Other changes include an improved Playground, which makes it easy to prototype with our models, an <u>example library</u> with dozens of prompts to get developers started, and <u>Codex</u>, a new model that translates natural language into code.

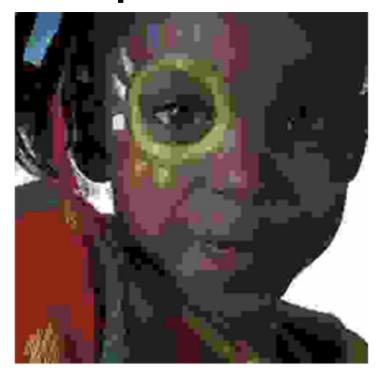
https://openai.com/api/

Compression - Lossless

Model	Bits per byte					
CIFAR-10						
PixelCNN (Oord et al., 2016)	3.03					
PixelCNN++ (Salimans et al., 2017)	2.92					
Image Transformer (Parmar et al., 2018)	2.90					
PixelSNAIL (Chen et al., 2017)	2.85					
Sparse Transformer 59M (strided)	2.80					
Enwik8						
Deeper Self-Attention (Al-Rfou et al., 2018)	1.06					
Transformer-XL 88M (Dai et al., 2018)	1.03					
Transformer-XL 277M (Dai et al., 2018)	0.99					
Sparse Transformer 95M (fixed)	0.99					
ImageNet 64x64						
PixelCNN (Oord et al., 2016)	3.57					
Parallel Multiscale (Reed et al., 2017)	3.7					
Glow (Kingma & Dhariwal, 2018)	3.81					
SPN 150M (Menick & Kalchbrenner, 2018)	3.52					
Sparse Transformer 152M (strided)	3.44					
Classical music, 5 seconds at 12 kHz						
Sparse Transformer 152M (strided)	1.97					

Generative models provide better bit-rates than distribution-unaware compression methods like JPEG, etc.

Compression - Lossy







JPEG

JPEG2000

WaveOne

[Rippel & Bourdev, 2017]

Downstream Task - Sentiment Detection

This is one of Crichton's best books. The characters of Karen Ross, Peter Elliot, Munro, and Amy are beautifully developed and their interactions are exciting, complex, and fast-paced throughout this impressive novel. And about 99.8 percent of that got lost in the film. Seriously, the screenplay AND the directing were horrendous and clearly done by people who could not fathom what was good about the novel. I can't fault the actors because frankly, they never had a chance to make this turkey live up to Crichton's original work. I know good novels, especially those with a science fiction edge, are hard to bring to the screen in a way that lives up to the original. But this may be the absolute worst disparity in quality between novel and screen adaptation ever. The book is really, really good. The movie is just dreadful.

Downstream Tasks - NLP (BERT Revolution)

	Ran	k Name	Model	URL	Score E	BoolQ (св сс	OPA I	MultiRC	ReCoRD	RTE	WiC	WSC	AX-b	AX-g
	1	JDExplore d-team	Vega v2		91.3	90.5 98.6/99	9.2 9	99.4 88	8.2/62.4	94.4/93.9	96.0	77.4	98.6	-0.4	100.0/50.0
+	2	Liam Fedus	ST-MoE-32B		91.2	92.4 96.9/98	3.0 9	99.2 8	9.6/65.8	95.1/94.4	93.5	77.7	96.6	72.3	96.1/94.1
	3	Microsoft Alexander v-team	Turing NLR v5		90.9	92.0 95.9/97	7.6 9	98.2 88	8.4/63.0	96.4/95.9	94.1	77.1	97.3	67.8	93.3/95.5
	4	ERNIE Team - Baidu	ERNIE 3.0		90.6	91.0 98.6/99	9.2 9	97.4 88	8.6/63.2	94.7/94.2	92.6	77.4	97.3	68.6	92.7/94.7
	5	Yi Tay	PaLM 540B		90.4	91.9 94.4/96	6.0 9	99.0 88	8.7/63.6	94.2/93.3	94.1	77.4	95.9	72.9	95.5/90.4
+	6	Zirui Wang	T5 + UDG, Single Model (Google Brain)		90.4	91.4 95.8/97	7.6 9	98.0 88	8.3/63.0	94.2/93.5	93.0	77.9	96.6	69.1	92.7/91.9
+	7	DeBERTa Team - Microsoft	DeBERTa / TuringNLRv4		90.3	90.4 95.7/97	7.6 9	98.4 88	8.2/63.7	94.5/94.1	93.2	77.5	95.9	66.7	93.3/93.8
	8	SuperGLUE Human Baselines	s SuperGLUE Human Baselines		89.8	89.0 95.8/98	3.9 10	0.08 [.]	1.8/51.9	91.7/91.3	93.6	80.0	100.0	76.6	99.3/99.7
+	9	T5 Team - Google	Т5		89.3	91.2 93.9/96	5.8 9	94.8 88	8.1/63.3	94.1/93.4	92.5	76.9	93.8	65.6	92.7/91.9
	10	SPoT Team - Google	Frozen T5 1.1 + SPoT		89.2	91.1 95.8/97	7.6 9	95.6 87	7.9/61.9	93.3/92.4	92.9	75.8	93.8	66.9	83.1/82.6

[https://super.gluebenchmark.com/leaderboard] 56

Downstream Tasks - Vision (Contrastive)

Method	Architecture	mAP	
<i>Transfer from labeled data:</i> Supervised baseline	ResNet-152	74.7	
<i>Transfer from unlabeled data:</i> Exemplar [17] by [13] Motion Segmentation [47] by [13] Colorization [64] by [13] Relative Position [14] by [13] Multi-task [13] Instance Discrimination [60] Deep Cluster [7] Deeper Cluster [8] Local Aggregation [66] Momentum Contrast [25]	ResNet-101 60.9 [13] ResNet-101 61.1 ResNet-101 65.5		"If, by the first day of autumn (Sept 23) of 2015, a method will exist that can match or beat the performance of R-CNN on Pascal VOC detection, without the use of any extra, human annotations (e.g. ImageNet) as pre- training, Mr. Malik promises to buy Mr. Efros one (1) gelato (2 scoops: one chocolate, one vanilla)."
Faster-RCNN trained on CPC v2	ResNet-161	76.6	Table: Data-Efficient Image Recognition using CPC
			[Henaff, Srinivas, et al.] 57

Why Unsupervised Learning?

- Given high-dimensional data $X = (x_1, \ldots, x_n)$ we want to find a low-dimensional model characterizing the population.
- Recent progress mostly in supervised DL
- Real challenges for unsupervised DL
- Potential benefits:
 - Exploit tons of unlabeled data
 - -Answer new questions about the variables observed
 - Regularizer transfer learning domain adaptation
 - Easier optimization (divide and conquer)
 - -Joint (structured) outputs

Why Latent Factors & Unsupervised Representation Learning? Because of Causality.

• If Ys of interest are among the causal factors of X, then

$$P(Y|X) = \frac{P(X|Y)P(Y)}{P(X)}$$

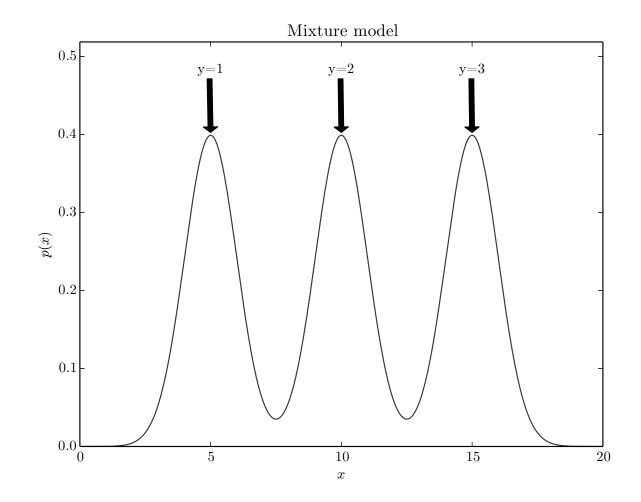
is tied to P(X) and P(X|Y), and P(X) is defined in terms of P(X|Y), i.e.

- The best possible model of X (unsupervised learning) MUST involve Y as a latent factor, implicitly or explicitly.
- Representation learning SEEKS the latent variables H that explain the variations of X, making it likely to also uncover Y.

On causal and anticausal learning, Janzing et al. ICML 2012

If Y is a Cause of X, Semi-Supervised Learning Works

- Just observing the x-density reveals the causes y (cluster ID)
- After learning p(x) as a mixture, a single labeled example per class suffices to learn p(y|x)



Invariance & Disentangling Underlying Factors

- Invariant features
- Which invariances?
- Alternative: learning to disentangle factors, i.e. keep all the explanatory factors in the representation
- Good disentangling \rightarrow avoid the curse of dimensionality
- Emerges from representation learning

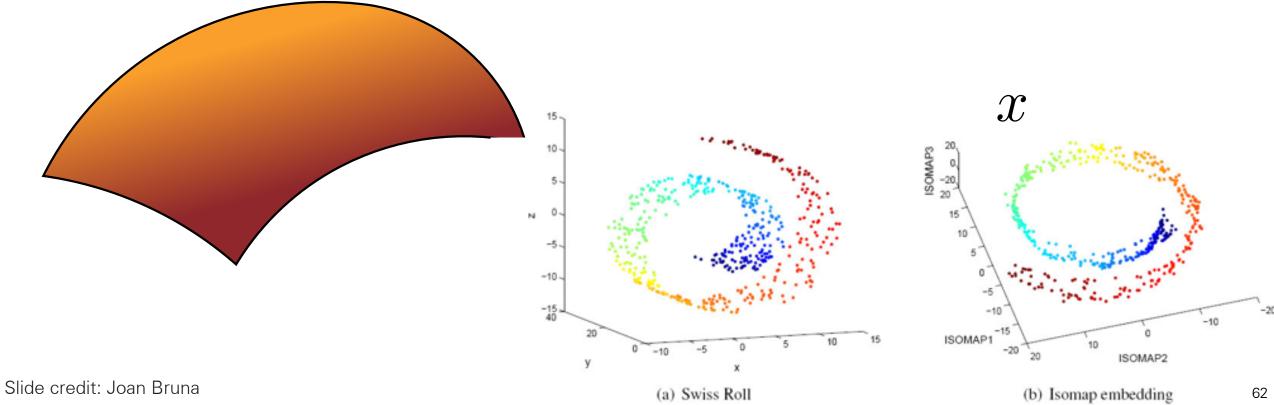


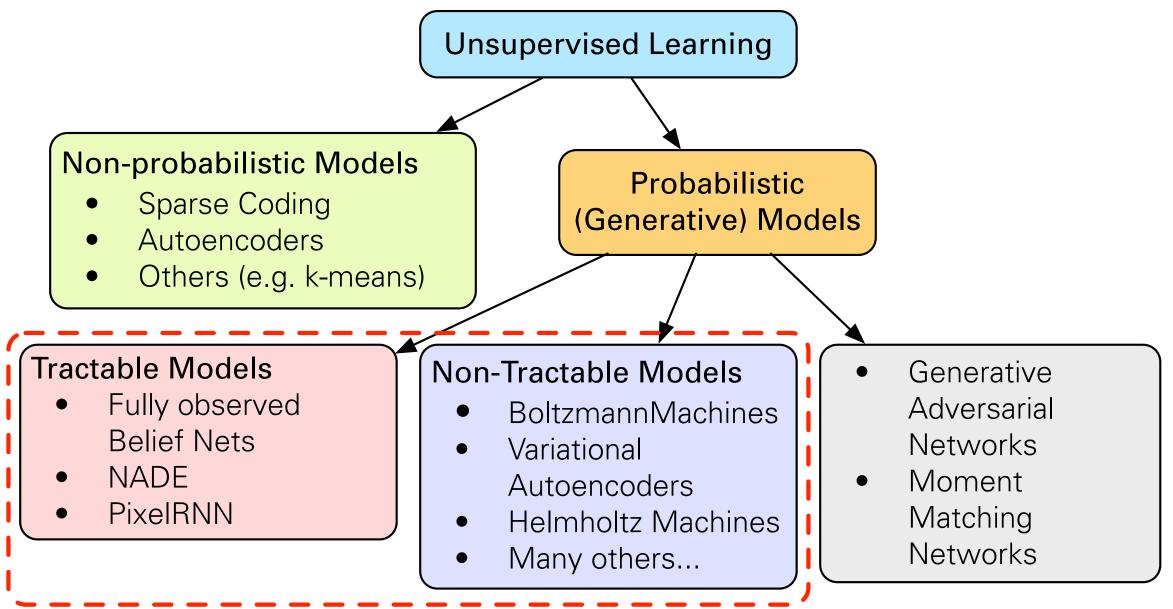


p(x), $x \in \mathbb{R}^{n}$ (or $x \in \Omega^{n}$) Curse of Dimensionality

• Challenge: How to model p(x), $x \in \mathbb{R}^N$ (or $x \in \Omega^N$) for grave N?

• An existing hypothesis is that, although the ambient dimensionality is high, the intrinsic dimensionality of x is low.





Explicit Density p(x)

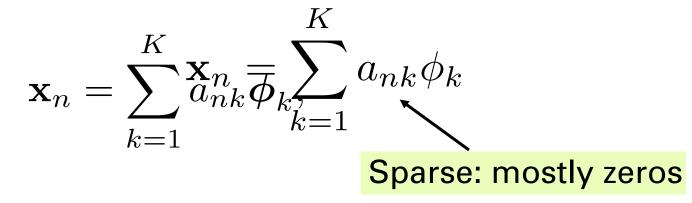
Implicit Density

Unsupervised Learning

- Basic Building Blocks:
 - Sparse Coding
 - Autoencoders
- Autoregressive Generative Models
- Generative Adversarial Networks
- Variational Autoencoders
- Normalizing Flow Models
- Diffusion Models

Sparse Coding

- Sparse coding (Olshausen & Field, 1996). Originally developed to explain early visual processing in the brain (edge detection).
- **Objective:** Given a set of input data vectors $\{\mathbf{x}_1, \mathbf{x}_2, ..., \mathbf{x}_N\}$, learn a dictionary of bases, such that: $\{\phi_1, \phi_2, ..., \phi_K\}$,



• Each data vector is represented as a sparse linear combination of bases.

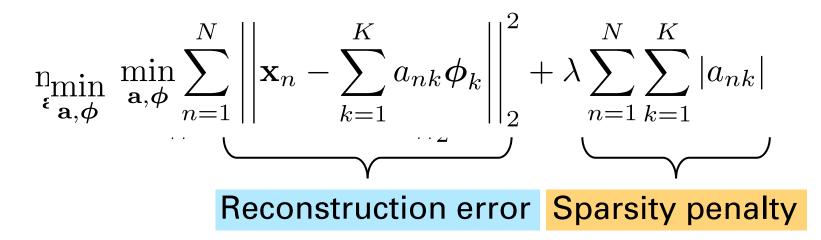
Sparse Coding

Natural Images Learned bases: "Edges" New example = 0.8 * +0.5 *+0.3 * $= 0.8 * \phi_{36} + 0.3 * \phi_{42} + 0.5 *$ ϕ_{65} X [0.0, 0.0, ... **0.8**, ..., **0.3**, ..., **0.5**, ...] = coefficients (feature representation)

Slide Credit: Honglak Lee

Sparse Coding: Training

- Input image patches: $\mathbf{x}_{\mathbf{X}_1}, \mathbf{x}_2, \dots, \mathbf{X}_N \in \mathbb{R}^D$ Learn dictionary of bases: $\phi_1, \phi_2, \dots, \phi_K \in \mathbb{R}^D$

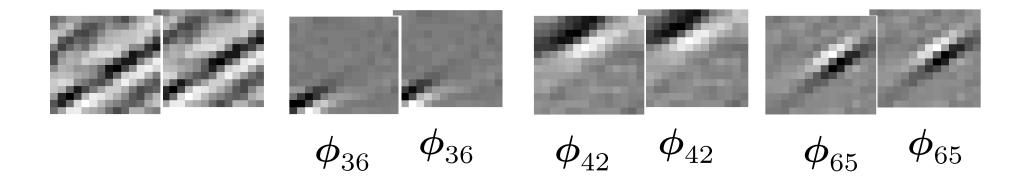


- Alternating Optimization:
 - 1. Fix dictionary of bases and $\hat{q}_{\phi_1}^{(h)} \hat{\phi}_{\phi_1}^{(h)} \phi_2^{(h)} \dots \phi_K^{(h)}$'s **a** (a standard Lasso problem).
 - Fix activations **a**, optimize the dictionary of bases (convex QP problem). 2.

Sparse Coding: Testing Time

- Input: a new image patch x* , and K learned bases $oldsymbol{\phi}_1, oldsymbol{\phi}_2, ..., oldsymbol{\phi}_K, ..., oldsymbol{\phi}_K$
- Output: sparse representation **a** of an image patch x*.

$$\min_{\mathbf{a}} \left\| \mathbf{x}^* - \sum_{k=1}^K a_k \boldsymbol{\phi}_k \right\|_2^2 + \lambda \sum_{k=1}^K \left| a_k \right|_{:=1}^K \left| a_k \right|$$



Sparse Coding: Testing Time

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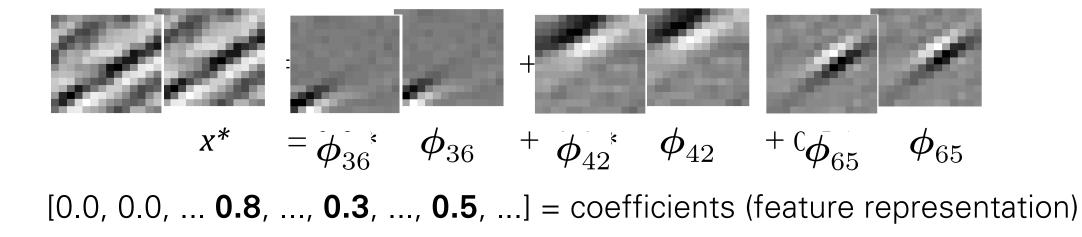
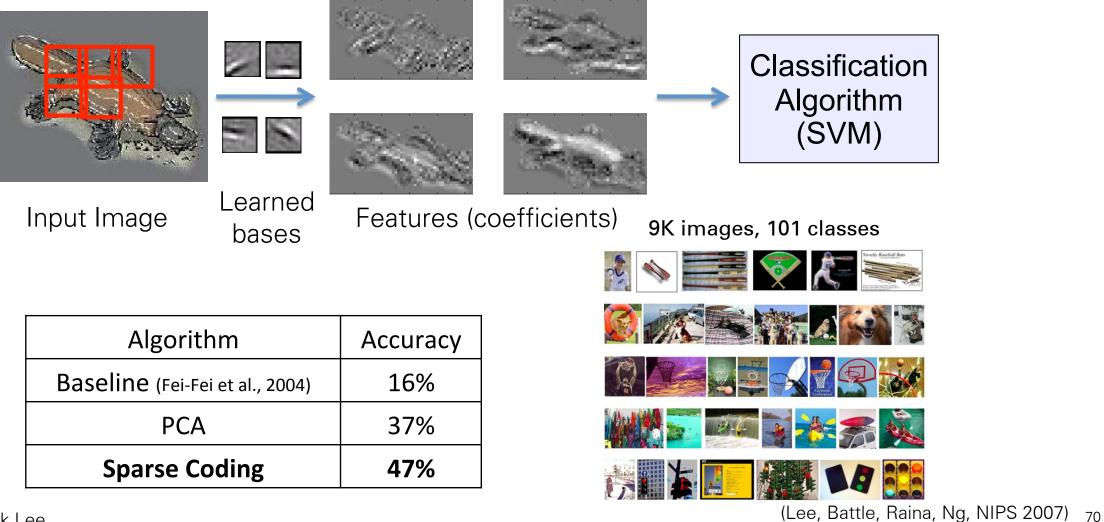


Image Classification

• Evaluated on Caltech101 object category dataset.



Slide Credit: Honglak Lee

Modeling Image Patches

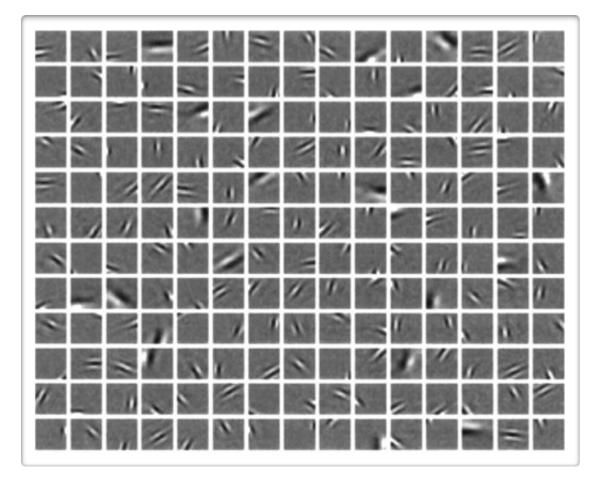
- Natural image patches:
 - small **image regions** extracted from an image of nature (forest, grass, ...)



Image taken from: Emergence of complex cell properties by learning to generalize in natural scenes. Karklin and Lewicki, 2009

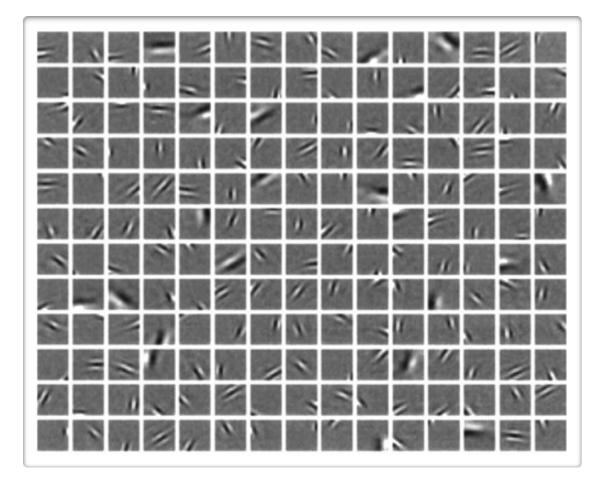
Relationship to V1

- When trained on natural image patches
 - the dictionary columns ('atoms'') look
 like edge detectors
 - each atom is tuned to a particular
 position, orientation and spatial
 frequency
 - V1 neurons in the mammalian brain have a similar behavior

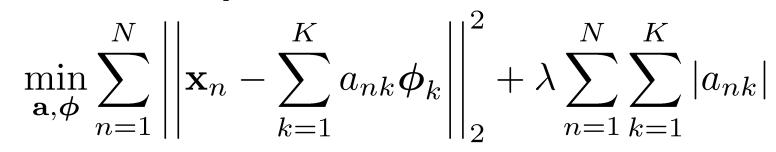


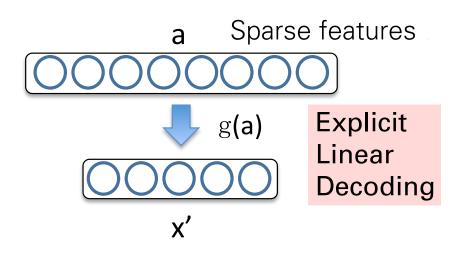
Relationship to V1

- Suggests that the brain might be learning a sparse code of visual stimulus
 - Since then, many other models have been shown to learn similar features
 - they usually all incorporate a notion of sparsity

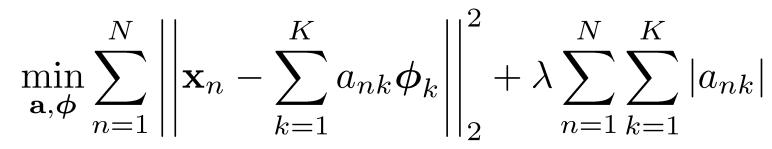


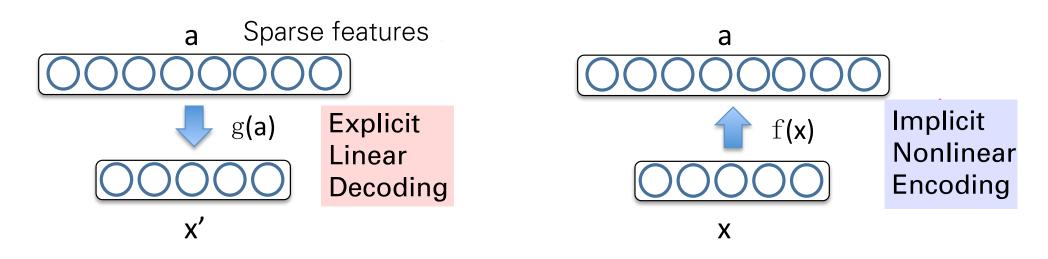
Interpreting Sparse Coding



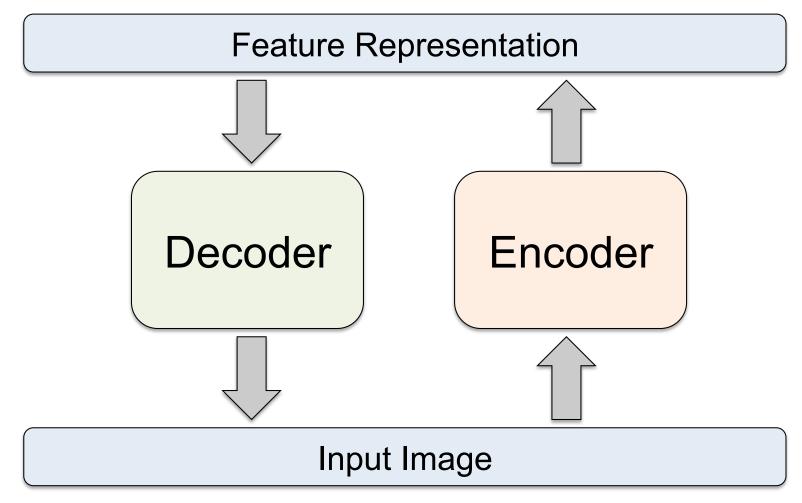


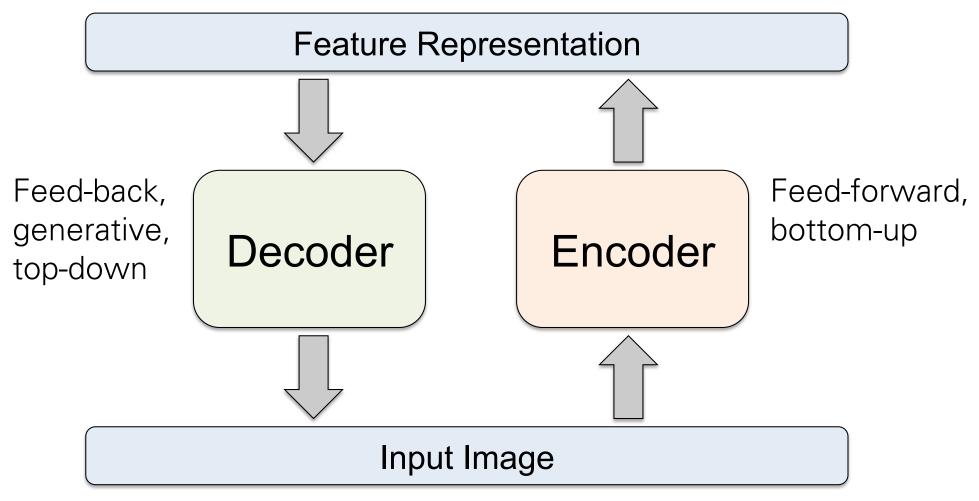
Interpreting Sparse Coding



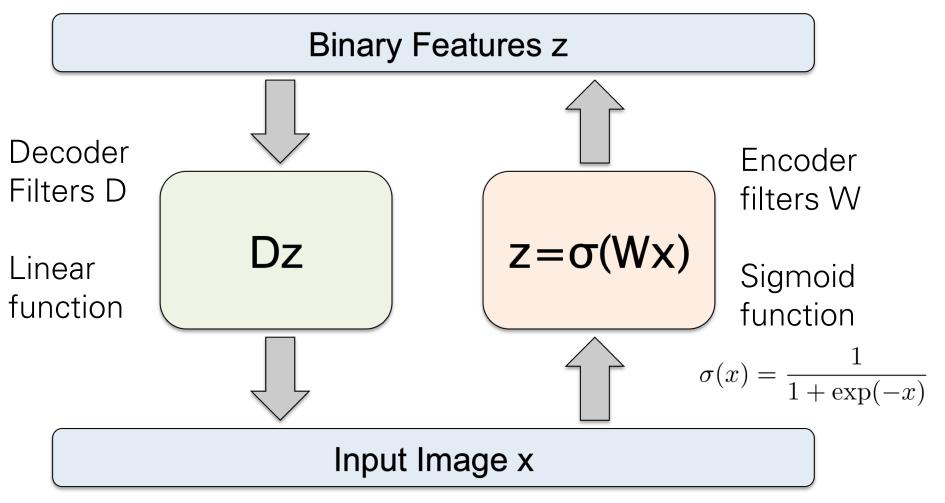


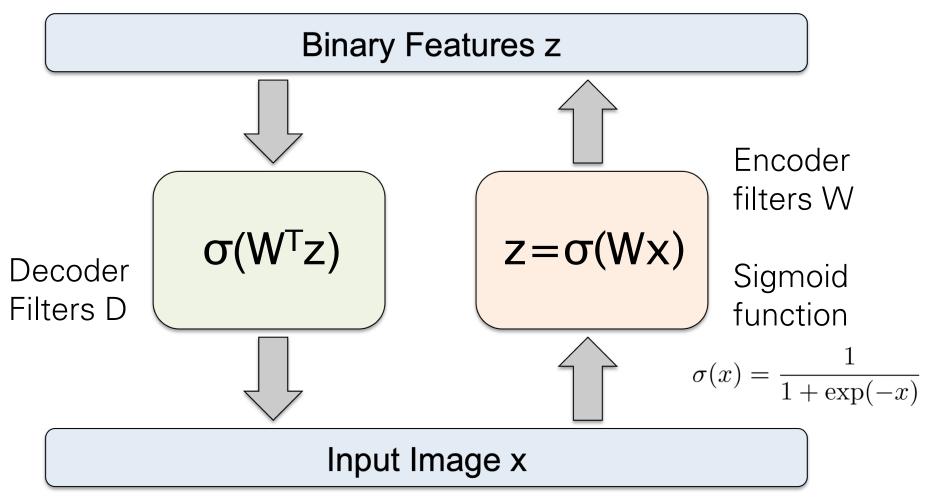
- Sparse, over-complete representation **a**.
- **Encoding** $\mathbf{a} = f(\mathbf{x})$ is implicit and nonlinear function of \mathbf{x} .
- **Reconstruction** (or decoding) $\mathbf{x'} = g(\mathbf{a})$ is linear and explicit.





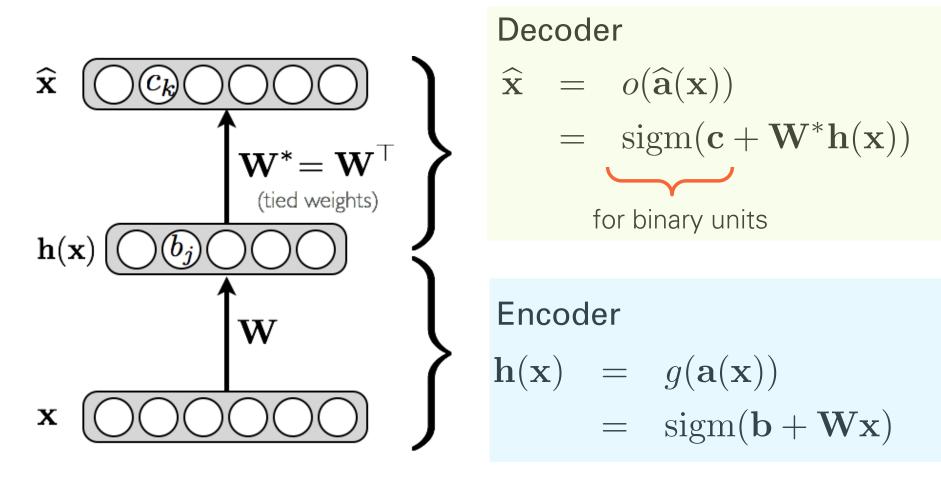
- Details of what goes insider the encoder and decoder matter!
- Need constraints to avoid learning an identity.





- Need additional constraints to avoid learning an identity.
- Relates to Restricted Boltzmann Machines (later).

• Feed-forward neural network trained to reproduce its input at the output layer



$Loss Function_{\widehat{\mathbf{x}} \to \widehat{\mathbf{y}} \to \widehat{\mathbf{y} \to \widehat{\mathbf{y}} \to \widehat{\mathbf{y}} \to$

 $\widehat{x}_{k} \xrightarrow{}^{2} x_{k} \left(2 f\left(\frac{1}{k} \left(\frac{1}{k} \right) \xrightarrow{}^{2} \sum_{k} \left(\frac{1}{k} \right) \xrightarrow{}^{2} \left(\frac{1}{k} \right) \xrightarrow{}^{2} \left(\frac{1}{k} \left(\frac{1}{k} \right) \xrightarrow{}^{2} \left(\frac{1}$

- Cross-entropy error function (reconstruction $\underbrace{\operatorname{sss}}_{\mathbf{X}} = \underbrace{\operatorname{sss}}_{\mathcal{S}} (\widehat{\mathbf{x}}_{\mathbf{X}}) = \sum_{k} (\widehat{x}_{k} - x) = \sum_{k} (\widehat{x}_{k} - x)$

 $== \operatorname{sign}(\operatorname{c}(\operatorname{c-WWh}^*(\operatorname{bx})))$

Loss function for real-valued inputs

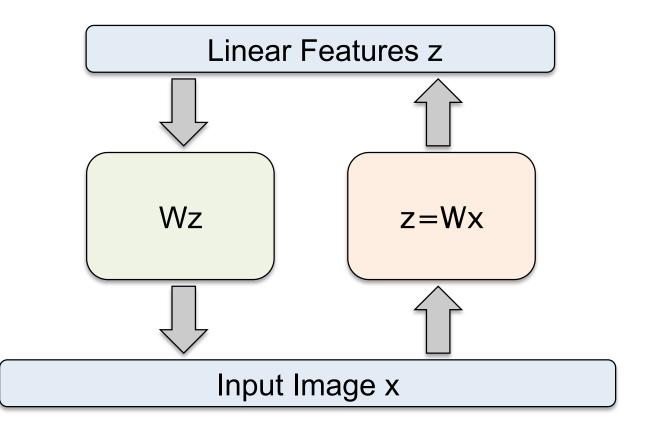
 $(\mathbf{x}) = \frac{1}{2} \sum_{k} (\hat{x}_{k} - x_{k})^{2} |_{k}^{2} l(\mathbf{x}) = \sum_{k} (x_{k}) \log(\widehat{g}(\mathbf{x})_{k}) + (1(1 - x_{k})_{k})$

 $T_{(\widehat{\mathbf{x}},\widehat{\mathbf{y}})} = \mathcal{T}_{(\widehat{\mathbf{x}},\widehat{\mathbf{y}})} = \mathcal{T}_{(\widehat{\mathbf{x}},\widehat{\mathbf{x}})} = \mathcal{T}_{(\widehat{\mathbf{x},\widehat{\mathbf{x}})} = \mathcal{T}_{(\widehat{\mathbf{x},\widehat{\mathbf{x},\widehat{\mathbf{x}})} = \mathcal{T}_{(\widehat{\mathbf{x},\widehat{\mathbf{x},\widehat{\mathbf{x}})}$

$$\mathbf{a}(\mathbf{x}(\mathbf{x}^{(t)})) \iff \mathbf{b} \vdash \mathbf{W} \mathbf{x}^{(t)}(t)$$

$$\mathbf{b}(\mathbf{x}^{(t)}(t)) \iff \mathbf{s}(\mathbf{a}(\mathbf{x}^{(t)}(t)))$$

81



- If the hidden and output layers are linear, it will learn hidden units that are a linear function of the data and minimize the squared error.
- The K hidden units will span the same space as the first k principal components. The weight vectors may not be orthogonal.

• With nonlinear hidden units, we have a nonlinear generalization of PCA.

Denoising Autoencoder1

- Idea: Representation should be robust to introduction $x = \frac{T}{T} + \frac{T}$
 - random assignment of subset of interaction $n(\mathbf{x})$ with probability $p(\mathbf{x}, \mathbf{x})$
- Gaussian addition and the mouth of the mouth of the source of the sour
- $\mathbf{x}^{(t)} \leftarrow \frac{1}{\sqrt{1}} \left(\frac{t}{\sqrt{1}} + \frac{1}{\sqrt{1}} + \frac{t}{\sqrt{1}} + \frac{1}{\sqrt{1}} + \frac{t}{\sqrt{1}} + \frac{1}{\sqrt{1}} + \frac{t}{\sqrt{1}} + \frac{1}{\sqrt{1}} + \frac{t}{\sqrt{1}} +$
- Reconstruction $\hat{\mathbf{x}}$ computed from $\hat{\mathbf{x}}$ $\hat{\mathbf$
- Loss function compares $\hat{\mathbf{x}}$ for struction $\hat{\mathbf{x}}$ is the structure in $\hat{\mathbf{x}$ is the structure in $\hat{\mathbf{x}}$ i

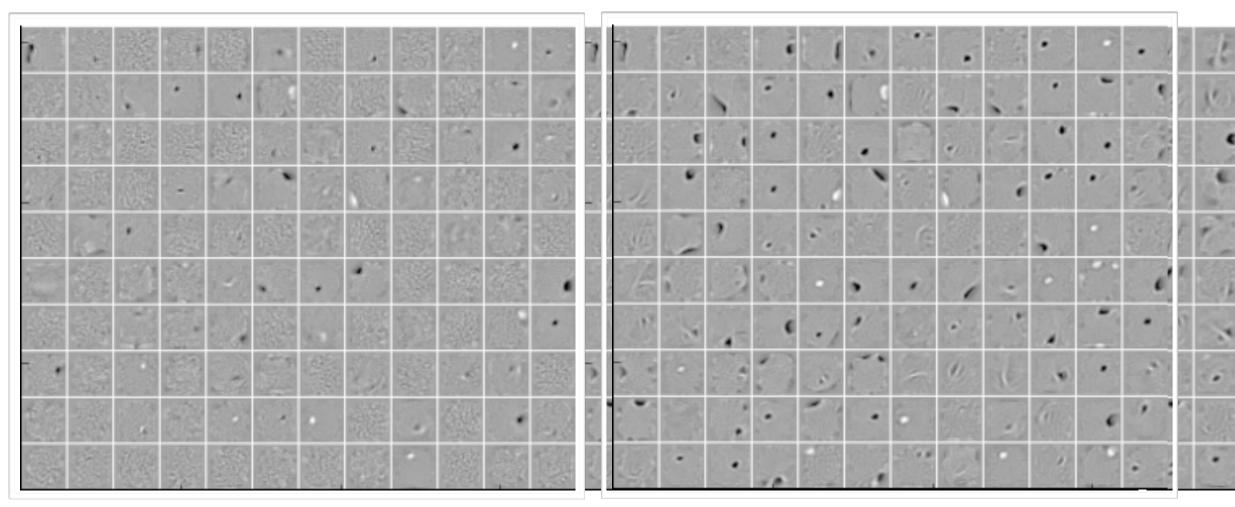
Denoising Autoencoder

 $\widehat{\mathbf{x}} = \operatorname{sigm}(\mathbf{c} + \mathbf{W}^* \mathbf{h}(\widetilde{\mathbf{x}}))^*$ $\widetilde{\mathbf{X}}$ \mathbf{X}

Learned Filters

Non-corrupted

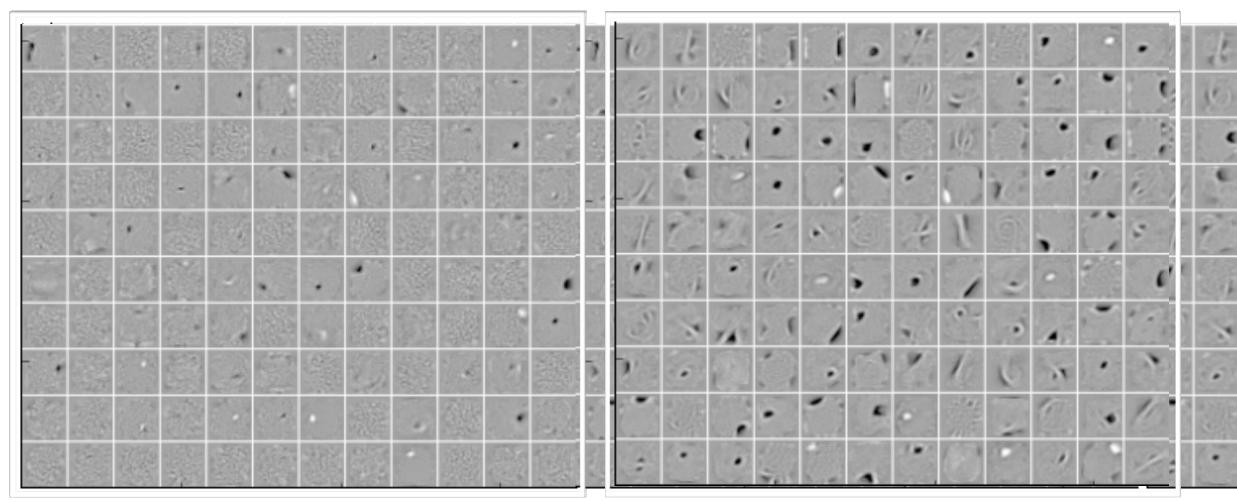
25% corrupted input



Learned Filters

Non-corrupted

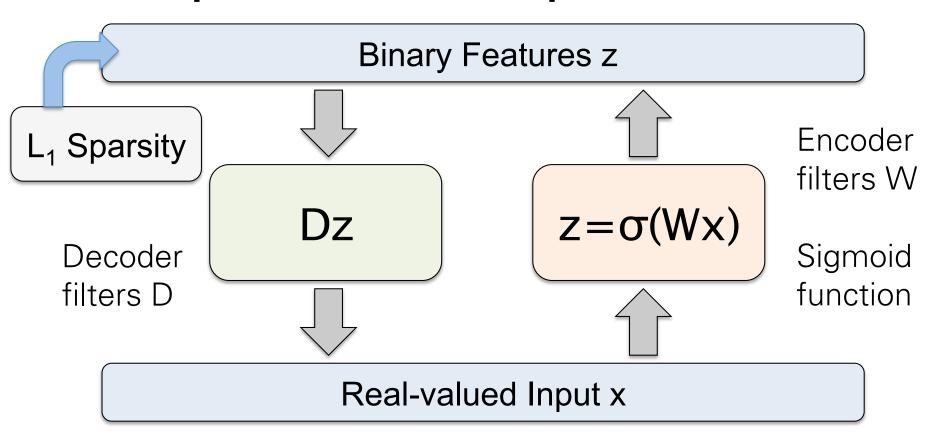
50% corrupted input



(a) a) and destroy of the property of the prop

(b) b2 525 Dedust ctiction

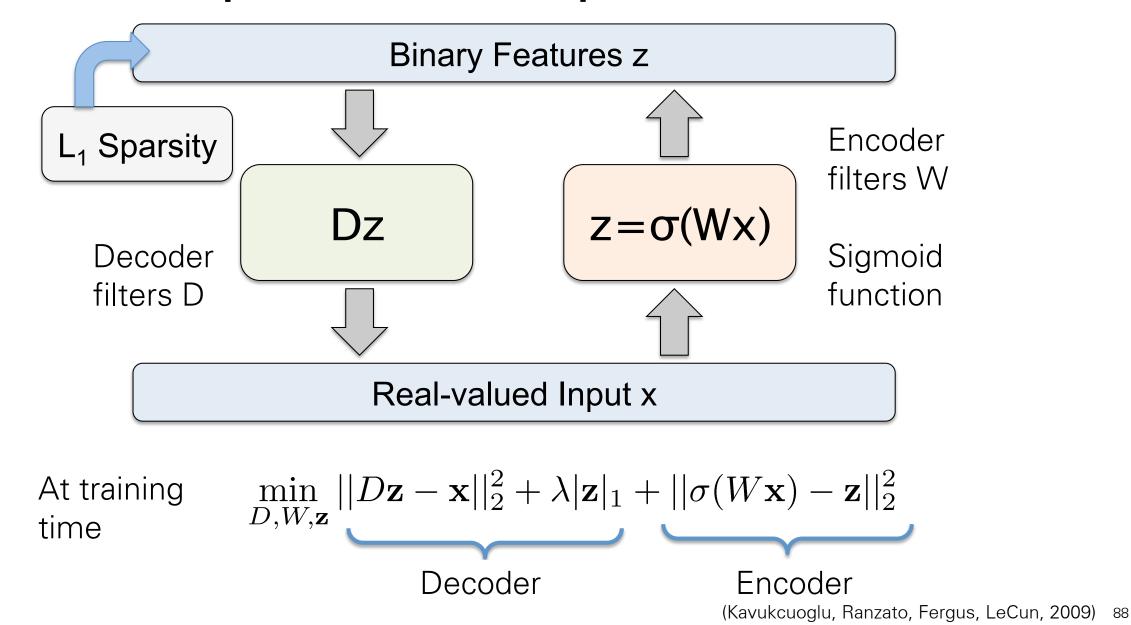
Predictive Sparse Decomposition

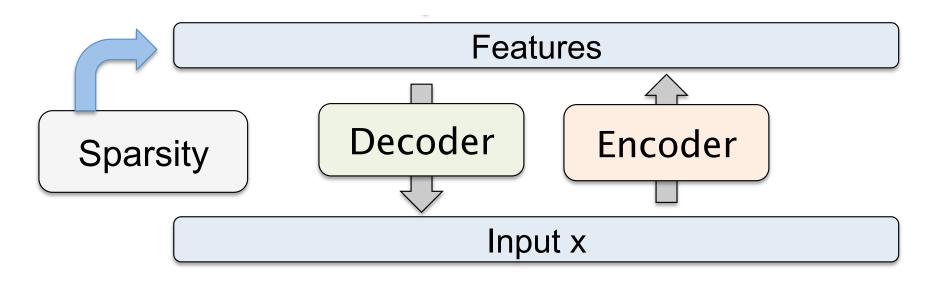


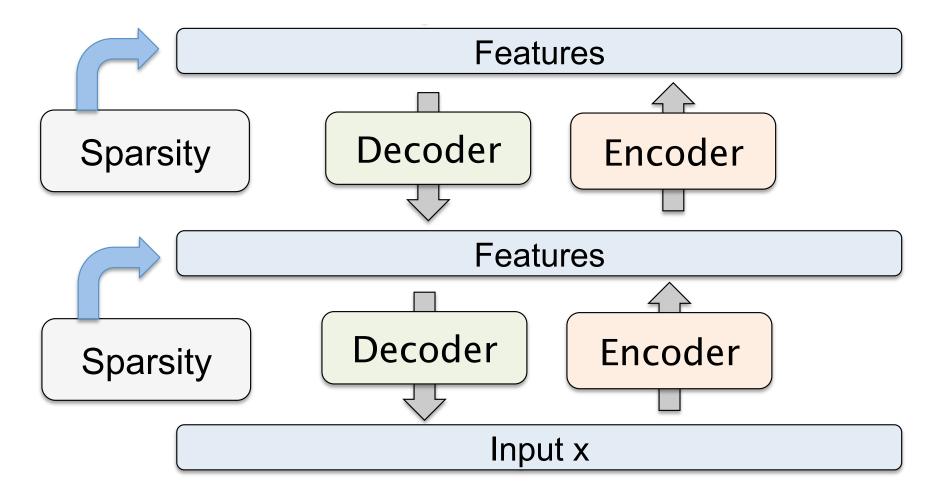
$$\min_{D,W,\mathbf{z}} ||D\mathbf{z} - \mathbf{x}||_2^2 + \lambda |\mathbf{z}|_1 + ||\sigma(W\mathbf{x}) - \mathbf{z}||_2^2$$

(Kavukcuoglu, Ranzato, Fergus, LeCun, 2009) 87

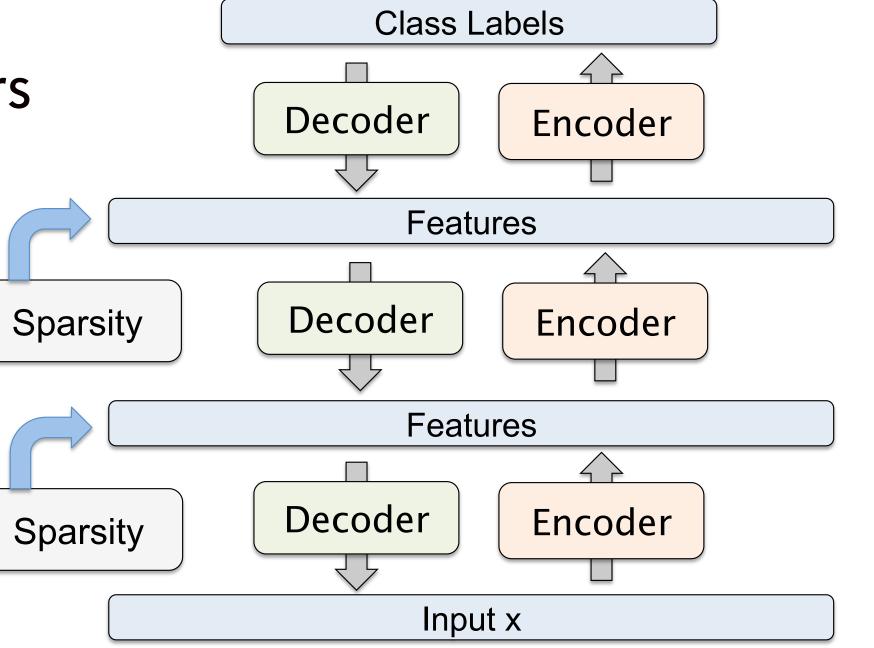
Predictive Sparse Decomposition

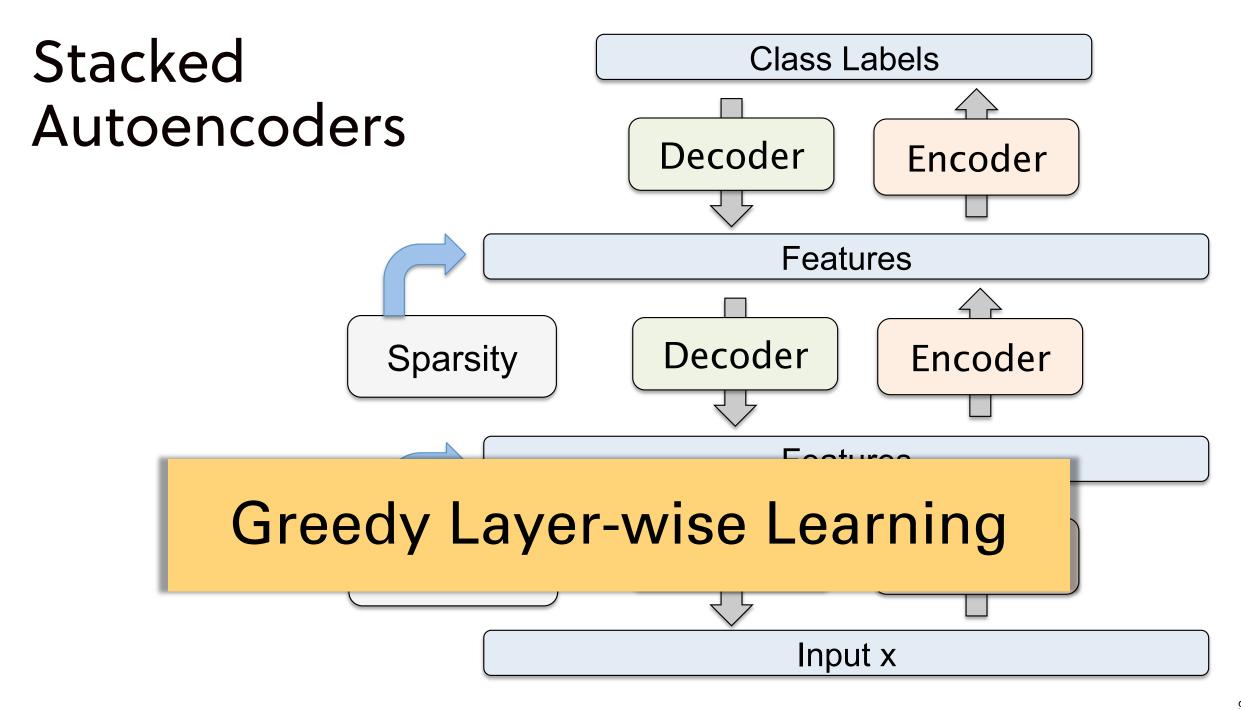




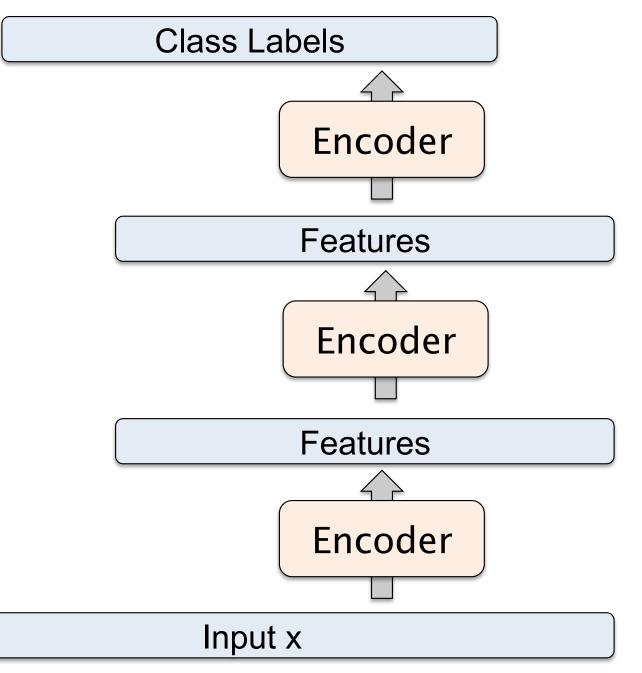




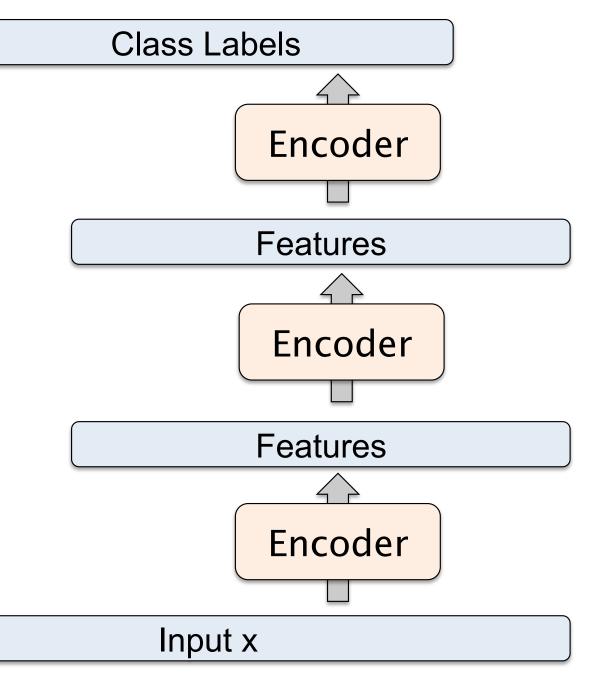




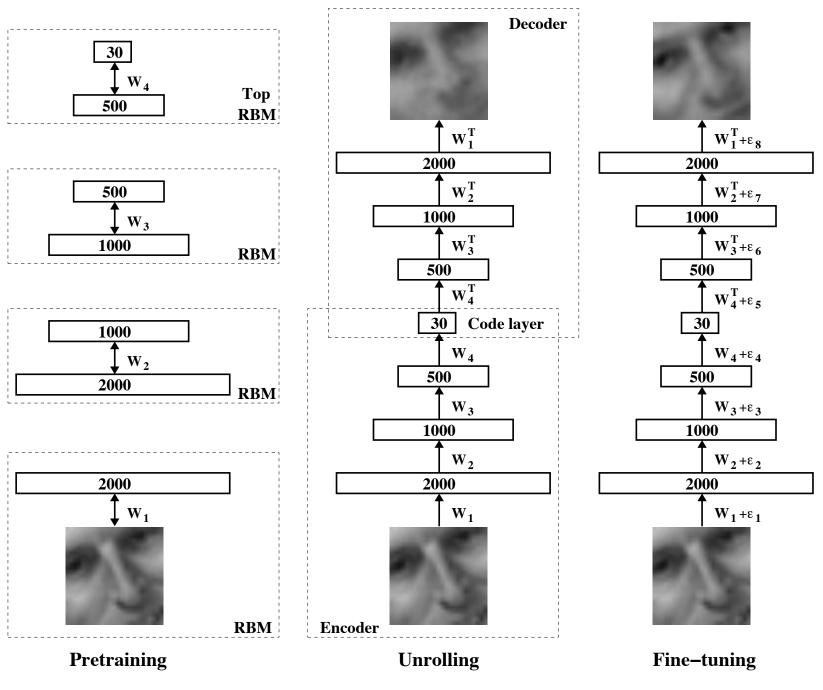
• Remove decoders and use feed-forward part.



- Remove decoders and use feed-forward part.
- Standard, or convolutional neural network architecture.
- Parameters can be fine-tuned using backpropagation.

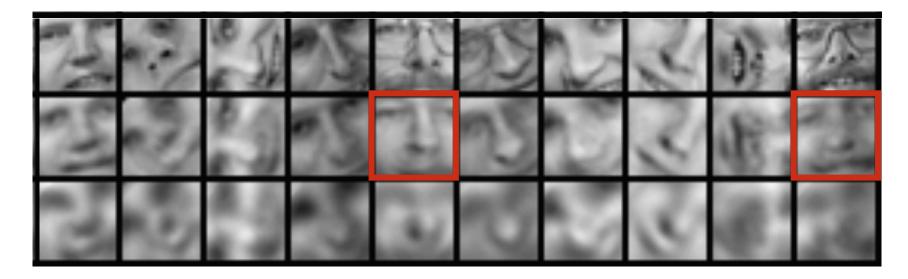


Deep Autoencoder



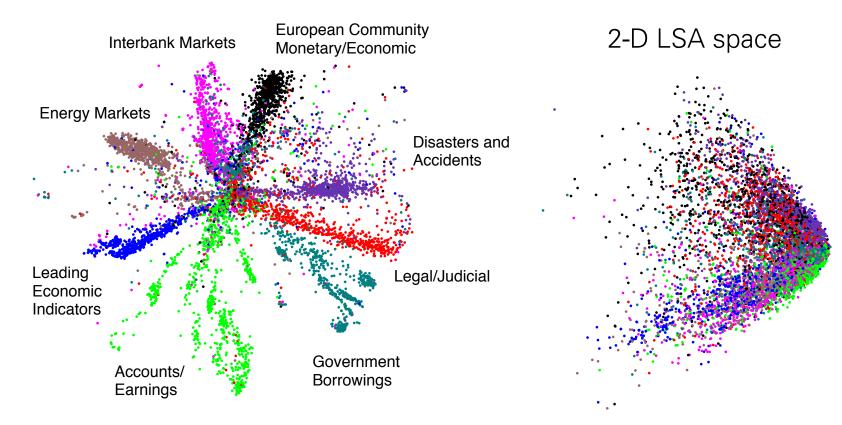
Deep Autoencoders

 25x25 – 2000 – 1000 – 500 – 30 autoencoder to extract 30-D realvalued codes for Oliver face patches.



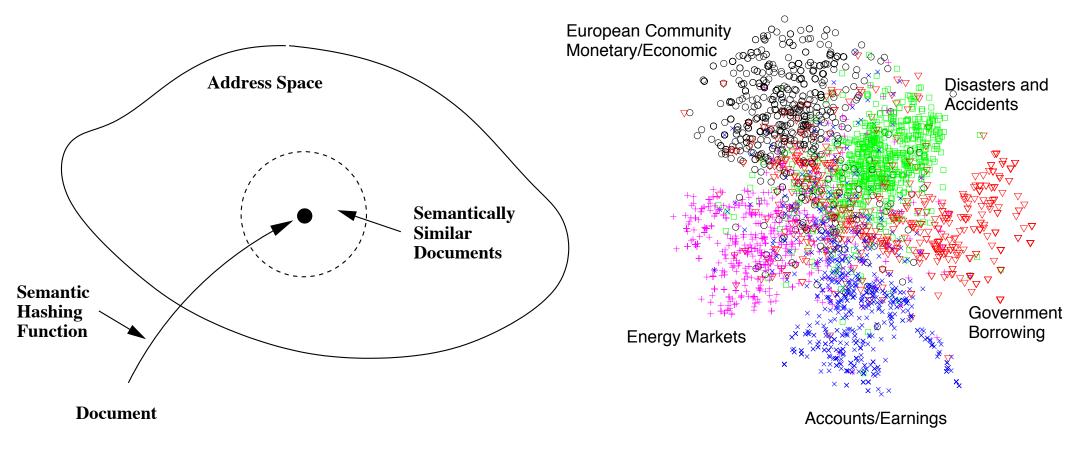
- **Top:** Random samples from the test dataset.
- Middle: Reconstructions by the 30-dimensional deep autoencoder.
- Bottom: Reconstructions by the 30-dimensional PCA.

Information Retrieval



- The Reuters Corpus Volume II contains 804,414 newswire stories (randomly split into **402,207 training** and **402,207 test**).
- "Bag-of-words" representation: each article is represented as a vector containing the counts of the most frequently used 2000 words in the training set.

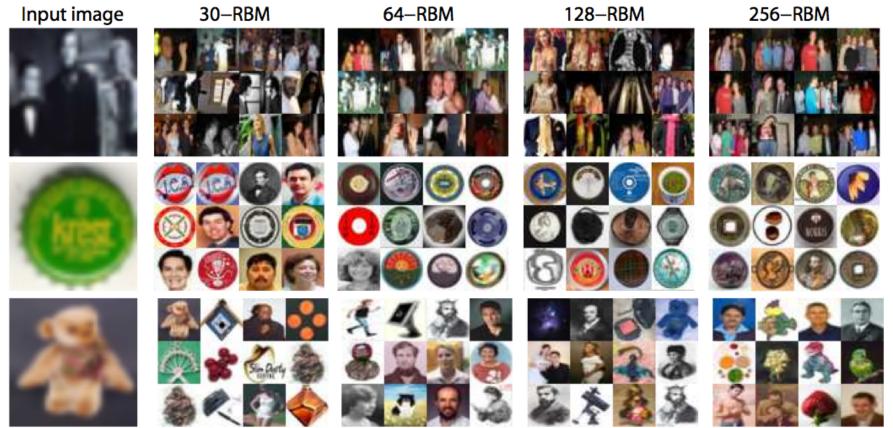
Semantic Hashing



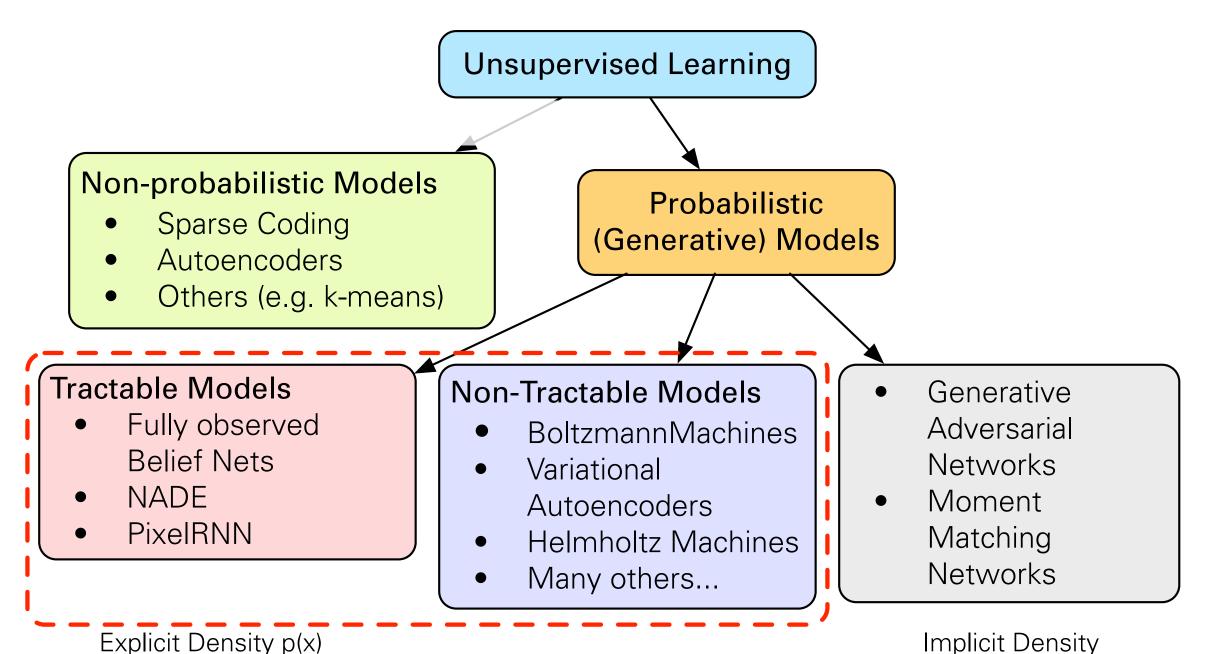
- Learn to map documents into semantic 20-D binary codes.
- Retrieve similar documents stored at the nearby addresses with no search at all.

Searching Large Image Database using Binary Codes

• Map images into binary codes for fast retrieval.

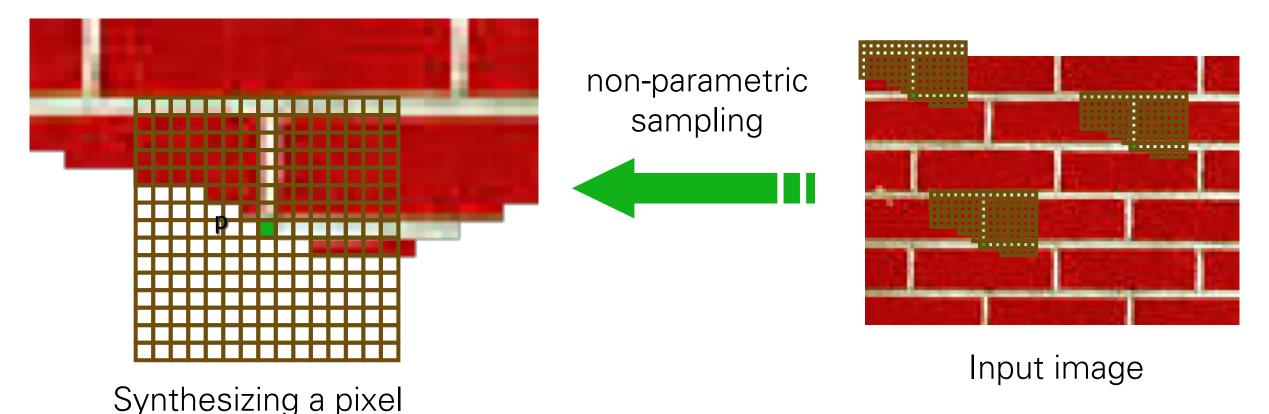


- Small Codes, Torralba, Fergus, Weiss, CVPR 2008
- Spectral Hashing, Y. Weiss, A. Torralba, R. Fergus, NIPS 2008
- Kulis and Darrell, NIPS 2009, Gong and Lazebnik, CVPR 2011
- Norouzi and Fleet, ICML 2011



Autoregressive Generative Models

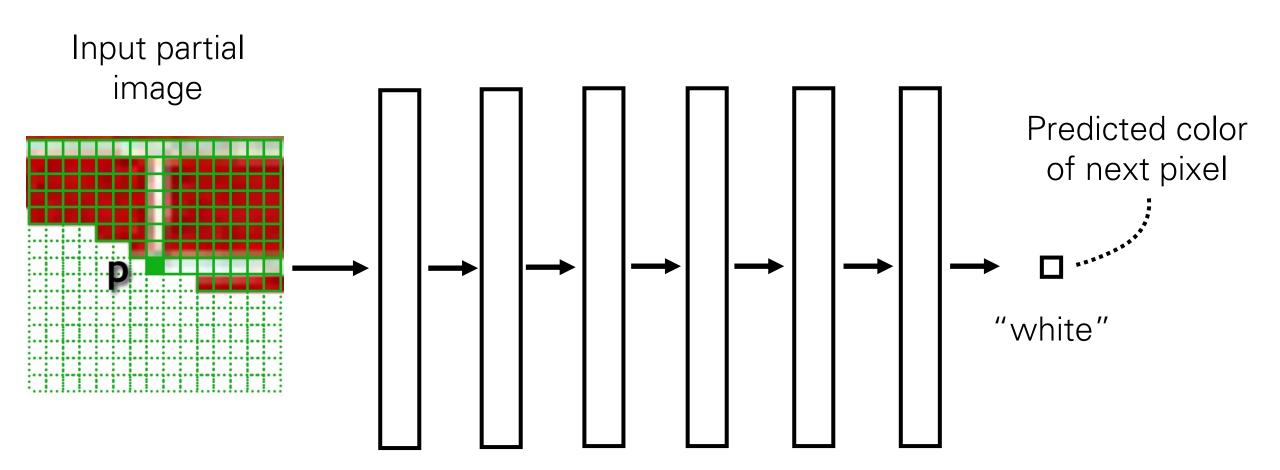
Texture synthesis by non-parametric sampling



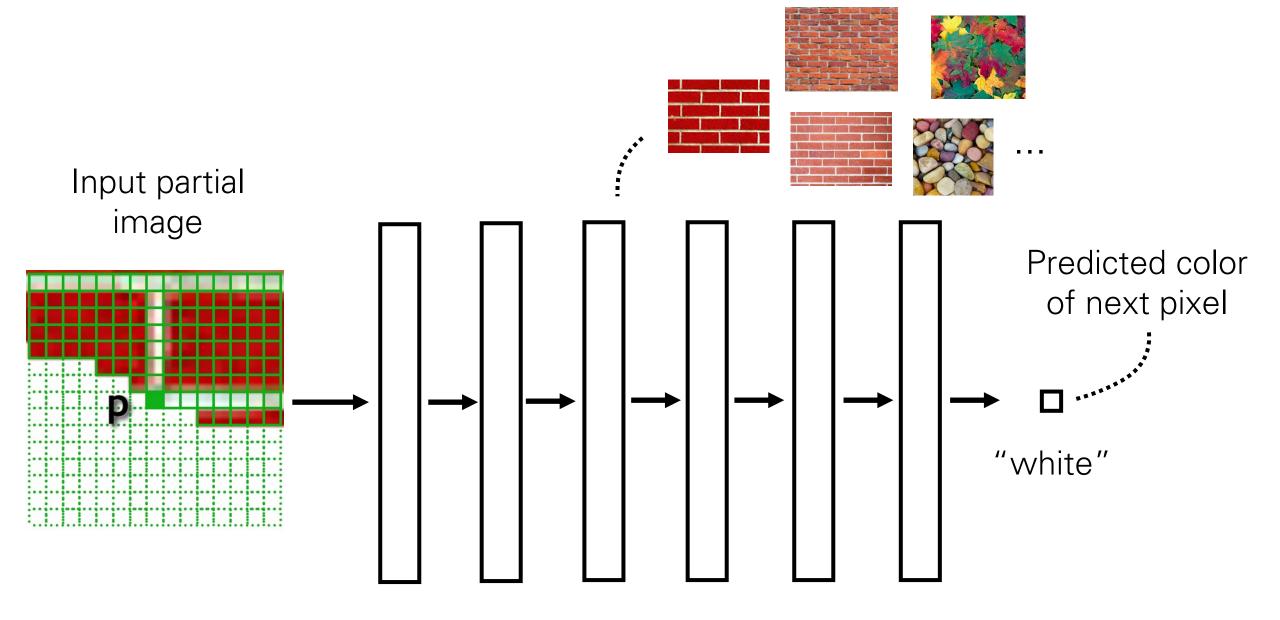
Models P(p|N(p))

[Efros & Leung 1999] 102

Texture synthesis with a deep net

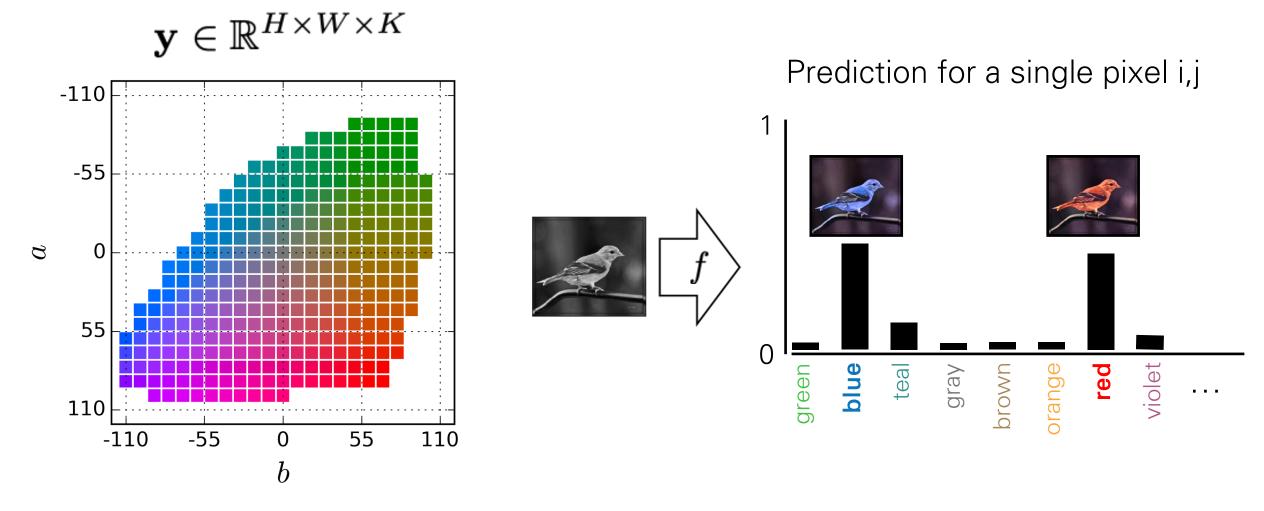


[PixelRNN, PixelCNN, van der Oord et al. 2016]₁₀₃



[PixeIRNN, PixeICNN, van der Oord et al. 2016]₁₀₄

Idea: We can represent colors as discrete classes



 $\mathcal{L}(\mathbf{y}, f_{\theta}(\mathbf{x})) = H(\mathbf{y}, \texttt{softmax}(f_{\theta}(\mathbf{x})))$

And we can interpret the learner as modeling P(next pixel | previous pixels):

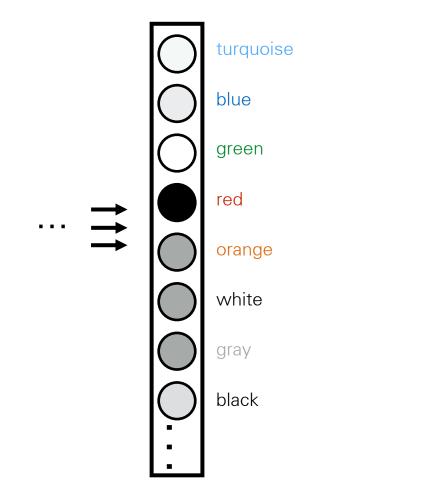
Softmax regression (a.k.a. multinomial logistic regression)

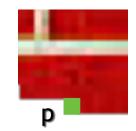
$$\hat{\mathbf{y}} \equiv [P_{\theta}(Y = 1 | X = \mathbf{x}), \dots, P_{\theta}(Y = K | X = \mathbf{x})] \quad \longleftarrow \text{ predicted probability of each class given input } \mathbf{x}$$

$$H(\mathbf{y}, \hat{\mathbf{y}}) = -\sum_{k=1}^{K} y_k \log \hat{y}_k \quad \longleftarrow \quad \text{picks out the -log likelihood} \\ \text{of the ground truth class } \mathbf{y} \\ \text{under the model prediction } \hat{\mathbf{y}}$$

$$f^* = \operatorname*{arg\,min}_{f \in \mathcal{F}} \sum_{i=1}^{N} H(\mathbf{y}_i, \hat{\mathbf{y}}_i) \longleftarrow \max$$
 likelihood learner!

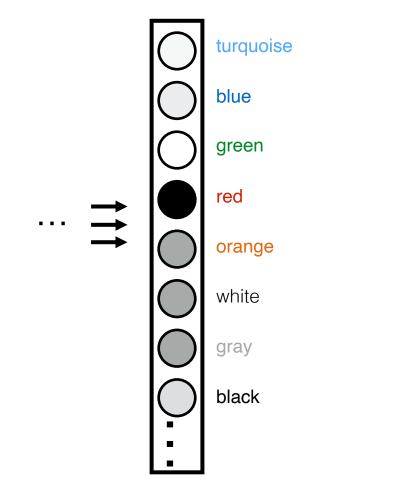
Network output

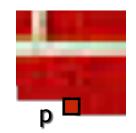


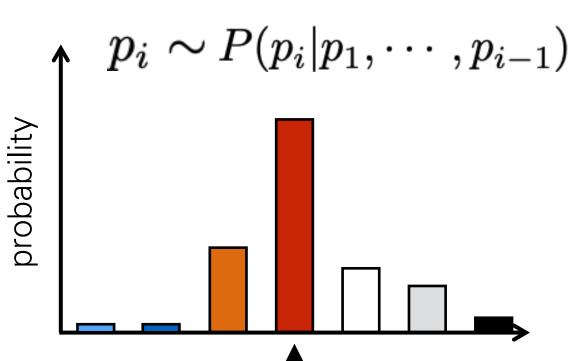


P(next pixel | previous pixels) $P(p_i|p_1,\cdots,p_{i-1})$ probability

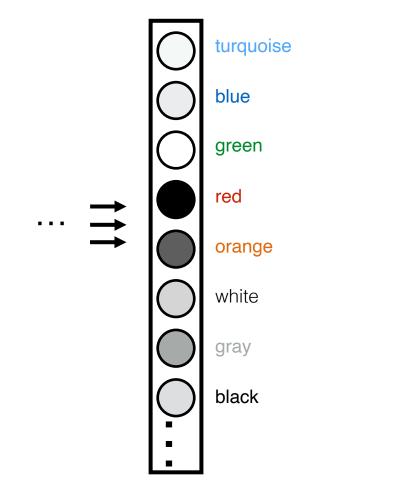


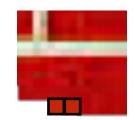


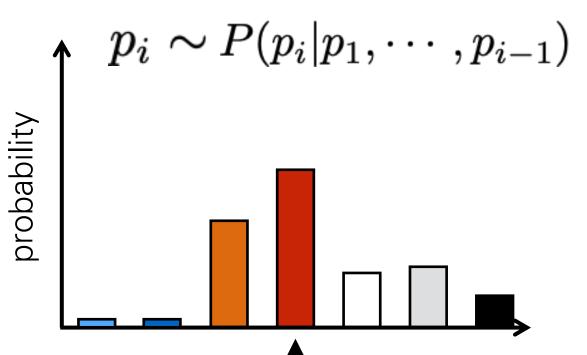




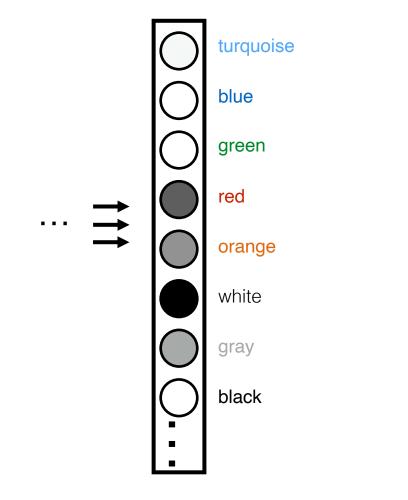


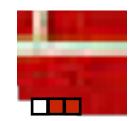


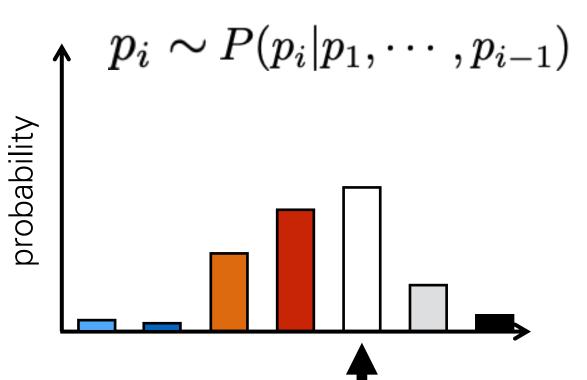




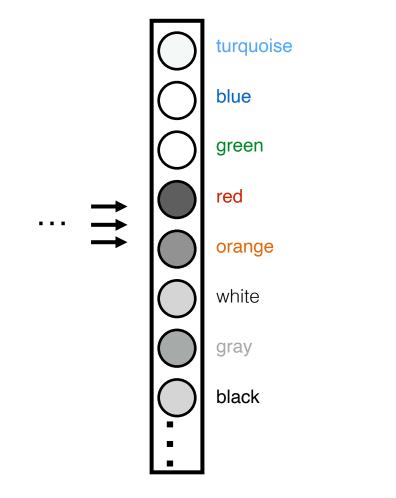


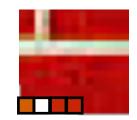


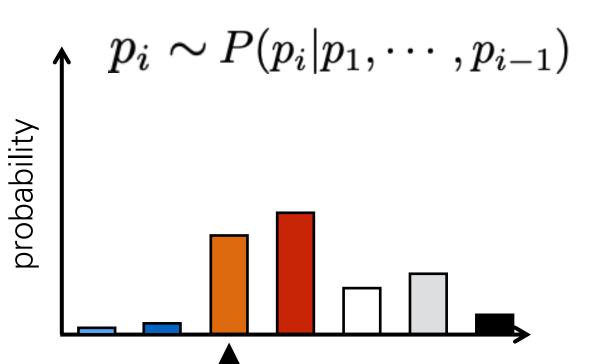












$$p_1 \sim P(p_1)$$

 $p_2 \sim P(p_2|p_1)$
 $p_3 \sim P(p_3|p_1, p_2)$
 $p_4 \sim P(p_4|p_1, p_2, p_3)$

$$p_3$$
 p_4 p_2 p_1

 $\{p_1, p_2, p_3, p_4\} \sim P(p_4|p_1, p_2, p_3) P(p_3|p_1, p_2) P(p_2|p_1) P(p_1)$

$$p_i \sim P(p_i | p_1, \ldots, p_{i-1})$$

$$\mathbf{p} \sim \prod_{i=1}^{N} P(p_i | p_1, \dots, p_{i-1})$$

Autoregressive probability model

$$\mathbf{p} \sim \prod_{i=1}^{N} P(p_i | p_1, \dots, p_{i-1})$$

$$P(\mathbf{p}) = \prod_{i=1}^{N} P(p_i | p_1, \dots, p_{i-1}) \quad \bigstar \quad \mathsf{General product rule}$$

The sampling procedure we defined above takes exact samples from the learned probability distribution (pmf).

Multiplying all conditionals evaluates the probability of a full joint configuration of pixels.

Learning the Distribution of Natural Data

$$p(\mathbf{x}) = \prod_{i} p(x_i | \mathbf{x}_{<})$$

1D sequences such as text or sound

j *i* 2D tensors such as images

 $p(\mathbf{x}) = \prod \prod p(x_{i,j} | \mathbf{x}_{<})$

$$p(\mathbf{x}) = \prod_{k} \prod_{j} \prod_{i} p(x_{i,j,k} | \mathbf{x})$$
3D tensors such as videos

- Fully visible belief networks
- NADE/MADE
- PixelRNN/PixelCNN (Images)
- Video Pixel Nets (Videos)
- ByteNet (Language/seq2seq)
- WaveNet (Audio)

[Frey et al.,1996] [Frey, 1998]

[Larochelle and Murray, 2011] [Germain et al., 2015]

[van den Oord, Kalchbrenner, Kavukcuoglu, 2016] [van den Oord, Kalchbrenner, Vinyals, et al., 2016]

[Kalchbrenner, van den Oord, Simonyan, et al., 2016]

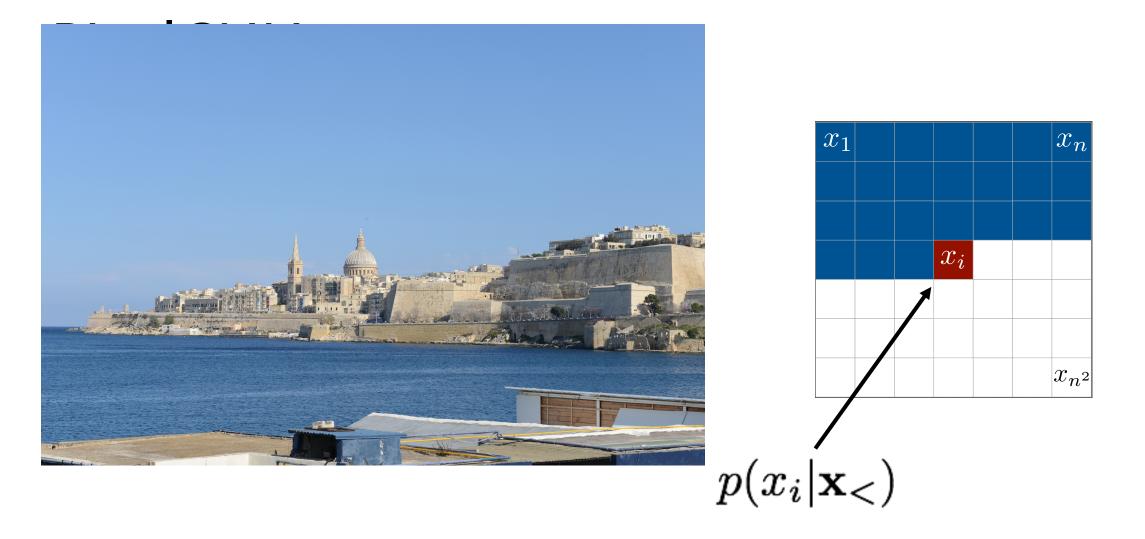
[Kalchbrenner, Espeholt, Simonyan, et al., 2016]

[van den Oord, Dieleman, Zen, et al., 2016]

Slide adapted from Nal Kalchbrenner



- approach the generation process as sequence modeling problem
- an explicit density model

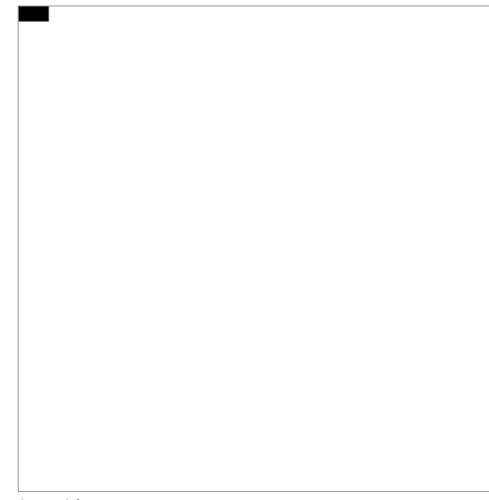


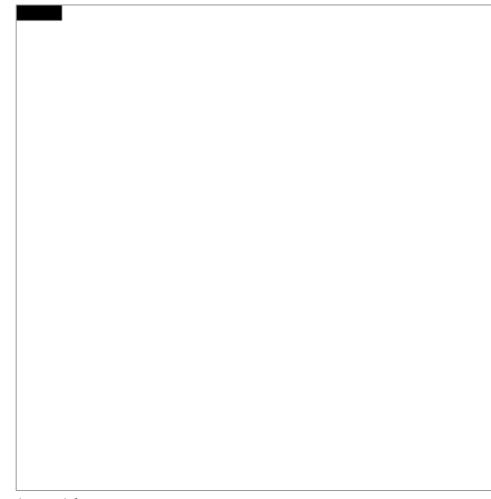
$$x_{i}$$

Slide adapted from Nal Kalchbrenner

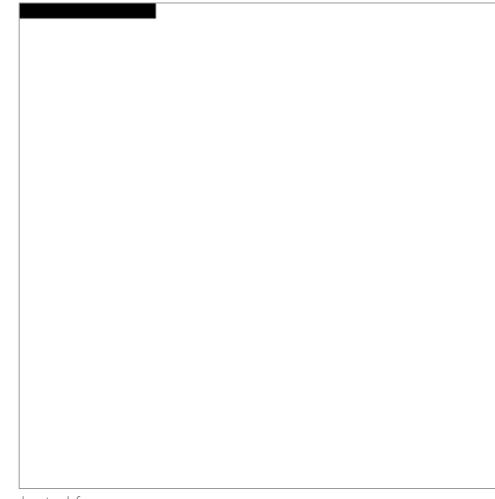
 $n(r \cdot | \mathbf{x} \cdot \cdot)$

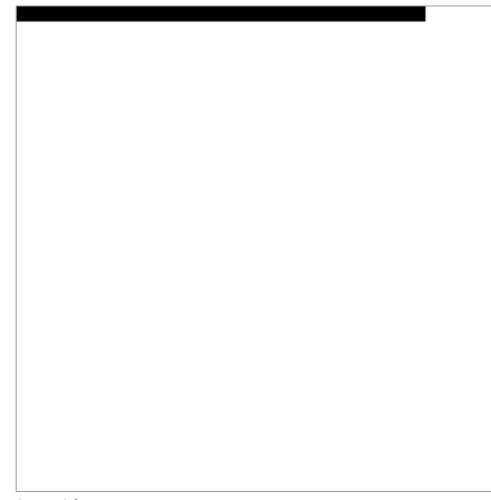


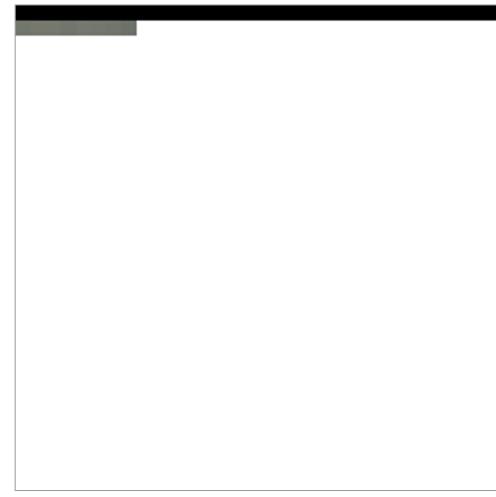


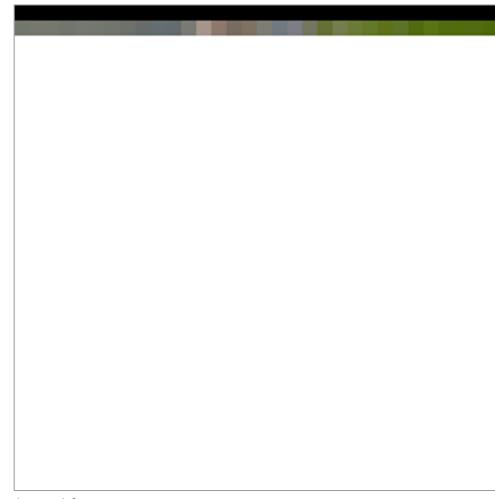


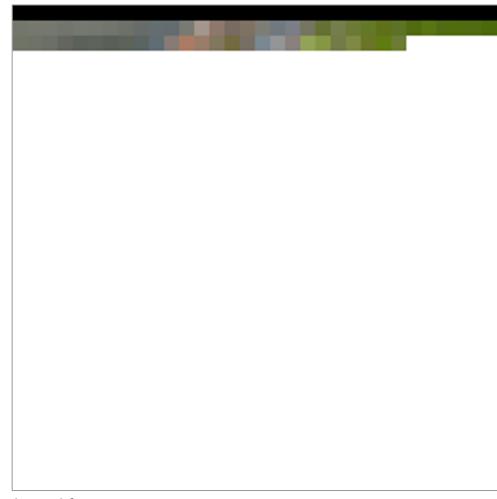


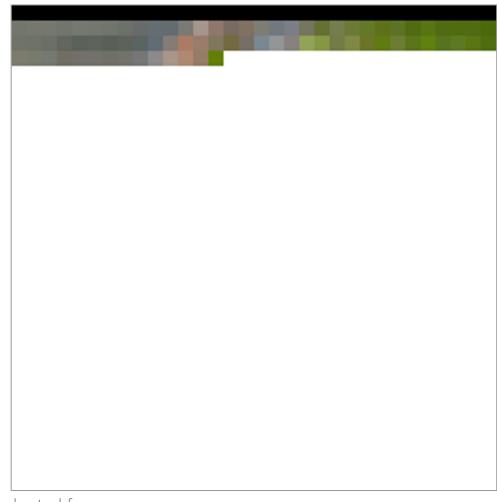


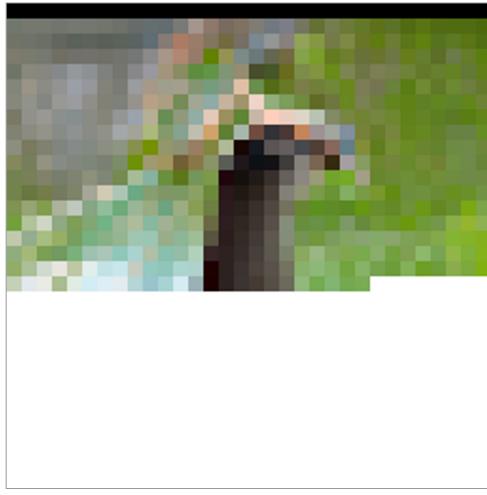


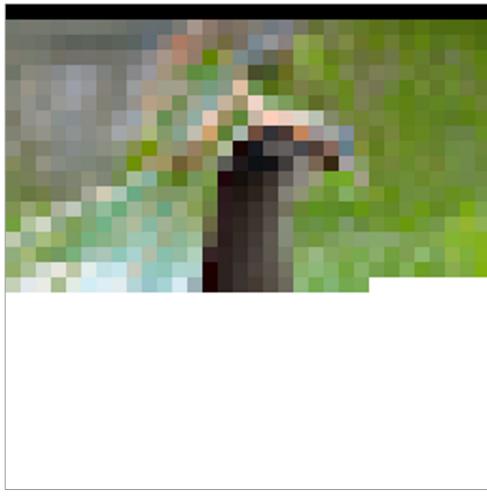


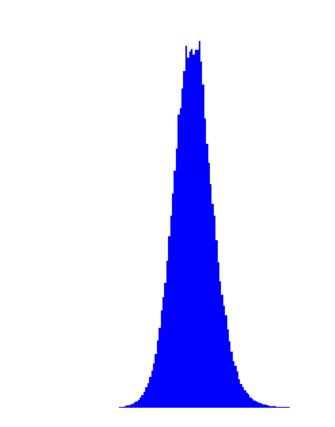


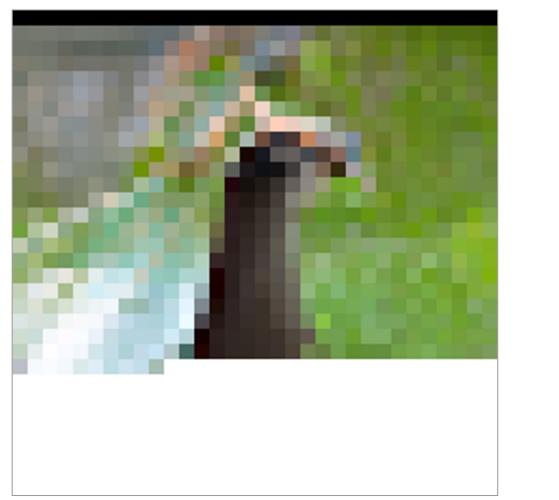


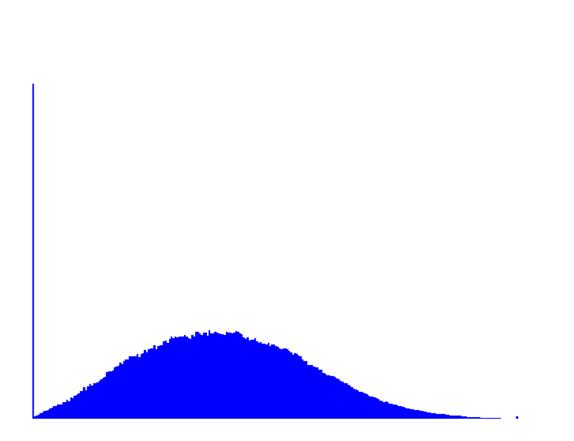


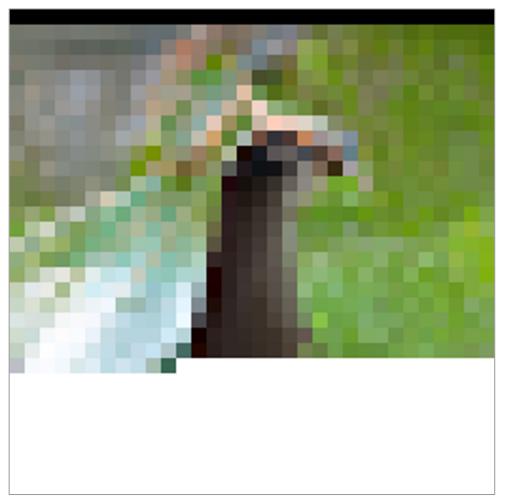


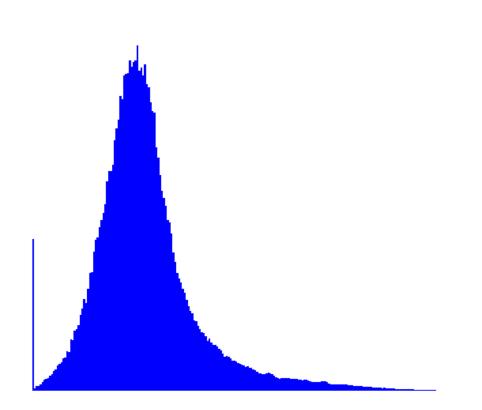


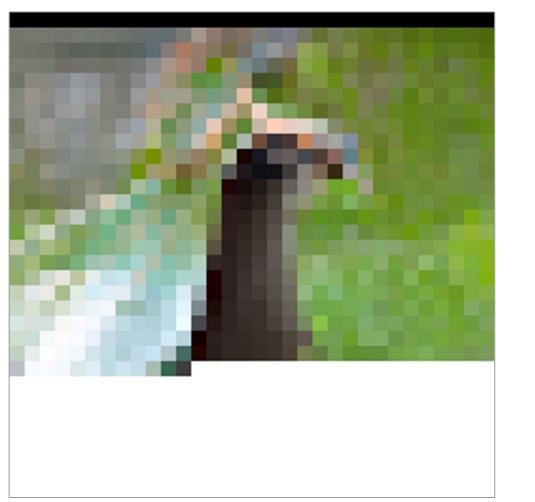


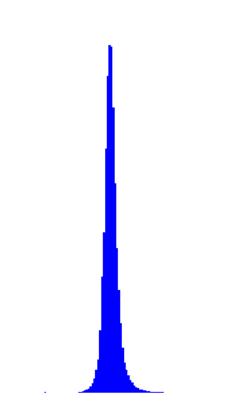




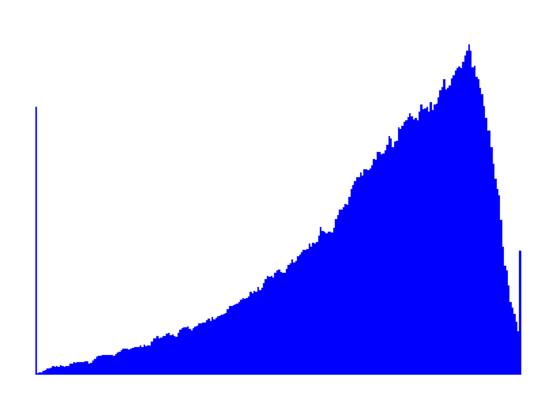




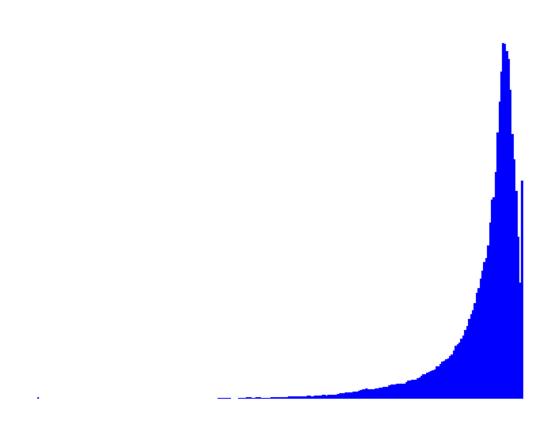




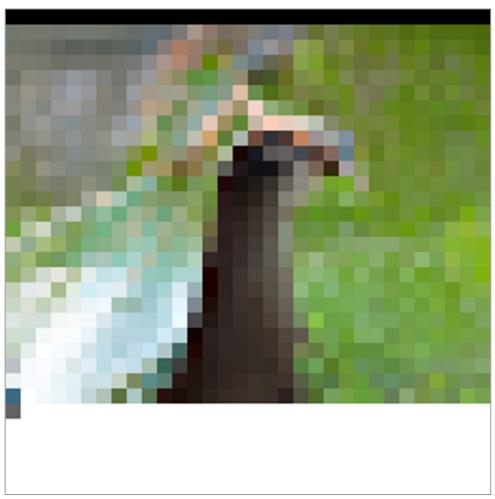




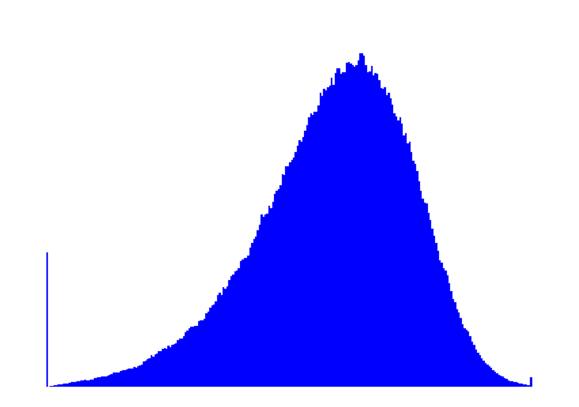




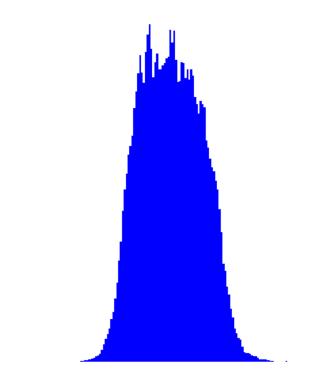


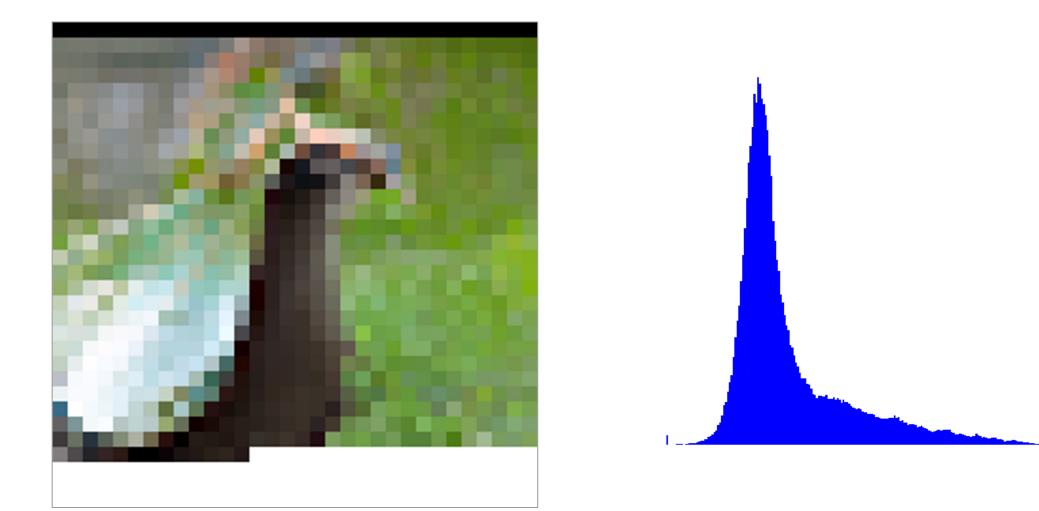




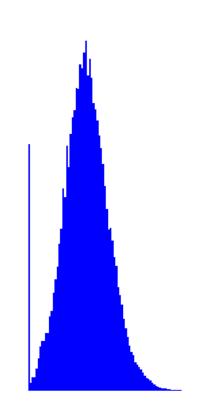


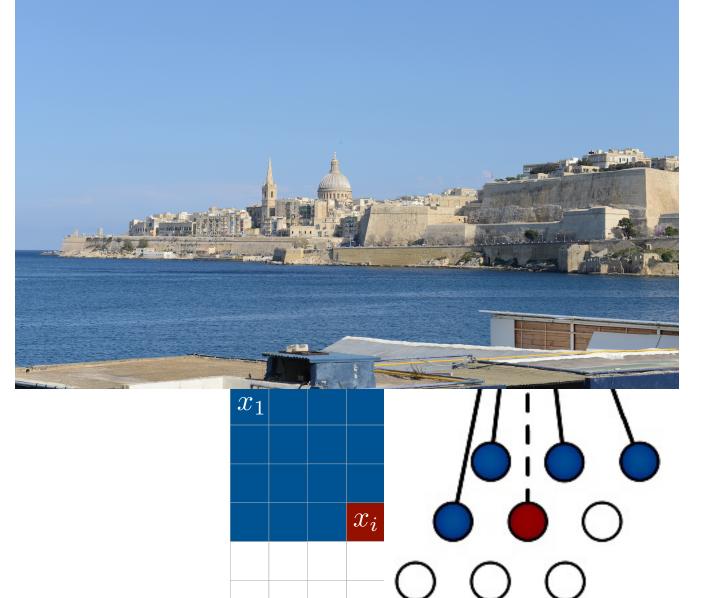












 x_{n^2}

x_1				x_n
		x_i		
				x_{n^2}

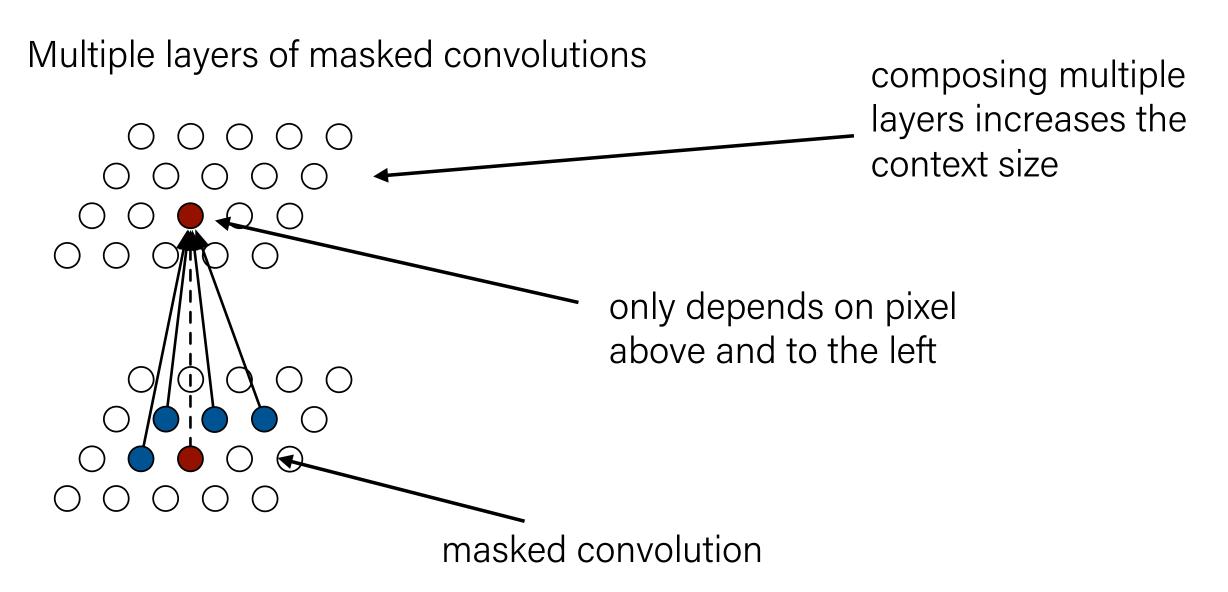
1	1	1	1	1
1	1	1	1	1
1	1	0	0	0
0	0	0	0	0
0	0	0	0	0

te interval [0, 1]), then the 1d discrete models are di- 2n). In our case, we can listribution as a piecewiseit has a constant value for $\dots 256$. This correspondne log-likelihood (on data 1 discrete distribution (on R + X < i) $P(X_{i,G} + X_{i})$

tive log-likelihood in *nats* ature. For CIFAR-10 and Aikelihoods in *bits* per diikelihood is normalized by $32 \times 32 \times 3 = 3072$ activationespfeoablehes the prinformations adout this olor categories of orgyalue ors, the disatibut 2015); 1 and a cadus to natithmetic Also not a statues bability as they are hediscrete distribusuchtbendistributioolbox. Dr Channels dateifildes foedetkingProp distributions. 1 for all ex-,G, $\mathbf{X}_{\leq i}$) anually set

alues that allowed fast con-142





Samples from PixelCNN

Conditional Image Generation with PixelC van den Oord, Kalchbrenner, Vinyals, Espeholt, Graves, K

Topics: CIFAR-10

• Samples from a class-conditioned PixelCNN



Coral Reef



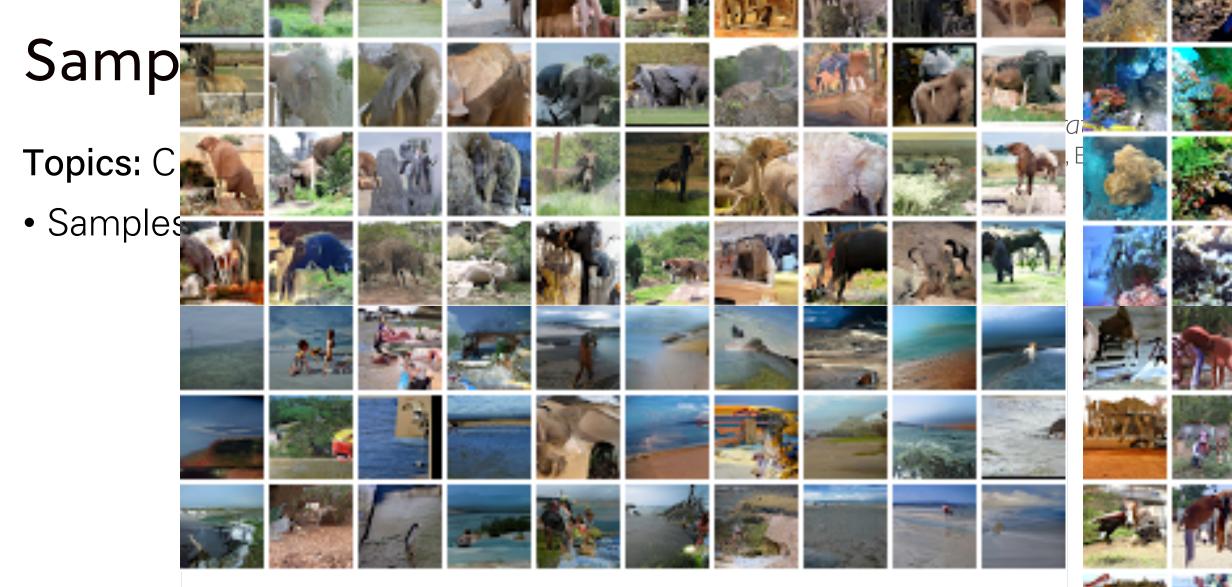
Samples from PixelCNN

Topics: CIFAR-10

• Samples from a class-conditioned PixelCNN



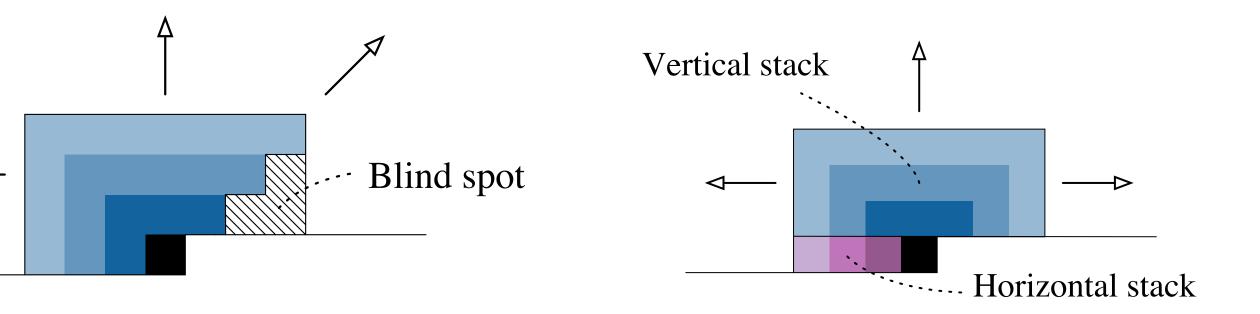
Sorrel horse



Sandbar

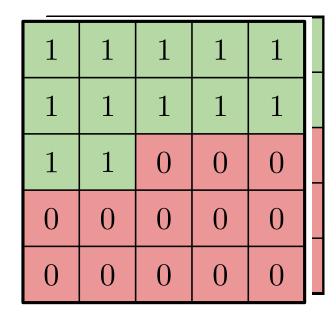


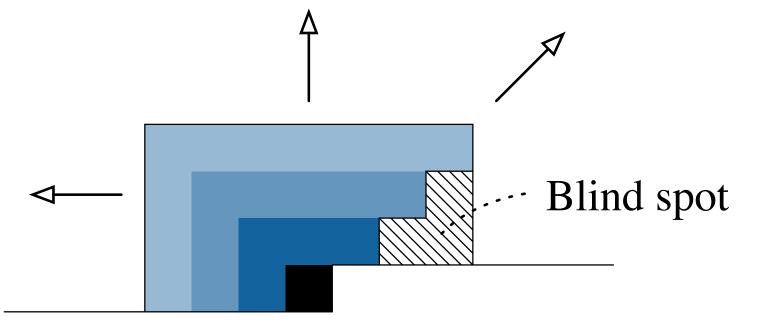
Slide credit: Nal Kalchbren



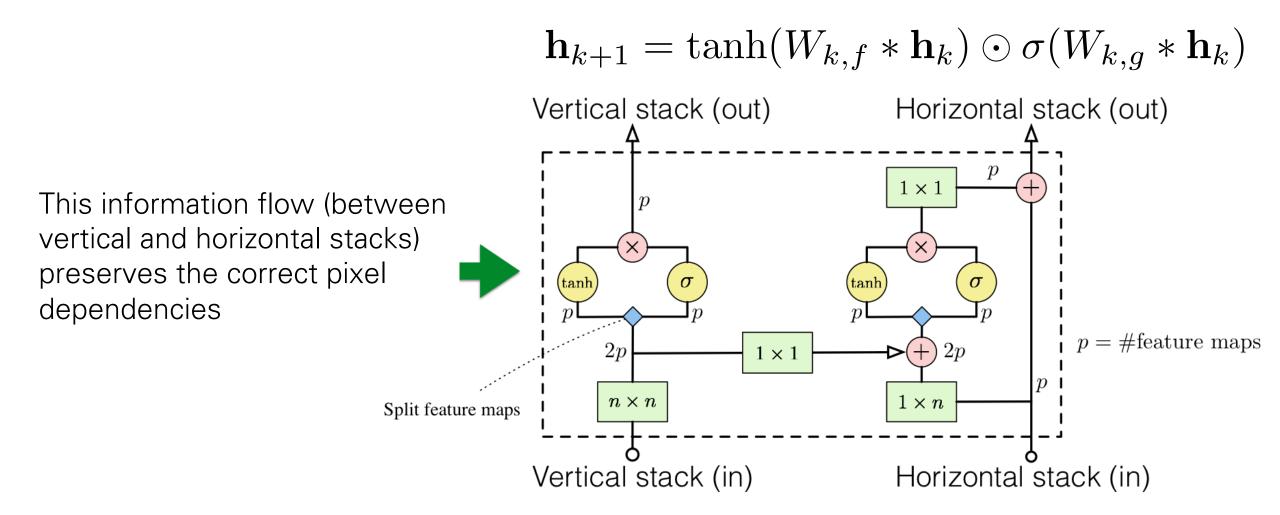
Improving PixelCNN I

There is a problem with this form of masked convolution.

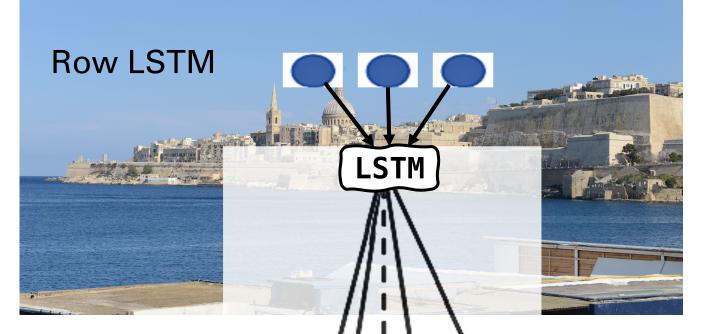


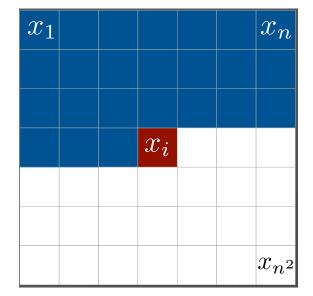


Stacking layers of masked convolution creates a blindspot

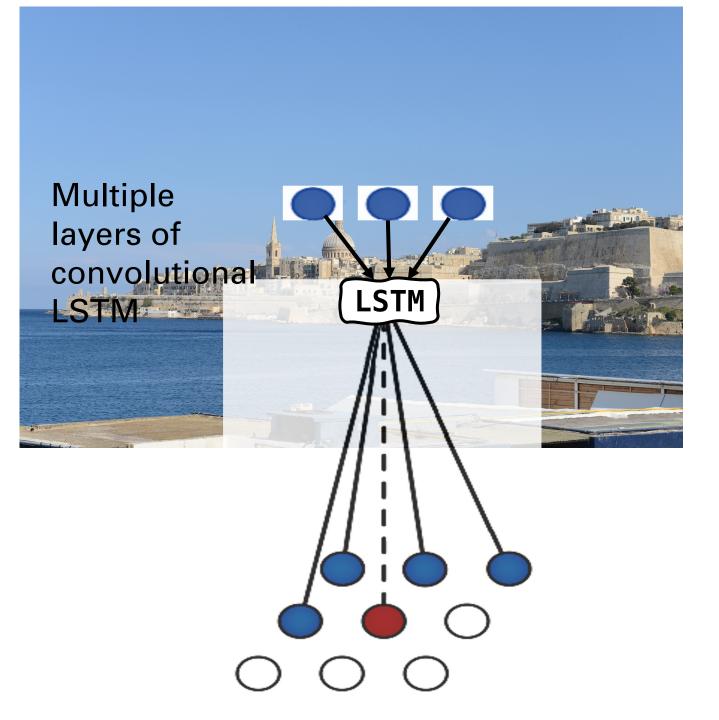


prt-Term Memory

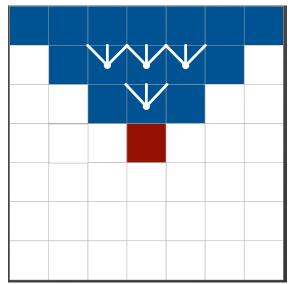




Stollenga et al, 2015 Oord, Kalchbrenner, Kavukcuoglu, 2016

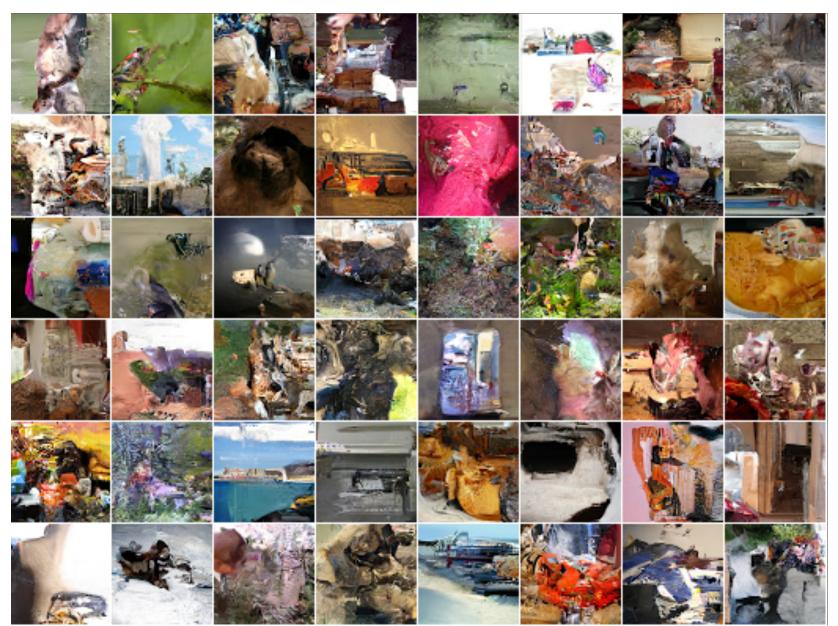


x_1				x_n
		x_i		
		x_i		
				x_{n^2}
				x_{n^2}



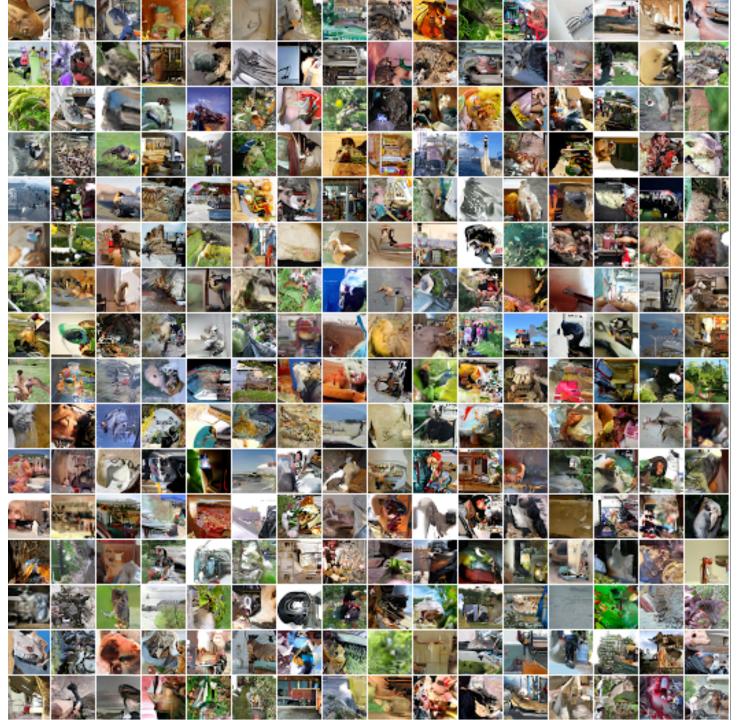
Oord, Kalchbrenner, Kavukcuoglu, 2016

Samples from PixelRNN



Slide credit: Nal Kalchbrenner

Samples from PixelRNN



Slide credit: Nal Kalchbrenner

Image completions (conditional samples) from PixelRNN

occluded

completions





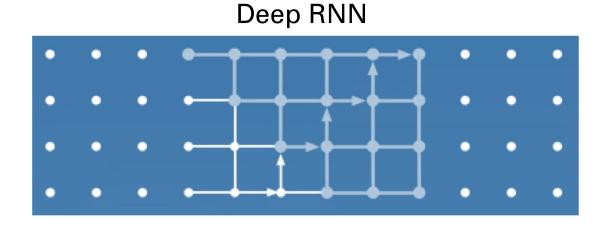
[PixelRNN, van der Oord et al. 2016]

Modeling Audio

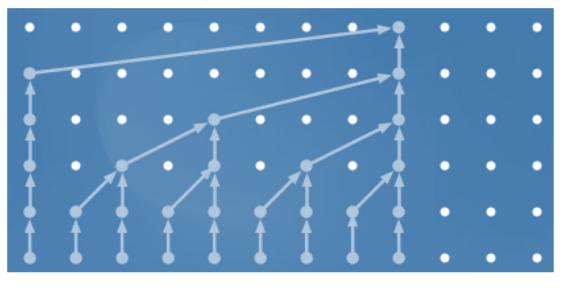


1 Second

Architecture for 1D sequences (Bytenet / Wavenet)



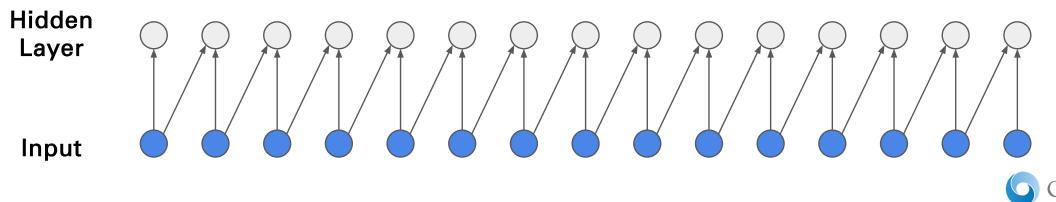
Bytenet decoder



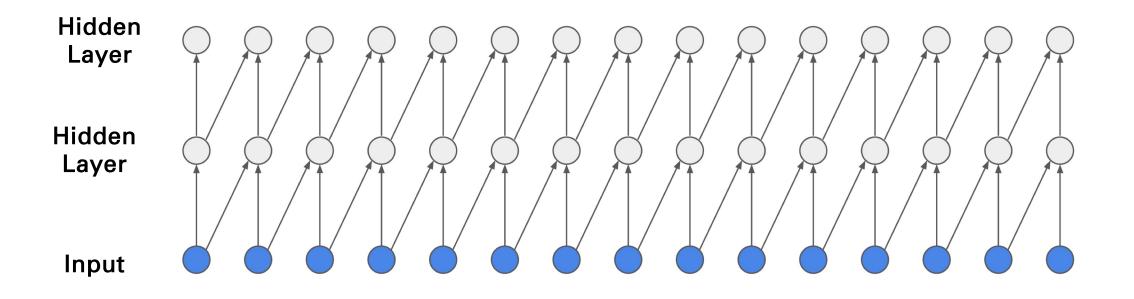
• Stack of **dilated**, **masked 1-D convolutions** in the decoder

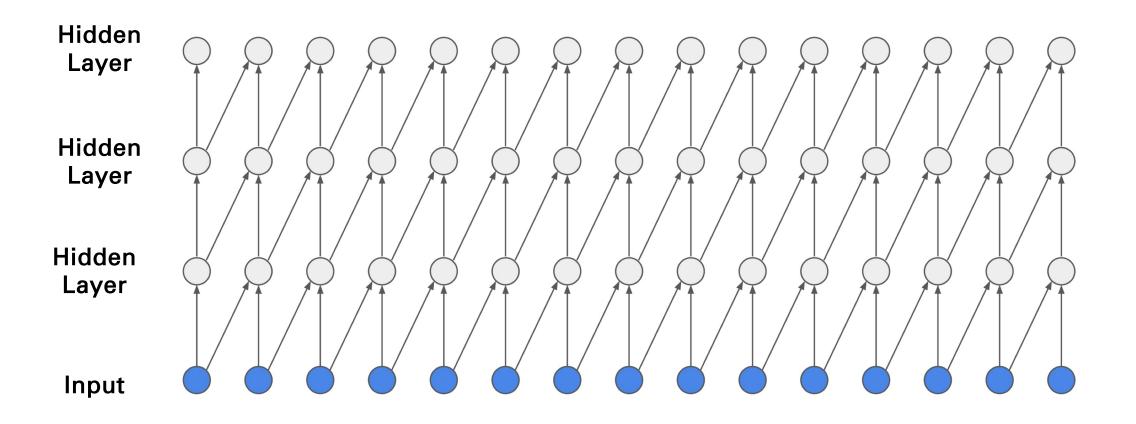
)

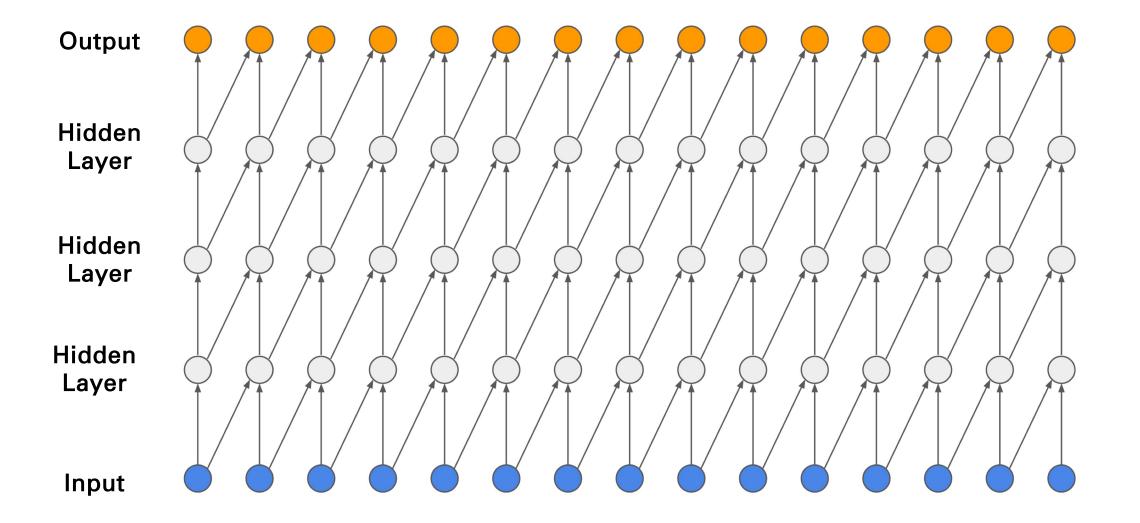
- The architecture is **parallelizable** along the time dimension (during training or scoring)
- Easy access to **many states** from the past

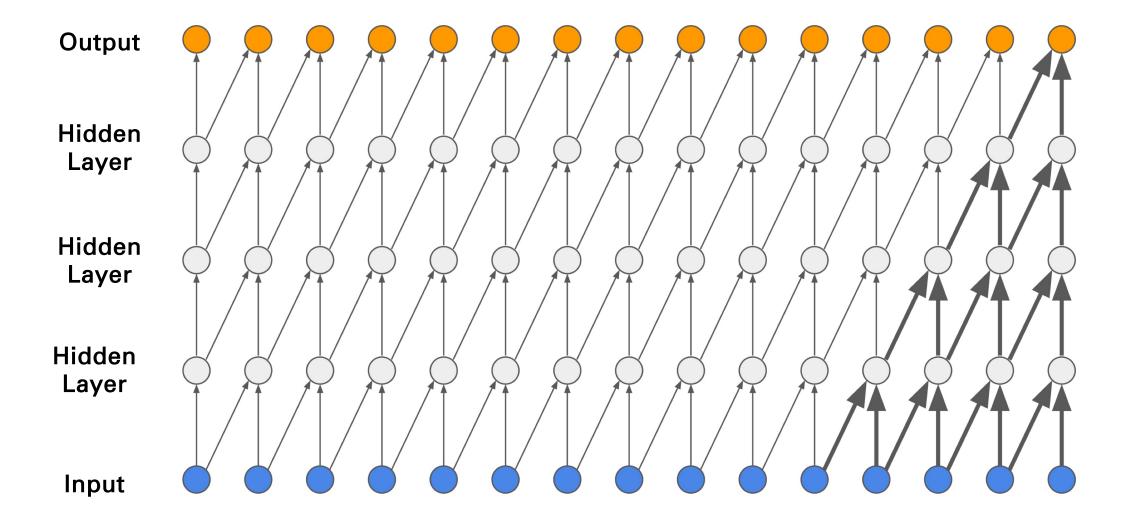


Google DeepMind 57

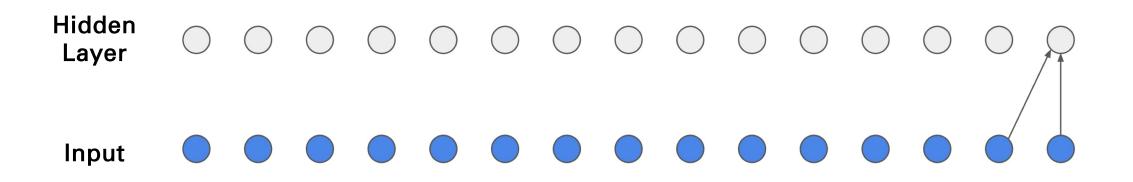


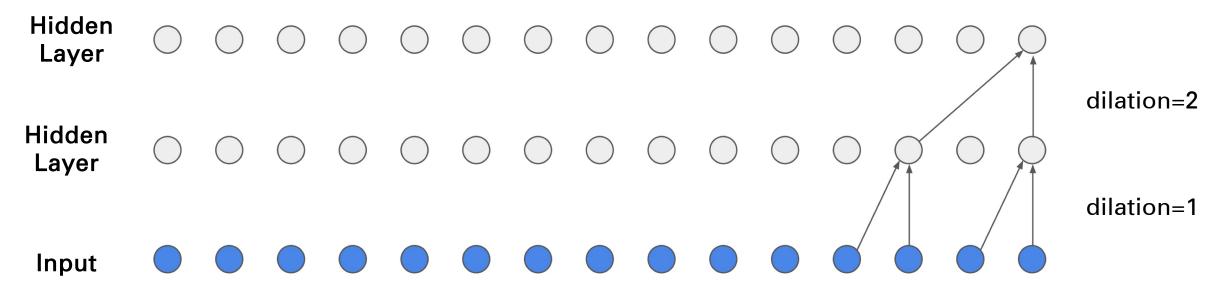


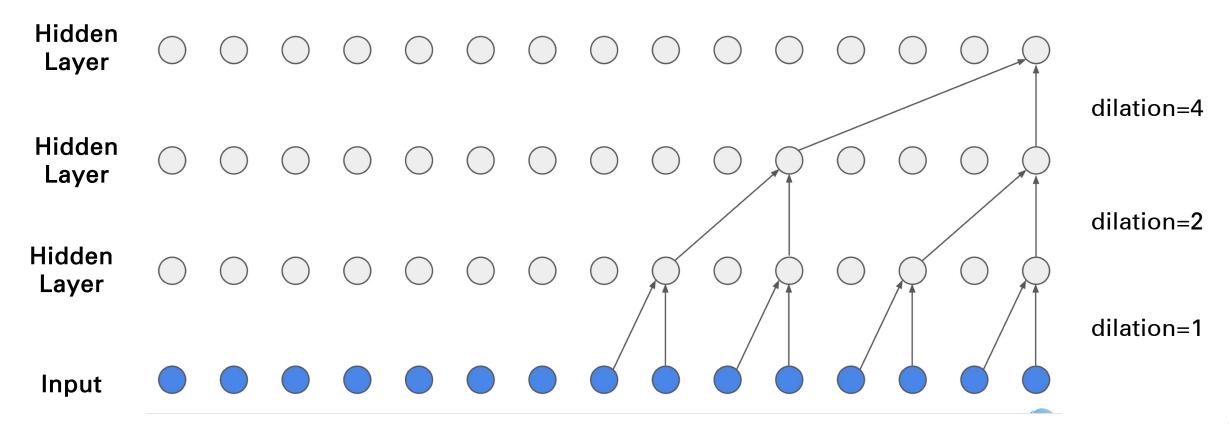


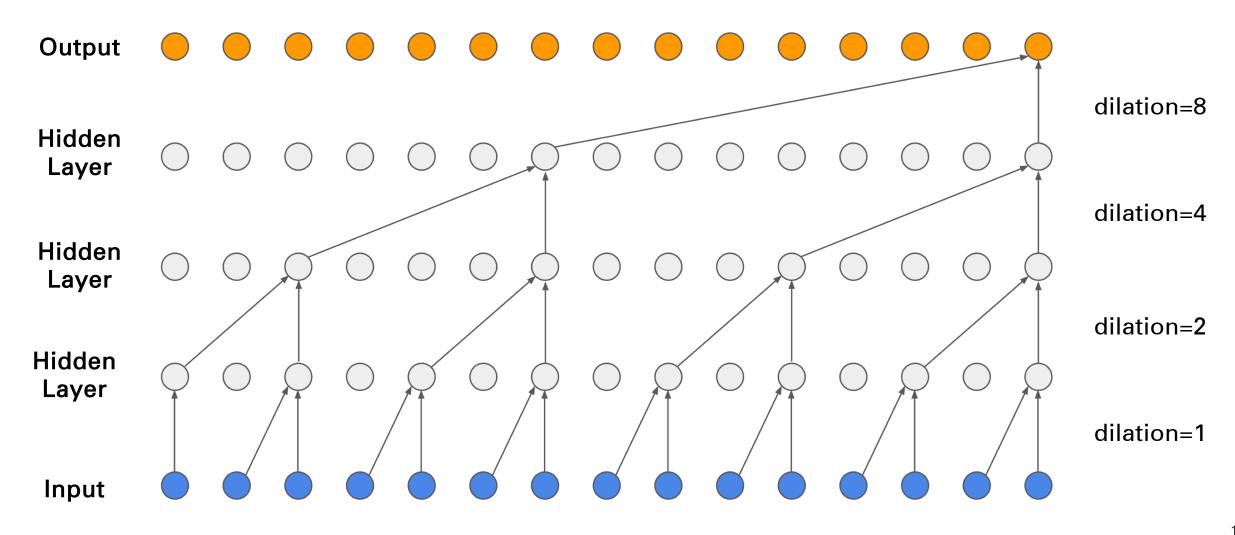


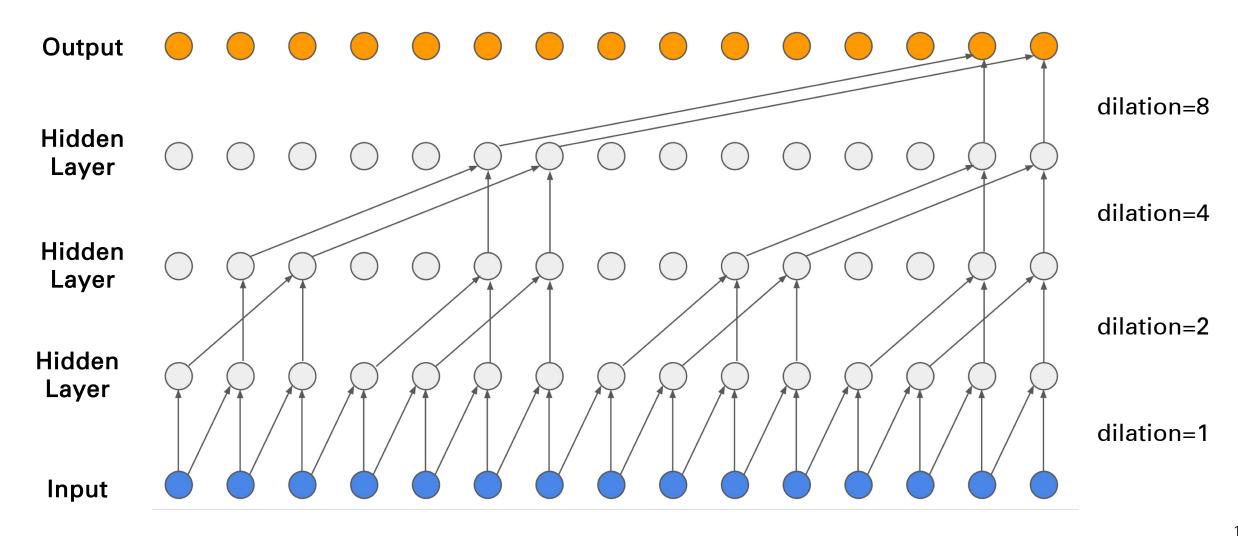






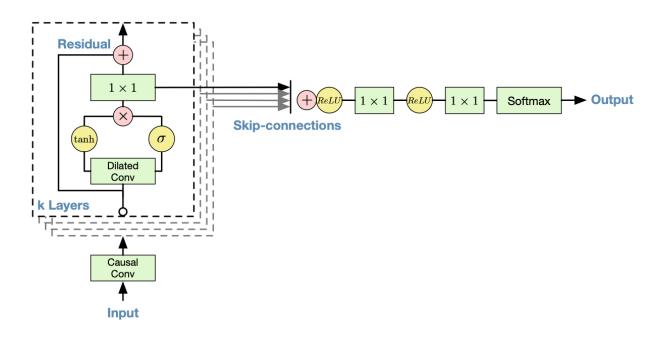


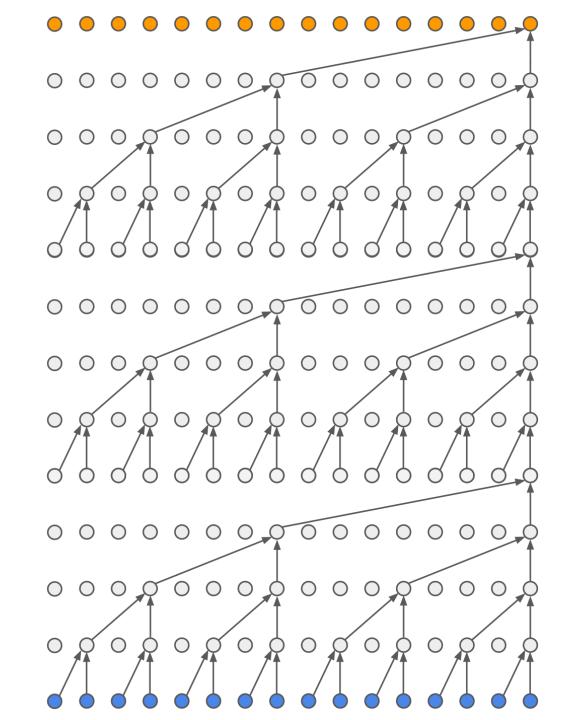




Multiple Stacks

- Improved receptive field with dilated convolutions
- Gated Residual block with skip connections





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Sampling

Output 😑 😑 😑 😑 😑 😑 😑 😑 😑 😑 😑 😑





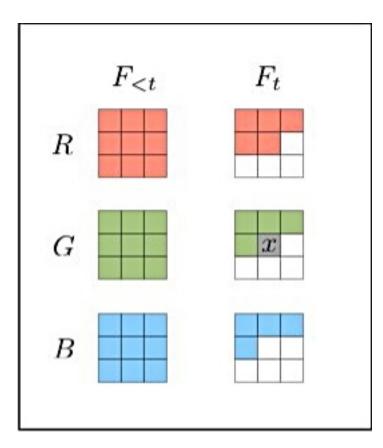


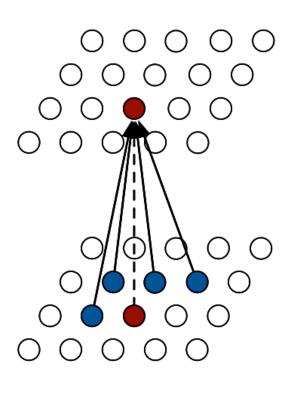
sample

music

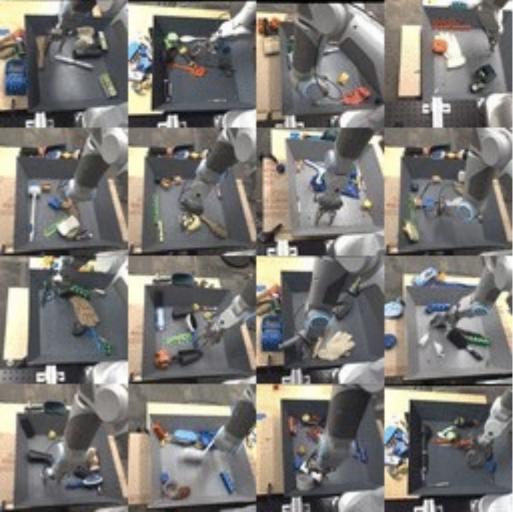
Output 🔴 🔴 🔴 🔴 🌕 🔴 🌑 🔴 🔴 🔴 🔴 🌑 🔴

Video Pixel Net (VPN)



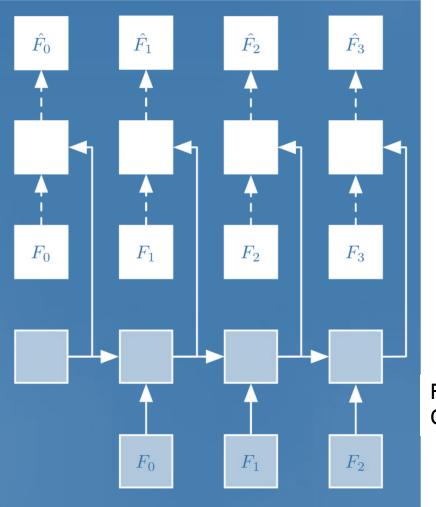


masked convolution



VPN Samples for Robotic Pushing

Video Pixel Net (VPN)



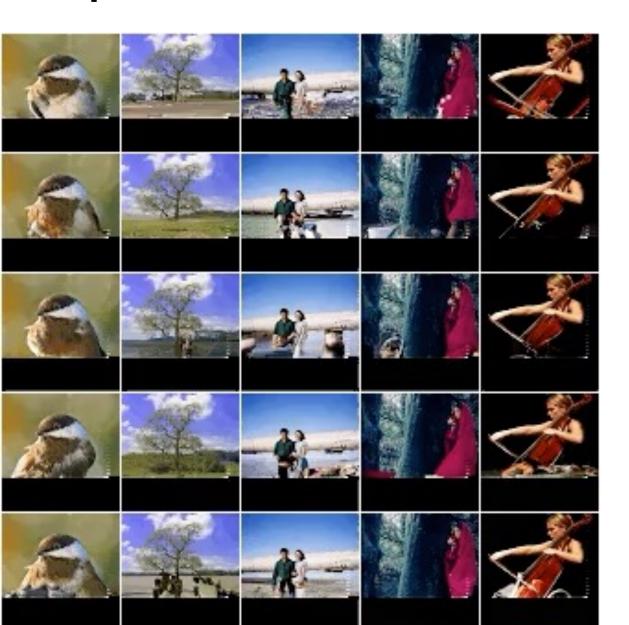
PixelCNN Decoders

Resolution Preserving CNN Encoders

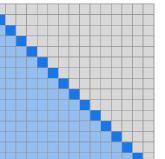


VPN Samples for Robotic Pushing

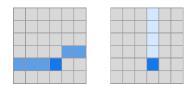
Sparse Transformers

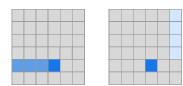


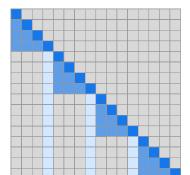












Sparse Transformer (fixed)

- Strided attention is roughly equivalent to each position attending to its row and its column
- Fixed attention attends to a fixed column and the elements after the latest column element (especially used for text).

Sparse

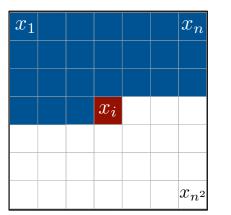
Transformer

(strided)

[Child, Gray, Radford, Sutskever, 2019] 173

Autoregressive Models

• Explicitly model conditional probabilities:



$$p_{\text{model}}(\boldsymbol{x}) = p_{\text{model}}(x_1) \prod_{i=2} p_{\text{model}}(x_i \mid x_1, \dots, x_{i-1})$$

n

Advantages:

• $p_{\text{model}}(x)$ is tractable (easy to train and sample

Disadvantages:

- Generation can be too costly
- Generation can not be controlled by a latent code

PixelCNN elephants (van den Ord et al. 2016)

Slide adapted from Ian Goodfellow

Next Lecture: Deep Generative Models Part 2